# Visualisation and Analysis of Geographic Information Algorithms and Data Structures

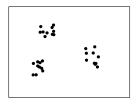
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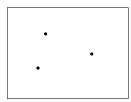
Department of Informatics Engineering University of Coimbra

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#### Motivation

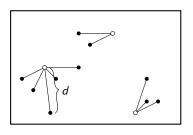
- Reduce visual information when displaying large numbers of geographic points
- ► Find a representative subset of a collection of geographic points

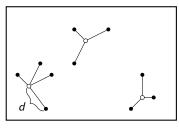




## Coverage

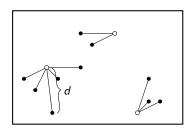
#### ► Minimising Coverage

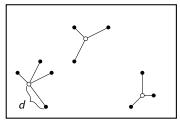




## Coverage

#### Minimising Coverage





 $\min_{\substack{P\subseteq N \\ |P|=k}} \max_{n\in N} \min_{p\in P} \|p-n\|$ 

#### Work Plan

#### ▶ 1<sup>st</sup> Semester

- Literature Review: Geographic Information Systems, OGC Standards WMS, WFS, Map Projections, algorithms and heuristics for clustering and facility-location problems.
- Development of a Branch-and-Bound approach.

#### 2<sup>nd</sup> Semester

- Development of heuristic approaches.
- Experimental analysis of the algorithms.
- Integration of the algorithms in the visualisation framework through web-mapping standards (WMS/WFS).
- Comparison between different approaches using Open Street Map data.

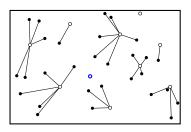
## Integer Linear Programming

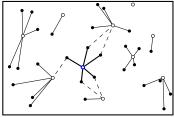
minimise 
$$D$$
 subject to  $\sum_{j=1}^{N}y_j=k$  
$$\sum_{j=1}^{N}x_{ij}=1 \qquad \qquad i=1,\ldots,N$$
 
$$\sum_{j=1}^{N}d_{ij}x_{ij}\leq D \qquad \qquad i=1,\ldots,N$$
 
$$x_{ij}\leq y_j \qquad \qquad i=1,\ldots,N; j=1,\ldots,N$$
 
$$x_{ji},y_i\in\{0,1\} \qquad i=1,\ldots,N; j=1,\ldots,N$$

- Branching
  - Divide search space in a binary tree
  - ▶ At each step, decide if a point is a centroid or non-centroid
  - Update objective function accordingly

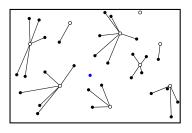
- Branching
  - Divide search space in a binary tree
  - ▶ At each step, decide if a point is a centroid or non-centroid
  - Update objective function accordingly
- Bound
  - ► Assume best possible case
  - Prune tree

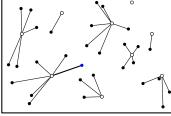
- ▶ Inserting a Centroid
  - ▶ Search all non-centroids for assignment update
  - ► Smaller coverage value



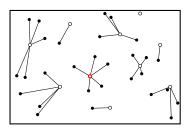


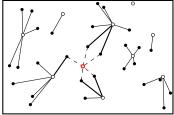
- ▶ Inserting a Non-centroid
  - Search for closest centroid
  - ► Higher coverage value



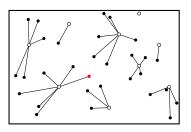


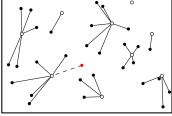
- Removing a Centroid
  - ► Update all non-centroids
  - ► Higher coverage value





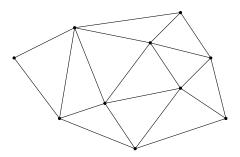
- Removing a Non-centroid
  - ▶ Update objective function
  - ► Smaller coverage value



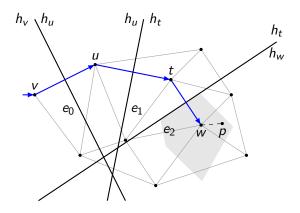


- Unnecessary number of calculations
  - ▶ Use geometric structures to speed objective function update

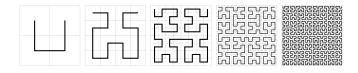
- Unnecessary number of calculations
  - ▶ Use geometric structures to speed objective function update
  - Delaunay triangulations



Greedy Routing



- Greedy Routing
- Use Hilbert curves to minimise distance between consecutive routing calls



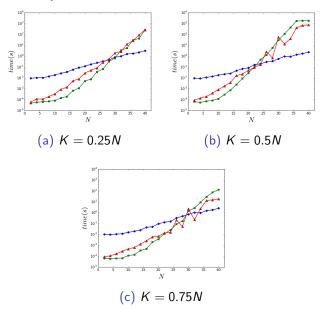
- Initialize triangulation
- Sort points using a Hilbert curve
- Inserting a Centroid
  - Insert centroid in triangulation
  - Search all neighbours for closer non-centroids for assignment update
  - Smaller coverage value
- Inserting a Non-centroid
  - Search for closest centroid using greedy routing
  - ▶ Higher coverage value

- Initialize triangulation
- Sort points using a Hilbert curve
- Inserting a Centroid
  - ► Insert centroid in triangulation
  - Search all neighbours for closer non-centroids for assignment update
  - Smaller coverage value
- Inserting a Non-centroid
  - Search for closest centroid using greedy routing
  - Higher coverage value
- Removing a Centroid
  - Revert assignment
  - Remove centroid from triangulation
  - Higher coverage value
- Removing a Non-centroid
  - Update objective function
  - ► Revert assignment
  - Smaller coverage value

# Algorithm Comparison

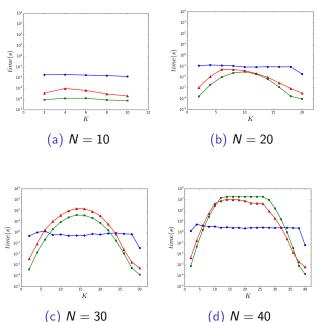
Algorithm	Insert		Remove	
	Centroid	Non-Centroid	Centroid	Non-Centroid
Naïve BB	$\Theta(N)$	Θ(K)	$\Theta(N)$	$\mathcal{O}(1)$
Geometric BB	$\mathcal{O}(\log K + N/K)$	$\mathcal{O}(\sqrt{K})$	$\mathcal{O}(N/K)$	$\mathcal{O}(1)$
Average Case				
Geometric BB	$\mathcal{O}(K+N)$	$\mathcal{O}(K)$	$\mathcal{O}(N)$	$\mathcal{O}(1)$
Worst Case				

## Algorithm Comparison



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## Algorithm Comparison



#### Future Work

- Integration with WFS standard
- Heuristic Approach
- Approximation Algorithms
- ► Benchmark with real data