

Module 2

February 11, 2023

*You are currently looking at **version 1.1** of this notebook. To download notebooks and datafiles, as well as get help on Jupyter notebooks in the Coursera platform, visit the [Jupyter Notebook FAQ](#) course resource.*

1 Applied Machine Learning: Module 2 (Supervised Learning, Part I)

1.1 Preamble and Review

```
[5]: %matplotlib inline
import numpy as np
import pandas as pd
import seaborn as sn
import matplotlib.pyplot as plt

from sklearn.model_selection import train_test_split
from sklearn.neighbors import KNeighborsClassifier

np.set_printoptions(precision=2)

fruits = pd.read_table('assets/fruit_data_with_colors.txt')

feature_names_fruits = ['height', 'width', 'mass', 'color_score']
X_fruits = fruits[feature_names_fruits]
y_fruits = fruits['fruit_label']
target_names_fruits = ['apple', 'mandarin', 'orange', 'lemon']

X_fruits_2d = fruits[['height', 'width']]
y_fruits_2d = fruits['fruit_label']

X_train, X_test, y_train, y_test = train_test_split(X_fruits, y_fruits,
                                                    random_state=0)

from sklearn.preprocessing import MinMaxScaler
```

```

scaler = MinMaxScaler()
X_train_scaled = scaler.fit_transform(X_train)
# we must apply the scaling to the test set that we computed for the training
→ set
X_test_scaled = scaler.transform(X_test)

knn = KNeighborsClassifier(n_neighbors = 5)
knn.fit(X_train_scaled, y_train)
print('Accuracy of K-NN classifier on training set: {:.2f}'
      .format(knn.score(X_train_scaled, y_train)))
print('Accuracy of K-NN classifier on test set: {:.2f}'
      .format(knn.score(X_test_scaled, y_test)))

example_fruit = [[5.5, 2.2, 10, 0.70]]
example_fruit_scaled = scaler.transform(example_fruit)
print('Predicted fruit type for ', example_fruit, ' is ',
      target_names_fruits[knn.predict(example_fruit_scaled)[0]-1])

```

Accuracy of K-NN classifier on training set: 0.95
 Accuracy of K-NN classifier on test set: 1.00
 Predicted fruit type for [[5.5, 2.2, 10, 0.7]] is mandarin

1.2 Datasets

```

[6]: from sklearn.datasets import make_classification, make_blobs
     from matplotlib.colors import ListedColormap
     from sklearn.datasets import load_breast_cancer
     from adspy_shared_utilities import load_crime_dataset

cmap_bold = ListedColormap(['#FFFF00', '#00FF00', '#0000FF', '#000000'])

# synthetic dataset for simple regression
from sklearn.datasets import make_regression
plt.figure()
plt.title('Sample regression problem with one input variable')
X_R1, y_R1 = make_regression(n_samples = 100, n_features=1,
                             n_informative=1, bias = 150.0,
                             noise = 30, random_state=0)
plt.scatter(X_R1, y_R1, marker= 'o', s=50)
plt.show()

# synthetic dataset for more complex regression
from sklearn.datasets import make_friedman1
plt.figure()
plt.title('Complex regression problem with one input variable')

```

```

X_F1, y_F1 = make_friedman1(n_samples = 100,
                             n_features = 7, random_state=0)

plt.scatter(X_F1[:, 2], y_F1, marker= 'o', s=50)
plt.show()

# synthetic dataset for classification (binary)
plt.figure()
plt.title('Sample binary classification problem with two informative features')
X_C2, y_C2 = make_classification(n_samples = 100, n_features=2,
                                n_redundant=0, n_informative=2,
                                n_clusters_per_class=1, flip_y = 0.1,
                                class_sep = 0.5, random_state=0)
plt.scatter(X_C2[:, 0], X_C2[:, 1], c=y_C2,
            marker= 'o', s=50, cmap=cmap_bold)
plt.show()

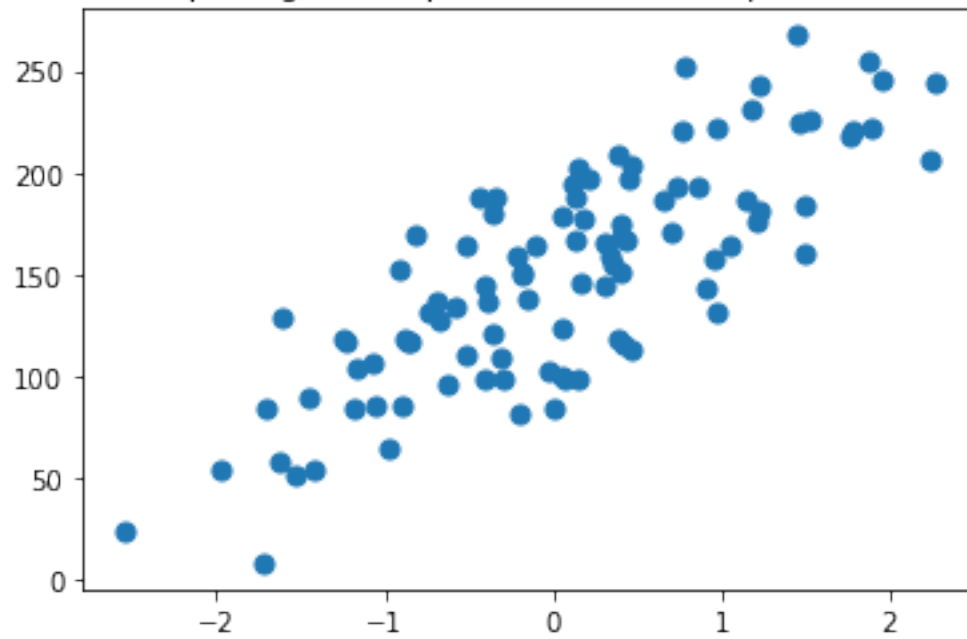
# more difficult synthetic dataset for classification (binary)
# with classes that are not linearly separable
X_D2, y_D2 = make_blobs(n_samples = 100, n_features = 2, centers = 8,
                        cluster_std = 1.3, random_state = 4)
y_D2 = y_D2 % 2
plt.figure()
plt.title('Sample binary classification problem with non-linearly separable_
↳classes')
plt.scatter(X_D2[:,0], X_D2[:,1], c=y_D2,
            marker= 'o', s=50, cmap=cmap_bold)
plt.show()

# Breast cancer dataset for classification
cancer = load_breast_cancer()
(X_cancer, y_cancer) = load_breast_cancer(return_X_y = True)

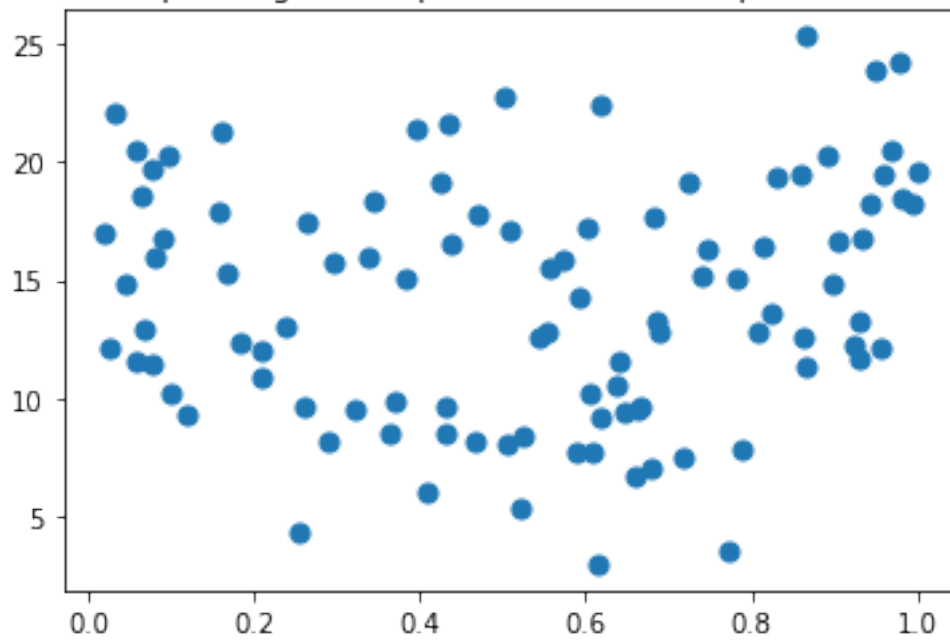
# Communities and Crime dataset
(X_crime, y_crime) = load_crime_dataset()

```

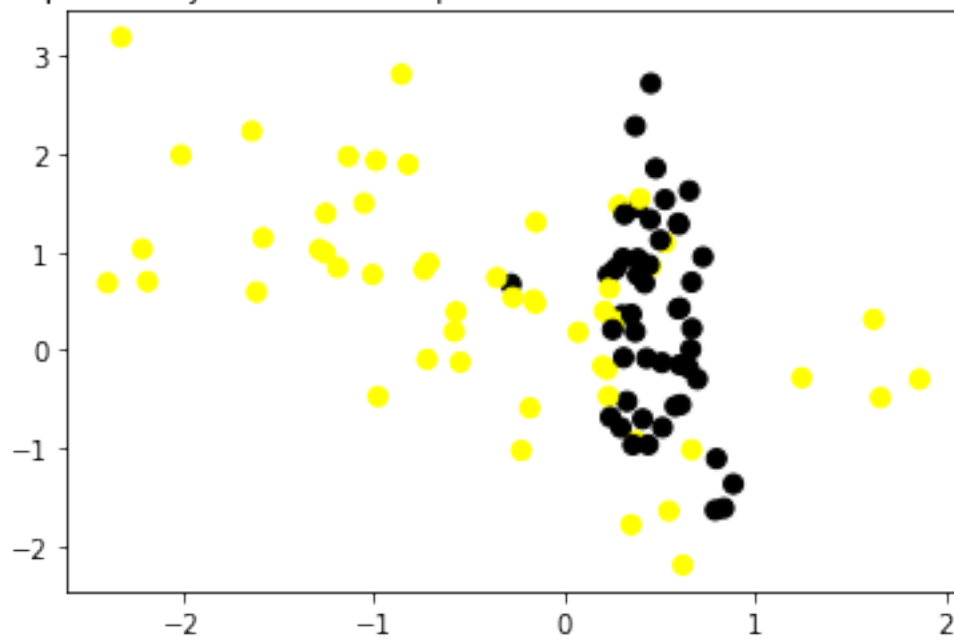
Sample regression problem with one input variable



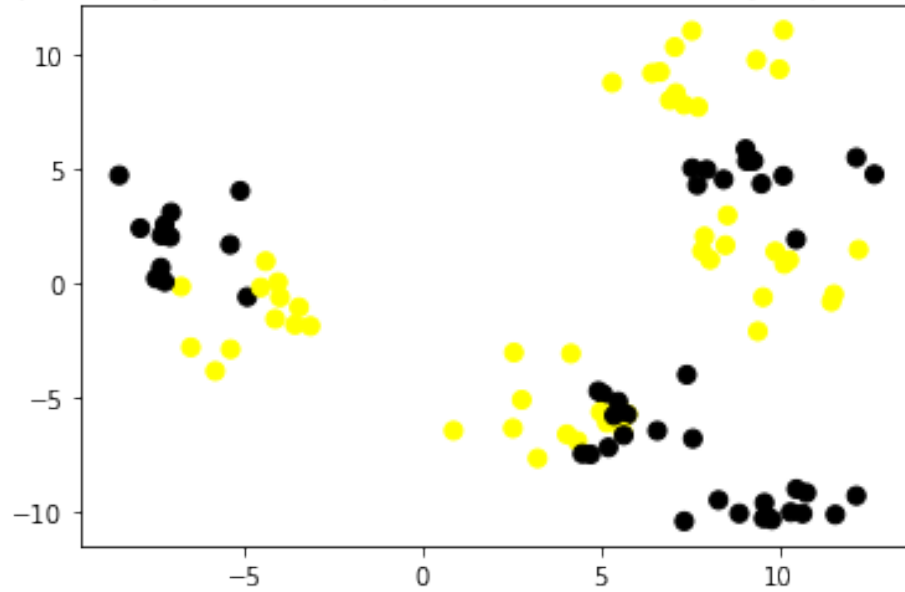
Complex regression problem with one input variable



Sample binary classification problem with two informative features



Sample binary classification problem with non-linearly separable classes



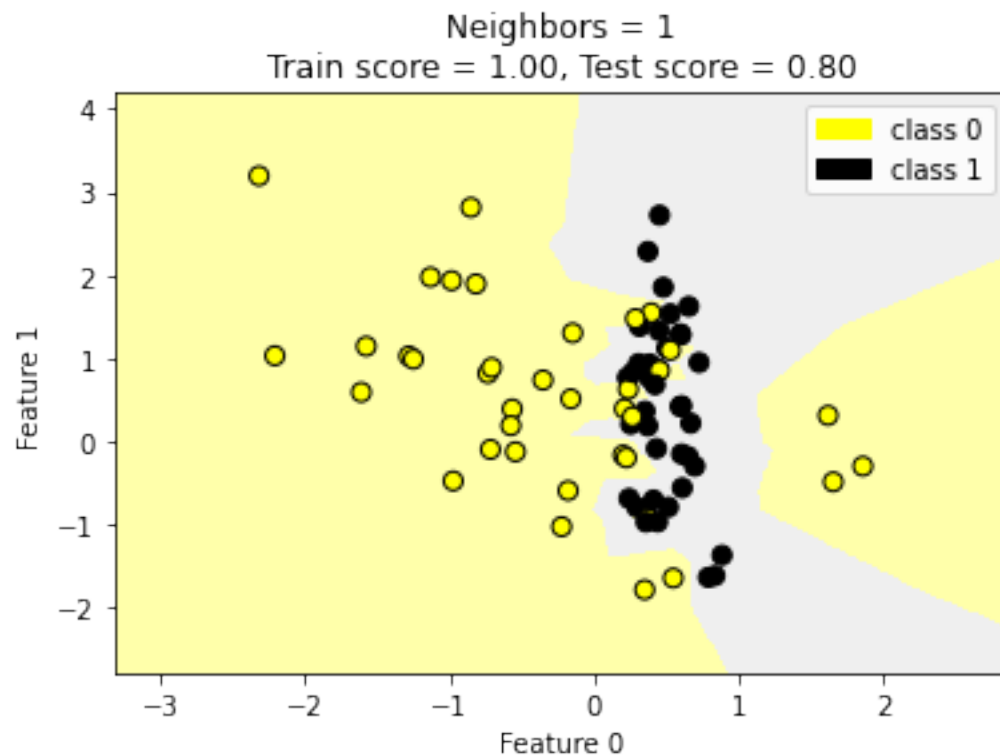
1.3 K-Nearest Neighbors

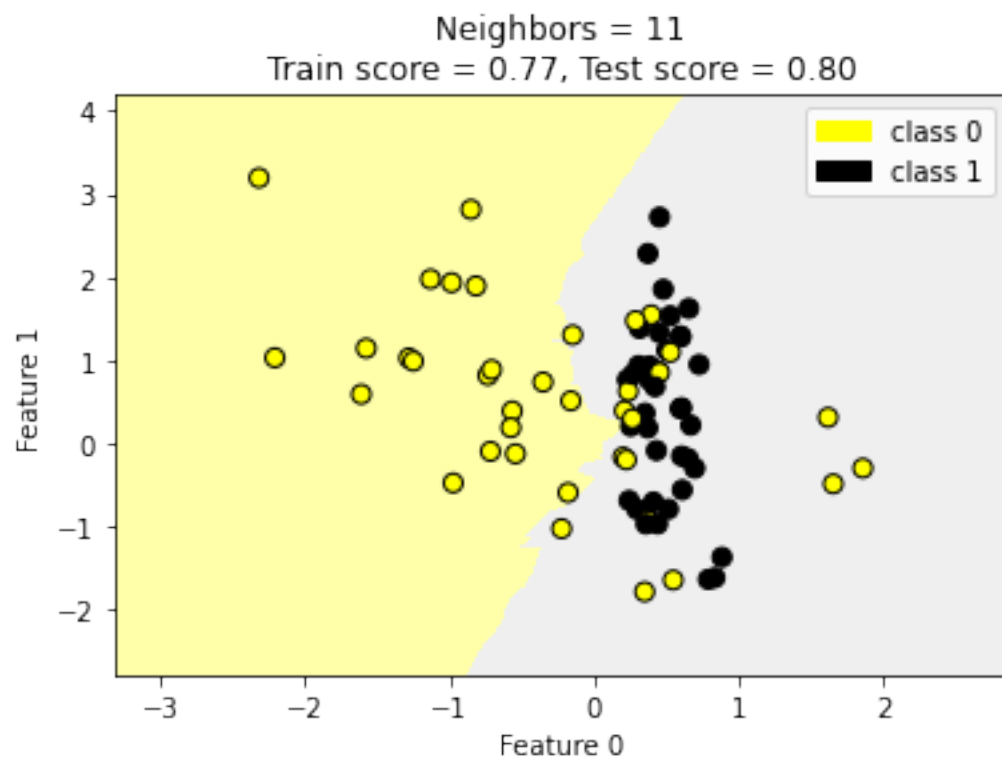
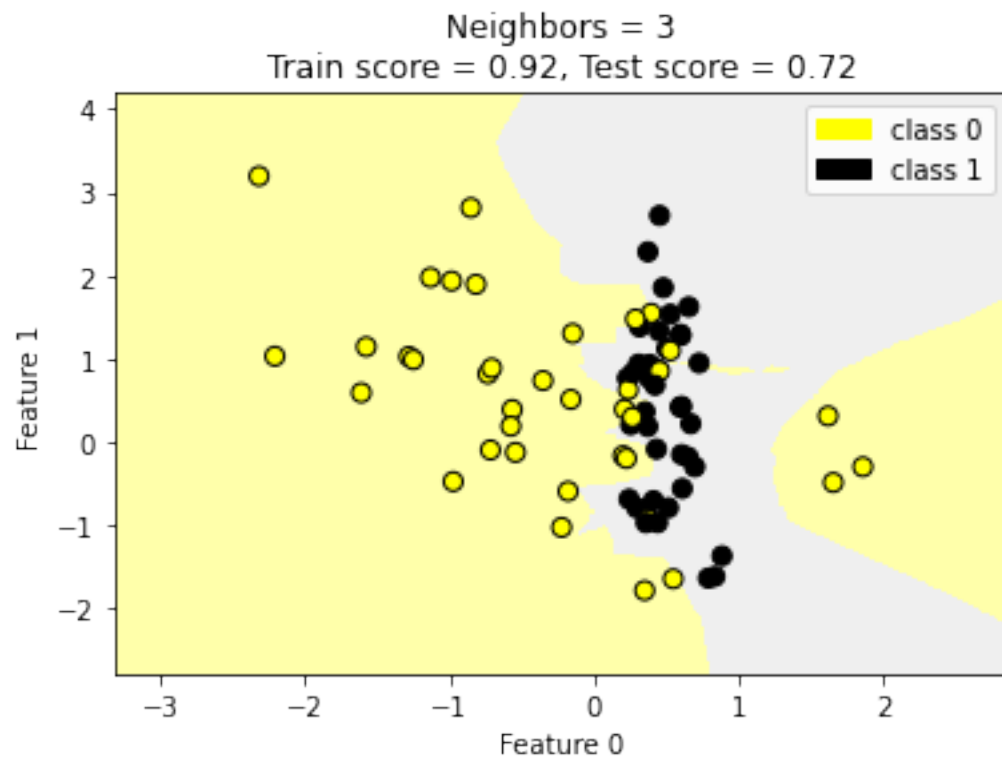
1.3.1 Classification

```
[7]: from adspy_shared_utilities import plot_two_class_knn

X_train, X_test, y_train, y_test = train_test_split(X_C2, y_C2,
                                                    random_state=0)

plot_two_class_knn(X_train, y_train, 1, 'uniform', X_test, y_test)
plot_two_class_knn(X_train, y_train, 3, 'uniform', X_test, y_test)
plot_two_class_knn(X_train, y_train, 11, 'uniform', X_test, y_test)
```





1.3.2 Regression

```
[8]: from sklearn.neighbors import KNeighborsRegressor

X_train, X_test, y_train, y_test = train_test_split(X_R1, y_R1, random_state = 0)

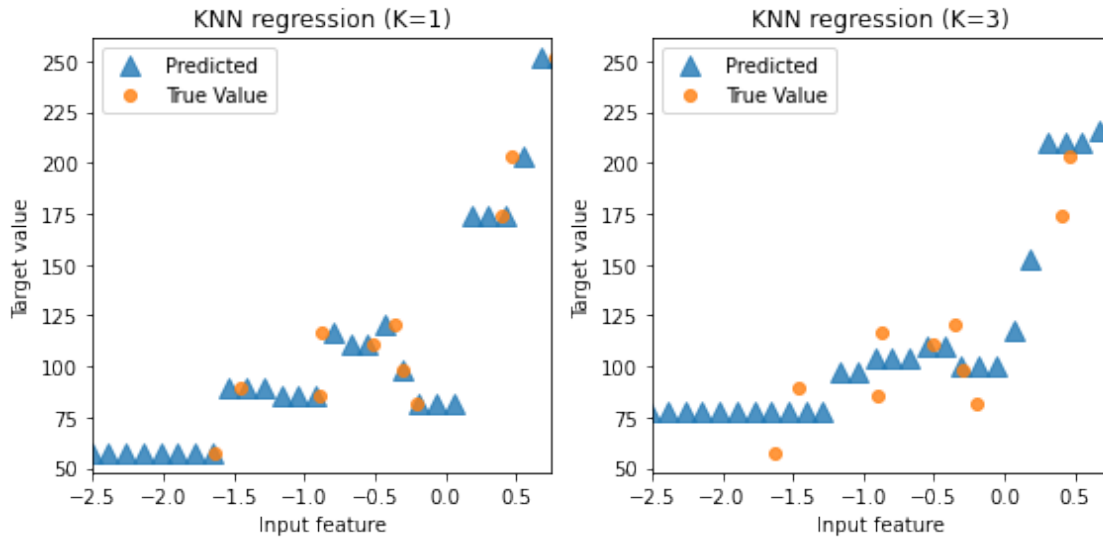
knnreg = KNeighborsRegressor(n_neighbors = 5).fit(X_train, y_train)

print(knnreg.predict(X_test))
print('R-squared test score: {:.3f}'
      .format(knnreg.score(X_test, y_test)))
```

```
[231.71 148.36 150.59 150.59  72.15 166.51 141.91 235.57 208.26 102.1
 191.32 134.5  228.32 148.36 159.17 113.47 144.04 199.23 143.19 166.51
 231.71 208.26 128.02 123.14 141.91]
R-squared test score: 0.425
```

```
[9]: fig, subaxes = plt.subplots(1, 2, figsize=(8,4))
X_predict_input = np.linspace(-3, 3, 50).reshape(-1,1)
X_train, X_test, y_train, y_test = train_test_split(X_R1[0::5], y_R1[0::5],
                                                    random_state = 0)

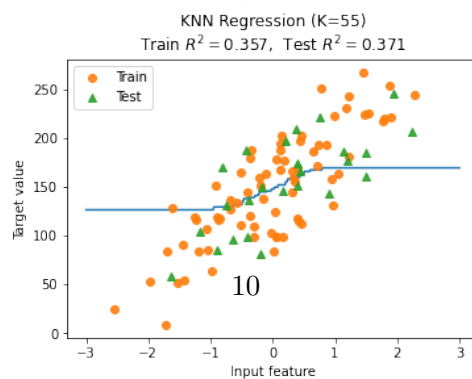
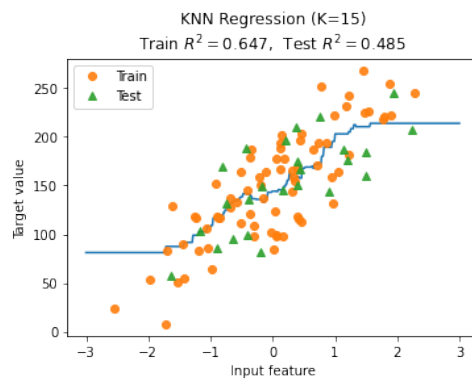
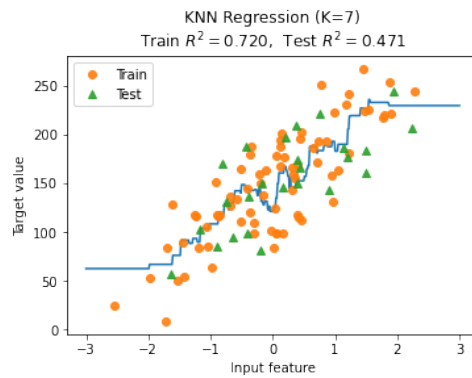
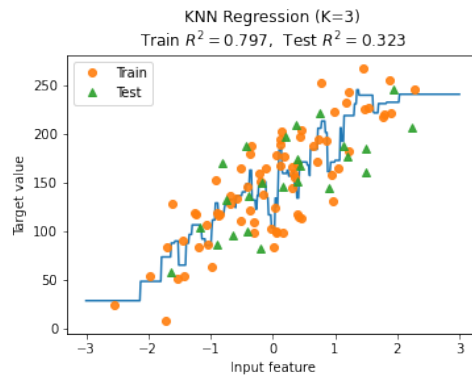
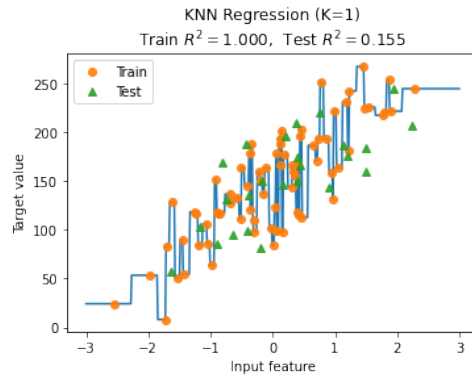
for thisaxis, K in zip(subaxes, [1, 3]):
    knnreg = KNeighborsRegressor(n_neighbors = K).fit(X_train, y_train)
    y_predict_output = knnreg.predict(X_predict_input)
    thisaxis.set_xlim([-2.5, 0.75])
    thisaxis.plot(X_predict_input, y_predict_output, '^', markersize = 10,
                  label='Predicted', alpha=0.8)
    thisaxis.plot(X_train, y_train, 'o', label='True Value', alpha=0.8)
    thisaxis.set_xlabel('Input feature')
    thisaxis.set_ylabel('Target value')
    thisaxis.set_title('KNN regression (K={})'.format(K))
    thisaxis.legend()
plt.tight_layout()
```

1.3.3 Regression model complexity as a function of K

```
[10]: # plot k-NN regression on sample dataset for different values of K
fig, subaxes = plt.subplots(5, 1, figsize=(5,20))
X_predict_input = np.linspace(-3, 3, 500).reshape(-1,1)
X_train, X_test, y_train, y_test = train_test_split(X_R1, y_R1,
                                                    random_state = 0)

for thisaxis, K in zip(subaxes, [1, 3, 7, 15, 55]):
    knnreg = KNeighborsRegressor(n_neighbors = K).fit(X_train, y_train)
    y_predict_output = knnreg.predict(X_predict_input)
    train_score = knnreg.score(X_train, y_train)
    test_score = knnreg.score(X_test, y_test)
    thisaxis.plot(X_predict_input, y_predict_output)
    thisaxis.plot(X_train, y_train, 'o', alpha=0.9, label='Train')
    thisaxis.plot(X_test, y_test, '^', alpha=0.9, label='Test')
    thisaxis.set_xlabel('Input feature')
    thisaxis.set_ylabel('Target value')
    thisaxis.set_title('KNN Regression (K={})\n\
Train $R^2 = {:.3f}$, Test $R^2 = {:.3f}$'
                      .format(K, train_score, test_score))
    thisaxis.legend()
plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=1.0)
```



1.4 Linear models for regression

1.4.1 Linear regression

```
[11]: from sklearn.linear_model import LinearRegression

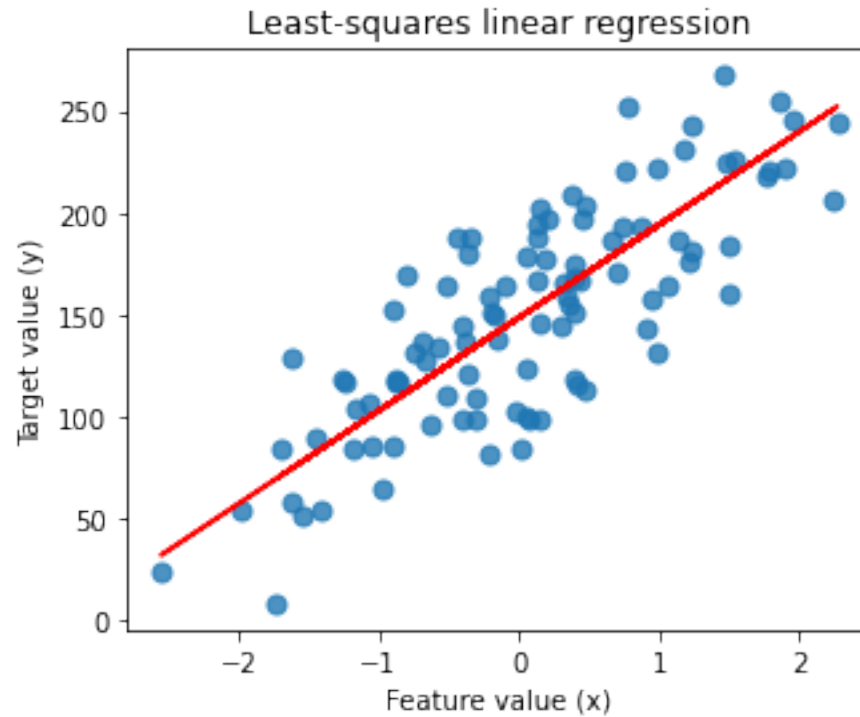
X_train, X_test, y_train, y_test = train_test_split(X_R1, y_R1,
                                                    random_state = 0)
linreg = LinearRegression().fit(X_train, y_train)

print('linear model coeff (w): {}'.format(linreg.coef_))
print('linear model intercept (b): {:.3f}'.format(linreg.intercept_))
print('R-squared score (training): {:.3f}'.format(linreg.score(X_train, y_train)))
print('R-squared score (test): {:.3f}'.format(linreg.score(X_test, y_test)))
```

```
linear model coeff (w): [45.71]
linear model intercept (b): 148.446
R-squared score (training): 0.679
R-squared score (test): 0.492
```

1.4.2 Linear regression: example plot

```
[12]: plt.figure(figsize=(5,4))
plt.scatter(X_R1, y_R1, marker= 'o', s=50, alpha=0.8)
plt.plot(X_R1, linreg.coef_ * X_R1 + linreg.intercept_, 'r-')
plt.title('Least-squares linear regression')
plt.xlabel('Feature value (x)')
plt.ylabel('Target value (y)')
plt.show()
```



```
[13]: X_train, X_test, y_train, y_test = train_test_split(X_crime, y_crime,
                                                         random_state = 0)
linreg = LinearRegression().fit(X_train, y_train)

print('Crime dataset')
print('linear model intercept: {}'.format(linreg.intercept_))
print('linear model coeff:\n{}'.format(linreg.coef_))
print('R-squared score (training): {:.3f}'.format(linreg.score(X_train, y_train)))
print('R-squared score (test): {:.3f}'.format(linreg.score(X_test, y_test)))
```

Crime dataset

linear model intercept: -1728.130672598154

linear model coeff:

```
[ 1.62e-03 -9.43e+01  1.36e+01 -3.13e+01 -8.15e-02 -1.69e+01 -2.43e-03
  1.53e+00 -1.39e-02 -7.72e+00  2.28e+01 -5.66e+00  9.35e+00  2.07e-01
 -7.43e+00  9.66e-03  4.38e-03  4.80e-03 -4.46e+00 -1.61e+01  8.83e+00
 -5.07e-01 -1.42e+00  8.18e+00 -3.87e+00 -3.54e+00  4.49e+00  9.31e+00
  1.74e+02  1.18e+01  1.51e+02 -3.30e+02 -1.35e+02  6.95e-01 -2.38e+01
  2.77e+00  3.82e-01  4.39e+00 -1.06e+01 -4.92e-03  4.14e+01 -1.16e-03
  1.19e+00  1.75e+00 -3.68e+00  1.60e+00 -8.42e+00 -3.80e+01  4.74e+01
```

```

-2.51e+01 -2.88e-01 -3.66e+01  1.90e+01 -4.53e+01  6.83e+02  1.04e+02
-3.29e+02 -3.14e+01  2.74e+01  5.12e+00  6.92e+01  1.98e-02 -6.12e-01
 2.65e+01  1.01e+01 -1.59e+00  2.24e+00  7.38e+00 -3.14e+01 -9.78e-05
 5.02e-05 -3.48e-04 -2.50e-04 -5.27e-01 -5.17e-01 -4.10e-01  1.16e-01
 1.46e+00 -3.04e-01  2.44e+00 -3.66e+01  1.41e-01  2.89e-01  1.77e+01
 5.97e-01  1.98e+00 -1.36e-01 -1.85e+00]
R-squared score (training): 0.673
R-squared score (test): 0.496

```

1.4.3 Ridge regression

```

[14]: from sklearn.linear_model import Ridge
X_train, X_test, y_train, y_test = train_test_split(X_crime, y_crime,
                                                    random_state = 0)

linridge = Ridge(alpha=20.0).fit(X_train, y_train)

print('Crime dataset')
print('ridge regression linear model intercept: {}'.format(linridge.intercept_))
print('ridge regression linear model coeff:\n{}'.format(linridge.coef_))
print('R-squared score (training): {:.3f}'.format(linridge.score(X_train, y_train)))
print('R-squared score (test): {:.3f}'.format(linridge.score(X_test, y_test)))
print('Number of non-zero features: {}'.format(np.sum(linridge.coef_ != 0)))

```

```

Crime dataset
ridge regression linear model intercept: -3352.4230358458803
ridge regression linear model coeff:
[ 1.95e-03  2.19e+01  9.56e+00 -3.59e+01  6.36e+00 -1.97e+01 -2.81e-03
 1.66e+00 -6.61e-03 -6.95e+00  1.72e+01 -5.63e+00  8.84e+00  6.79e-01
-7.34e+00  6.70e-03  9.79e-04  5.01e-03 -4.90e+00 -1.79e+01  9.18e+00
-1.24e+00  1.22e+00  1.03e+01 -3.78e+00 -3.73e+00  4.75e+00  8.43e+00
 3.09e+01  1.19e+01 -2.05e+00 -3.82e+01  1.85e+01  1.53e+00 -2.20e+01
 2.46e+00  3.29e-01  4.02e+00 -1.13e+01 -4.70e-03  4.27e+01 -1.23e-03
 1.41e+00  9.35e-01 -3.00e+00  1.12e+00 -1.82e+01 -1.55e+01  2.42e+01
-1.32e+01 -4.20e-01 -3.60e+01  1.30e+01 -2.81e+01  4.39e+01  3.87e+01
-6.46e+01 -1.64e+01  2.90e+01  4.15e+00  5.34e+01  1.99e-02 -5.47e-01
 1.24e+01  1.04e+01 -1.57e+00  3.16e+00  8.78e+00 -2.95e+01 -2.32e-04
 3.14e-04 -4.14e-04 -1.79e-04 -5.74e-01 -5.18e-01 -4.21e-01  1.53e-01
 1.33e+00  3.85e+00  3.03e+00 -3.78e+01  1.38e-01  3.08e-01  1.57e+01
 3.31e-01  3.36e+00  1.61e-01 -2.68e+00]
R-squared score (training): 0.671
R-squared score (test): 0.494
Number of non-zero features: 88

```

Ridge regression with feature normalization

```
[15]: from sklearn.preprocessing import MinMaxScaler
scaler = MinMaxScaler()

from sklearn.linear_model import Ridge
X_train, X_test, y_train, y_test = train_test_split(X_crime, y_crime,
                                                    random_state = 0)

X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)

linridge = Ridge(alpha=20.0).fit(X_train_scaled, y_train)

print('Crime dataset')
print('ridge regression linear model intercept: {}'.format(linridge.intercept_))
print('ridge regression linear model coeff:\n{}'.format(linridge.coef_))
print('R-squared score (training): {:.3f}'.format(linridge.score(X_train_scaled, y_train)))
print('R-squared score (test): {:.3f}'.format(linridge.score(X_test_scaled, y_test)))
print('Number of non-zero features: {}'.format(np.sum(linridge.coef_ != 0)))
```

Crime dataset

ridge regression linear model intercept: 933.3906385044143

ridge regression linear model coeff:

```
[ 88.69  16.49 -50.3  -82.91 -65.9  -2.28  87.74 150.95 18.88
 -31.06 -43.14 -189.44  -4.53 107.98 -76.53  2.86  34.95 90.14
  52.46 -62.11 115.02   2.67   6.94  -5.67 -101.55 -36.91 -8.71
  29.12 171.26  99.37  75.07 123.64  95.24 -330.61 -442.3 -284.5
 -258.37  17.66 -101.71 110.65 523.14  24.82   4.87 -30.47 -3.52
  50.58  10.85  18.28  44.11  58.34  67.09 -57.94 116.14  53.81
  49.02  -7.62  55.14 -52.09 123.39  77.13  45.5  184.91 -91.36
   1.08 234.09  10.39  94.72 167.92 -25.14  -1.18  14.6  36.77
  53.2  -78.86  -5.9  26.05 115.15  68.74  68.29  16.53 -97.91
 205.2   75.97  61.38 -79.83  67.27  95.67 -11.88]
```

R-squared score (training): 0.615

R-squared score (test): 0.599

Number of non-zero features: 88

Ridge regression with regularization parameter: alpha

```
[16]: print('Ridge regression: effect of alpha regularization parameter\n')
for this_alpha in [0, 1, 10, 20, 50, 100, 1000]:
    linridge = Ridge(alpha = this_alpha).fit(X_train_scaled, y_train)
    r2_train = linridge.score(X_train_scaled, y_train)
```

```

r2_test = linridge.score(X_test_scaled, y_test)
num_coeff_bigger = np.sum(abs(linridge.coef_) > 1.0)
print('Alpha = {:.2f}\nnum abs(coef) > 1.0: {}, \
r-squared training: {:.2f}, r-squared test: {:.2f}\n'
      .format(this_alpha, num_coeff_bigger, r2_train, r2_test))

```

Ridge regression: effect of alpha regularization parameter

```

Alpha = 0.00
num abs(coef) > 1.0: 88, r-squared training: 0.67, r-squared test: 0.50

```

```

Alpha = 1.00
num abs(coef) > 1.0: 87, r-squared training: 0.66, r-squared test: 0.56

```

```

Alpha = 10.00
num abs(coef) > 1.0: 87, r-squared training: 0.63, r-squared test: 0.59

```

```

Alpha = 20.00
num abs(coef) > 1.0: 88, r-squared training: 0.61, r-squared test: 0.60

```

```

Alpha = 50.00
num abs(coef) > 1.0: 86, r-squared training: 0.58, r-squared test: 0.58

```

```

Alpha = 100.00
num abs(coef) > 1.0: 87, r-squared training: 0.55, r-squared test: 0.55

```

```

Alpha = 1000.00
num abs(coef) > 1.0: 84, r-squared training: 0.31, r-squared test: 0.30

```

1.4.4 Lasso regression

```

[17]: from sklearn.linear_model import Lasso
      from sklearn.preprocessing import MinMaxScaler
      scaler = MinMaxScaler()

      X_train, X_test, y_train, y_test = train_test_split(X_crime, y_crime,
                                                            random_state = 0)

      X_train_scaled = scaler.fit_transform(X_train)
      X_test_scaled = scaler.transform(X_test)

      linlasso = Lasso(alpha=2.0, max_iter = 10000).fit(X_train_scaled, y_train)

      print('Crime dataset')
      print('lasso regression linear model intercept: {}'.format(linlasso.intercept_))

```

```

print('lasso regression linear model coeff:\n{}'
      .format(linlasso.coef_))
print('Non-zero features: {}'.format(np.sum(linlasso.coef_ != 0)))
print('R-squared score (training): {:.3f}'
      .format(linlasso.score(X_train_scaled, y_train)))
print('R-squared score (test): {:.3f}\n'
      .format(linlasso.score(X_test_scaled, y_test)))
print('Features with non-zero weight (sorted by absolute magnitude):')

for e in sorted(list(zip(list(X_crime), linlasso.coef_)),
                 key = lambda e: -abs(e[1])):
    if e[1] != 0:
        print('\t{ }, {:.3f}'.format(e[0], e[1]))

```

Crime dataset

lasso regression linear model intercept: 1186.6120619985784

lasso regression linear model coeff:

```

[  0.    0.   -0.  -168.18   -0.   -0.    0.   119.69
   0.   -0.    0.  -169.68   -0.    0.   -0.    0.
   0.    0.   -0.   -0.    0.   -0.    0.    0.
 -57.53  -0.   -0.    0.  259.33  -0.    0.    0.
   0.   -0. -1188.74  -0.   -0.   -0.  -231.42   0.
1488.37   0.   -0.   -0.   -0.    0.    0.    0.
   0.    0.   -0.    0.   20.14   0.    0.    0.
   0.    0.   339.04   0.    0.   459.54  -0.    0.
  122.69  -0.   91.41   0.   -0.    0.    0.   73.14
   0.   -0.    0.    0.   86.36   0.    0.    0.
 -104.57 264.93   0.   23.45  -49.39   0.    5.2    0. ]

```

Non-zero features: 20

R-squared score (training): 0.631

R-squared score (test): 0.624

Features with non-zero weight (sorted by absolute magnitude):

```

PctKidsBornNeverMar, 1488.365
PctKids2Par, -1188.740
HousVacant, 459.538
PctPersDenseHous, 339.045
NumInShelters, 264.932
MalePctDivorce, 259.329
PctWorkMom, -231.423
pctWInvInc, -169.676
agePct12t29, -168.183
PctVacantBoarded, 122.692
pctUrban, 119.694
MedOwnCostPctIncNoMtg, -104.571
MedYrHousBuilt, 91.412

```



```
RentQrange, 86.356
OwnOccHiQuart, 73.144
PctEmplManu, -57.530
PctBornSameState, -49.394
PctForeignBorn, 23.449
PctLargHouseFam, 20.144
PctSameCity85, 5.198
```

Lasso regression with regularization parameter: alpha

```
[18]: print('Lasso regression: effect of alpha regularization\n\
parameter on number of features kept in final model\n')

for alpha in [0.5, 1, 2, 3, 5, 10, 20, 50]:
    linlasso = Lasso(alpha, max_iter = 10000).fit(X_train_scaled, y_train)
    r2_train = linlasso.score(X_train_scaled, y_train)
    r2_test = linlasso.score(X_test_scaled, y_test)

    print('Alpha = {:.2f}\nFeatures kept: {}, r-squared training: {:.2f}, \
r-squared test: {:.2f}\n'
          .format(alpha, np.sum(linlasso.coef_ != 0), r2_train, r2_test))
```

Lasso regression: effect of alpha regularization
parameter on number of features kept in final model

Alpha = 0.50
Features kept: 35, r-squared training: 0.65, r-squared test: 0.58

Alpha = 1.00
Features kept: 25, r-squared training: 0.64, r-squared test: 0.60

Alpha = 2.00
Features kept: 20, r-squared training: 0.63, r-squared test: 0.62

Alpha = 3.00
Features kept: 17, r-squared training: 0.62, r-squared test: 0.63

Alpha = 5.00
Features kept: 12, r-squared training: 0.60, r-squared test: 0.61

Alpha = 10.00
Features kept: 6, r-squared training: 0.57, r-squared test: 0.58

Alpha = 20.00
Features kept: 2, r-squared training: 0.51, r-squared test: 0.50

Alpha = 50.00
Features kept: 1, r-squared training: 0.31, r-squared test: 0.30

1.4.5 Polynomial regression

```
[19]: from sklearn.linear_model import LinearRegression
      from sklearn.linear_model import Ridge
      from sklearn.preprocessing import PolynomialFeatures

X_train, X_test, y_train, y_test = train_test_split(X_F1, y_F1,
                                                    random_state = 0)
linreg = LinearRegression().fit(X_train, y_train)

print('linear model coeff (w): {}'.format(linreg.coef_))
print('linear model intercept (b): {:.3f}'.format(linreg.intercept_))
print('R-squared score (training): {:.3f}'.format(linreg.score(X_train, y_train)))
print('R-squared score (test): {:.3f}'.format(linreg.score(X_test, y_test)))

print('\nNow we transform the original input data to add\n\
polynomial features up to degree 2 (quadratic)\n')
poly = PolynomialFeatures(degree=2)
X_F1_poly = poly.fit_transform(X_F1)

X_train, X_test, y_train, y_test = train_test_split(X_F1_poly, y_F1,
                                                    random_state = 0)
linreg = LinearRegression().fit(X_train, y_train)

print('(poly deg 2) linear model coeff (w):\n{}'.format(linreg.coef_))
print('(poly deg 2) linear model intercept (b): {:.3f}'.format(linreg.intercept_))
print('(poly deg 2) R-squared score (training): {:.3f}'.format(linreg.score(X_train, y_train)))
print('(poly deg 2) R-squared score (test): {:.3f}\n'.format(linreg.score(X_test, y_test)))

print('\nAddition of many polynomial features often leads to\n\
overfitting, so we often use polynomial features in combination\n\
with regression that has a regularization penalty, like ridge\n\
regression.\n')

X_train, X_test, y_train, y_test = train_test_split(X_F1_poly, y_F1,
                                                    random_state = 0)
```

```

linreg = Ridge().fit(X_train, y_train)

print('(poly deg 2 + ridge) linear model coeff (w):\n{:.3f}'
      .format(linreg.coef_))
print('(poly deg 2 + ridge) linear model intercept (b): {:.3f}'
      .format(linreg.intercept_))
print('(poly deg 2 + ridge) R-squared score (training): {:.3f}'
      .format(linreg.score(X_train, y_train)))
print('(poly deg 2 + ridge) R-squared score (test): {:.3f}'
      .format(linreg.score(X_test, y_test)))

```

```

linear model coeff (w): [ 4.42  6.    0.53 10.24  6.55 -2.02 -0.32]
linear model intercept (b): 1.543
R-squared score (training): 0.722
R-squared score (test): 0.722

```

Now we transform the original input data to add polynomial features up to degree 2 (quadratic)

```

(poly deg 2) linear model coeff (w):
[ 3.41e-12  1.66e+01  2.67e+01 -2.21e+01  1.24e+01  6.93e+00  1.05e+00
  3.71e+00 -1.34e+01 -5.73e+00  1.62e+00  3.66e+00  5.05e+00 -1.46e+00
  1.95e+00 -1.51e+01  4.87e+00 -2.97e+00 -7.78e+00  5.15e+00 -4.65e+00
  1.84e+01 -2.22e+00  2.17e+00 -1.28e+00  1.88e+00  1.53e-01  5.62e-01
 -8.92e-01 -2.18e+00  1.38e+00 -4.90e+00 -2.24e+00  1.38e+00 -5.52e-01
 -1.09e+00]
(poly deg 2) linear model intercept (b): -3.206
(poly deg 2) R-squared score (training): 0.969
(poly deg 2) R-squared score (test): 0.805

```

Addition of many polynomial features often leads to overfitting, so we often use polynomial features in combination with regression that has a regularization penalty, like ridge regression.

```

(poly deg 2 + ridge) linear model coeff (w):
[ 0.    2.23  4.73 -3.15  3.86  1.61 -0.77 -0.15 -1.75  1.6   1.37  2.52
  2.72  0.49 -1.94 -1.63  1.51  0.89  0.26  2.05 -1.93  3.62 -0.72  0.63
 -3.16  1.29  3.55  1.73  0.94 -0.51  1.7  -1.98  1.81 -0.22  2.88 -0.89]
(poly deg 2 + ridge) linear model intercept (b): 5.418
(poly deg 2 + ridge) R-squared score (training): 0.826
(poly deg 2 + ridge) R-squared score (test): 0.825

```

1.5 Linear models for classification

1.5.1 Logistic regression

Logistic regression for binary classification on fruits dataset using height, width features (positive class: apple, negative class: others)

```
[20]: from sklearn.linear_model import LogisticRegression
      from adspy_shared_utilities import (
      plot_class_regions_for_classifier_subplot)

      fig, subaxes = plt.subplots(1, 1, figsize=(7, 5))
      y_fruits_apple = y_fruits_2d == 1  # make into a binary problem: apples vs_
      ↪ everything else
      X_train, X_test, y_train, y_test = (
      train_test_split(X_fruits_2d.values,
                        y_fruits_apple.values,
                        random_state = 0))

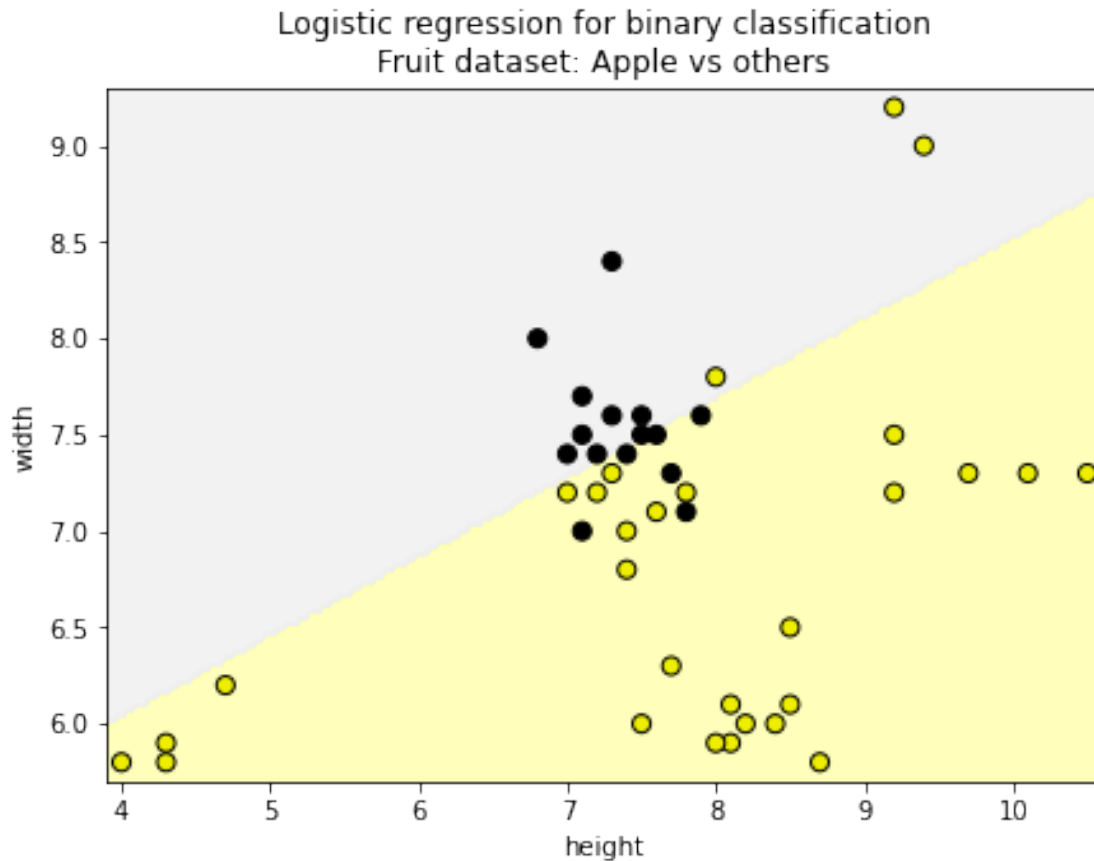
      clf = LogisticRegression(C=100).fit(X_train, y_train)
      plot_class_regions_for_classifier_subplot(clf, X_train, y_train, None,
      None, 'Logistic regression \
      for binary classification\nFruit dataset: Apple vs others',
      subaxes)

      h = 6
      w = 8
      print('A fruit with height {} and width {} is predicted to be: {}'.
      .format(h,w, ['not an apple', 'an apple'][int(clf.predict([[h,w]])[0])]))

      h = 10
      w = 7
      print('A fruit with height {} and width {} is predicted to be: {}'.
      .format(h,w, ['not an apple', 'an apple'][int(clf.predict([[h,w]])[0])]))
      subaxes.set_xlabel('height')
      subaxes.set_ylabel('width')

      print('Accuracy of Logistic regression classifier on training set: {:.2f}'
      .format(clf.score(X_train, y_train)))
      print('Accuracy of Logistic regression classifier on test set: {:.2f}'
      .format(clf.score(X_test, y_test)))
```

A fruit with height 6 and width 8 is predicted to be: an apple
A fruit with height 10 and width 7 is predicted to be: not an apple
Accuracy of Logistic regression classifier on training set: 0.80
Accuracy of Logistic regression classifier on test set: 0.73



Logistic regression on simple synthetic dataset

```
[21]: from sklearn.linear_model import LogisticRegression
      from adspy_shared_utilities import (
      plot_class_regions_for_classifier_subplot)

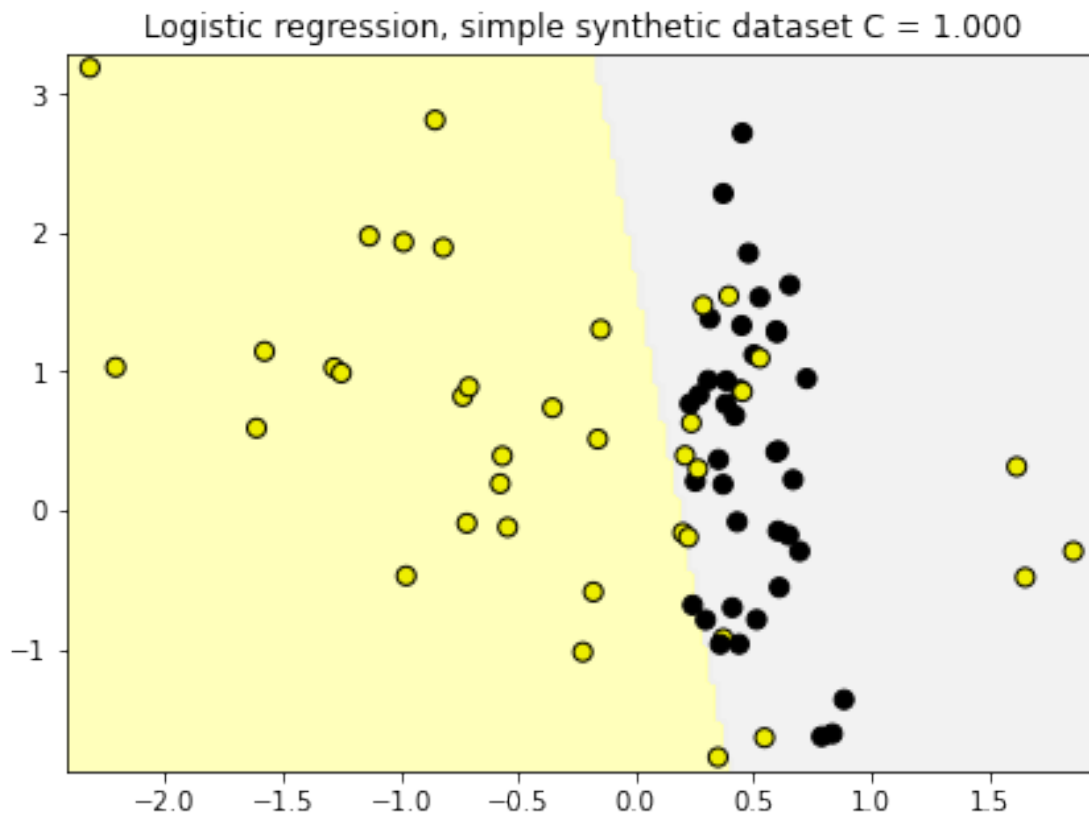
      X_train, X_test, y_train, y_test = train_test_split(X_C2, y_C2,
                                                          random_state = 0)

      fig, subaxes = plt.subplots(1, 1, figsize=(7, 5))
      clf = LogisticRegression().fit(X_train, y_train)
      title = 'Logistic regression, simple synthetic dataset C = {:.3f}'.format(1.0)
      plot_class_regions_for_classifier_subplot(clf, X_train, y_train,
                                              None, None, title, subaxes)

      print('Accuracy of Logistic regression classifier on training set: {:.2f}'
            .format(clf.score(X_train, y_train)))
      print('Accuracy of Logistic regression classifier on test set: {:.2f}'
            .format(clf.score(X_test, y_test)))
```

Accuracy of Logistic regression classifier on training set: 0.81

Accuracy of Logistic regression classifier on test set: 0.84



Logistic regression regularization: C parameter

```
[22]: X_train, X_test, y_train, y_test = (
    train_test_split(X_fruits_2d.values,
                    y_fruits_apple.values,
                    random_state=0))

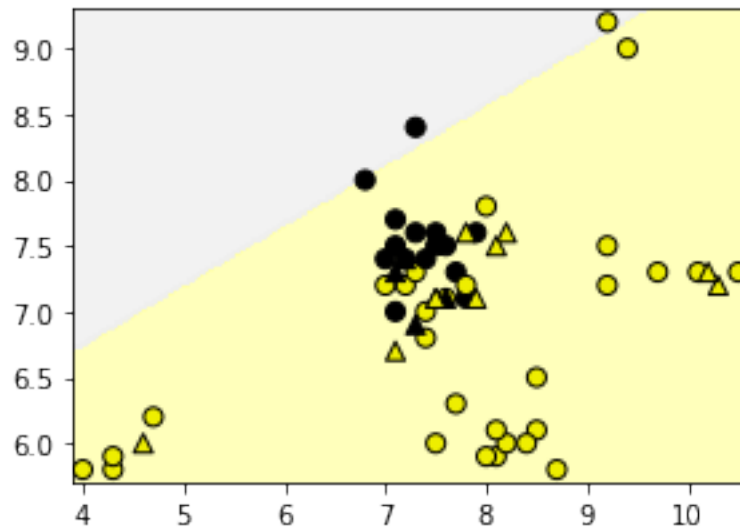
fig, subaxes = plt.subplots(3, 1, figsize=(4, 10))

for this_C, subplot in zip([0.1, 1, 100], subaxes):
    clf = LogisticRegression(C=this_C).fit(X_train, y_train)
    title = 'Logistic regression (apple vs rest), C = {:.3f}'.format(this_C)

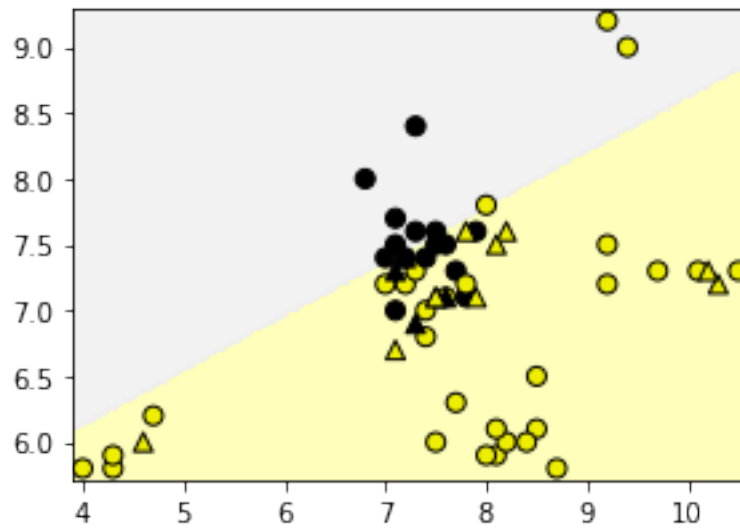
    plot_class_regions_for_classifier_subplot(clf, X_train, y_train,
                                             X_test, y_test, title,
                                             subplot)
```

```
plt.tight_layout()
```

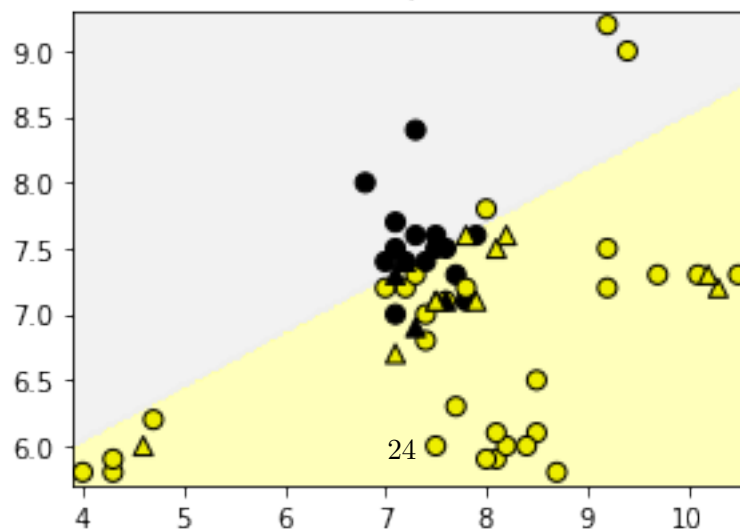
Logistic regression (apple vs rest), $C = 0.100$
Train score = 0.66, Test score = 0.67



Logistic regression (apple vs rest), $C = 1.000$
Train score = 0.75, Test score = 0.67



Logistic regression (apple vs rest), $C = 100.000$
Train score = 0.80, Test score = 0.73



Application to real dataset

```
[23]: from sklearn.linear_model import LogisticRegression

X_train, X_test, y_train, y_test = train_test_split(X_cancer, y_cancer,
    random_state = 0)

clf = LogisticRegression().fit(X_train, y_train)
print('Breast cancer dataset')
print('Accuracy of Logistic regression classifier on training set: {:.2f}'
    .format(clf.score(X_train, y_train)))
print('Accuracy of Logistic regression classifier on test set: {:.2f}'
    .format(clf.score(X_test, y_test)))
```

Breast cancer dataset

Accuracy of Logistic regression classifier on training set: 0.95

Accuracy of Logistic regression classifier on test set: 0.94

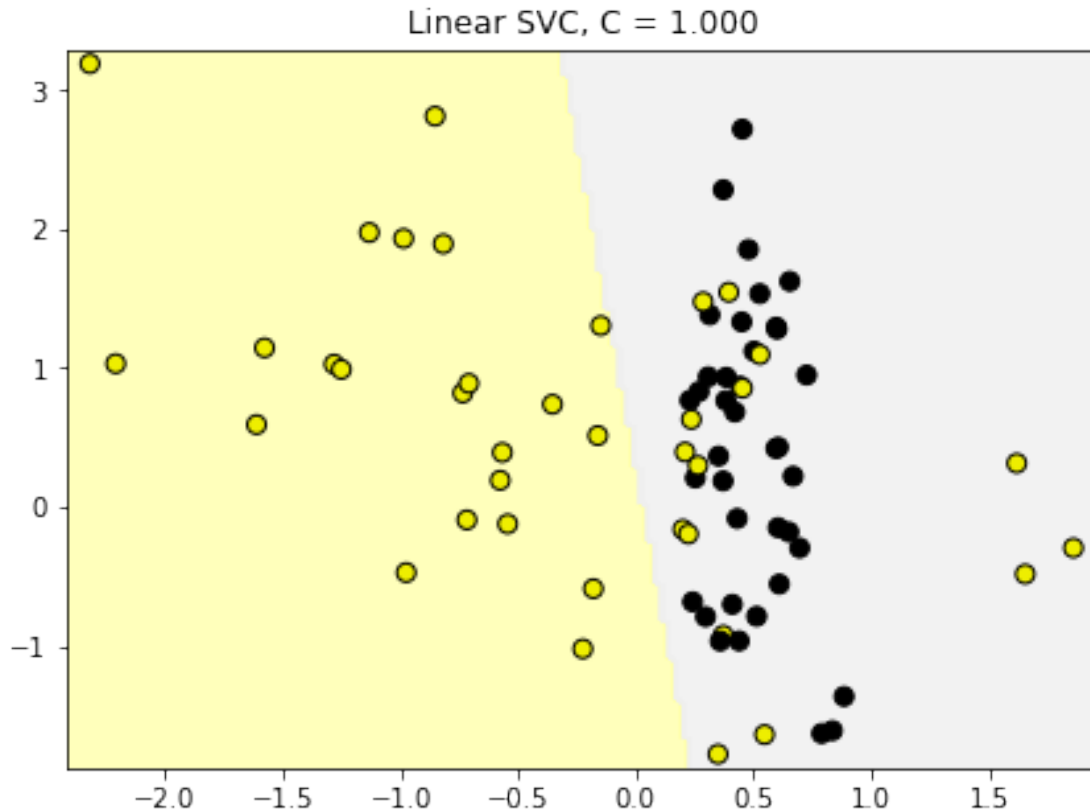
1.5.2 Support Vector Machines

Linear Support Vector Machine

```
[24]: from sklearn.svm import SVC
from adspy_shared_utilities import plot_class_regions_for_classifier_subplot

X_train, X_test, y_train, y_test = train_test_split(X_C2, y_C2, random_state =
    0)

fig, subaxes = plt.subplots(1, 1, figsize=(7, 5))
this_C = 1.0
clf = SVC(kernel = 'linear', C=this_C).fit(X_train, y_train)
title = 'Linear SVC, C = {:.3f}'.format(this_C)
plot_class_regions_for_classifier_subplot(clf, X_train, y_train, None, None,
    title, subaxes)
```



Linear Support Vector Machine: C parameter

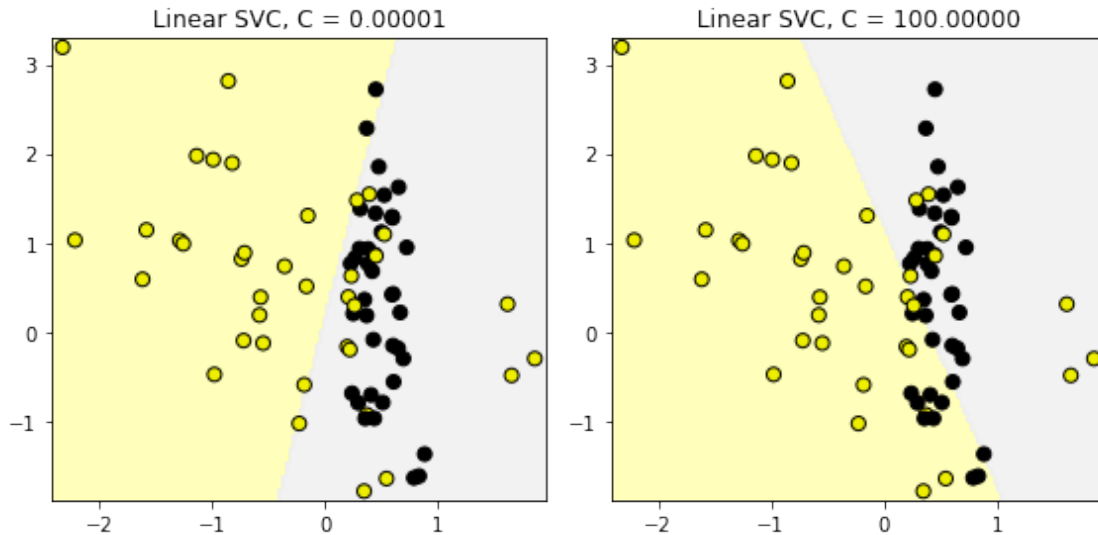
```
[25]: from sklearn.svm import LinearSVC
      from adspy_shared_utilities import plot_class_regions_for_classifier

      X_train, X_test, y_train, y_test = train_test_split(X_C2, y_C2, random_state = 0)

      fig, subaxes = plt.subplots(1, 2, figsize=(8, 4))

      for this_C, subplot in zip([0.00001, 100], subaxes):
          clf = LinearSVC(C=this_C).fit(X_train, y_train)
          title = 'Linear SVC, C = {:.5f}'.format(this_C)
          plot_class_regions_for_classifier_subplot(clf, X_train, y_train,
                                                    None, None, title, subplot)

      plt.tight_layout()
```



Application to real dataset

```
[26]: from sklearn.svm import LinearSVC
X_train, X_test, y_train, y_test = train_test_split(X_cancer, y_cancer,
    random_state = 0)

clf = LinearSVC().fit(X_train, y_train)
print('Breast cancer dataset')
print('Accuracy of Linear SVC classifier on training set: {:.2f}'
    .format(clf.score(X_train, y_train)))
print('Accuracy of Linear SVC classifier on test set: {:.2f}'
    .format(clf.score(X_test, y_test)))
```

Breast cancer dataset

Accuracy of Linear SVC classifier on training set: 0.90

Accuracy of Linear SVC classifier on test set: 0.90

1.5.3 Multi-class classification with linear models

LinearSVC with M classes generates M one vs rest classifiers.

```
[27]: from sklearn.svm import LinearSVC

X_train, X_test, y_train, y_test = train_test_split(X_fruits_2d, y_fruits_2d,
    random_state = 0)

clf = LinearSVC(C=5, random_state = 67).fit(X_train, y_train)
print('Coefficients:\n', clf.coef_)
print('Intercepts:\n', clf.intercept_)
```

Coefficients:

```
[[ -0.3   0.72]
 [ -1.63  1.16]
 [  0.01  0.43]
 [  1.25 -1.64]]
```

Intercepts:

```
[-3.29  1.2  -3.04  1.16]
```

Multi-class results on the fruit dataset

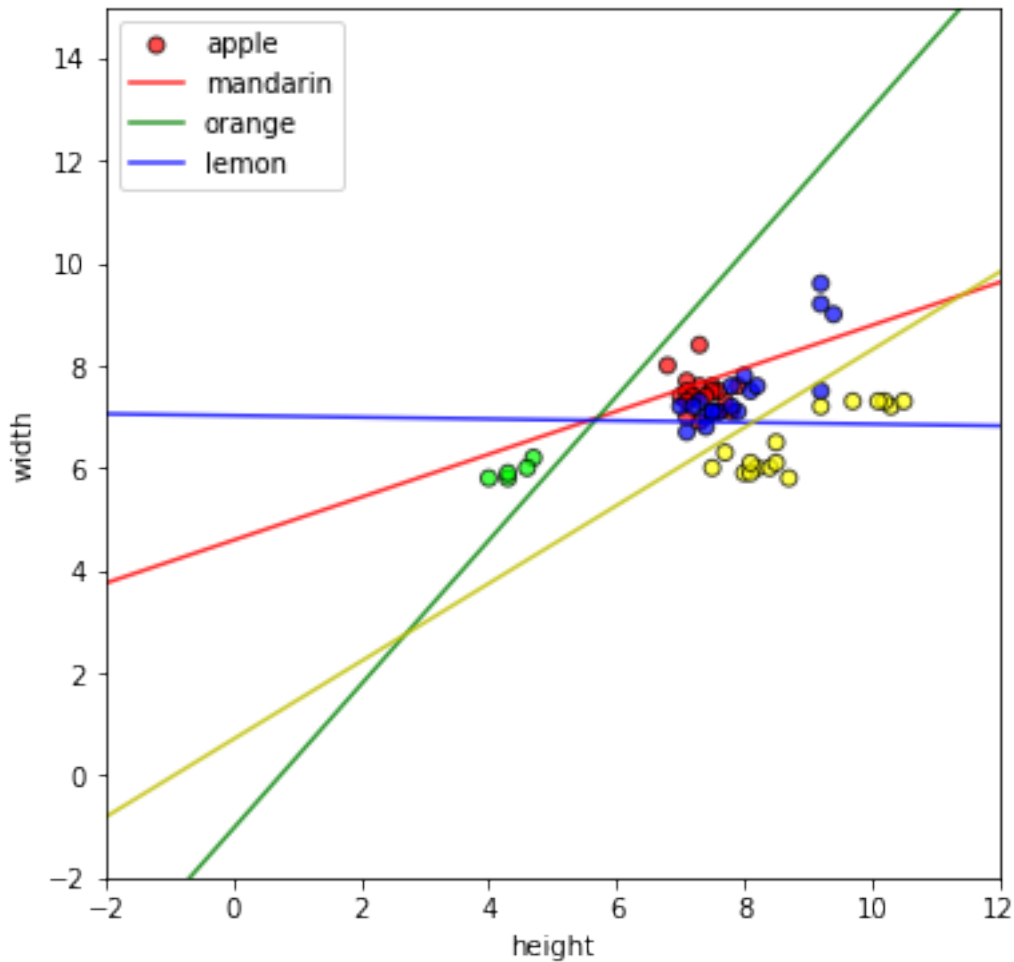
```
[28]: plt.figure(figsize=(6,6))
      colors = ['r', 'g', 'b', 'y']
      cmap_fruits = ListedColormap(['#FF0000', '#00FF00', '#0000FF', '#FFFF00'])

      plt.scatter(X_fruits_2d[['height']], X_fruits_2d[['width']],
                  c=y_fruits_2d, cmap=cmap_fruits, edgecolor = 'black', alpha=.7)

      x_0_range = np.linspace(-10, 15)

      for w, b, color in zip(clf.coef_, clf.intercept_, ['r', 'g', 'b', 'y']):
          # Since class prediction with a linear model uses the formula  $y = w_0 x_0 +$ 
           $\rightarrow w_1 x_1 + b$ ,
          # and the decision boundary is defined as being all points with  $y = 0$ , to
           $\rightarrow$  plot  $x_1$  as a
          # function of  $x_0$  we just solve  $w_0 x_0 + w_1 x_1 + b = 0$  for  $x_1$ :
          plt.plot(x_0_range, -(x_0_range * w[0] + b) / w[1], c=color, alpha=.8)

      plt.legend(target_names_fruits)
      plt.xlabel('height')
      plt.ylabel('width')
      plt.xlim(-2, 12)
      plt.ylim(-2, 15)
      plt.show()
```



1.6 Kernelized Support Vector Machines

1.6.1 Classification

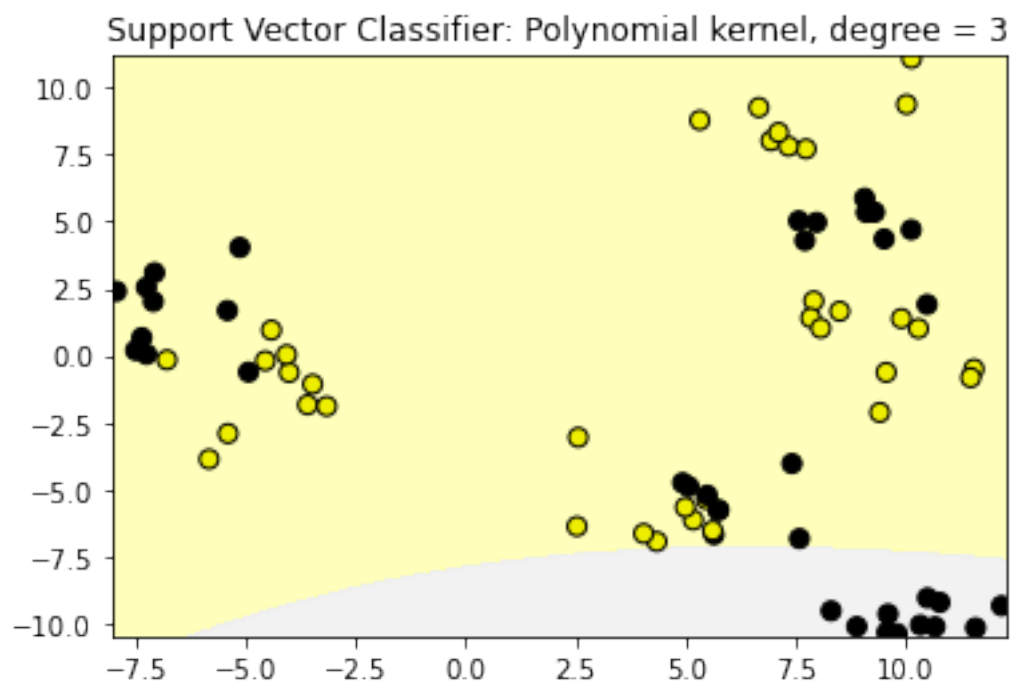
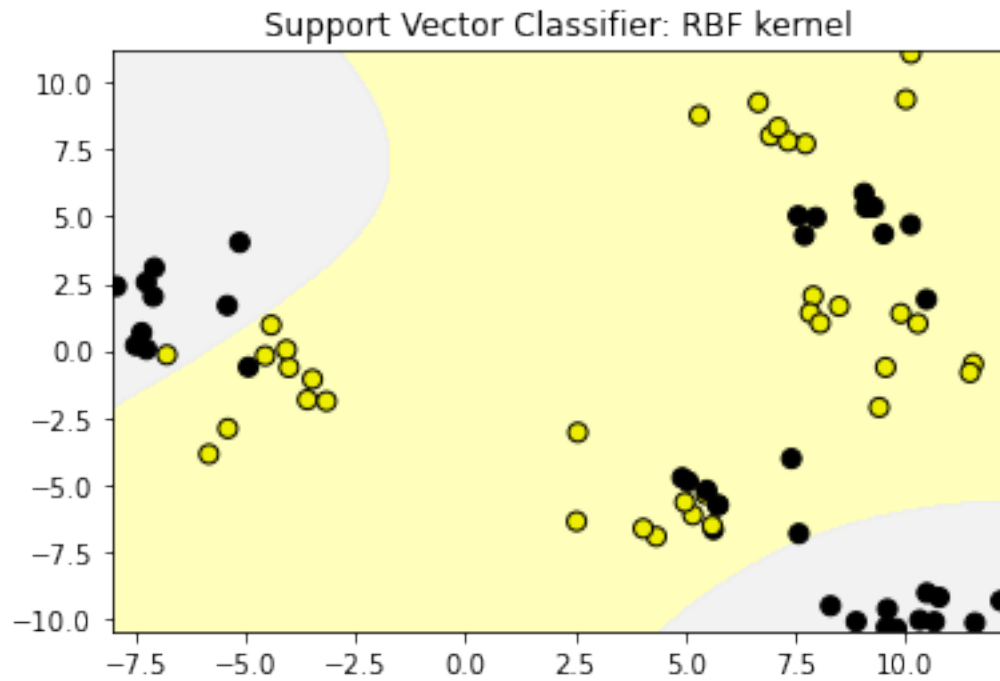
```
[29]: from sklearn.svm import SVC
from adspy_shared_utilities import plot_class_regions_for_classifier

X_train, X_test, y_train, y_test = train_test_split(X_D2, y_D2, random_state = 0)

# The default SVC kernel is radial basis function (RBF)
plot_class_regions_for_classifier(SVC().fit(X_train, y_train),
                                X_train, y_train, None, None,
                                'Support Vector Classifier: RBF kernel')

# Compare decision boundaries with polynomial kernel, degree = 3
plot_class_regions_for_classifier(SVC(kernel = 'poly', degree = 3))
```

```
.fit(X_train, y_train), X_train,
y_train, None, None,
'Support Vector Classifier: Polynomial kernel,
↪degree = 3')
```



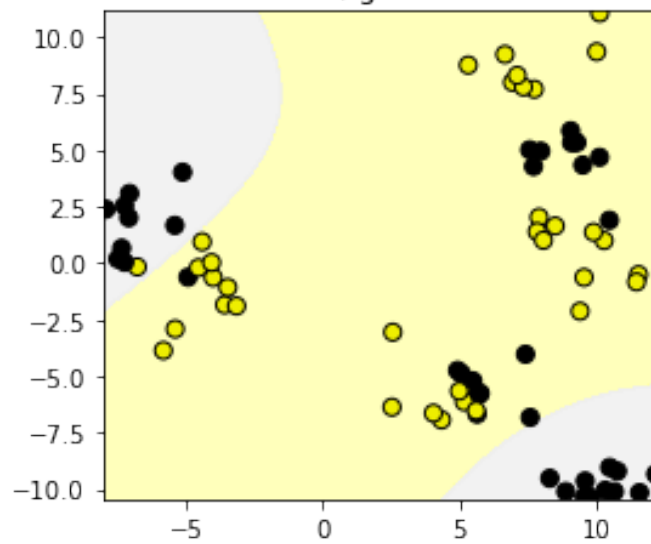
Support Vector Machine with RBF kernel: gamma parameter

```
[30]: from adspy_shared_utilities import plot_class_regions_for_classifier

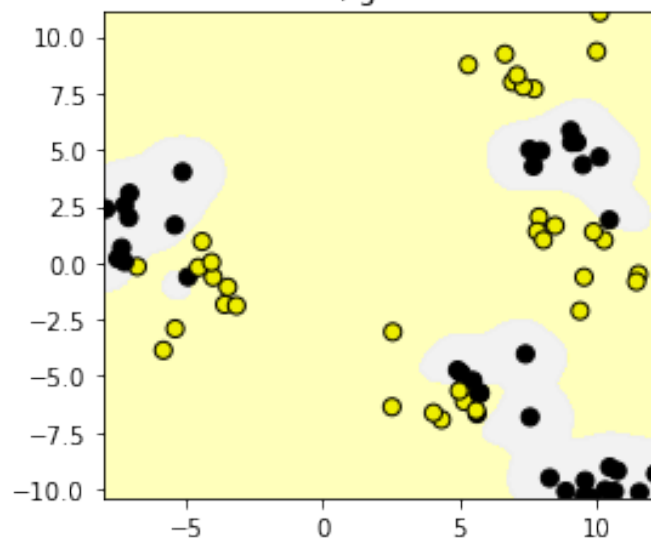
X_train, X_test, y_train, y_test = train_test_split(X_D2, y_D2, random_state = 0)
fig, subaxes = plt.subplots(3, 1, figsize=(4, 11))

for this_gamma, subplot in zip([0.01, 1.0, 10.0], subaxes):
    clf = SVC(kernel = 'rbf', gamma=this_gamma).fit(X_train, y_train)
    title = 'Support Vector Classifier: \nRBF kernel, gamma = {:.2f}'.
    format(this_gamma)
    plot_class_regions_for_classifier_subplot(clf, X_train, y_train,
                                             None, None, title, subplot)
plt.tight_layout()
```

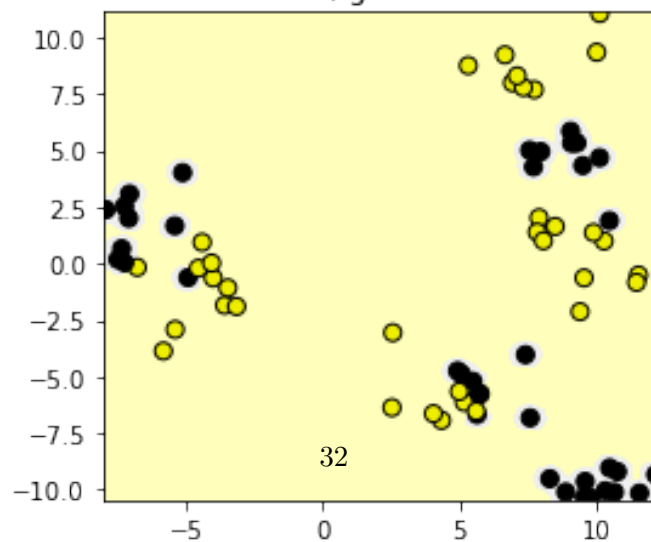
Support Vector Classifier:
RBF kernel, gamma = 0.01



Support Vector Classifier:
RBF kernel, gamma = 1.00



Support Vector Classifier:
RBF kernel, gamma = 10.00



Support Vector Machine with RBF kernel: using both C and gamma parameter

```
[31]: from sklearn.svm import SVC
from adspy_shared_utilities import plot_class_regions_for_classifier_subplot

from sklearn.model_selection import train_test_split

X_train, X_test, y_train, y_test = train_test_split(X_D2, y_D2, random_state = 0)

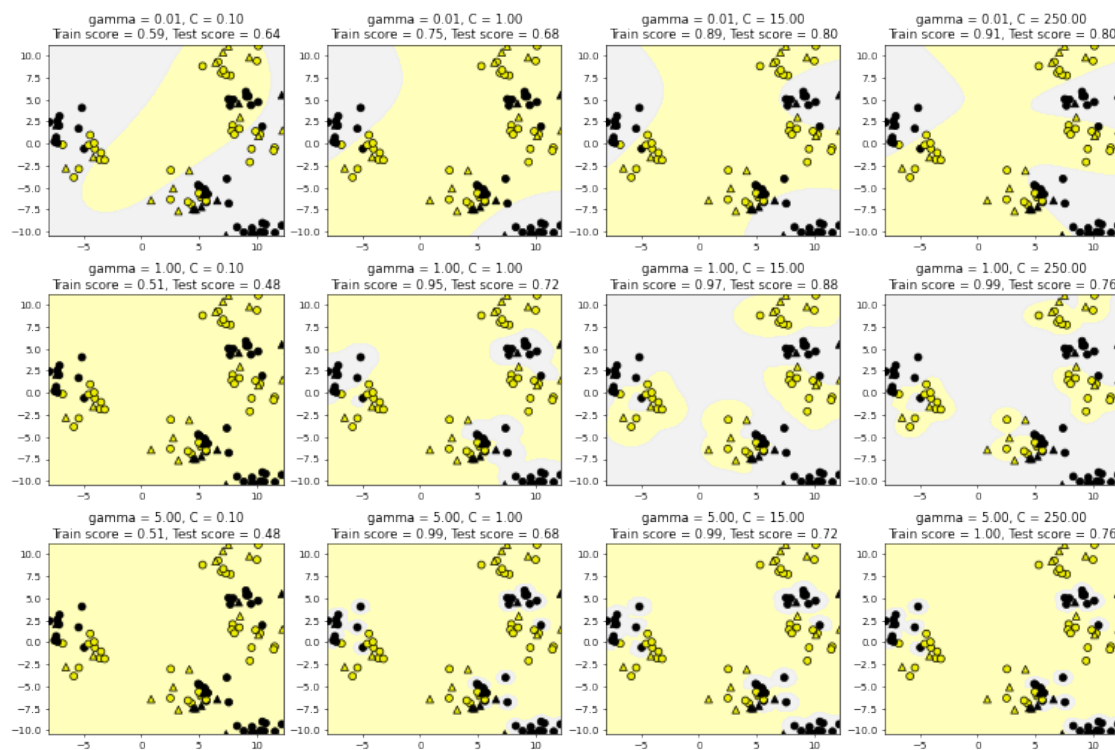
fig, subaxes = plt.subplots(3, 4, figsize=(15, 10), dpi=50)

for this_gamma, this_axis in zip([0.01, 1, 5], subaxes):

    for this_C, subplot in zip([0.1, 1, 15, 250], this_axis):

        title = 'gamma = {:.2f}, C = {:.2f}'.format(this_gamma, this_C)
        clf = SVC(kernel = 'rbf', gamma = this_gamma,
                   C = this_C).fit(X_train, y_train)
        plot_class_regions_for_classifier_subplot(clf, X_train, y_train,
                                                X_test, y_test, title,
                                                subplot)

        plt.tight_layout(pad=0.4, w_pad=0.5, h_pad=1.0)
```



1.6.2 Application of SVMs to a real dataset: unnormalized data

```
[32]: from sklearn.svm import SVC
X_train, X_test, y_train, y_test = train_test_split(X_cancer, y_cancer,
                                                    random_state = 0)

clf = SVC(C=10).fit(X_train, y_train)
print('Breast cancer dataset (unnormalized features)')
print('Accuracy of RBF-kernel SVC on training set: {:.2f}'
      .format(clf.score(X_train, y_train)))
print('Accuracy of RBF-kernel SVC on test set: {:.2f}'
      .format(clf.score(X_test, y_test)))
```

Breast cancer dataset (unnormalized features)
Accuracy of RBF-kernel SVC on training set: 0.92
Accuracy of RBF-kernel SVC on test set: 0.94

1.6.3 Application of SVMs to a real dataset: normalized data with feature preprocessing using minmax scaling

```
[33]: from sklearn.preprocessing import MinMaxScaler
scaler = MinMaxScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)

clf = SVC(C=10).fit(X_train_scaled, y_train)
print('Breast cancer dataset (normalized with MinMax scaling)')
print('RBF-kernel SVC (with MinMax scaling) training set accuracy: {:.2f}'
      .format(clf.score(X_train_scaled, y_train)))
print('RBF-kernel SVC (with MinMax scaling) test set accuracy: {:.2f}'
      .format(clf.score(X_test_scaled, y_test)))
```

Breast cancer dataset (normalized with MinMax scaling)
RBF-kernel SVC (with MinMax scaling) training set accuracy: 0.99
RBF-kernel SVC (with MinMax scaling) test set accuracy: 0.97

1.7 Cross-validation

1.7.1 Example based on k-NN classifier with fruit dataset (2 features)

```
[34]: from sklearn.model_selection import cross_val_score

clf = KNeighborsClassifier(n_neighbors = 5)
X = X_fruits_2d.values
y = y_fruits_2d.values
cv_scores = cross_val_score(clf, X, y)
```

```
print('Cross-validation scores (3-fold):', cv_scores)
print('Mean cross-validation score (3-fold): {:.3f}'
      .format(np.mean(cv_scores)))
```

```
Cross-validation scores (3-fold): [0.75 0.75 0.83 0.83 0.82]
Mean cross-validation score (3-fold): 0.797
```

1.7.2 A note on performing cross-validation for more advanced scenarios.

In some cases (e.g. when feature values have very different ranges), we've seen the need to scale or normalize the training and test sets before use with a classifier. The proper way to do cross-validation when you need to scale the data is *not* to scale the entire dataset with a single transform, since this will indirectly leak information into the training data about the whole dataset, including the test data (see the lecture on data leakage later in the course). Instead, scaling/normalizing must be computed and applied for each cross-validation fold separately. To do this, the easiest way in scikit-learn is to use *pipelines*. While these are beyond the scope of this course, further information is available in the scikit-learn documentation here:

<http://scikit-learn.org/stable/modules/generated/sklearn.pipeline.Pipeline.html>

or the Pipeline section in the recommended textbook: Introduction to Machine Learning with Python by Andreas C. Müller and Sarah Guido (O'Reilly Media).

1.8 Validation curve example

```
[35]: # We can see the effect of different values of parameter affects the accuracy,
      ↪ scores (in this case)
```

```
from sklearn.svm import SVC
from sklearn.model_selection import validation_curve

param_range = np.logspace(-3, 3, 4)
train_scores, test_scores = validation_curve(SVC(), X, y,
                                             param_name='gamma',
                                             param_range=param_range, cv=3)
```

```
[36]: print(train_scores)
      # We obtain a matrix of 4x3
      # 4 rows because of the 4 gamma values tested
      # 3 columns because of the 3 cross-folds, so we could calculate the mean and
      ↪ std deviation
```

```
[[0.46 0.44 0.42]
 [0.85 0.72 0.75]
 [0.92 0.9  0.93]
 [1.   1.   0.97]]
```

```
[37]: # We obtain the same for the test dataset
print(test_scores)
```

```
[[0.5  0.3  0.32]
 [0.85 0.7  0.63]
 [0.55 0.85 0.68]
 [0.4  0.2  0.37]]
```

```
[38]: # This code based on scikit-learn validation_plot example
# See: http://scikit-learn.org/stable/auto\_examples/model\_selection/plot\_validation\_curve.html
plt.figure()

train_scores_mean = np.mean(train_scores, axis=1)
train_scores_std = np.std(train_scores, axis=1)
test_scores_mean = np.mean(test_scores, axis=1)
test_scores_std = np.std(test_scores, axis=1)

plt.title('Validation Curve with SVM')
plt.xlabel('$\gamma$ (gamma)')
plt.ylabel('Score')
plt.ylim(0.0, 1.1)
lw = 2

plt.semilogx(param_range, train_scores_mean, label='Training score',
              color='darkorange', lw=lw)

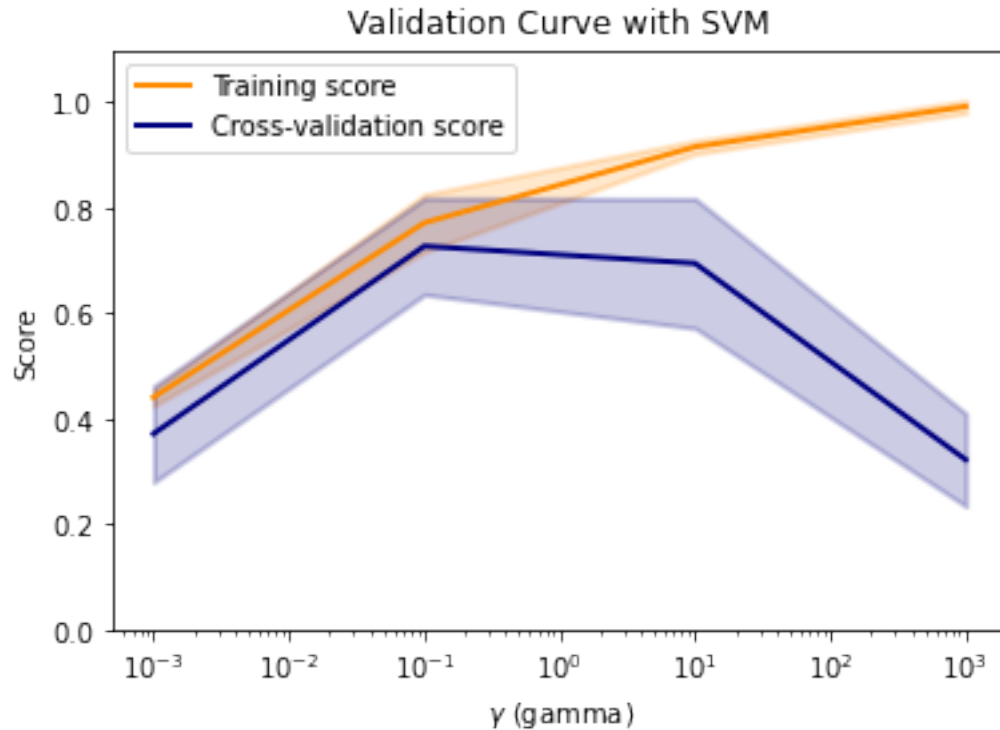
plt.fill_between(param_range, train_scores_mean - train_scores_std,
                 train_scores_mean + train_scores_std, alpha=0.2,
                 color='darkorange', lw=lw)

plt.semilogx(param_range, test_scores_mean, label='Cross-validation score',
              color='navy', lw=lw)

plt.fill_between(param_range, test_scores_mean - test_scores_std,
                 test_scores_mean + test_scores_std, alpha=0.2,
                 color='navy', lw=lw)

plt.legend(loc='best')
plt.show()

# We can see how the accuracy changes for the train and test datasets according
# to the different values of gamma chosen for the SVC model
```



1.9 Decision Trees

```
[39]: from sklearn.datasets import load_iris
from sklearn.tree import DecisionTreeClassifier
from adspy_shared_utilities import plot_decision_tree
from sklearn.model_selection import train_test_split

iris = load_iris()

X_train, X_test, y_train, y_test = train_test_split(iris.data, iris.target,
    random_state = 3)
clf = DecisionTreeClassifier().fit(X_train, y_train)

print('Accuracy of Decision Tree classifier on training set: {:.2f}'
      .format(clf.score(X_train, y_train)))
print('Accuracy of Decision Tree classifier on test set: {:.2f}'
      .format(clf.score(X_test, y_test)))
```

Accuracy of Decision Tree classifier on training set: 1.00

Accuracy of Decision Tree classifier on test set: 0.97

Setting max decision tree depth to help avoid overfitting

```
[40]: clf2 = DecisionTreeClassifier(max_depth = 3).fit(X_train, y_train)

print('Accuracy of Decision Tree classifier on training set: {:.2f}'
      .format(clf2.score(X_train, y_train)))
print('Accuracy of Decision Tree classifier on test set: {:.2f}'
      .format(clf2.score(X_test, y_test)))
```

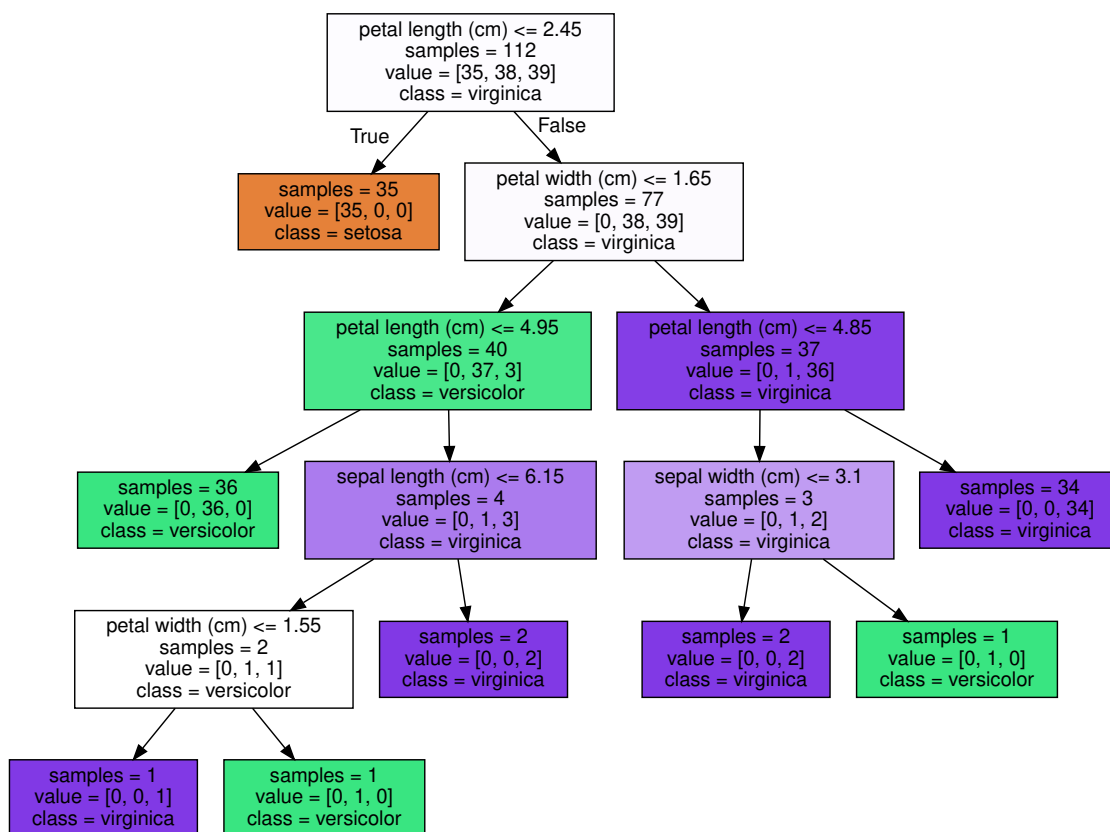
Accuracy of Decision Tree classifier on training set: 0.98

Accuracy of Decision Tree classifier on test set: 0.97

Visualizing decision trees

```
[41]: plot_decision_tree(clf, iris.feature_names, iris.target_names)
```

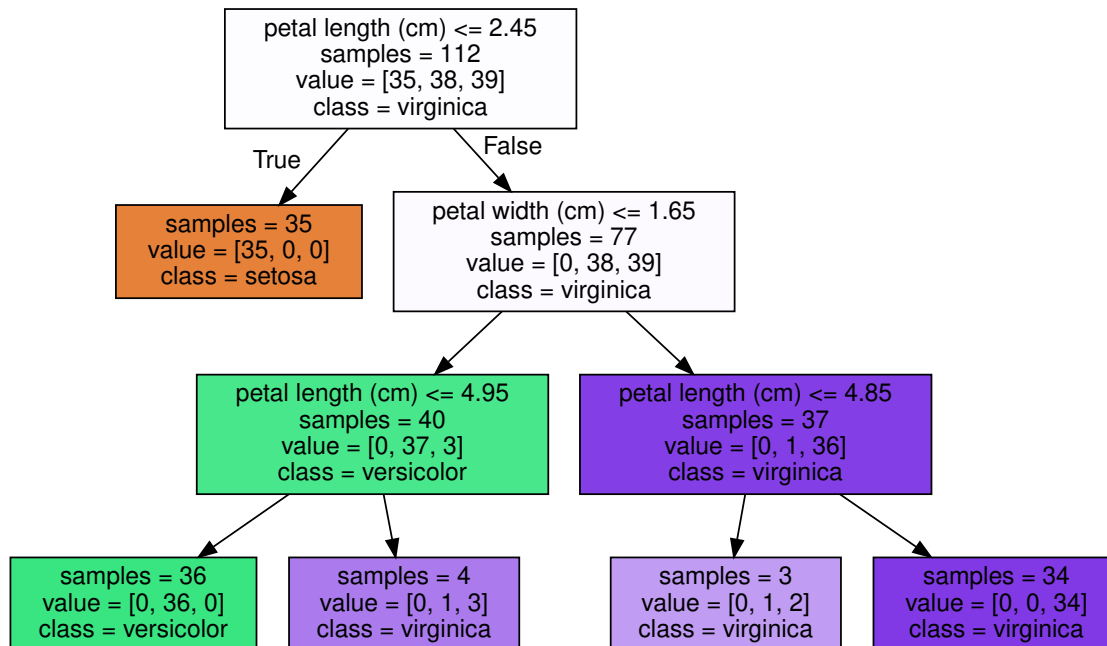
[41]:



Pre-pruned version (max_depth = 3)

```
[42]: plot_decision_tree(clf2, iris.feature_names, iris.target_names)
```

[42]:

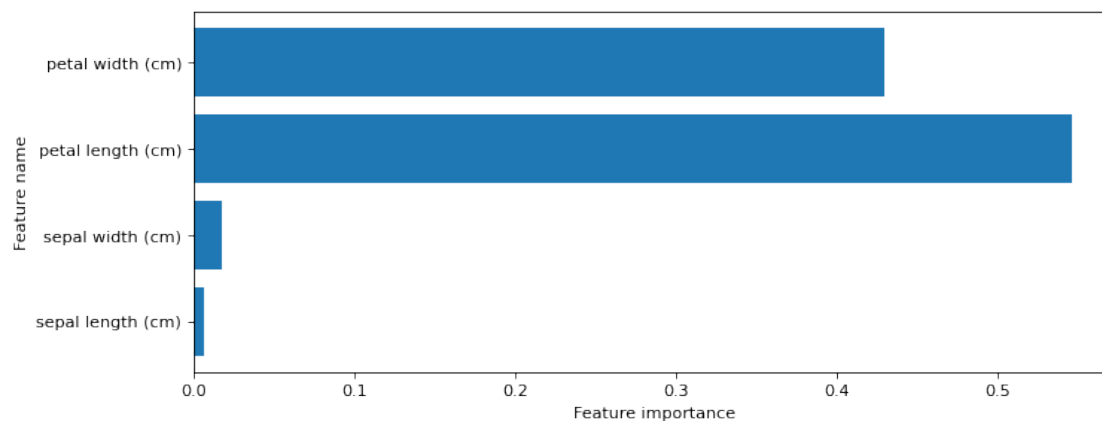


Feature importance

```
[43]: from adspy_shared_utilities import plot_feature_importances

plt.figure(figsize=(10,4), dpi=80)
plot_feature_importances(clf, iris.feature_names)
plt.show()

print('Feature importances: {}'.format(clf.feature_importances_))
```



Feature importances: [0.01 0.02 0.55 0.43]

```
[44]: from sklearn.tree import DecisionTreeClassifier
from adspy_shared_utilities import plot_class_regions_for_classifier_subplot

X_train, X_test, y_train, y_test = train_test_split(iris.data, iris.target,
    random_state = 0)
fig, subaxes = plt.subplots(6, 1, figsize=(6, 32))

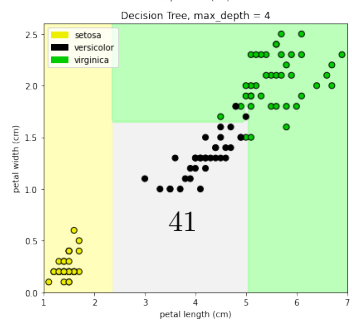
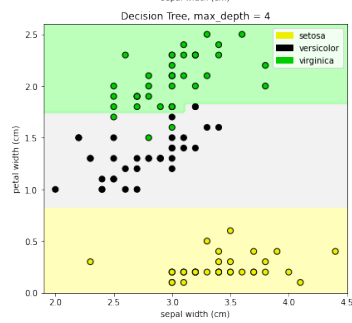
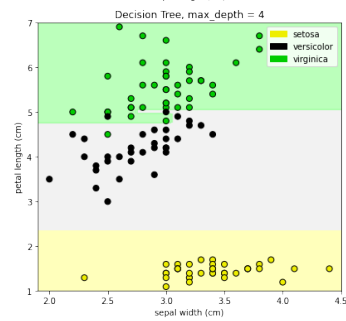
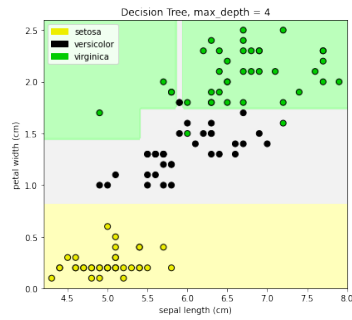
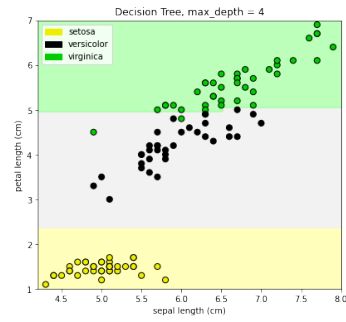
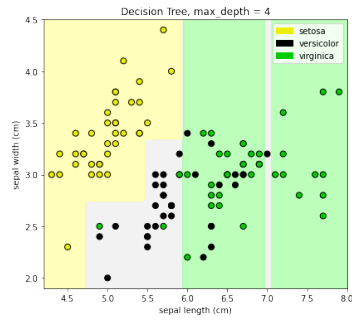
pair_list = [[0,1], [0,2], [0,3], [1,2], [1,3], [2,3]]
tree_max_depth = 4

for pair, axis in zip(pair_list, subaxes):
    X = X_train[:, pair]
    y = y_train

    clf = DecisionTreeClassifier(max_depth=tree_max_depth).fit(X, y)
    title = 'Decision Tree, max_depth = {:d}'.format(tree_max_depth)
    plot_class_regions_for_classifier_subplot(clf, X, y, None,
        None, title, axis,
        iris.target_names)

    axis.set_xlabel(iris.feature_names[pair[0]])
    axis.set_ylabel(iris.feature_names[pair[1]])

plt.tight_layout()
plt.show()
```

Decision Trees on a real-world dataset

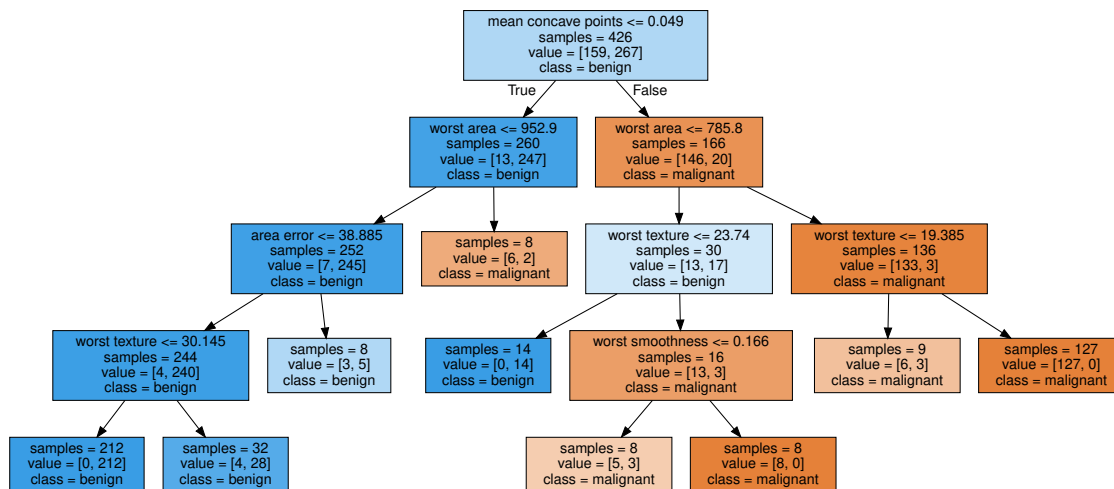
```
[45]: from sklearn.tree import DecisionTreeClassifier
from adspy_shared_utilities import plot_decision_tree
from adspy_shared_utilities import plot_feature_importances

X_train, X_test, y_train, y_test = train_test_split(X_cancer, y_cancer,
                                                    random_state = 0)

clf = DecisionTreeClassifier(max_depth = 4, min_samples_leaf = 8,
                             random_state = 0).fit(X_train, y_train)

plot_decision_tree(clf, cancer.feature_names, cancer.target_names)
```

[45]:



```
[46]: print('Breast cancer dataset: decision tree')
print('Accuracy of DT classifier on training set: {:.2f}'
      .format(clf.score(X_train, y_train)))
print('Accuracy of DT classifier on test set: {:.2f}'
      .format(clf.score(X_test, y_test)))

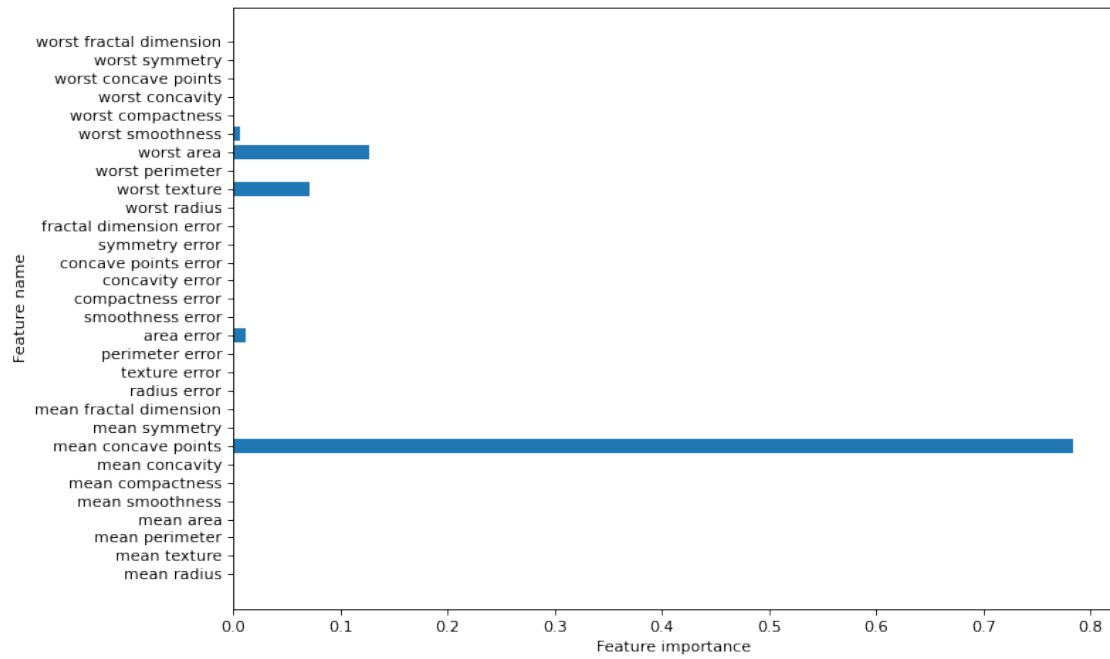
plt.figure(figsize=(10,6),dpi=80)
plot_feature_importances(clf, cancer.feature_names)
plt.tight_layout()

plt.show()
```

Breast cancer dataset: decision tree

Accuracy of DT classifier on training set: 0.96

Accuracy of DT classifier on test set: 0.94



[]: