



*Based on unstructured centroidal Voronoi  
(hexagonal) meshes using C-grid staggering and  
selective grid refinement.*

Jointly developed, primarily by NCAR and LANL/DOE

MPAS infrastructure - NCAR, LANL, others.

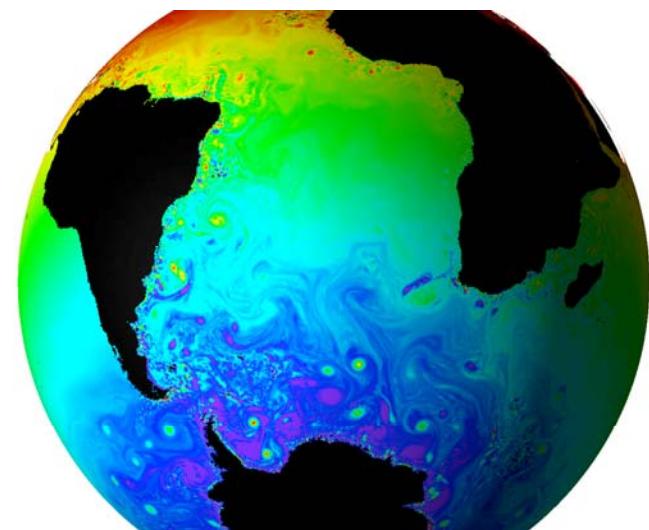
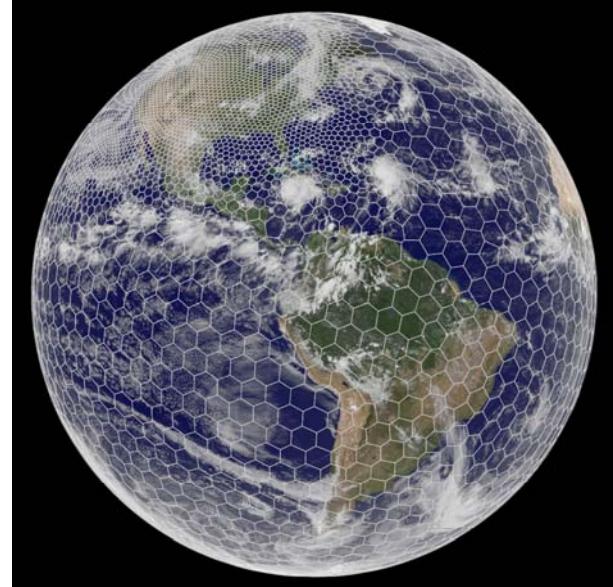
MPAS - Atmosphere (NCAR)

MPAS - Ocean (LANL)

MPAS - Ice, etc. (LANL and others)

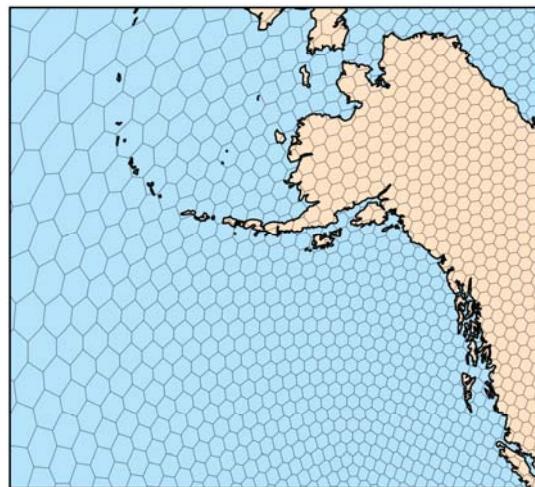
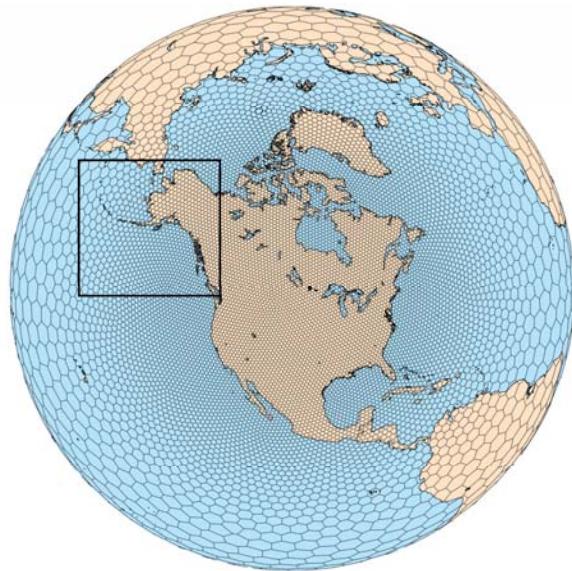
Project leads: Todd Ringler (LANL)

Bill Skamarock (NCAR)





# C-Grid Spherical Centroidal Voronoi Meshes



## Unstructured mesh

Mesh generation uses a density function.

Uniform resolution – traditional icosahedral mesh.

## Centroidal Voronoi

Mostly *hexagons*, some pentagons and 7-sided cells.

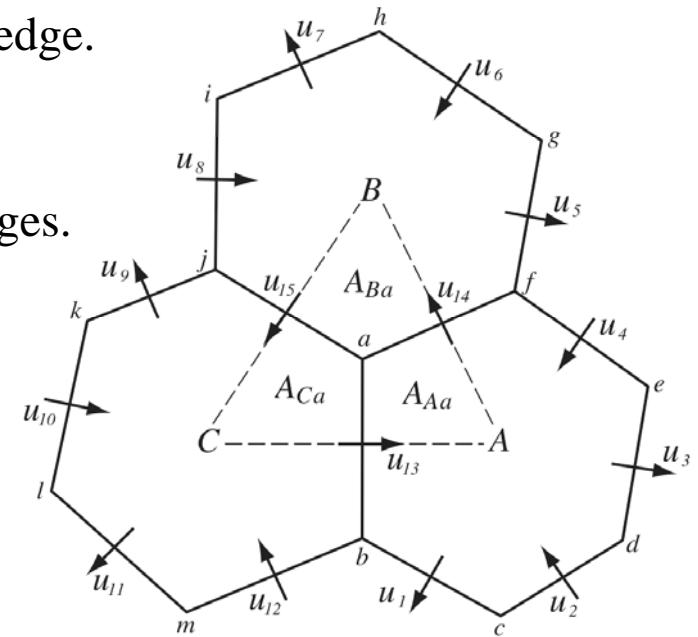
Cell centers are at cell center-of-mass.

Lines connecting cell centers intersect cell edges at right angles.

Lines connecting cell centers  
are bisected by cell edge.

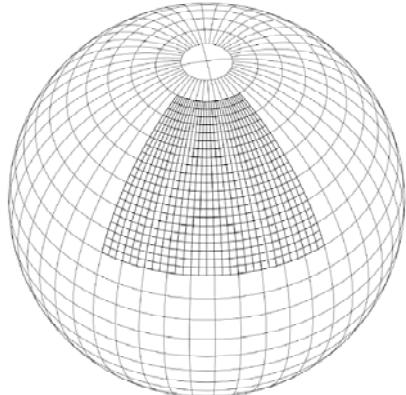
## C-grid

Solve for normal  
velocities on cell edges.

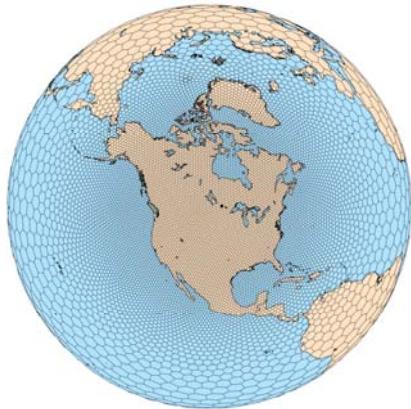




# Why Voronoi Meshes (hexagons)?



lat-long grid



Voronoi grid  
(MPAS)

## Lat-long grid issues:

Poor scaling on computers with  $O(10^4 - 10^5)$  processors because of polar filters.  
Local refinement limited to nesting or problematic coordinate transformations.

## Advantages over lat-long grid:

Scales well on MPP architectures (no poles).  
Flexible local refinement using variable-resolution grids.



# MPAS: Current Status

## Ocean (MPAS-O)

### Hydrostatic solver (MPAS-O):

*Being implemented in a CESM/CAM branch (2013).*

*Testing uniform and variable meshes.*

*Parallelization - MPI only at present.*

## Atmosphere (MPAS-A)

### Hydrostatic solver (MPAS-AH):

*Implemented in a CESM/CAM branch (2010).*

*Testing uniform and variable meshes with APE and AMIP simulations.*

### Nonhydrostatic solver (MPAS-ANH):

*NWP testing on uniform and variable-resolution meshes is underway.*

*Testing within cycling DA system (DART) has begun.*

*Year-long free forecasts are being produced for comparison with WRF-NRCM.*

*Will replace MPAS-AH in CESM/CAM in early 2013, then APE and AMIP testing.*

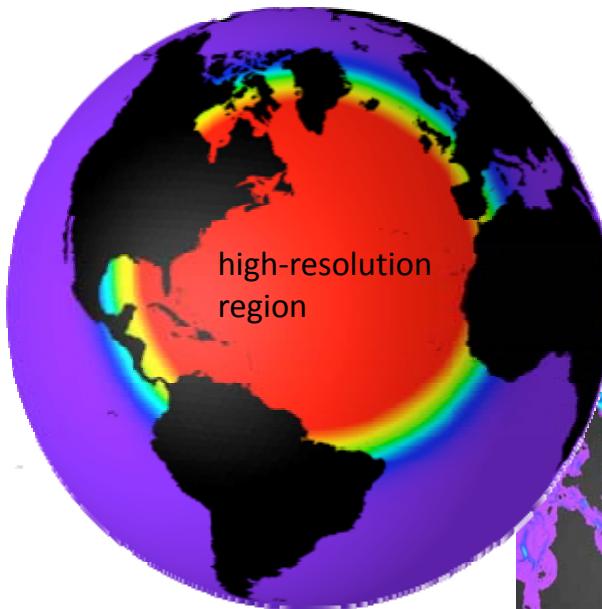
*Physics - WRF-NRCM, NCEP GFS/CFS (port in progress), CESM/CAM.*

*Parallelization - MPI only at present.*

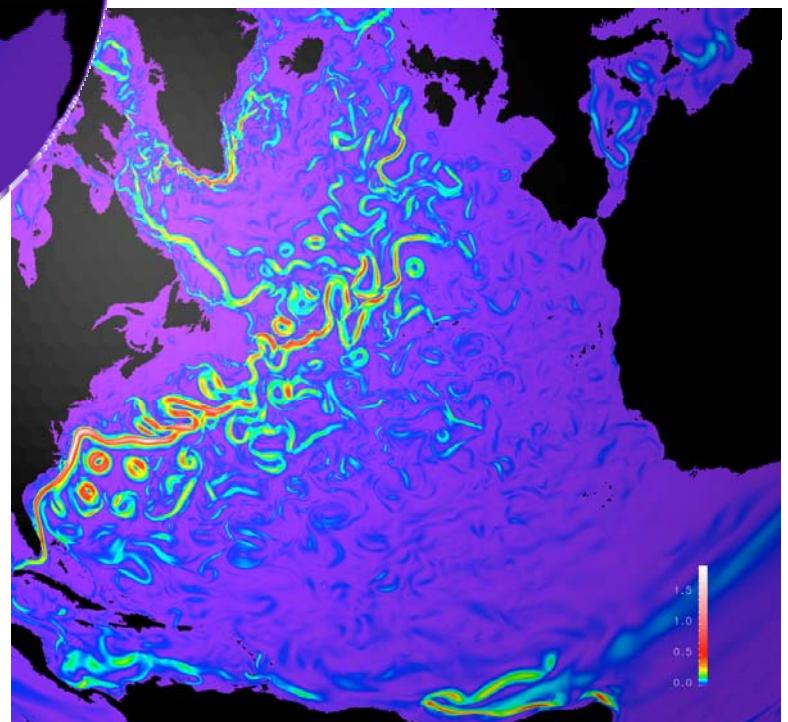


MPAS-O: hydrostatic PE solver, explicit time-split integration. Supports both quasi-uniform and variable resolution meshing of the sphere.

## MPAS-O: A Global, Multi-Scale Ocean Model

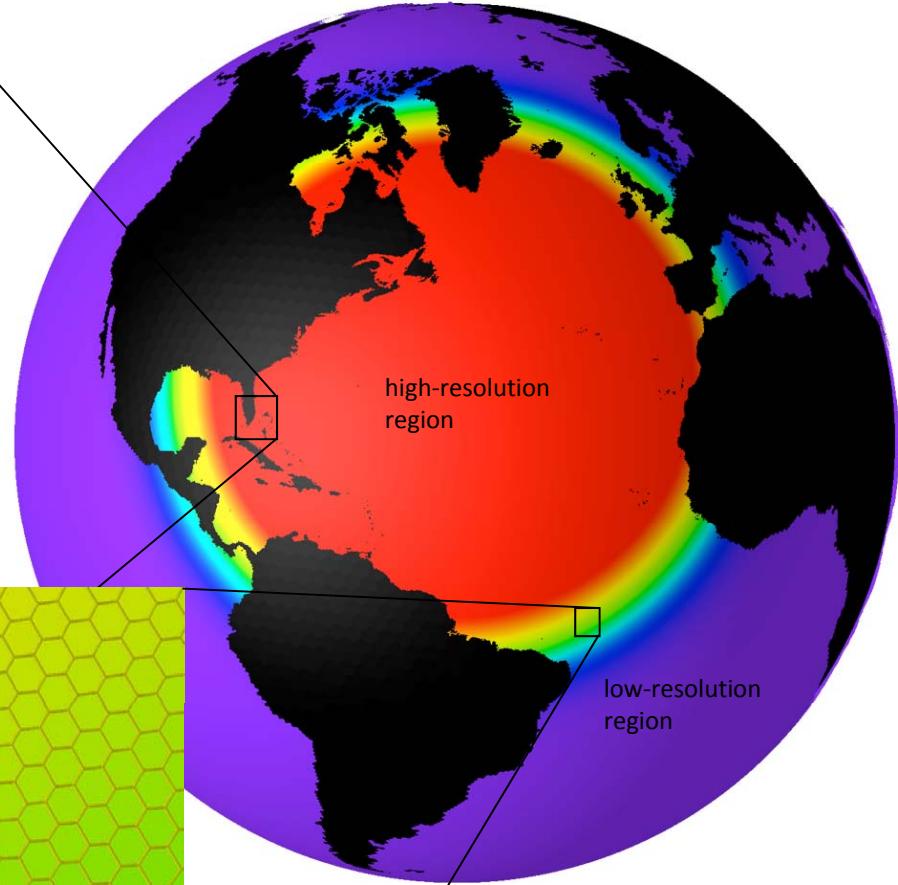
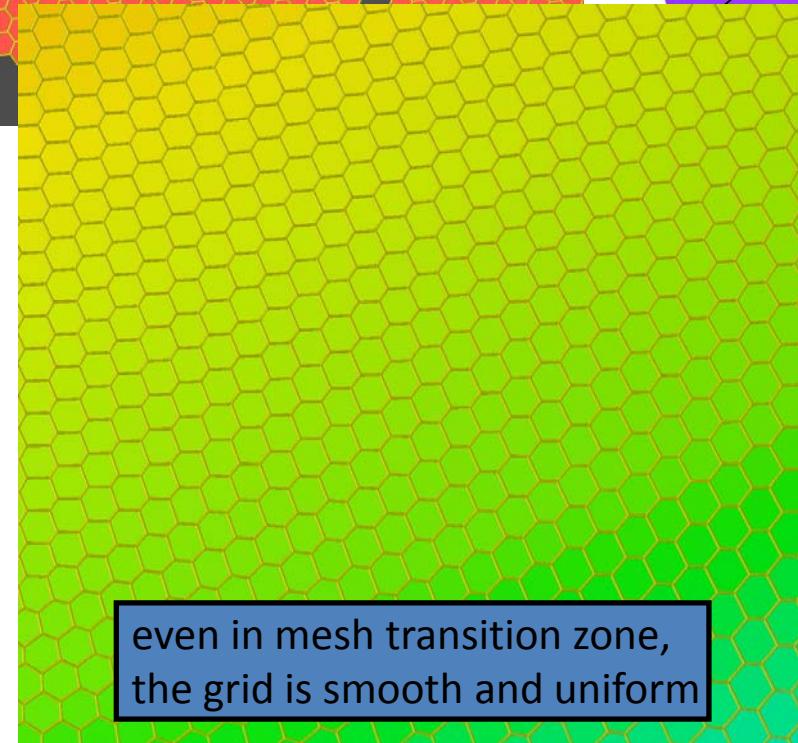
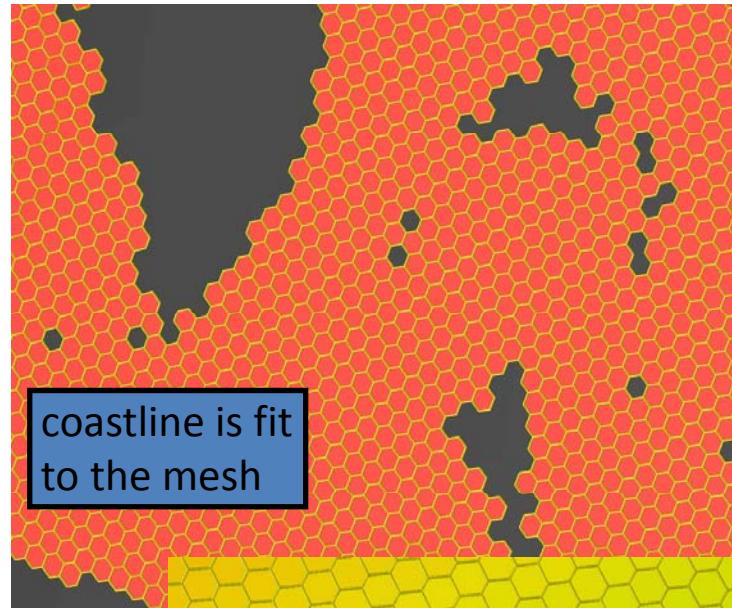


Below: Snapshot of kinetic energy from a global ocean simulation with 7.5 km resolution in the North Atlantic. The rest of the global ocean is resolved with a 38 km mesh.



### MPAS-O: Questions

1. Is it viable as a global, quasi-uniform ocean model?
2. Is the multi-resolution configuration able to reproduce aspects of its quasi-uniform counterpart?
3. Can the multi-resolution configuration produce a better climate than its quasi-uniform counterpart at a fixed cost?

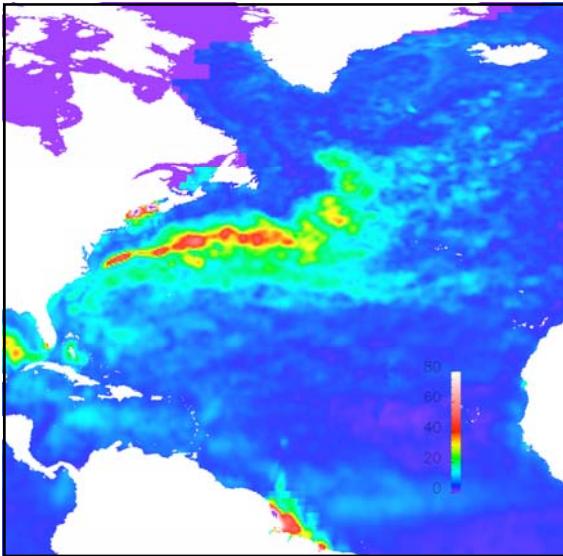


A closer look at the  
structure of the  
variable-resolution  
meshes.



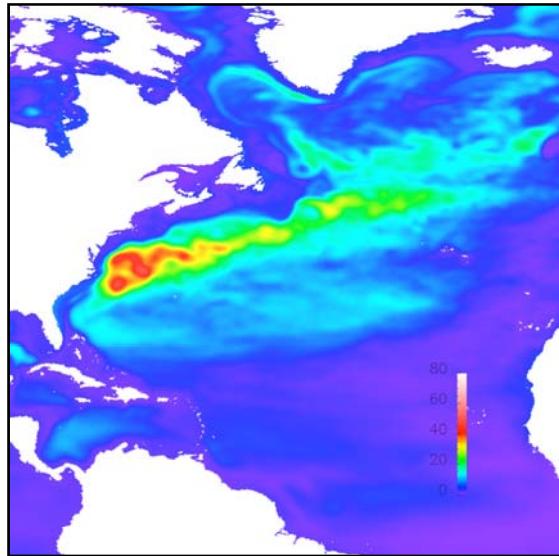
# Simulating Mesoscale Eddies on a Variable Resolution Mesh.

Observations: AVISO



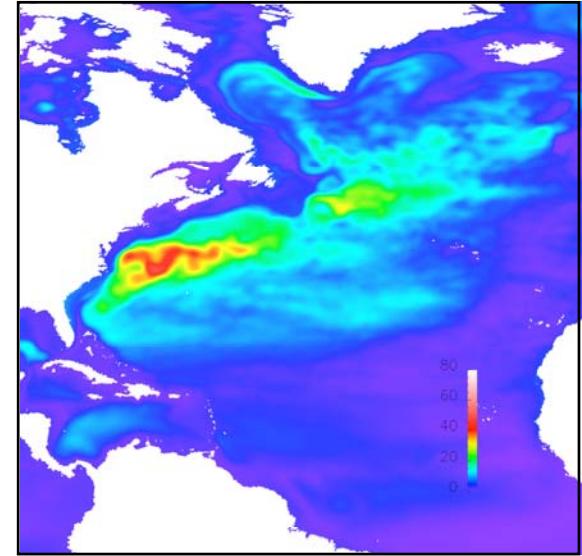
## Traditional Approach:

Global, quasi-uniform mesh  
15 km resolution everywhere



## New Approach:

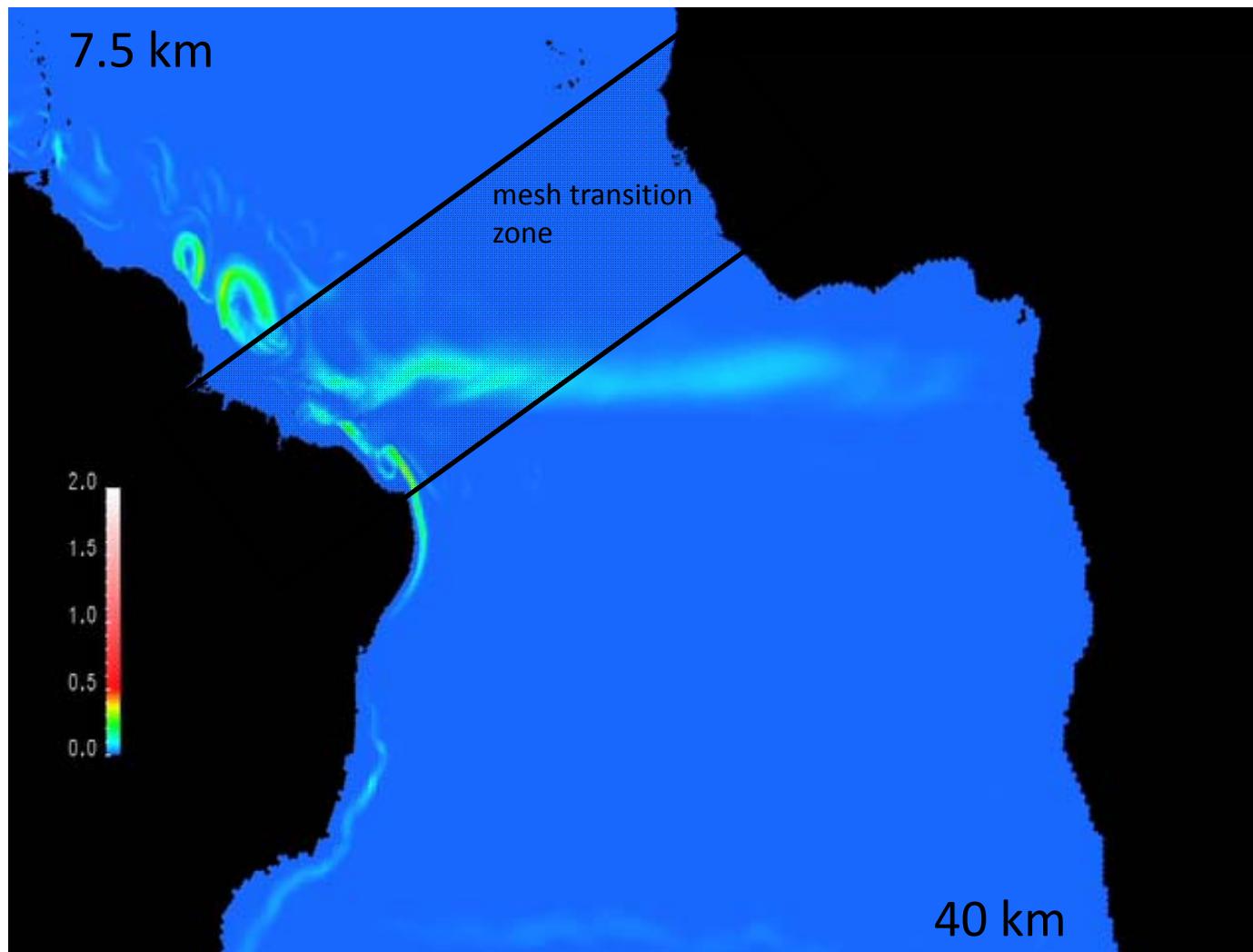
Global, variable-resolution mesh  
15 km in North Atlantic, 75 km elsewhere



Figures show sea-surface height RMS which is a proxy for the amplitude of mesoscale ocean eddies.

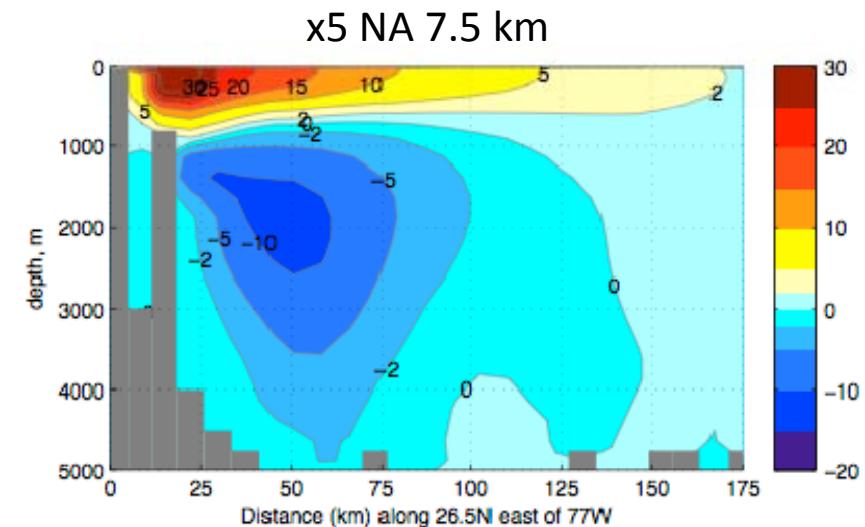
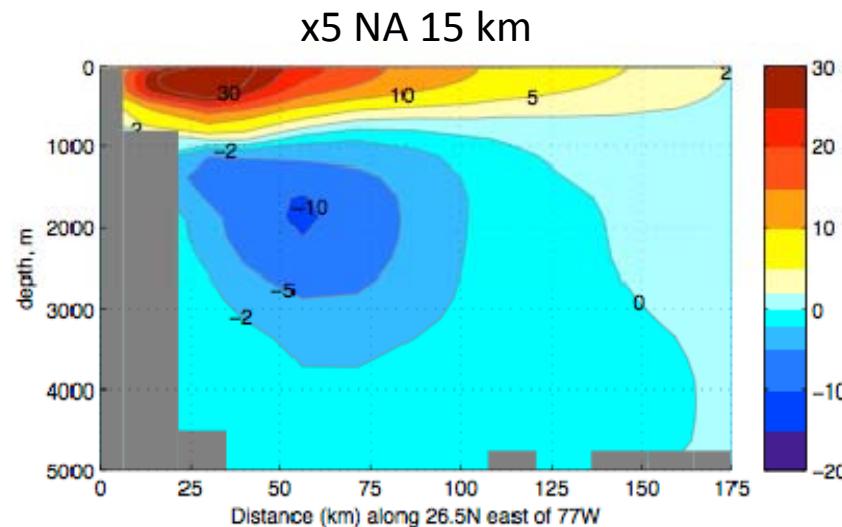
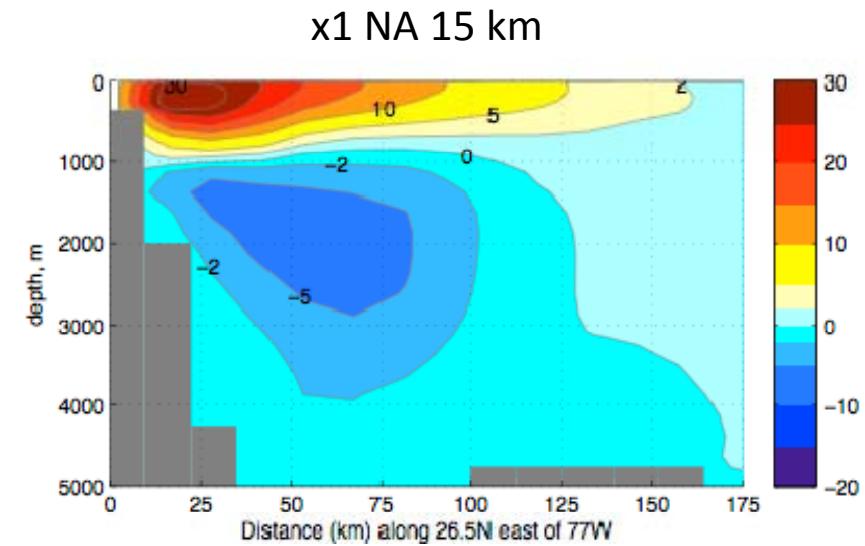
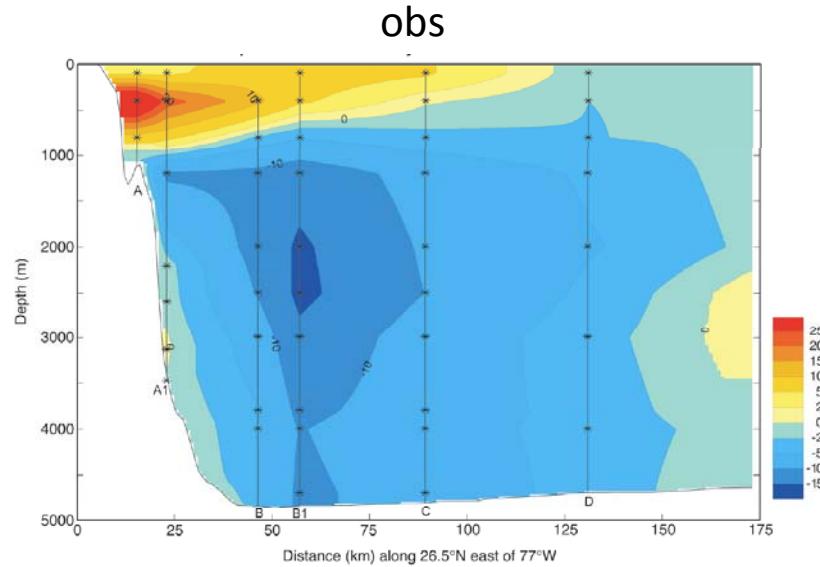
The mesoscale eddies in the North Atlantic are simulated as well on the variable resolution mesh as on the uniform-resolution mesh, but at only 15% the cost.

Retroflection of north Brazil current  
data: snapshots of KE @ 100 m depth  
movie: one frame per month for 20 years





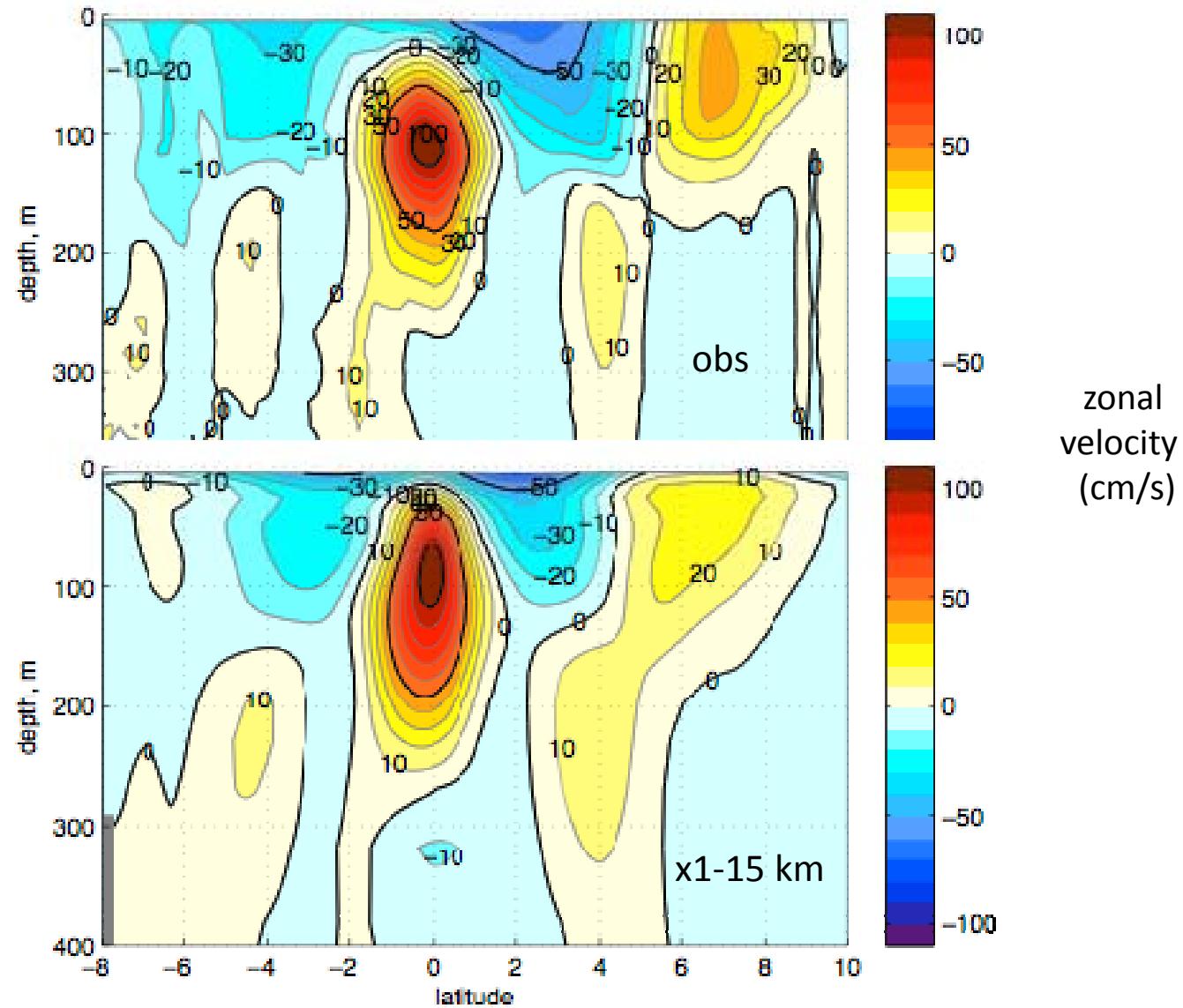
# Deep Western Boundary Current



meridional velocity (cm/s)



The equatorial currents are surprisingly accurate.





## Revisiting the three questions ....

Q: Is the quasi-uniform model viable?

(Compare [x1.15km](#) to observations.)

A: The model is competitive with its peers, e.g. the [x1.15km](#) simulation is simulating equatorial currents and mesoscale activity slightly better than the POP 1/10 degree model.

Is the multi-resolution viable at fixed resolution?

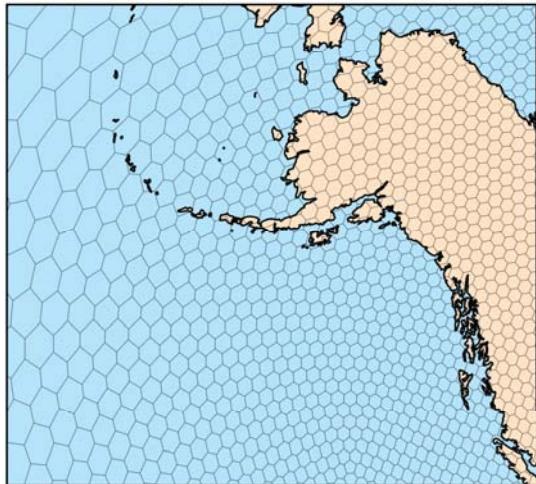
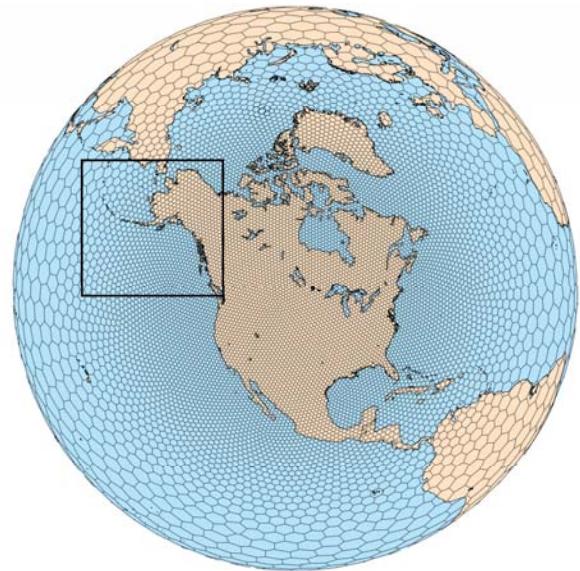
(Compare [x5.NA.15km](#) to [x1.15km](#) in North Atlantic region.)

A: Unequivocally, yes. For all practical purposes the [x5.NA.15km](#) is an exact reproduction of the [x1.15km](#) in the North Atlantic.

Q: Is the multi-resolution viable at fixed computation cost?

(Compare [x5.NA.7.5km](#) to [x1.15km](#) in North Atlantic region.)

A: Maybe. Certainly nothing got worse. Some aspect of the climate improved marginally.



# MPAS-Atmosphere

## Applications

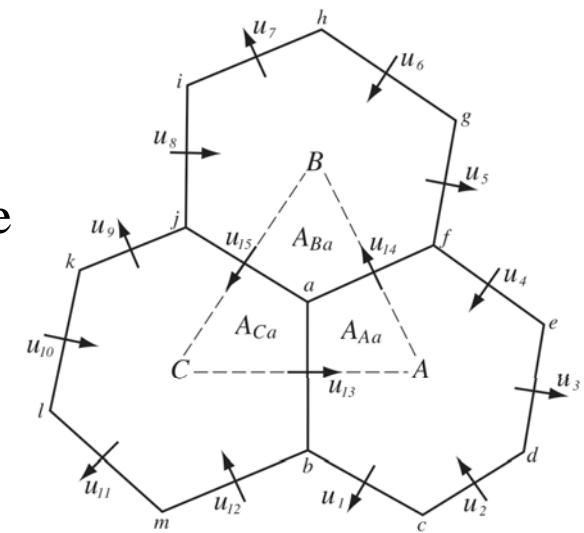
- NWP, Regional Climate and Climate

## Equations

- Fully compressible nonhydrostatic equations  
(*explicit* simulation of clouds)

## Solver Technology

- Most of the techniques for integrating the nonhydrostatic equations come from WRF.
- C-grid centroidal Voronoi mesh.
- ARW physics (Nested Regional Climate model configuration).



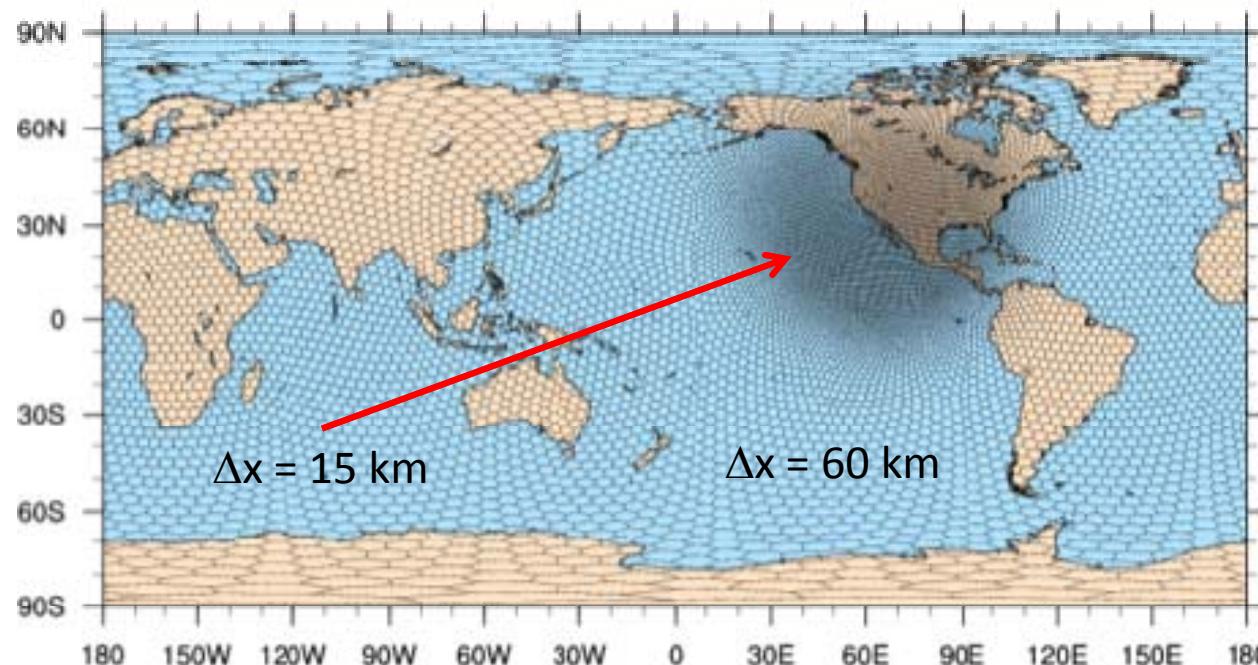


# MPAS-A Forecast Tests

Current MPAS  
Physics:

WSM6 cloud microphysics  
Kain\_Fritsch or Tiedtke convection  
Monin-Obukhov surface layer  
YSU pbl, Noah land-surface  
RRTMG lw and sw or CAM radiation.

MPAS mesh (4x finer than below), 41 levels



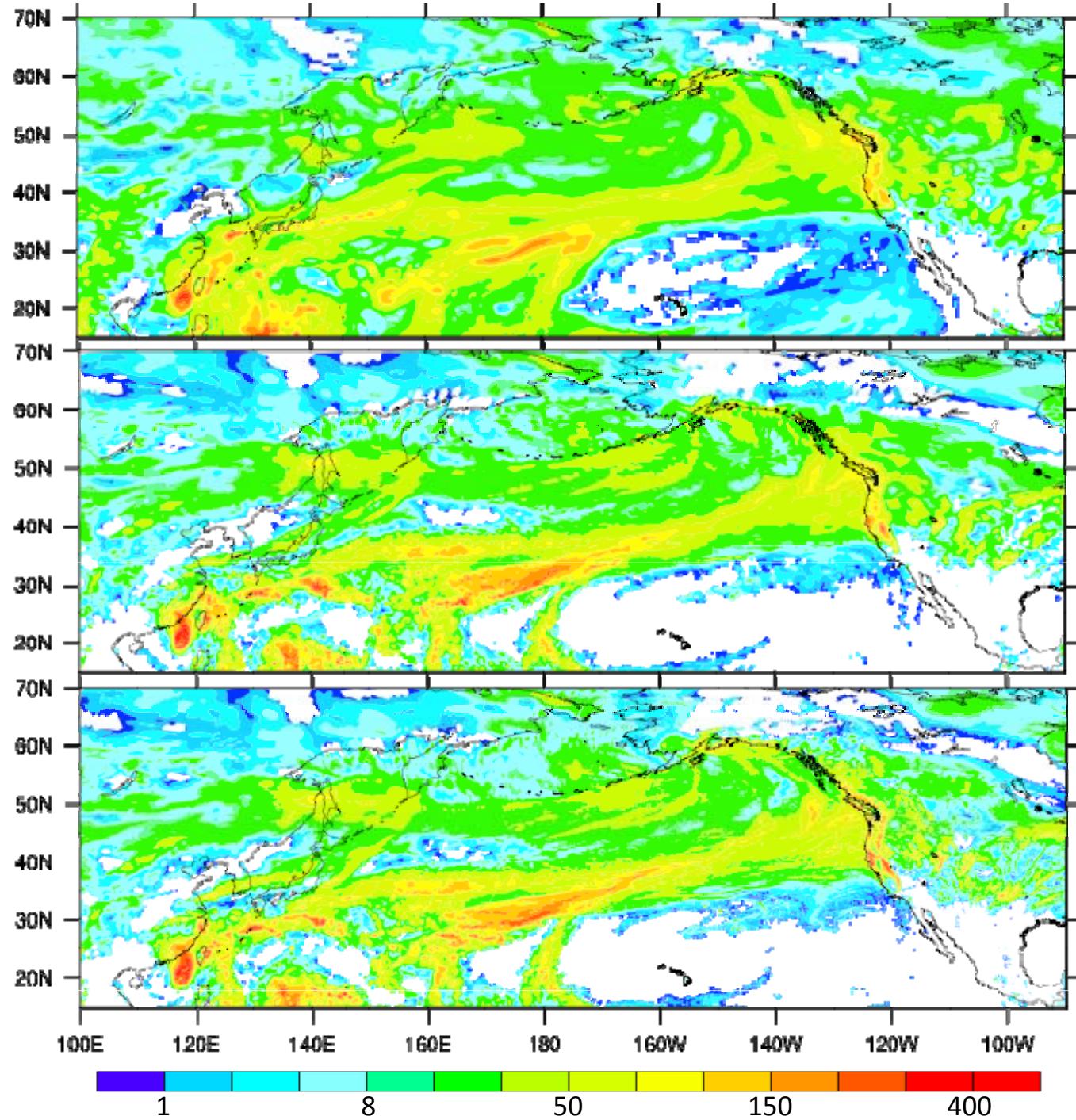
Eastern Pacific refinement

26 October 2010  
5 day accumulated  
precipitation (mm)

CFSR (~ 40 km)

MPAS-A (60 km)  
uniform resolution  
Smagorinsky

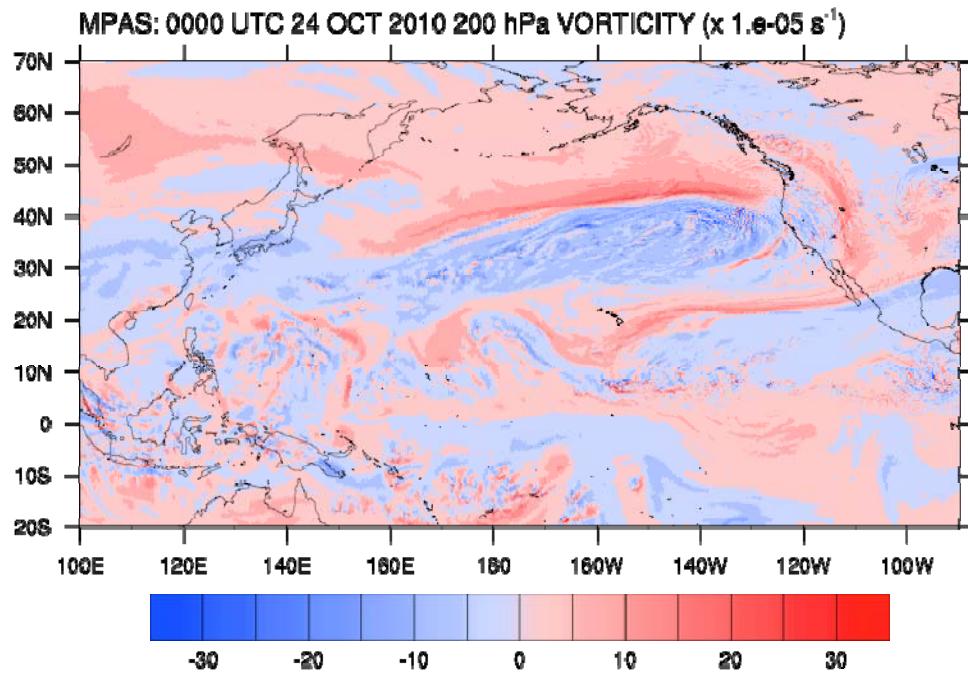
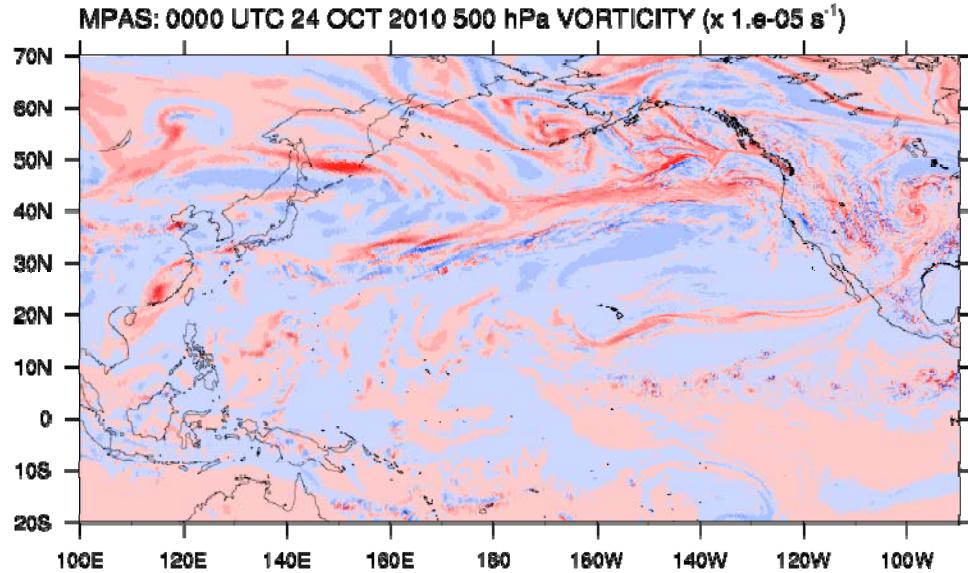
MPAS-A (60-15 km)  
variable resolution  
Eastern Pacific ref.  
Smagorinsky,  
 $(\Delta x^2$  scaling)





MPAS-A (60 – 15 km mesh)  
Eastern Pacific refinement  
21 October initialization

East-Pac mesh ( $\Delta x = 60\text{-}15 \text{ km}$ )  
Smagorinsky,  $\Delta x^2$  scaling;  
background  $K_4 = 1 \times 10^{11} \text{ m}^4 \text{s}^{-1}$   
(15 km mesh value,  $\Delta x^4$  scaling)





# MPAS-A simulations on Yellowstone

Global, uniform resolution.

6 simulations using average cell-center spacings:

60, 30, 15, 7.5 (2 - with and without convective param) and 3 km.

Cells in a horizontal plane: 163,842 (60 km), 655,362 (30 km),  
2,621,442 (15 km), 10,485,762 (7.5 km) and 65,536,002 (3 km).

41 vertical levels, WRF-NRCM physics, prescribed SSTs.

Hindcast periods:

Completed:

23 October – 2 November 2010 (60, 30, 15 – (2 conv params))

23 October – 31 October (7.5 meshes, convective param on/off)

23 October – 29 October 2010 (3 km mesh)

In progress:

27 August – 6 September 2010

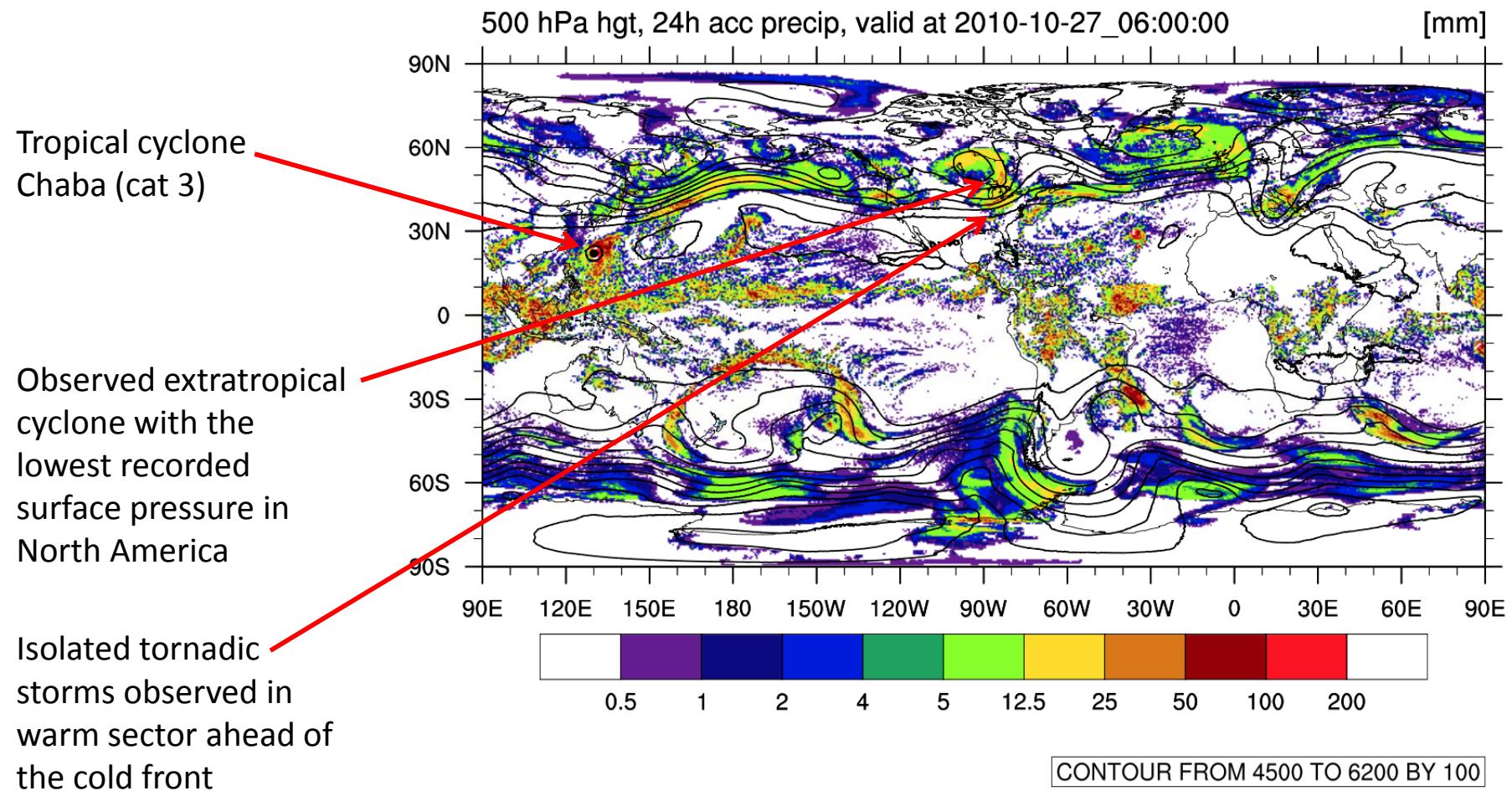
Next up:

MJO event, period TBD (after 2010 simulations complete)



# 3 km global MPAS-A simulation

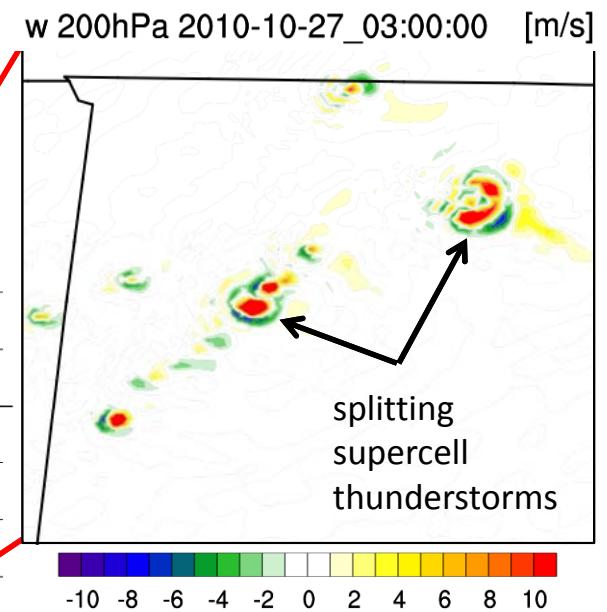
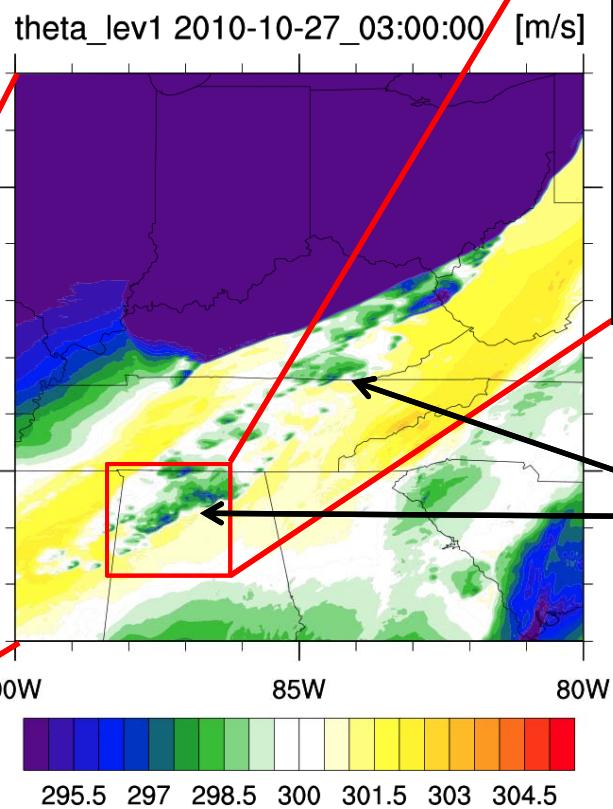
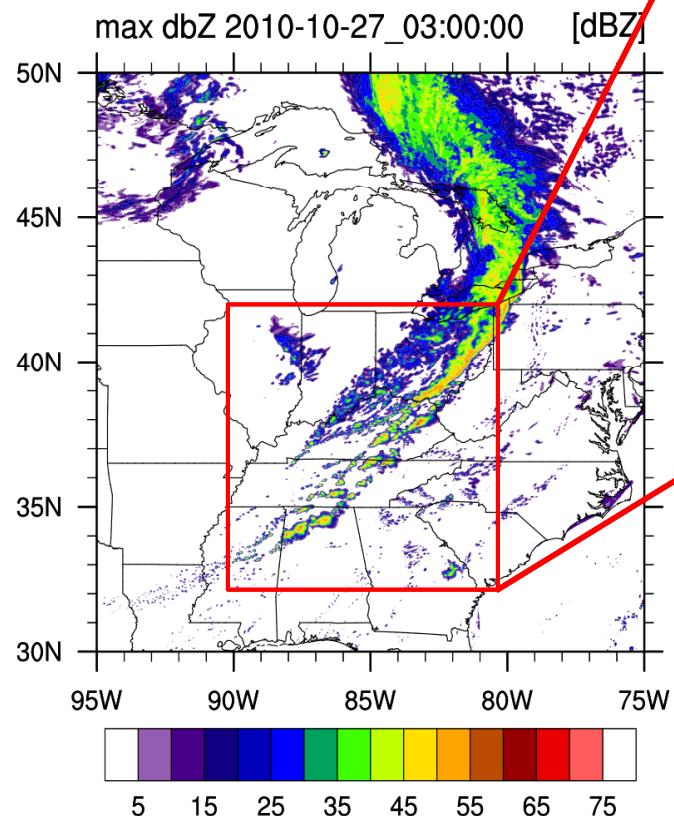
## 2010-10-23 init





# 3 km global MPAS-A simulation

## 2010-10-23 init



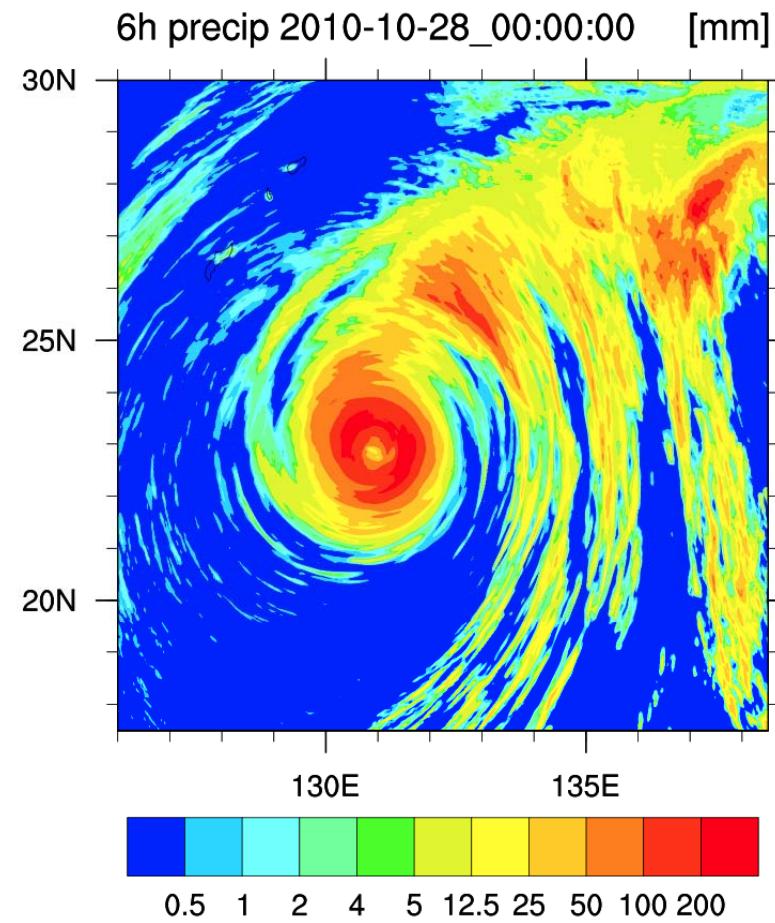
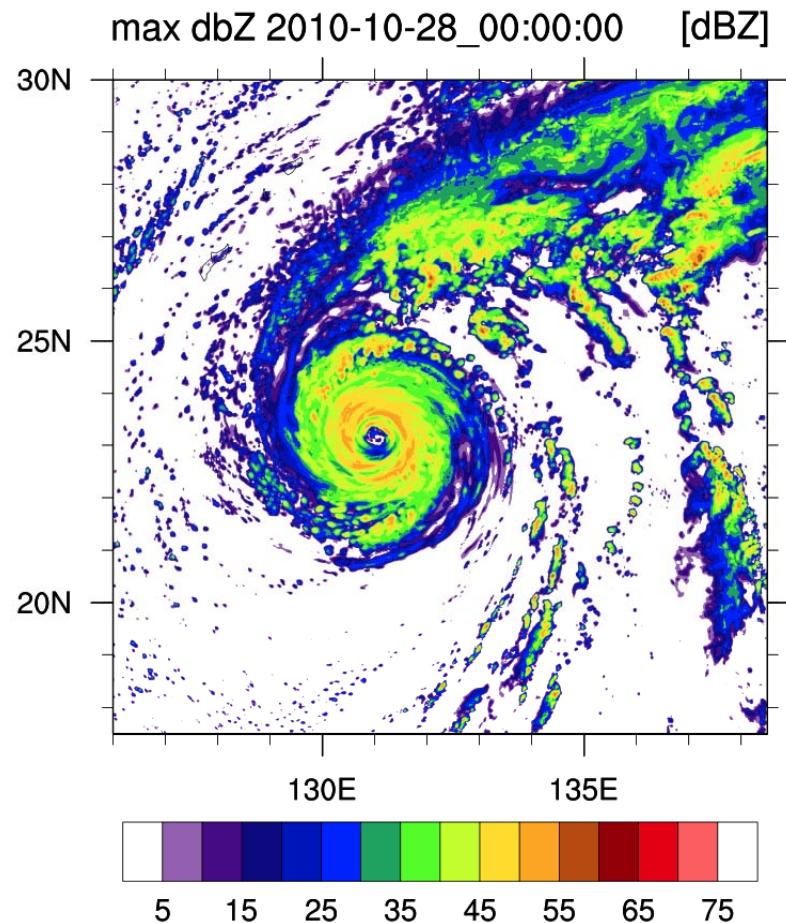
Cold-pools from isolated storms ahead of the cold front



# 3 km global MPAS-A simulation

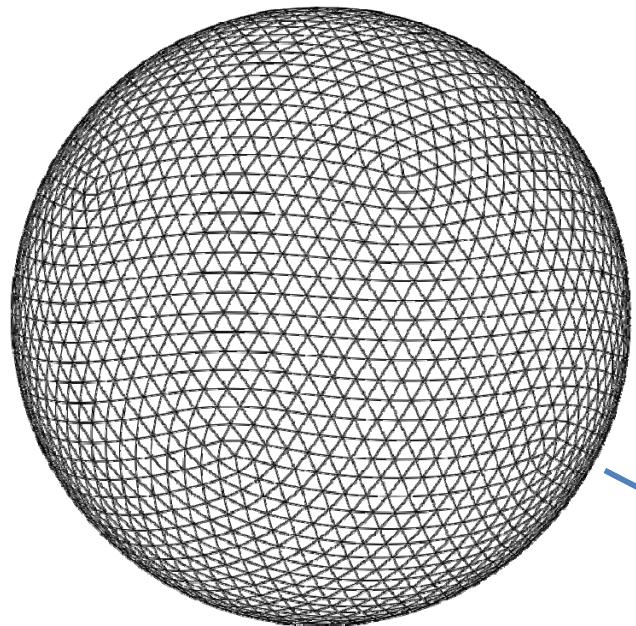
## 2010-10-23 init

### Typhoon Chaba





# Parallel decomposition



The *dual* mesh of a Voronoi tessellation is a Delaunay triangulation – essentially the connectivity graph of the cells

Parallel decomposition of an MPAS mesh then becomes a graph partitioning problem: ***equally distribute nodes among partitions (give each process equal work) while minimizing the edge cut (minimizing parallel communication)***

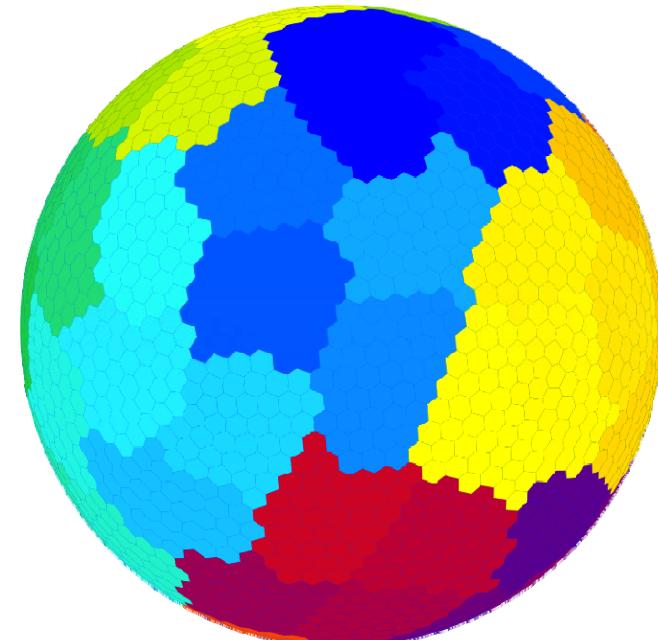
Graph partitioning

We use the Metis package for parallel graph decomposition

- Currently done as a pre-processing step, but could be done “on-line”

Metis also handles weighted graph partitioning

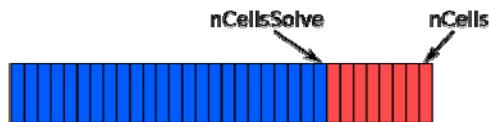
- Given *a priori* estimates for the computational costs of each grid cell, we can better balance the load among processes



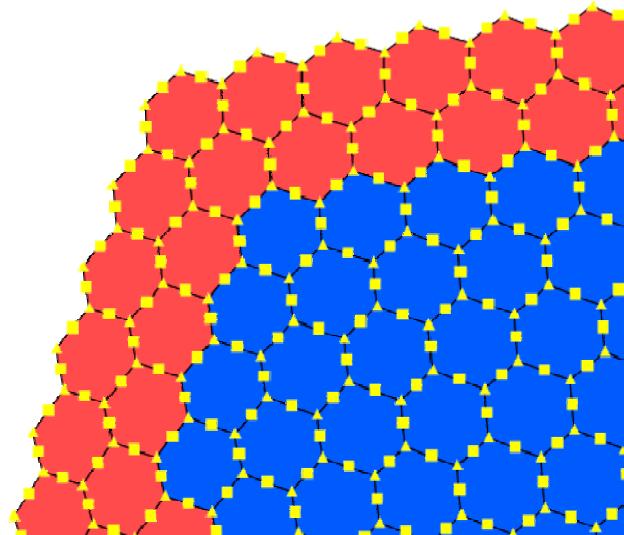


# Parallel decomposition

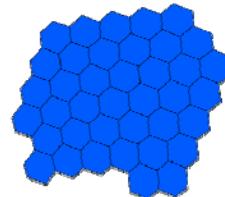
Given an assignment of cells to a process, any number of layers of halo (ghost) cells may be added



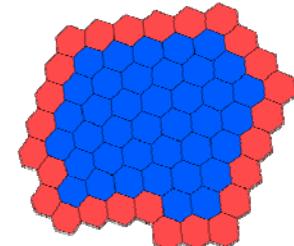
Cells are stored in a 1d array (2d with vertical dimension, etc.), with halo cells at the end of the array; the order of real cells may be updated to provide better cache re-use



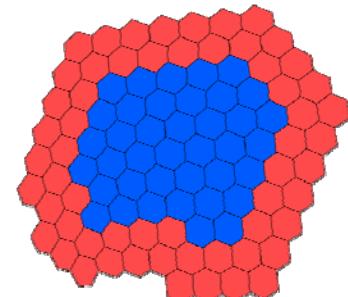
With a complete list of cells stored in a block, adjacent edge and vertex locations can be found; we apply a simple rule to determine ownership of edges and vertices adjacent to real cells in different blocks



*Block of cells owned by a process*



*Block plus one layer of halo/ghost cells*

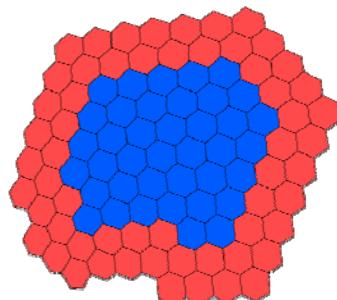


*Block plus two layers of halo/ghost cells*

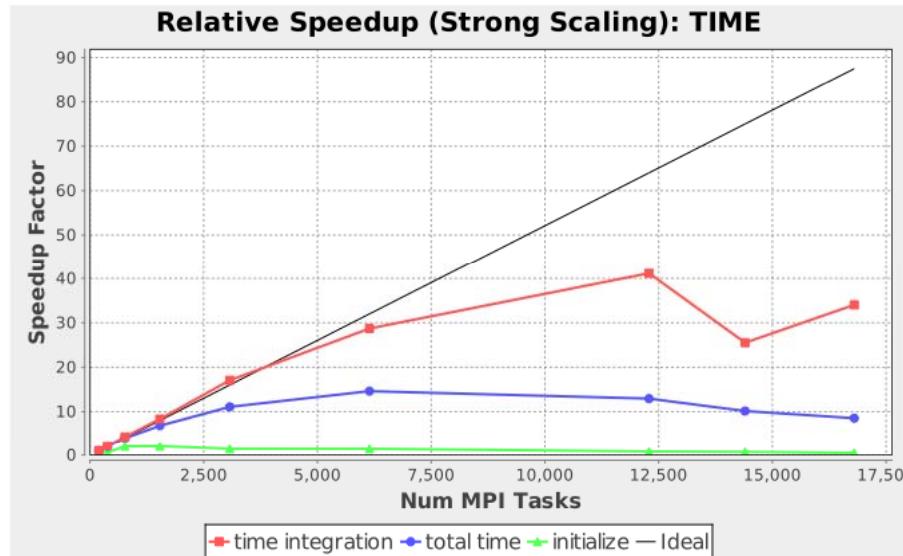


# MPAS-Ocean scaling

15 km global mesh  
(1.8M horizontal cells).  
5 simulation days.  
40 vertical levels.  
3 scalars with FCT.



*Block plus two layers of  
halo/ghost cells*

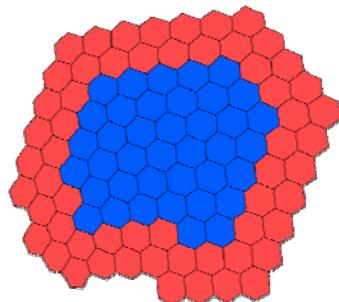


Processors	Cells Per Proc	Speed Up	Efficiency	SYPD
192	9626	1.00	100.00%	0.19
384	4813	2.19	102.58%	0.43
768	2406	4.32	107.94%	0.85
1536	1203	8.34	104.26%	1.64
3072	602	16.00	106.62%	3.35
6144	301	28.71	89.71%	5.63
12288	150	41.16	64.32%	8.11
14400	128	25.51	34.02%	5.02
16800	110	34.03	38.89%	6.70



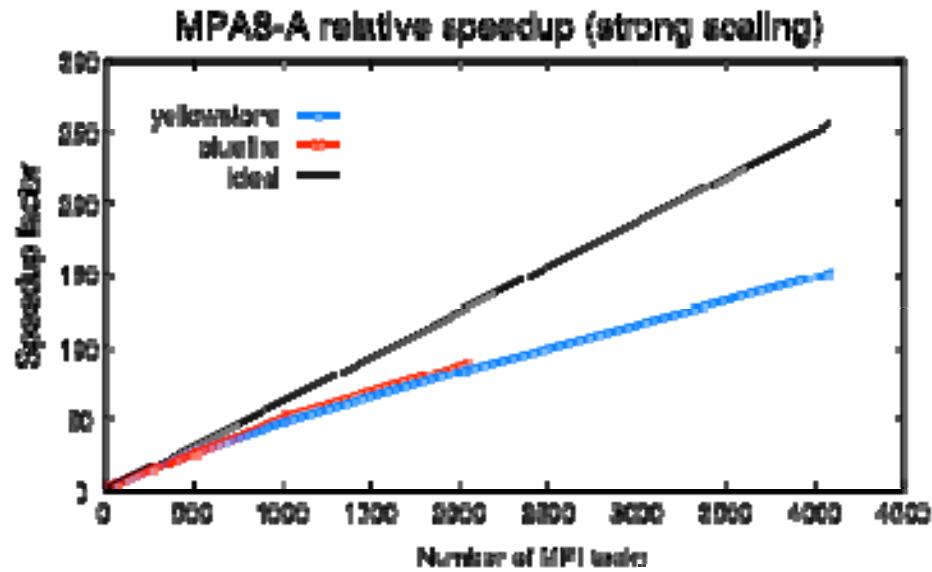
# MPAS-Atmosphere scaling

60 km global mesh  
(163,842 horizontal cells).  
6 hour simulation  
40 vertical levels.  
8 scalars with FCT.  
Full physics



*Block plus two layers of  
halo/ghost cells*

Yellowstone  
results



MPI tasks	Cells per task	Speedup	Efficiency
16	10240	1.00	100.00%
32	5120	1.97	98.40%
64	2560	3.90	97.49%
128	1280	7.67	95.88%
256	640	14.65	91.57%
512	320	27.56	86.12%
1024	160	48.49	75.77%
2048	80	85.21	66.57%
4096	40	151.43	59.15%



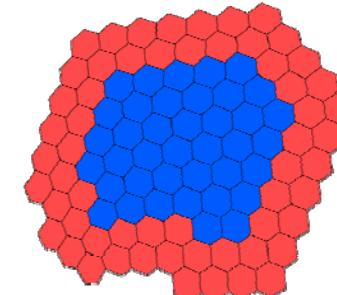
# MPAS optimizations

Communication optimizations to be implemented:

- Aggregation of same-stencil halo communications
- Overlap computation and communication
- Switch to one-sided communication?

Computation optimizations to be implemented:

- Tighter loop bounds to minimize redundant computation

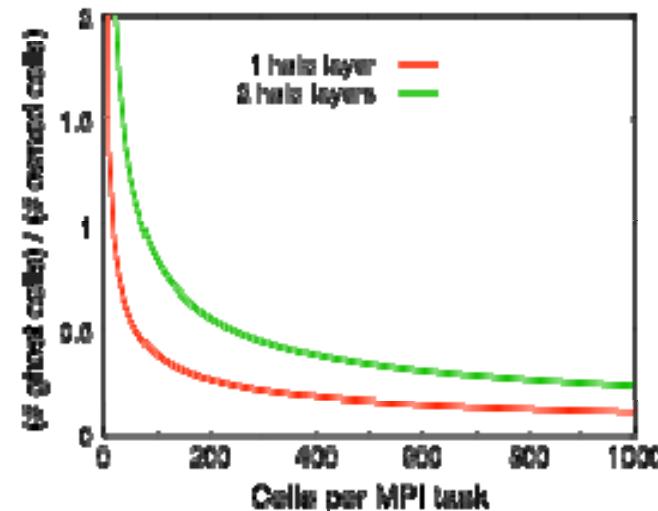


*Block plus two layers of  
halo/ghost cells*

SMP plans: (1) Multiple blocks per MPI task, (2) loop-level parallelism.

For 2 halo layers, the number of ghost (halo) cells,  $N_G$ , is approximately related to the number of owned cells,  $N_O$ , by

$$N_g = \pi \left( \sqrt{\frac{N_o}{\pi}} + 2 \right)^2 - N_o$$





# Summary

- MPAS-Ocean and MPAS-Atmosphere (nonhydrostatic) are being tested using full-physics NWP and climate tests.
- Variable-resolution capabilities of the MPAS solvers shows some promise for NWP, regional climate and climate applications.
- Initial MPI implementations of MPAS-O/A are showing efficiencies and parallel scaling similar to other NWP and ocean models.
- Much optimization work remains; we are considering some solver design changes to accommodate accelerators.
- MPAS-A: Our use of variable-resolution meshes is leading us to consider scale-awareness issues in our physics.
- Release of MPAS-O and MPAS-A is scheduled for early June 2013.

*Further information:*

MPAS-O: <http://public.lanl.gov/ringler/files/multiResolutionOceanR1.pdf>

MPAS-A: [http://www.mmm.ucar.edu/people/skamarock/mpas\\_mwr\\_2012\\_final.pdf](http://www.mmm.ucar.edu/people/skamarock/mpas_mwr_2012_final.pdf)

MPAS: <http://mpas.sourceforge.net/> (to be updated soon)





# Nonhydrostatic Atmospheric Solver

## Nonhydrostatic formulation

### Equations

- Prognostic equations for coupled variables.
- Generalized height coordinate.
- Horizontally vector invariant eqn set.
- Continuity equation for dry air mass.
- Thermodynamic equation for coupled potential temperature.

### Time integration scheme

As in Advanced Research WRF -  
Split-explicit Runge-Kutta (3rd order)

Variables:

$$(U, V, \Omega, \Theta, Q_j) = \tilde{\rho}_d \cdot (u, v, \dot{\eta}, \theta, q_j)$$

Vertical coordinate:

$$z = \zeta + A(\zeta) h_s(x, y, \zeta)$$

Prognostic equations:

$$\begin{aligned} \frac{\partial \mathbf{V}_H}{\partial t} &= -\frac{\rho_d}{\rho_m} \left[ \nabla_\zeta \left( \frac{p}{\zeta_z} \right) - \frac{\partial \mathbf{z}_H p}{\partial \zeta} \right] - \eta \mathbf{k} \times \mathbf{V}_H \\ &\quad - \mathbf{v}_H \nabla_\zeta \cdot \mathbf{V} - \frac{\partial \Omega \mathbf{v}_H}{\partial \zeta} - \rho_d \nabla_\zeta K - eW \cos \alpha_r - \frac{uW}{r_e} + \mathbf{F}_{V_H}, \\ \frac{\partial W}{\partial t} &= -\frac{\rho_d}{\rho_m} \left[ \frac{\partial p}{\partial \zeta} + g \tilde{\rho}_m \right] - (\nabla \cdot \mathbf{v} W)_\zeta \\ &\quad + \frac{uU + vV}{r_e} + e(U \cos \alpha_r - V \sin \alpha_r) + F_W, \\ \frac{\partial \Theta_m}{\partial t} &= -(\nabla \cdot \mathbf{V} \theta_m)_\zeta + F_{\Theta_m}, \\ \frac{\partial \tilde{\rho}_d}{\partial t} &= -(\nabla \cdot \mathbf{V})_\zeta, \\ \frac{\partial Q_j}{\partial t} &= -(\nabla \cdot \mathbf{V} q_j)_\zeta + \rho_d S_j + F_{Q_j}, \end{aligned}$$

Diagnostics and definitions:

$$\theta_m = \theta [1 + (R_v/R_d)q_v] \quad p = p_0 \left( \frac{R_d \zeta_z \Theta_m}{p_0} \right)^\gamma$$

$$\frac{\rho_m}{\rho_d} = 1 + q_v + q_c + q_r + \dots$$