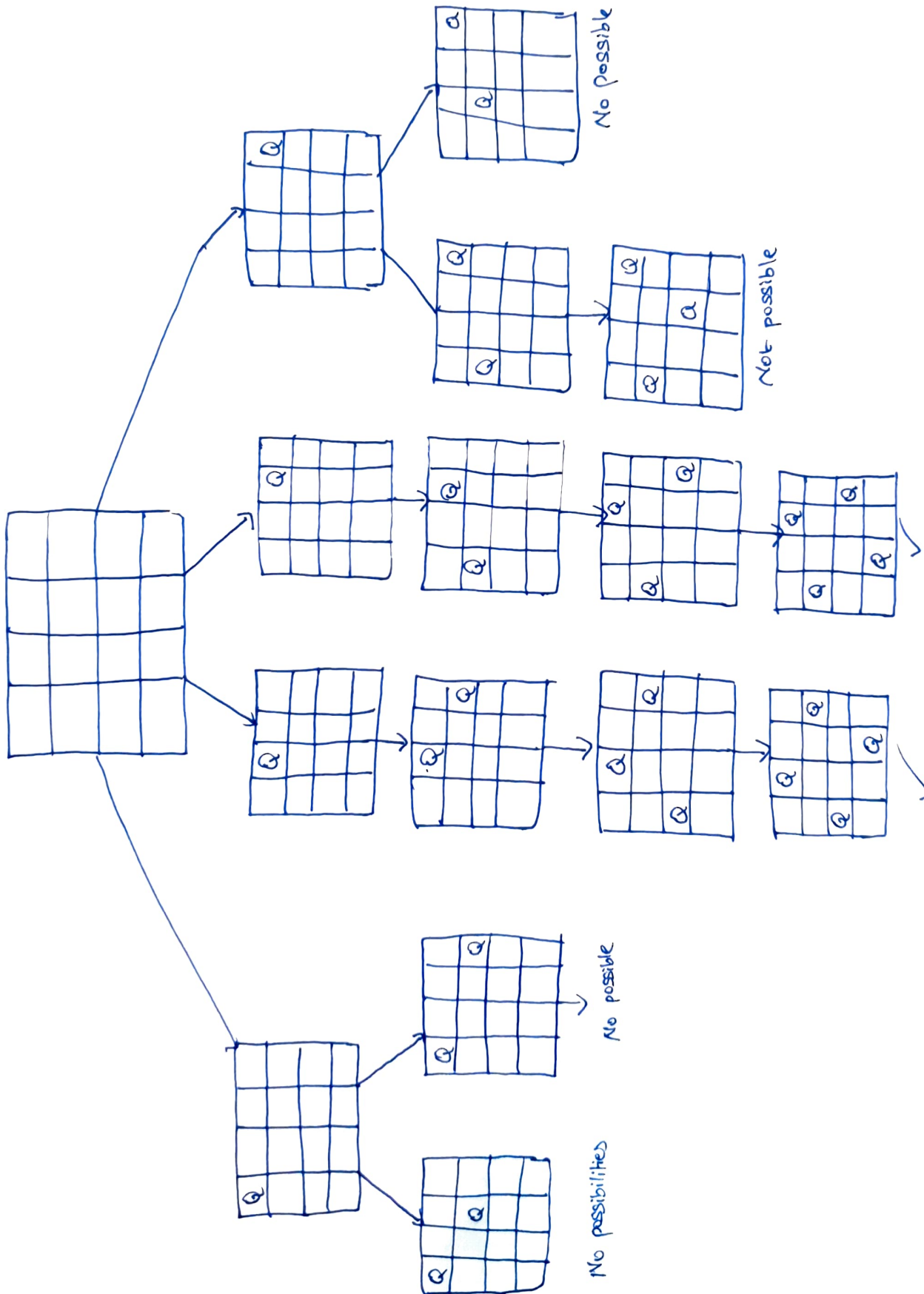
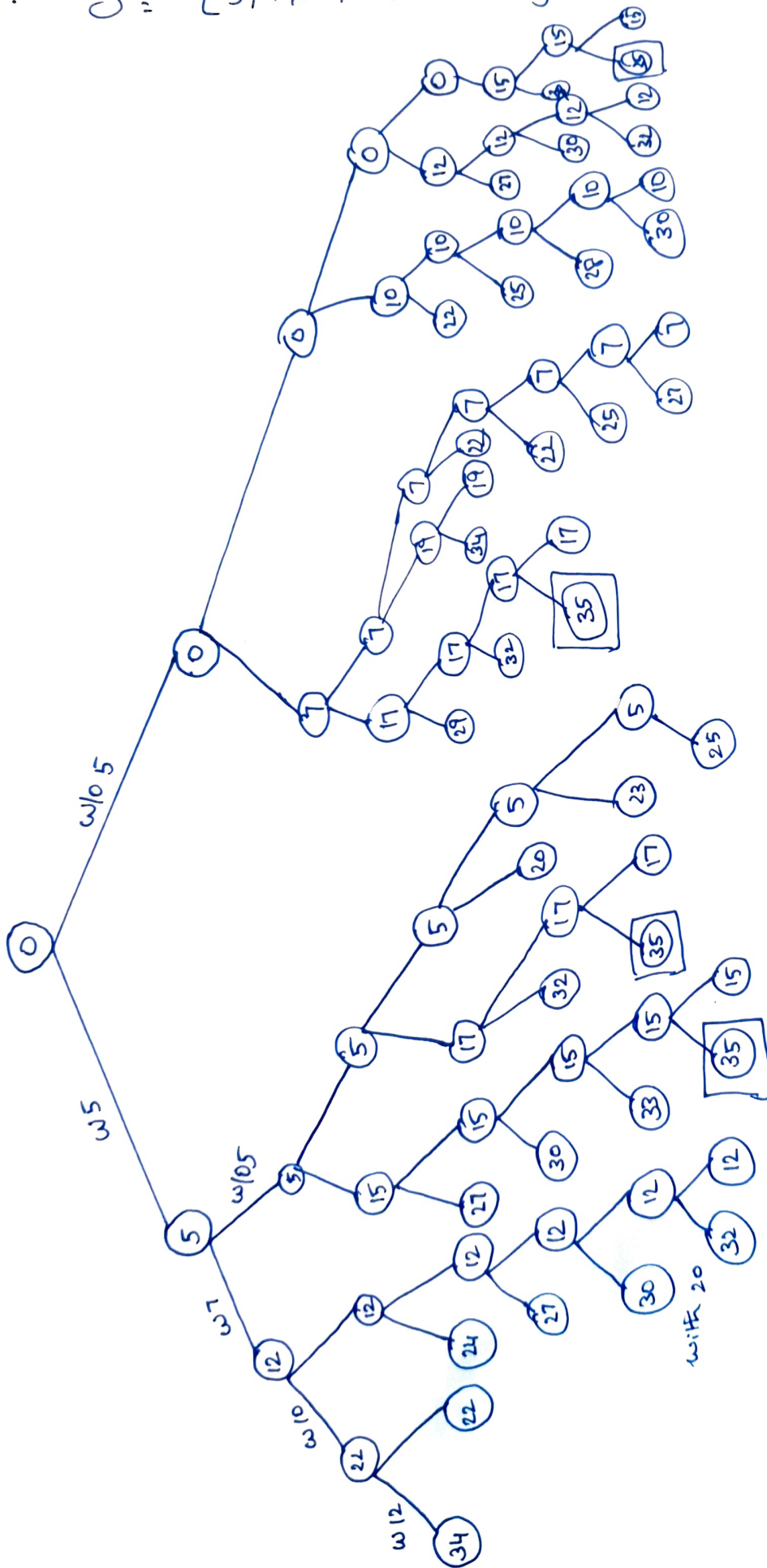


1. 4-Queen's problem



2. $S = \{5, 7, 10, 12, 15, 18, 20\}$ $d = 35$



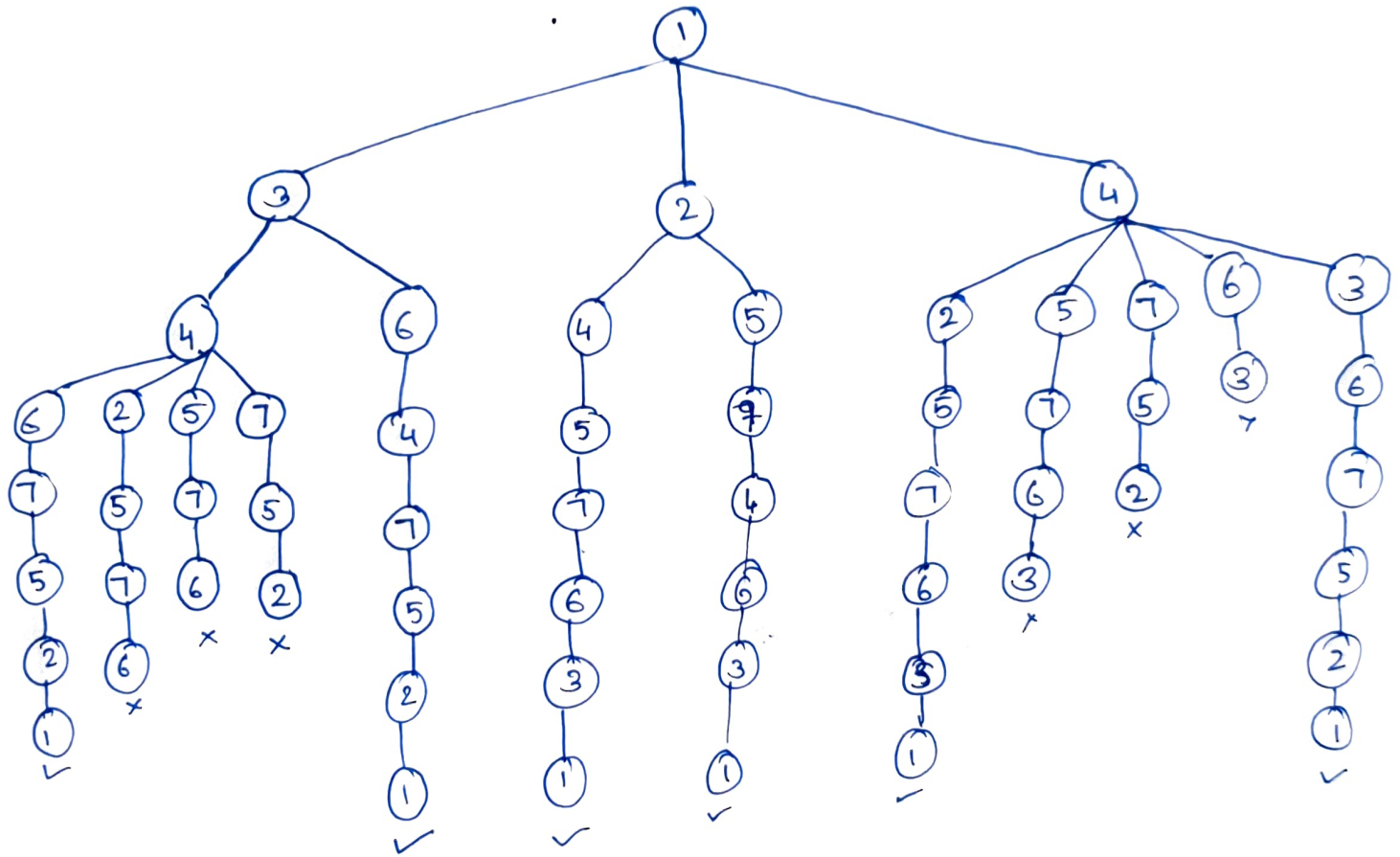
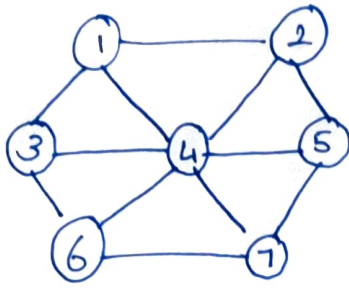
$$S_1 = \{20, 10, 5\}$$

$$S_2 = \{18, 12, 5\}$$

$$S_3 = \{18, 10, 7\}$$

$$S_U = \{20, 15\}$$

3.



Solution:

- 1, 3, 4, 6, 7, 5, 2, 1
- 1, 3, 6, 4, 7, 5, 2, 1
- 1, 2, 4, 5, 7, 6, 3, 1
- 1, 2, 5, 7, 4, 6, 3, 1
- 1, 4, 2, 5, 7, 6, 3, 1
- 1, 4, 3, 6, 7, 5, 2, 1

4. Solve Gaussian Elimination algorithm

$$2x_1 + x_2 - x_3 = 4$$

$$x_1 + x_2 + x_3 = 2$$

$$x_1 - x_2 + 2x_3 = 8$$

$$\begin{bmatrix} 2 & 1 & -1 & 4 \\ 1 & 1 & 1 & 2 \\ 1 & -1 & 2 & 8 \end{bmatrix} \quad \begin{array}{l} R_2 = R_2 - \frac{1}{2}R_1 \\ R_3 = R_3 - \frac{1}{2}R_1 \end{array}$$

$$\begin{bmatrix} 2 & 1 & -1 & 4 \\ 0 & 1/2 & 3/2 & 0 \\ 0 & -3/2 & 5/2 & 6 \end{bmatrix} \quad R_3 = R_3 + 3R_2$$

$$\begin{bmatrix} 2 & 1 & -1 & 4 \\ 0 & 1/2 & 3/2 & 0 \\ 0 & 0 & 7 & 6 \end{bmatrix}$$

$$7x_3 = 6 \Rightarrow x_3 = 6/7$$

$$\frac{1}{2}x_2 + \frac{3}{2}x_3 = 0 \Rightarrow \frac{1}{2}x_2 + \frac{9}{7} = 0 \Rightarrow \frac{x_2}{2} = -\frac{9}{7} \Rightarrow x_2 = -\frac{18}{7}$$

$$2x_1 + x_2 - x_3 = 4$$

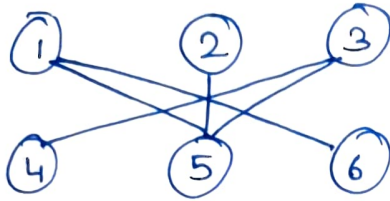
$$2x_1 - 18/7 - 6/7 = 4$$

$$2x_1 = 4 + \frac{24}{7}$$

$$2x_1 = \frac{52}{7}$$

$$x_1 = \frac{26}{7}$$

5.



Algorithm for graph Colouring

mcolouring(k)

// This algorithm was formed using recursive backtracking

// The graph is represented by its boolean adjacency matrix

// $G[1:n, 1:n]$

// All the vertices are assigned distinct integers

// k is the index of the next colour to vertex.

Repeat

{ // Generate all legal assignment for $x[k]$

if ($x[k] = 0$) then return; // No new

if ($k = n$) then // Almost m colors possible

write($x[1:n]$);

else mcolouring($k+1$);

until (false);

} }

Algorithm Nextvalue(k)

// Generate next color

// $x[1] \dots x[k-1]$ have been assigned int values.

// value of k is determined in the range of $[0, m]$

// If no color exist then $x[k]$ is 0.

```

repeat {
     $x[k] = (x[k] + 1) \bmod (M+1)$ ; // Next high color
    if ( $x[k] = 0$ ) then return; // All colors used
    for  $j \leftarrow 1$  to  $n$  do
        ↩
        if (( $G[k,j] \neq 0$ ) and ( $x[k] = x[j]$ ))
            // if (k,j) is edge & if adjacent have same color
            then break;
    }
    if ( $j = n+1$ ) then return; // new color found
    until (false); // otherwise find next color
}

```

