

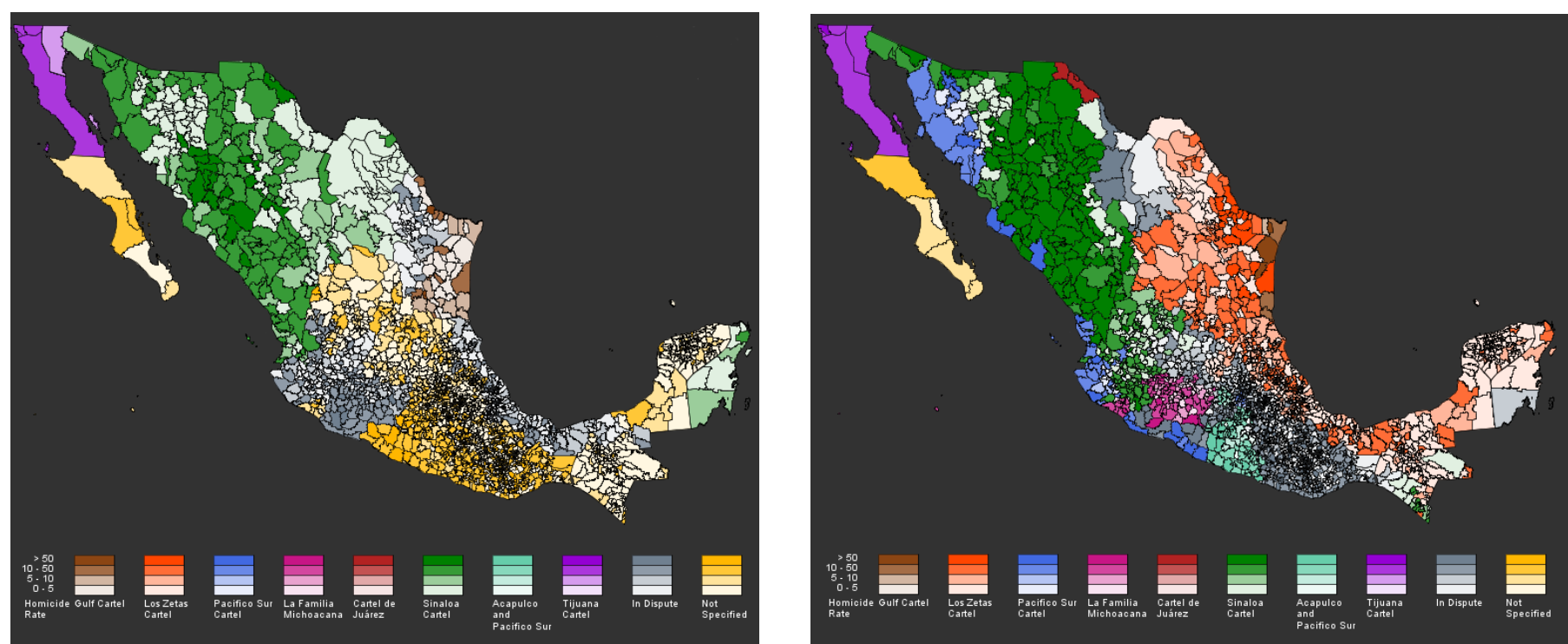
Visualization and Causal Inference of the Mexican Drug War

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Visualize the problem



(a) 2007

(b) 2010

We attempt to answer whether **homicide rates increase significantly after a military intervention**.

Estimand

Let $Y_i(1)$ denote the homicide rate change in region i from 2006 to one year after receiving a military intervention, and $Y_i(0)$ what it would have been if it hadn't received it (Rubin Causal Model). Our estimand is the average causal effect of the military intervention, W , for the regions that were intervened ($W = 1$),

$$\tau = \bar{Y}(1) - \bar{Y}(0) = \frac{\sum_{i=1}^I Y_i(1) - Y_i(0)}{I}.$$

Let N_i denote the number of municipalities that correspond to region i , then

$$Y_i(1) = \sum_{j=1}^{N_i} w_{ij} Y_{ij}(1) \text{ and } Y_i(0) = \sum_{j=1}^{N_i} w_{ij} Y_{ij}(0),$$

$$\text{where } w_{ij} = \frac{\text{Pop}_{ij}}{\text{Pop}_i} \text{ and } \text{Pop}_i = \sum_j \text{Pop}_{ij}.$$

However, $Y_i(0)$ and $Y_{ij}(0)$ are missing $\forall i, j$.

Key Assumptions

- **SUTVA**
 - **No hidden values of treatments** Broad definition of treatment: at least one municipality in the region received an intervention between 2007-2010, or not ([2]).
 - **No interference between units** Grouped close regions that received an intervention, and their neighboring municipalities to make the “no interference” assumption more reasonable.
- **Unconfoundedness** We assume we have all covariates, \mathbf{X} , such that given \mathbf{X} , treatment assignment is independent of \mathbf{Y} .
- **Missing Data** One covariate had missing values. We exactly matched on missingness pattern and Political Party in municipality before

Estimation

The control pool consists of 2213 municipalities. There are 13 treated regions considered (205 municipalities). Propensity score matching was used to identify 5 control municipalities that look like each treated ones, and estimate $Y_{ij}(0)$ and $Y_i(0)$. Let M_{ij} be the number of municipalities matched to the j th municipality in region i , and $\text{PopM}_{ij} = \sum_{k=1}^{M_{ij}} \text{PopM}_{ijk}$ is the sum of their populations. Then,

$$\hat{Y}_{ij}(0) = \sum_{k=1}^{M_{ij}} v_{ijk} Y_{ijk}(0), \text{ where } v_{ijk} = \frac{\text{PopM}_{ijk}}{\text{PopM}_{ij}}.$$

Therefore,

$$\hat{Y}_i(0) = \sum_{j=1}^{N_i} w_{ij} \hat{Y}_{ij}(0) = \sum_{j=1}^{N_i} w_{ij} \sum_{k=1}^{M_{ij}} v_{ijk} Y_{ijk}(0) = \sum_{j=1}^{N_i} \sum_{k=1}^{M_{ij}} \tilde{w}_{ijk} Y_{ijk}(0) \text{ with } \tilde{w}_{ijk} = w_{ij} v_{ijk},$$

and

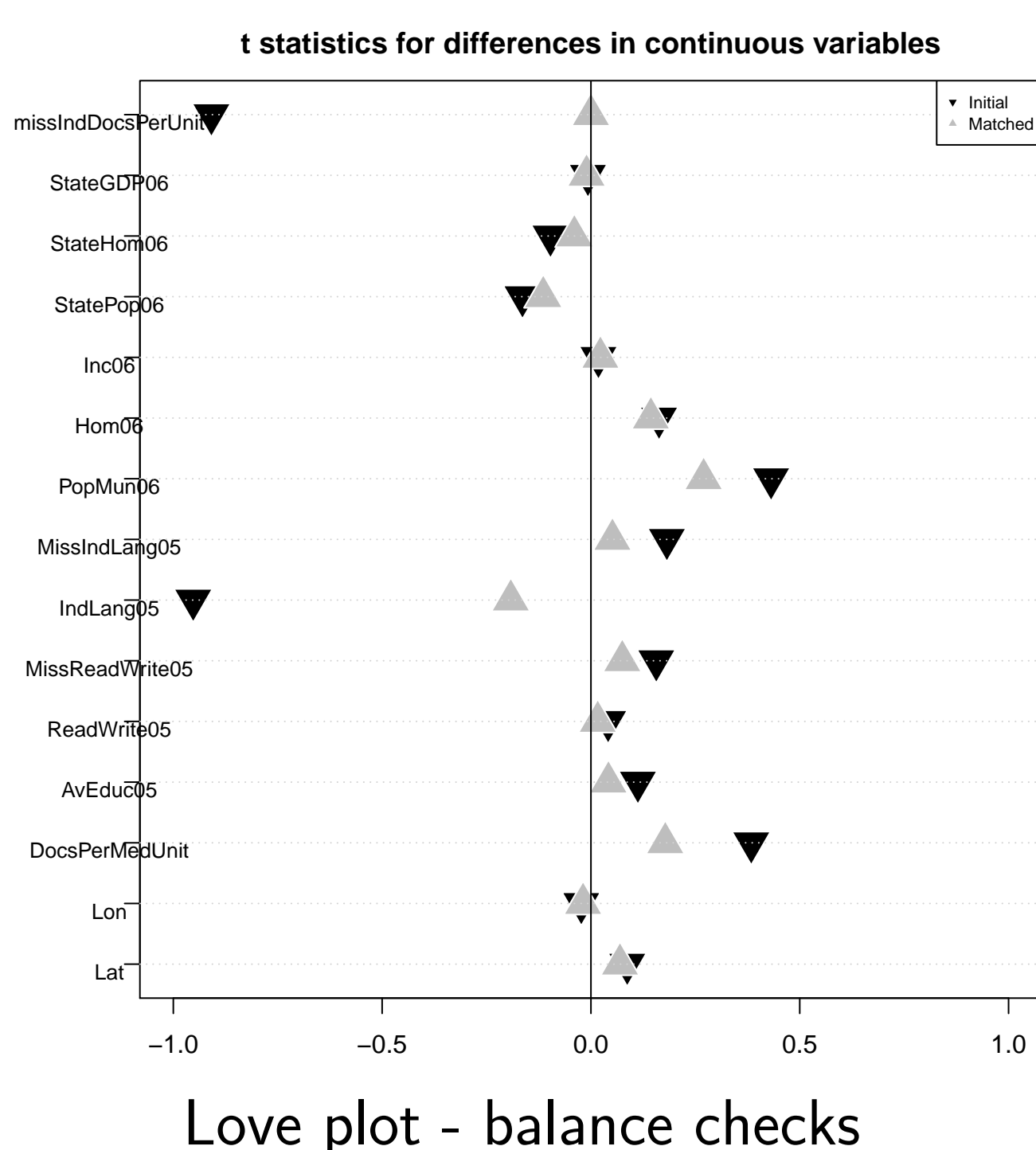
$$\hat{\tau} = \frac{\sum_j Y_j(1)}{J} - \frac{\sum_{j=1}^J \hat{Y}_j(0)}{J} = \bar{Y}(1) + \bar{Y}(0).$$

We know that $\text{var}(\hat{\tau})$ is largest under additivity of potential outcomes. In that case $\text{var}(\hat{\tau}) = \text{var}(\bar{Y}(1)) + \text{var}(\bar{Y}(0))$. We use that over estimate to get confidence intervals. Now,

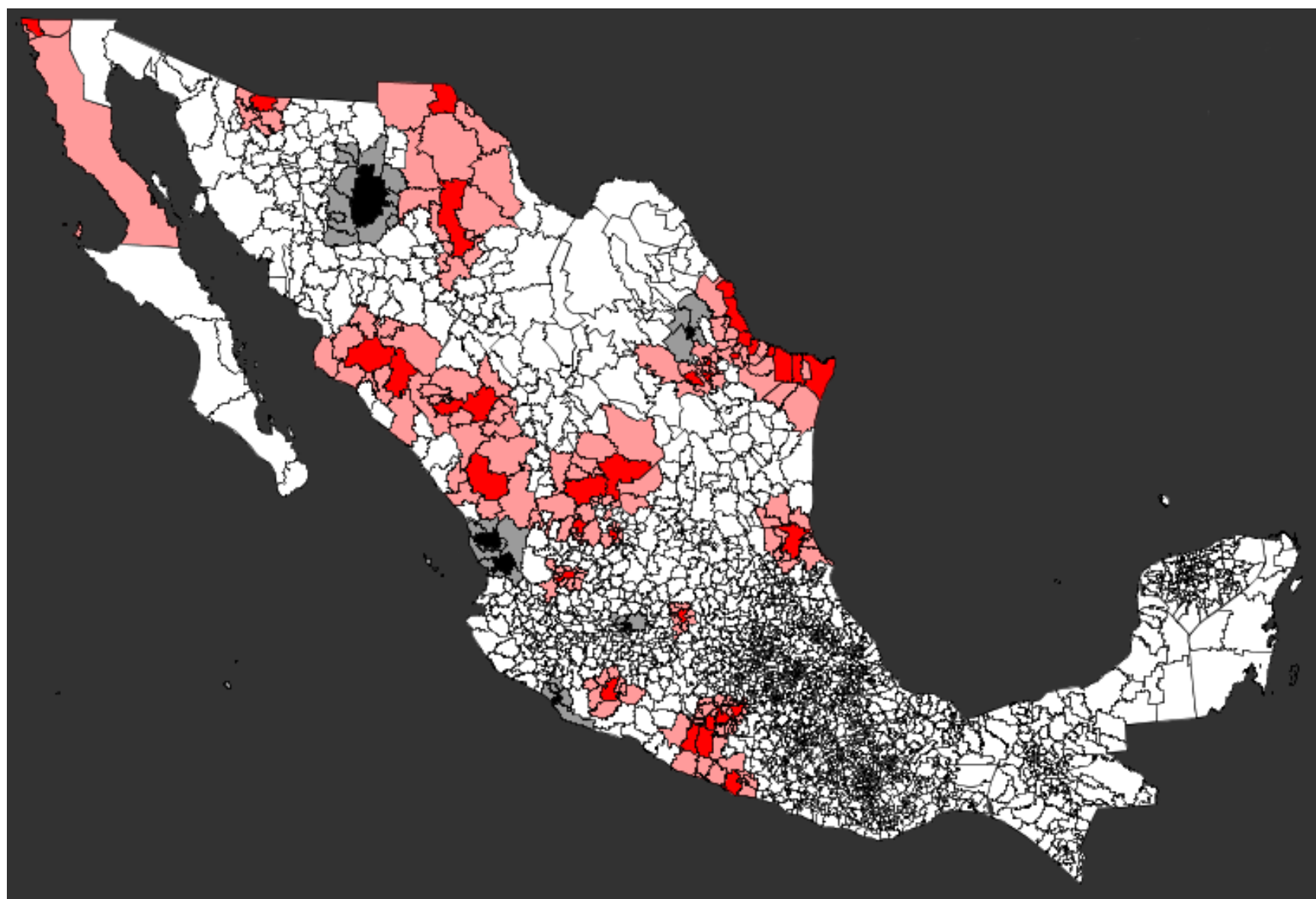
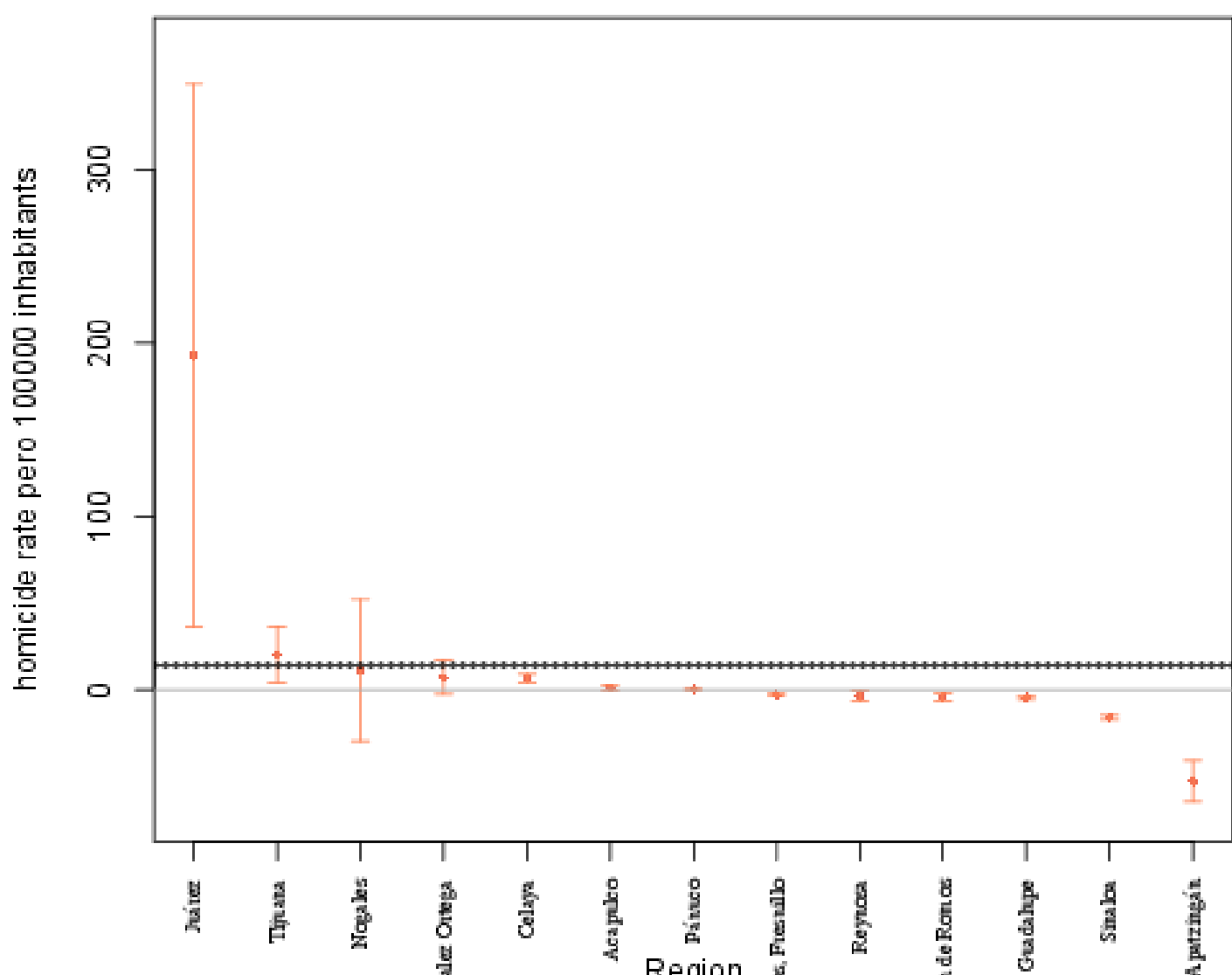
$$\begin{aligned} \text{var}(\hat{Y}(0)) &= E(\text{var}(\hat{Y}(0)|Y_i(0)\forall i)) + \text{var}(E(\hat{Y}(0)|Y_i(0)\forall i)) = E(\sum \text{var}(\hat{Y}_i(0))/I) + \text{var}(\sum_i Y_i(0))/I \\ &= E\left(\frac{\sum_{j,k} w_{ijk} (Y_{ijk}(0) - Y_i(0))^2}{1 - \sum_{j,k} w_{ijk}^2}\right) + \text{var}(Y(0))/I = \frac{\sum_{i,j,k} w_{ijk} (Y_{ijk}(0) - Y_i(0))^2}{I(1 - \sum_{j,w} w_{ijk}^2)} + S^2(0)/I. \end{aligned}$$

Now, $\text{var}(\hat{Y}(1)) = S^2(1)/I$ because the all $Y_j(1)$ are observed.

Visualization



Love plot - balance checks



Interventions and SUTVA

unit Region		number of municipalities intervention	Date of first $Y_j(1) - Y_j(0)$ (SD)
4	Juárez	15	2009 192.99 (79.88)
1	Tijuana	5	2008 20.49 (8.27)
2	Nogales	5	2008 11.41 (20.90)
10	Teúl de González Ortega	10	2009 7.32 (4.99)
15	Celaya	9	2009 6.74 (1.37)
18	Acapulco	35	2008 1.19 (0.77)
5	Pánuco	14	2007 0.37 (0.24)
9	Villa de Cos, Fresnillo	18	2008 -2.87 (0.34)
6	Reynosa	24	2008 -3.49 (1.48)
11	Rincón de Romos	8	2008 -4.10 (1.05)
8	Guadalupe	20	2009 -4.27 (0.58)
12	Sinaloa, Badiraguato, Pueblo Nuevo	27	2007 -15.84 (0.74)
16	Apatzingán	10	2007 -52.81 (5.97)
$\hat{\tau}$		205	- 14.61 (23.14)

Results

Processing

Details about processing? We're running out of room the left perhaps we can put Visualize the problem over here?

Key References & Data Source

- [1] Abadie Synthetic Matching
- [2] Escalante F, *Homicidios 2008-2009 La muerte tiene permiso*
- [3] Imbens G. & Rubin D.R., (2012)
- [4] Rubin D.R. ,*Matched Sampling for Causal Effects*,
- [5] CIDAC
- [6] INEGI
- [7] Stratfor Maps