

1.

Variables :

X1 = number of collegiate bags

X2 = number of mini bags

Y = maximum profit

Objection Function :

$Y = 32(\text{unit profit})x_1(\text{number of collegiate bags}) + 24(\text{unit profit})x_2(\text{number of mini bags})$

$$Y = 32x_1 + 24x_2$$

Constraints :

Labor is measured in hours, so the labor in each bag needs to be converted.

X1 requires 45 minutes of labor which is $\frac{3}{4}$ hours

X2 requires 40 minutes of labor which is $\frac{2}{3}$ hours

$$3x_1 + 2x_2 \leq 5000$$

This is telling us that the 3 square feet of nylon is required for each unit of collegiate bags and 2 square feet of nylon is required for the mini bags.

$$\text{Labor : } X_1\left(\frac{3}{4}\right) + X_2\left(\frac{2}{3}\right) =$$

$$35 \times 40 = 1400 \text{ (hrs of production)}$$

$$X_1\left(\frac{3}{4}\right) + X_2\left(\frac{2}{3}\right) \leq 1400$$

2.

Variables :

X = # of units produced by plant 1

Y = # of units produced by plant 2

V = # of units produced by plant 3

x1 = Number of units of the large size produced by Plant 1

x2 = Number of units of the medium size produced by Plant 1

x3 = Number of units of the small size produced by Plant 1

y1 = Number of units of the large size produced by Plant 2

y2 = Number of units of the medium size produced by Plant 2

y3 = Number of units of the small size produced by Plant 2

v1 = Number of units of the large size produced by Plant 3

v2 = Number of units of the medium size produced by Plant 3

v3 = Number of units of the small size produced by Plant 3

Maximize :

$$Z = 420(x1+y1+v1) + 360(x2+y2+v2) + 300(x3+y3+v3)$$

Capacity Constraints :

$$x1+x2+x3 \leq 750 \text{ (plant 1)}$$

$$y1+y2+y3 \leq 900 \text{ (plant 2)}$$

$$v1+v2+v3 \leq 450 \text{ (plant 3)}$$

Storage Space Constraints :

$$20x1+15x2+12x3 \leq 13,000 \text{ (plant 1)}$$

$$20y1+15y2+12y3 \leq 12,000 \text{ (plant 2)}$$

$$20v1+15v2+12v3 \leq 5,000 \text{ (plant 3)}$$

Constraint for large sz :

$$x1+y1+v1 = 900$$

Constraint for medium sz :

$$x2+y2+v2 = 1200$$

Constraint for large sz :

$$x3+y3+v3 = 750$$

Non-negativity constraint:

$$x1, x2, x3, y1, y2, y3, v1, v2, v3 \geq 0$$