

## Introduction to Augmented Reality

### Exercise 4 (P,H) Thresholding

In order to detect monochrome markers in the camera image, we first convert the color image into a white-and-black image.

- (a) First, convert the camera image to a grey image by `cv::cvtColor`, as the thresholding algorithms work only with grey images. `cv::cvtColor` requires a conversion type—`CV_BGR2GRAY`, indicating from color to gray scale.
- (b) Two thresholding functions exist: `cv::threshold` and `cv::AdaptiveThreshold`. Try both methods and show the result in a new window. For `cv::threshold`, create a slider using `cv::createTrackbar` to easily change the thresholding parameter.
- (c) Experiment with the parameters. Choose parameters such that the markers are clearly visible under all lighting conditions and viewing angles. They should have a continuous frame which does not merge with the environment.
- (d) Briefly describe the advantages and drawbacks of both thresholding algorithms.

### Exercise 5 (P,H) Finding Rectangles

In the last exercise, you have generated a thresholded black-and-white image.

- (a) Expand your program using the functions `cvFindContours` and `cvApproxPoly` to first extract object boundaries and then approximate these with straight line segments. Hint: for the second-to-last parameter of `cvApproxPoly`, try a value of `cvContourPerimeter(contours) * 0.02`. Note: `cvFindContours` uses the OpenCV heap. Use `cvCreateMemStorage`, `cvClearMemStorage` and `cvReleaseMemStorage` to manage it.
- (b) Traverse all found contours and determine each bounding box using `cv::boundingRect`. Skip all polygons with more or less than 4 corners or too small bounding boxes (experiment with constraint values). Use `cv::cvarrToMat` for converting (`CvSeq*`) to (`cv::Mat`).
- (c) Mark the rectangles you have found with red lines using `cv::polylines`. Do this in the original camera image and display it afterwards.
- (d) Subdivide each edge of the rectangles into 7 parts of equal length and draw a small circle around each of the dividing points. You will need these in the next exercise.

**Exercise 6 (H) Cross Product**

- (a) What is the definition of a Cross Product of two vectors?

$$\vec{a} \times \vec{b} = \vec{n}$$

The cross product  $\vec{a} \times \vec{b}$  is defined as  $\vec{n}$  that is orthogonal to  $\vec{a}$  and  $\vec{b}$ .

$$\|\vec{a} \times \vec{b}\| = \|\vec{a}\| \|\vec{b}\| \sin \xi, \text{ where } \xi \text{ is the angle between } \vec{a} \text{ and } \vec{b}.$$

- (b) Calculate the Cross Product for

$$\vec{a} = \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}; \vec{b} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix}$$

$$\vec{a} \times \vec{b} = \vec{n} = \begin{pmatrix} 1 \\ -1 \\ -1 \end{pmatrix}$$

- (c) Show that the plane - containing  $\vec{a}$  and  $\vec{b}$  - and  $\vec{n}$  are orthogonal by using scalar and cross product.

$$\vec{a} \cdot (\vec{a} \times \vec{b}) = 0 \Leftrightarrow \cos 90^\circ = 0;$$

$$\vec{b} \cdot (\vec{a} \times \vec{b}) = 0 \Leftrightarrow \cos 90^\circ = 0;$$