

Binary Search

- ① Implement lower bound
- you're basically finding the lowest index with value greater than or equal to X
 - So just divide the whole array 2 for mid if mid value is greater than or equal to X store that as ans for now
 - then decrease the search space to left since it can only be less than mid
 - only if $X > \text{mid}$ then decrease search space only for right half

- ② upper bound - same as lower bound but index value should be greater than X

- ③ Search insert position of X
- basically you just have to insert X in lower bound position.

//_

⑤ Floor - Find the largest number in the array
i.e. less or equal to x

- So check with midpoint if mid is greater than x there might be elements ahead of mid that is smaller or equal to x .

⑤.1 ~~5.1~~ Ceil - Find the smallest number in the array
i.e. greater or equal to x .

- Check with midpoint if mid is $\leq x$ then there might be smaller elements on left so check left.

⑥ Find first & last occurrence of x
(i.e. starting index of x & ending index)

- Binary search
- if $arr[mid] = x$
 - ↳ first index will be on left of mid
So reduce search space to 1st half
 - if $not = mid$ then look for in either halves
 - ↳ last index will be on right of mid
So reduce search space to second half

⑦ find total occurrence

- find first & last occurrence & do
 $last - first + 1$ will give total count.

⑧ Search element in rotated sorted array

- basically first divide the array and check if mid is the element target
- if not now check if left half array is sorted if yes then ~~check~~ check if target lies in left half & reduce search space to left half
- else if right half is sorted check if target lies in right half & decrease ~~search~~ search space
- if element doesn't exist in both halves return -1.

⑨ Search element in rotate sorted array but it has Duplicates

- Same logic as previous one but
- but just skip over duplicates by checking if ~~low~~ mid & high are equal.

(10) Find minimum in rotated sorted array

- # - first check which half is sorted then get the minimum from that half
- then check for the other ~~half~~ half & get the minimum there
- finally return the minimum.

(10) Ex 1.1 use this minimum & how many times array rotated.

- # - start by keeping min index = 0
- # - Basically 1st check which half is sorted
- then in that sorted half compare the min value i.e $arr[low] < arr[mid]$ or $arr[mid] < arr[high]$
- if you find the minimum then update the index
- then discard that half
- then finally return the index or $arr[index]$.

1 2 3 4 5

0 1 2 3 4

3 4 5 1 2

this has been rotate
3 times which is min index

①P

Search Single element in sorted array

- basically using binary search you have to check which half the missing element lies on
- i.e by checking the pattern
- when mid is odd reduce it to even & check even odd pair if its equal then element is before mid are in Even odd pattern so reduce space to left half
- if its not equal then ~~pattern~~ even odd pattern has been broken & single ele lies on left
so $high = mid$
- & finally return $arr[low]$.

E	O	E	O	E	O	E
0	1	2	3	4	5	6
1	1	2	3	3	4	4

⑩

Single element in a sorted array

- While runs from low to high ($low \leq high$)
cuz when $array[mid] = low$ or $high$
i.e if $a[mid] = 0$ or $n-1$ the execution will stop
or like if $low = high$ execution stops
cuz that point will be the single element.
- you find the midpoint
- now if mid is odd you reduce mid to prev index ($mid--$) making it even & you check if even = odd place - if this is true that means the even odd pairing hasn't been disrupted till mid point so single element will be on right part of mid (so do $low = mid + 2$)
- else if when mid is odd & you reduce mid to even & check if even = mid & if it's not equal that means the even odd pattern is disrupted already & the single element is on left half
- & finally when $low = high$ return $arr[low]$.

E O (E) O E O E O E
1 1 (2) 3 3 4 4 5 5

Pattern break ← E O E O (E) O E
2 2 3 3 (4) 5 5

↓
Pattern break