

In the first part, we derive new B-spline bases on sparse grids

grids are well-suited for obtaining smooth interpolants for higher

dimensionalities. The thesis is organized in two main parts:

This thesis demonstrates that hierarchical B-splines on sparse

of convergence and the accuracy of the results.

second part, we consider three real-world applications in optimization: topology optimization, biomechanical continuummechanics, and dynamic portfolio choice models in finance. The

results reveal that the optimization problems of these applica-

tions can be solved accurately and efficiently with hierarchical

B-splines on sparse grids.

and study their implications on theory and algorithms. In the

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In simulation technology, computationally expensive objective

obtained by interpolation. Full grid interpolation methods suffer

functions are often replaced by cheap

from the so-called curse of dimensionality, rendering them infeasi ble if the parameter domain of the function is higher-dimensional (four or more parameters). Sparse grids constitute a discretization method that drastically eases the curse, while the approximation

quality deteriorates only insignificantly. However, conventional

basis functions such as piecewise linear functions are not smooth

(continuously differentiable). Hence,

these basis functions are

unsuitable for applications in which gradients are required. One

example for such an application is gradient-based optimization, in which the availability of gradients greatly improves the speed

surrogates, which can be



B-SPLINES FOR SPARSE GRIDS

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Algorithms and Application to Higher-Dimensional Optimization