

Recursion

① 1 to N

- 1- get a number N
- 2- base case - run the loop till $n=0$
- 3- keep calling the function ~~for~~ by doing $n-1$
- 4- Print n

basically in every recursive call you're first executing 3rd step & pausing which keeps happening till $n=0$ where it returns back to calling function i.e. ~~f(5)~~ $f(1)$ where $n=1$ moves to next step prints 1

ex: $N=5$ $f(5) \rightarrow f(4) \rightarrow f(3) \rightarrow f(2) \rightarrow f(1) \rightarrow f(0)$
5 4 3 2 1

② N to 1

with the above same condition
if you place cout before calling it starts printing from n to 0.

//_

③ Sum of N $\left(\frac{n(n+1)}{2} \right)$ if no rec

1. base case if $N = 0$ return 0

2. $Sum = n + func(n-1)$

ex: $n = 5$

~~$$5 = 5 + f(4) - 4 = 9$$~~

~~$$9 = 4 + f(3) - 3 =$$~~

~~$$3 + f(2) - 2 =$$~~

~~$$2 + f(1) - 1 =$$~~

~~$$1 + f(0) - 0 =$$~~

ex: $n = 5$

$$f(5) = 15$$



$$5 + f(4)10 = 5 + 10 = 15$$

$$4 + f(3)6 = 4 + 6 = 10$$

$$3 + f(2)3 = 3 + 3 = 6$$

$$2 + f(1)1 = 2 + 1 = 3$$

$$1 + f(0)0 = 1 + 0 = 1$$

here the base case is till 0 if 0 then return 0
and $Sum = n + f(n-1)$ what it does is basically
add the current function's n to the previous number
like it goes up to $f(0)$ & returns 0 for $f(0)$

$$f(1)$$



$$n = 1$$

$$1 + f(1-1)f(0)$$

then add $1 + 0$

& the sum is $f(1) = 1$

④ Factorial

Just like the previous steps you're multiplying the current n with the result of the previous multiplied n & $n-1$

but base case till 1 if 0 return 0.

ex: $n=3$

$f(3)$

$$3 \times f(2) \rightarrow 3 \times 2 = 6$$

$$2 \times f(1) \rightarrow 2 \times 1 = 2$$

↓

return 1

⑤ Reversing the array

- Get the input array
- call the function by sending (arr, size, start, end)
- base case ($start \geq end$)
- ~~call the recursive function by increasing start and decreasing end~~
- swap start & end
- then call recursive function by moving start & end inwards
i.e. ($start+1, end-1$)
- and swap again till base case.

⑥ Palindrome string

- 1- get a string
- 2- get the size of the string

basically just like with array you keep 2 pointers for start & end when index comes to midpoint then its a palindrome cuz you compare start & end if its the same char you move ahead or you just return false

but comparing can be done in 2 ways.

- one is by calling start & end by assigning $s[0]$ to start $\rightarrow \text{Pali}(s, \text{start}+1, \text{end}-1)$
 $s.size()-1$ to end

- another is just passing i
 $\text{Pali}(s, i) \rightarrow \text{if } (s[i] \neq s[s.size()-i-1])$
 $\text{Pali}(s, i+1)$

⑦ finding n^{th} fibonacci

using recursion

basically you're getting running the recursion loop till $n \leq 1$ once it gets there return 0 or 1

& for calling the function its last & second last
ex: $n = 5$ 5th Fib number is 5

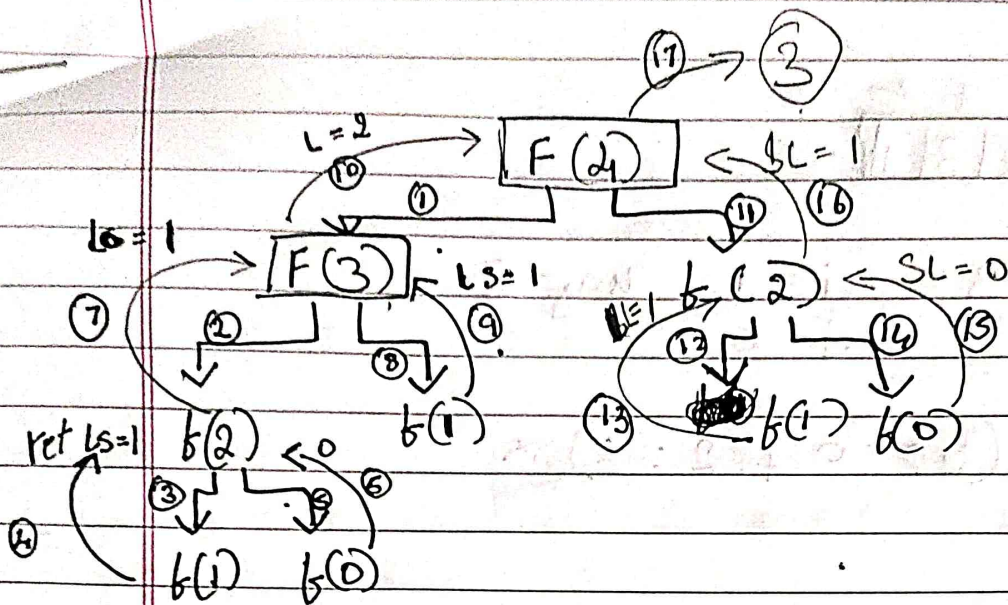
0, 1, 1, 2, 3, 5
 ↓ ↓
 slast last

So $n - 1 = \text{last}$

$n - 2 = \text{slast}$

So goes down till 0 & 1 and starts adding up from there

and finally return $\text{last} + \text{slast}$



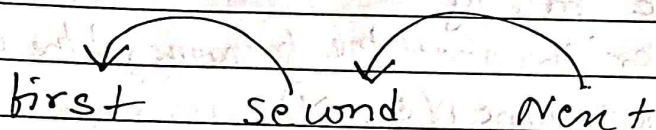
$$i = 4, j = 4$$

using for loop to find N^{th} fib

basically three variables for.

first = 0	}	first = 1
second = 1		second = 2
next = 2		next = 3

first second next



~~1st~~ 1st + 2nd = next

1st = 2nd

2nd = next

} this order cuz
if it is like 2nd = next
then 1st = 2nd

then 1st will also get next's
value which is in 2nd.