

CS571: Programming Languages

1

List

Cs571 Programming Languages

2

List

List in Prolog similar to list in Haskell

```
|?- [H|T] = [1,2,3].
```

```
H = 1
```

```
T = [2,3].
```

```
No
```

```
| ?- [1|T] = [1,2,3].
```

```
T = [2,3].
```

```
no
```

Cs571 Programming Languages

3

List in Haskell vs Prolog

- Haskell:

- * A template for a **primitive recursive definition** over lists is:

```
f [] = ... (base case)
```

```
f (x:xs) = ... (recursive case)
```

- * **Question:** how to define $f(x:xs)$ from $f xs$.

- Prolog

- * A template for a **primitive recursive definition** over lists:

```
pred([], ...) (base case)
```

```
pred([H|T],...) (recursive case)
```

- * **Question:** how to define $\text{pred}([H|T],...)$ from $\text{pred}(T,...)$.

4

member

- Is a given integer in an integer list.

Haskell:

```
member a [] = False
```

```
member a (b:xs)
```

```
  | a == b = True
```

```
  | otherwise = member a xs
```

Prolog:

```
my_member(H, [H|_]).
```

```
my_member(X, [_|T]) :- my_member(X,T).
```

or

```
my_member(H, [H1|_]) :- H = H1.
```

```
my_member(X, [_|T]) :- my_member(X,T).
```

5

Example: my_member

- Is a given integer in a list.

```
my_member(H, [H|_]).
```

```
my_member(X, [_|T]) :- my_member(X,T).
```

- Testing membership

```
| ?- my_member(a, [a,b,a])
```

Cs571 Programming Languages

6

Example: my_member

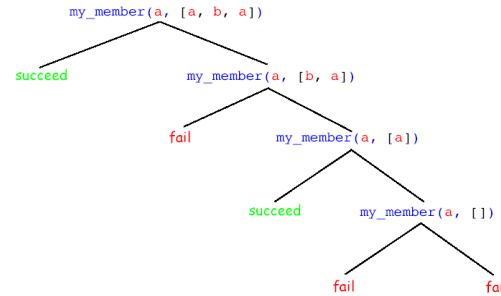
- Is a given integer in a list.
`my_member(H, [H|_T]).`
`my_member(X, [_|T]) :- my_member(X,T).`
- Testing membership
`| ?- my_member(a, [a,b,a])`
 yes

Cs571 Programming Languages

7

Derivations

```
my_member(H, [H | T]).
my_member(X, [_ | T]) :- my_member(X, T).
```



Cs571 Programming Languages

Example: my_member

- Is a given integer in a list.
`my_member(H, [H|_T]).`
`my_member(X, [_|T]) :- my_member(X,T).`
- Testing membership
`| ?- my_member(a, [a,b,a])`
 yes
- Enumerating members
`| ?- my_member(E, [a,b,a])`

Cs571 Programming Languages

9

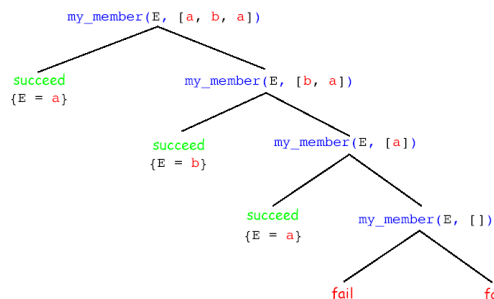
Example: my_member

- Is a given integer in a list.
`my_member(H, [H|_T]).`
`my_member(X, [_|T]) :- my_member(X,T).`
- Testing membership
`| ?- my_member(a, [a,b,a])`
 yes
- Enumerating members
`| ?- my_member(E, [a,b,a])`
`E = a.`
`E = b.`
`E = a.`
 no

10

Derivations

```
my_member(H, [H | T]).
my_member(X, [_ | T]) :- my_member(X, T).
```



Cs571 Programming Languages

11

= vs. ==

- Can we use `my_member` to check if a variable is in a list? E.g. `my_member(X, [Y,Z]).`
`my_member(H, [H|_T]).`
`my_member(X, [_|T]) :- my_member(X,T).`

Cs571 Programming Languages

12

= vs. ==

- Can we use `my_member` to check if a variable is in a list? E.g. `my_member(X, [Y,Z])`.

`my_member(H, [H|_T]).`

`my_member(X, [H|T]) :- my_member(X,T).`

No.

Revised `my_member`:

`my_member(H, [H1|_T]) :- H == H1.`

`my_member(X, [H|T]) :-`

`X \== H, my_member(X,T).`

13

Example: length

- Finding the length of a list

E.g. `length([1,2,3], X)` should return 3.

Haskell:

`length [] = 0`

`length (x:xs) = 1 + length xs`

Prolog:

Cs571 Programming Languages

14

Example: length

- Finding the length of a list

E.g. `length([1,2,3], X)` should return 3.

Haskell:

`length [] = 0`

`length (x:xs) = 1 + length xs`

Prolog:

`length([], 0).`

`length([H|T], N) :- length(T, N1), N is N1 + 1.`

15

Example: length

- Finding the length of a list

`length([], 0).`

`length([H|T], N) :-`

`length(T, N1), N is N1 + 1.`

- Testing the length

`| ?- length([a,b,c], 3).`

- Computing the length

`| ?- length([a,b,c], X).`

Cs571 Programming Languages

16

Example: length

- Finding the length of a list

`length([], 0).`

`length([H|T], N) :-`

`length(T, N1), N is N1 + 1.`

- Testing the length

`| ?- length([a,b,c], 3).`

yes

- Computing the length

`| ?- length([a,b,c], X).`

Cs571 Programming Languages

17

Example: length

- Finding the length of a list

`length([], 0).`

`length([H|T], N) :-`

`length(T, N1), N is N1 + 1.`

- Testing the length

`| ?- length([a,b,c], 3).`

yes

- Computing the length

`| ?- length([a,b,c], X).`

`X = 3.`

no

Cs571 Programming Languages

18

Example: append

- Append two lists:
 | ?- `append([1,2], [3,4], X)`
`X = [1,2,3,4].`
`no`
 | ?- `append(X, [3,4], [1,2,3,4])`
`X = [1,2].`
`No`

Cs571 Programming Languages

19

Example: append

- Append two lists:
 Haskell:
`append [] ys = ys`
`append (x:xs) ys = x: append xs ys`
 Prolog:

Cs571 Programming Languages

20

Example: append

- Append two lists:
 Haskell:
`append [] ys = ys`
`append (x:xs) ys = x: append xs ys`
 Prolog:
`append([], L, L).`
`append([H1|T1], L, Res) :-`
`append(T1, L, T2), Res = [H1|T2].`
`or`
`append([], L, L).`
`append([H1|T1], L, [H1|T2]) :- append(T1, L, T2).`

21

Example: Reverse a List

- `rev/2` finds the reverse of a given list
 e.g. `rev([1,2,3], X)` should succeed with `X = [3,2,1]`.
 what is the relationship between the reverse of `[1,2,3]`
 and the reverse of `[2,3]`

Cs571 Programming Languages

22

Example: Reverse a List

- `rev/2` finds the reverse of a given list
 e.g. `rev([1,2,3], X)` should succeed with `X = [3,2,1]`.
 what is the relationship between the reverse of `[1,2,3]`
 and the reverse of `[2,3]`
`rev([], []).`
`rev([X|Xs], Ys) :- rev(Xs, Zs), append(Zs, [X], Ys).`

23

Examples: my_last, last_but_one

- Find the last element of a list. Assume that the list contains at least one elements.
`?- my_last([a,b,c,d],X)`
`X = d`
- Find the last but one element of a list. Assume that the list contains at least two elements.
`?- last_but_one([a,b,c,d],X)`
`X = c`

Cs571 Programming Languages

24

Examples: my_last, last_but_one

- Find the last element of a list. Assume that the list contains at least one elements.
?- my_last([a,b,c,d],X)
X = d
- Find the last but one element of a list. Assume that the list contains at least two elements.
?- last_but_one([a,b,c,d],X)
X = c

my_last([X], X).
my_last([X,Y|Ys],Res) :- my_last([Y|Ys],Res).

Cs571 Programming Languages

25

Examples: my_last, last_but_one

- Find the last element of a list. Assume that the list contains at least one elements.
?- my_last([a,b,c,d],X)
X = d
- Find the last but one element of a list. Assume that the list contains at least two elements.
?- last_but_one([a,b,c,d],X)
X = c

my_last([X], X).
my_last([X,Y|Xs],Res) :- my_last([Y|Ys],Res).

last_but_one([X,_], X).
last_but_one([X,Y,Z|Ys],Res) :- last_but_one([Y,Z|Ys],Res).

Cs571 Programming Languages

26

Example: nth

- Find the nth element of a list ($N \geq 1$). Assume that the list contains at least N element.
?- nth([a,b,c,d],3,X)
X = c

Cs571 Programming Languages

27

Example: nth

- Find the nth element of a list ($N \geq 1$). Assume that the list contains at least N element.
?- nth([a,b,c,d],3,X)
X = c

nth([X|_],1,X).
nth([_|L],N,X) :-
N > 1, N1 is N - 1, nth(L,N1,X).

Cs571 Programming Languages

28

Example: dupli

- Duplicate the elements of a list
?- dupli([a,b],L)
L = [a,a,b,b]

Cs571 Programming Languages

29

Example: dupli

- Duplicate the elements of a list
?- dupli([a,b],L)
L = [a,a,b,b]

dupli([], []).
dupli([X|Xs],Res) :- dupli(Xs,Ys), Res=[X,X|Ys].
Or
dupli([], []).
dupli([X|Xs],[X,X|Ys]) :- dupli(Xs,Ys).

Cs571 Programming Languages

30

Example: inc_odd

- Define a prolog predicate `inc_odd(L,L1)` which increases every element occurring at the odd position of L and stores the result in L1.

E.g. | ?- `inc_odd([2,3,5,8],L)`.

L = [3,3,6,8].

no

Cs571 Programming Languages

31

Example: inc_odd

- Define a prolog predicate `inc_odd(L,L1)` which increases every element occurring at the odd position of L and stores the result in L1.

E.g. | ?- `inc_odd([2,3,5,8],L)`.

L = [3,3,6,8].

no

`inc_odd([],[]).`

`inc_odd([X],[X1]) :- X1 is X+1.`

`inc_odd([X,Y|Xs], [X1,Y|Res1]) :-`

`inc_odd(Xs, Res1),`

`X1 is X+1.`

32

Example: remove

- Remove the nth element from a list. If the list contains less than n elements, then return the list.

?- `remove([a,b,c,d],2,L)`

L = [a,c,d]

Cs571 Programming Languages

33

Example: remove

- Remove the nth element from a list. If the list contains less than n elements, then return the list.

?- `remove([a,b,c,d],2,L)`

L = [a,c,d]

`remove([],_,[]).`

`remove([_Xs],1,Xs).`

`remove([Y|Xs],N,[Y|Ys]) :-`

`N > 1,`

`N1 is N - 1,`

`remove(Xs,N1,Ys).`

Cs571 Programming Languages

34

If-then-else

Write a Prolog program `add(X,L1,L2)` that adds X to list L1 if X is not in L1, and stores the result in list L2.

`add(X,L1,L2) :-`

`(member(X,L1) -> L2 = L1`

`; L2 = [X|L1]`

`).`

`member(X,[H|_]) :- X==H.`

`member(X,[H|T]) :- member(X,T).`

Cs571 Programming Languages

35

Example: length

- Finding the length of a list

`length([], 0).`

`length([H|T], N) :- length(T, N1), N is N1 + 1.`

Using if-then-else:

Cs571 Programming Languages

36

Example: length

- Finding the length of a list
`length([], 0).`
`length([H|T], N) :- length(T, N1), N is N1 + 1.`

Using if-then-else:

```
length(L,N) :-
    (L == [] -> N is 0
    ;
     L = [_|T],
     length(T, N1),
     N is N1 + 1
    ).
```

Cs571 Programming Languages

37

Example: delete

- `delete(X, L1, L2)`: Removes all occurrences of X from list L1 and stores the result in L2
`?- delete(1, [2, 1, 3, 1, 4], L2).`
`L2 = [2, 3, 4]`

Cs571 Programming Languages

38

Example: delete

- `delete(X, L1, L2)`: Removes all occurrences of X from list L1 and stores the result in L2
`?- delete(1, [2, 1, 3, 1, 4], L2).`
`L2 = [2, 3, 4]`

```
delete(X, [], []).
delete(X, [_|T], Res) :- X == _, delete(X, T, Res).
delete(X, [_|T], [_|Res]) :- X \== _, delete(X, T, Res).
```

Using if-then-else:

```
delete(X, [], []).
delete(X, [_|T], Res) :- (X == _ -> delete(X, T, Res)
                          ; delete(X, T, Res1),
                            Res = [_|Res1]
                          ).
```

Cs571 Programming Languages

39

Example: split

- Write a prolog program `split(L, L1, L2)` that splits a list L into two lists L1 and L2 such that L1 contains all elements of L occurring at odd positions in L, and L2 contains all elements of L occurring at even positions in L. E.g.

```
?- split([1, 2, 4, 5, 6], L1, L2).
```

```
L1 = [1, 4, 6]
```

```
L2 = [2, 5].
```

```
no.
```

Cs571 Programming Languages

40

Example: split

- Write a prolog program `split(L, L1, L2)` that splits a list L into two lists L1 and L2 such that L1 contains all elements of L occurring at odd positions in L, and L2 contains all elements of L occurring at even positions in L. E.g.

```
?- split([1, 2, 4, 5, 6], L1, L2).
```

```
L1 = [1, 4, 6]
```

```
L2 = [2, 5].
```

```
no.
```

```
split([], [], []).
split([_], [_], []).
split([_|T], [_|L1], [_|L2]) :- split(T, L1, L2).
```

Cs571 Programming Languages

41

sum_odd

- Define a prolog predicate `sum_odd(L, L1)` which computes the sum of elements occurring at odd position L and store the result in L1. If the list is empty, then the sum is 0.

```
E.g. ?- sum_odd([2, 3, 4, 5, 6, 7, 8], L).
```

```
L = 20.
```

Cs571 Programming Languages

42

sum_odd

- Define a prolog predicate `sum_odd(L,L1)` which computes the sum of elements occurring at odd position L and store the result in L1. If the list is empty, then the sum is 0.

E.g. `?- sum_odd([2,3,4,5,6,7,8],L).`

`L = 20.`

```
sum_odd([],0).
sum_odd([X],X).
sum_odd([X,Y|Xs], Res) :-
    sum_odd(Xs, Res1),
    Res is X + Res1.
```

CS571 Programming Languages

43

splitn

- Define a prolog predicate `splitn(L,N,L1,L2)` to split a list L into two parts L1 and L2; the length of the first part is N.

`?- splitn([a,b,c,d,e,f,g,h,i,k],3,L1,L2).`

`L1 = [a,b,c]`

`L2 = [d,e,f,g,h,i,k].`

CS571 Programming Languages

44

splitn

- Define a prolog predicate `splitn(L,N,L1,L2)` to split a list L into two parts L1 and L2; the length of the first part is N.

`?- splitn([a,b,c,d,e,f,g,h,i,k],3,L1,L2).`

`L1 = [a,b,c]`

`L2 = [d,e,f,g,h,i,k].`

```
splitn(L,0,[],L).
splitn([X|Xs],N,L1,L2) :-
    N > 0, N1 is N - 1,
    splitn(Xs,N1,L3,L4),
    L1 = [X|L3], L2 = L4.
```

CS571 Programming Languages

45