

3 1/2 hours; 1:00 pm CT or 1:30?

Using qiskit pulse for Grover's

- Measure qubit energy w/ freq./energy pulses
- Classification into 3 states
- Learn how to manipulate qubits (gates?)

$$Z(+2) = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} b \\ c \\ a \end{bmatrix} = Z(+1)^2 \text{ or } Z(01) \cdot Z(02) \quad \boxed{4 \text{ pulses}}$$

$$Z(+1) = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} c \\ a \\ b \end{bmatrix} = Z(01) Z(12) \quad \boxed{2 \text{ pulses}}$$

$$Z(01) = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} b \\ a \\ c \end{bmatrix} \quad 0 \rightarrow 1 \quad \boxed{1 \text{ pulse}}$$

$$Z(02) = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} c \\ b \\ a \end{bmatrix} \quad 0 \rightarrow 2 = Z(01) Z(12) Z(01) \quad \boxed{3 \text{ pulses}}$$

$$Z(12) = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} a \\ c \\ b \end{bmatrix} \quad 1 \rightarrow 2 \quad \boxed{1 \text{ pulse}}$$

$$Z(01) Z(12) = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix}$$

$$Z(01) Z(12) Z(01) = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$Z(01) Z(12) = \begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} = Z(+1)$$

$$Z(+2) = Z(01) \cdot Z(02) \quad (4 \text{ pulses})$$

$$\text{or } Z(+1) \cdot Z(+1) \quad (4 \text{ pulses})$$

$$S_Z = \begin{pmatrix} \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{3}} & \frac{-2}{\sqrt{6}} & 0 \\ \frac{1}{\sqrt{3}} & \frac{1}{\sqrt{6}} & \frac{1}{\sqrt{2}} \end{pmatrix}$$

$$M = S_Z(a_1, a_2, \dots, a_n) = \begin{cases} \text{Shift by } Z & \text{if } a_i = Z \text{ for } i=1, \dots, n \\ C & \text{otherwise} \end{cases}$$

↳ Only applies  $Z(x)$  on  $C$  if all  $a_i = Z$

$$P = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} \quad Z \rightarrow -Z$$

$$\gamma(t) = I(t) + iQ(t) = R(t)e^{i\phi(t)}$$

$$I = R \cos \phi \quad Q = R \sin \phi \Rightarrow \phi = \pi$$