```
A_5 := Transpose[{Coefficient[L_5[1], w, #] & /@Range[0, 8], Coefficient[L_5[w], w, #] & /@Range[0, 8],}
              Coefficient [L_5[w^2], w, \#] \& /@Range[0, 8], Coefficient <math>[L_5[w^3], w, \#] \& /@Range[0, 8],
              Coefficient[L_5[w^4], w, \#] \& /@ Range[0, 8], Coefficient[L_5[w^5], w, \#] \& /@ Range[0, 8],
             Coefficient [L_5[w^6], w, \#] \& /@Range[0, 8], Coefficient <math>[L_5[w^7], w, \#] \& /@Range[0, 8]
B_5 := Drop[A_5, 1]
v_5 := Take[A_5, 1]
r<sub>5</sub> := LinearSolve[B<sub>5</sub>, Coefficient[P<sub>5</sub>, w, #] & /@ Range[1, 8]]
R_5 := r_5 \cdot \{1, w, w^2, w^3, w^4, w^5, w^6, w^7\}
F_5 := Simplify[v_5.r_5 - Coefficient[P_5, w, 0]][[1]]
q_6 := S_6 + 3 * C_2 * S_5 * r + (C_3 / 2 + 3 * C_2^2) * S_4 * r^2 +
          (-c_4/3+c_3*c_2/6+c_2^3)*S_3*r^3+(-3*c_5/4-3*c_4*c_2/2-c_3^2/8-3*c_3*c_2^2/4)*S_2*r^4
\tilde{q}_6 := \tilde{S}_6 + 3 * \tilde{c}_2 * \tilde{S}_5 * r + (\tilde{c}_3 / 2 + 3 * \tilde{c}_2 \wedge 2) * \tilde{S}_4 * r \wedge 2 + (-\tilde{c}_4 / 3 + \tilde{c}_3 * \tilde{c}_2 / 6 + \tilde{c}_2 \wedge 3) * \tilde{S}_3 * r \wedge 3 + \tilde{c}_3 * \tilde{c}_4 / \tilde{c}_5 * \tilde{c}_5 / 6 + \tilde{c}_5 \times \tilde{c}_5
          \left(-3*\tilde{c}_{5}/4-3*\tilde{c}_{4}*\tilde{c}_{2}/2-\tilde{c}_{3}^{2}/8-3*\tilde{c}_{3}*\tilde{c}_{2}^{2}/4\right)*\tilde{S}_{2}*r^{4}
P_6 := \tilde{q}_6 - q_6 + \tilde{q}_4 * R_3 - (1/2) * S_2 * R_3 ^2 - S_3 * R_4 - 3 * S_2 * R_5
L_6[f_] := D[f, w] * r + 5 * (s - 2 * w) * f
Coefficient [L_6[w^2], w, \#] \& /@Range[0, 10], Coefficient [L_6[w^3], w, \#] \& /@Range[0, 10],
              Coefficient [L_6[w^4], w, \#] \& /@Range[0, 10], Coefficient[L_6[w^5], w, \#] \& /@Range[0, 10],
              Coefficient [L_6[w^6], w, \#] \& /@Range[0, 10], Coefficient [L_6[w^7], w, \#] \& /@Range[0, 10],
              Coefficient[L6[w^8], w, #] & /@ Range[0, 10], Coefficient[L6[w^9], w, #] & /@ Range[0, 10]}]
B_6 := Drop[A_6, 1]
v_6 := Take[A_6, 1]
r_6 := LinearSolve[B_6, Coefficient[P_6, w, #] & /@ Range[1, 10]]
F_6 := Simplify[v_6.r_6 - Coefficient[P_6, w, 0]][[1]]
```

Now that we have expresions for the polynomials  $F_d$ , we proceed to compute the resultants defined in Section 3.3.

```
\begin{split} &R_{14} := Resultant[F_3, F_4, \beta_2] \\ &R_{15} := Resultant[F_3, F_5, \beta_2] \\ &R_{16} := Resultant[F_3, F_6, \beta_2] \\ &R_{25} := Resultant[R_{14}, R_{15}, \beta_1] \\ &R_{26} := Resultant[R_{14}, R_{16}, \beta_1] \\ &R_{36} := Resultant[PolynomialQuotient[R_{25}, \beta_0 - \alpha_0, \beta_0], R_{26}, \beta_0] \end{split}
```

In order to prove that  $R_{36}$  is not identically zero as a function of  $(\lambda, \alpha)$  we evaluate it at the following specific values to obtain a non-zero complex number:

```
\lambda_1 = 2 - \dot{\mathbf{n}};
\lambda_2 = 2 * \dot{\mathbf{n}};
\alpha_0 = 1;
\alpha_1 = 0;
\alpha_2 = 0;
```