

$$A_{ijk}^{cc} = \int_{\Omega} \underline{\underline{E}} \left[\underline{\underline{C}} : (\Delta \underline{\underline{F}}^T \underline{\underline{F}}) \right] : \delta \underline{\underline{F}} \, dV$$

$$= \int_{\Omega} \underline{\underline{F}} \left[\underline{\underline{C}}_{ijk} : (\Delta \underline{\underline{F}}^T \underline{\underline{F}})_{ij} \right] : \delta \underline{\underline{F}} \, dV$$

$$= \int_{\Omega} F_{io} \left[C_{ojm} : \Delta \hat{F}_{ki}^T F_{ki} \right] : \delta F_{km} \, dV$$

$$= \int_{\Omega} F_{io} \left[C_{ojkm} : \Delta F_{ki} F_{kj} \right] : \delta F_{km} \, dV$$

$$= \int_{\Omega_{ref}} F_{io} C_{ojkm} \hat{\Delta u}_{ki} N_{s,n} J_{r,i} F_{kj} \int_{\Omega_e} N_{p,q} J_{qm} \det J^{-1} \, dV$$

$$= \int_{\Omega_{ref}} F_{in} C_{nnop} N_{l,q} J_{qo} F_{kp} N_{j,r} J_{rn} \det J^{-1} \, dV$$

$$F_{ij}^{int} = \int_{\Omega} (\underline{\underline{F}} \underline{\underline{S}}) : \delta \underline{\underline{F}} \, dV$$

$$= \int_{\Omega} (F S)_{ij} : \delta F_{ij} \, dV$$

$$= \int_{\Omega} F_{ik} S_{ki} \delta F_{ij} \, dV$$

$$= \int_{\Omega} F_{ik} S_{ki} J_{il} N_{l,m} J_{mi} \det J^{-1} \, dV$$

$$= \int_{\Omega_{ref}} T_{ik} S_{kj} J_{ie} \cdot N_{e,m} J_{mj} \det J \, dV$$

$$= \int_{\Omega_{ref}} F_{ik} S_{kj} N_{i,m} J_{mj} \det J^{-1} \, dV$$