```
alpine:~/Projets/Homo<sup>2</sup>rphOS/SEAL/native/examples/build# ./bin/sealexamples
Microsoft SEAL version: 4.1.2
                                +-----+
| The following examples should be executed while reading |
                                                                | comments in
associated files in native/examples/.
                                  ----+
                     | Examples
                                        | Source Files
                                                          | 1. BFV Basics
1_bfv_basics.cpp
                               | 2. Encoders
                                                  2_encoders.cpp
                    4. BGV Basics
3. Levels
                | 3_levels.cpp
4_bgv_basics.cpp
                               | 5. CKKS Basics
                                                   | 5_ckks_basics.cpp
                   1
| 6. Rotation
                 |6_rotation.cpp |
                                                 7. Serialization
                              | 8. Performance Test | 8 performance.cpp
7 serialization.cpp
+-----+
                                                      [ 0 MB] Total allocation
                                                     > Run example (1 ~ 8) or exit
from the memory pool
                         +-----+ |
(0): 1
                                                            Example: BFV Basics
I +-----+ Line 132 --> Set encryption parameters and print
                  | Encryption parameters :
                                                | scheme: BFV
poly_modulus_degree: 4096
                             | coeff_modulus size: 109 (36 + 36 + 37) bits
| plain_modulus: 1024
                             \
                                                Parameter validation (success):
                        ~~~~ A naive way to calculate 4(x^2+1)(x+1)^2. ~~~~~
valid
Line 212 --> Express x = 6 as a plaintext polynomial 0x6.
                                                              Line 223 --> Encrypt
                                        + size of freshly encrypted x: 2
x_plain to x_encrypted.
budget in freshly encrypted x: 55 bits
                                                  + decryption of x encrypted: 0x6
                         Line 270 --> Compute x_sq_plus_one(x^2+1).
..... Correct.
+ size of x sq plus one: 3
                              + noise budget in x_sq_plus_one: 33 bits
+ decryption of x_sq_plus_one: 0x25 ...... Correct.
                                                         Line 300 --> Compute
x_plus_one_sq((x+1)^2).
                                         + size of x_plus_one_sq: 3
                                                                       + noise
budget in x_plus_one_sq: 33 bits
                                                + decryption of x_plus_one_sq:
0x31 ..... Correct.
                            Line 315 --> Compute encrypted_result
(4(x^2+1)(x+1)^2).
                              + size of encrypted_result: 5
                                                            + noise budget in
encrypted_result: 4 bits
                                      NOTE: Decryption can be incorrect if noise
budget is zero.
                                          ~~~~ A better way to calculate
4(x^2+1)(x+1)^2. ~~~~~
                                  Line 353 --> Generate relinearization keys.
Line 361 --> Compute and relinearize x squared (x^2),
                                                                    then
compute x_sq_plus_one (x^2+1)
                                               + size of x_squared: 3
                                                                           + size
of x squared (after relinearization): 2
                                                  + noise budget in x_sq_plus_one:
                         + decryption of x_sq_plus_one: 0x25 ..... Correct.
33 bits
Line 376 --> Compute x_plus_one (x+1),
                                           then compute and relinearize
x_plus_one_sq((x+1)^2).
                               + size of x_plus_one_sq: 3
                                                              + noise budget in
x_plus_one_sq: 33 bits
                                       + decryption of x_plus_one_sq: 0x31 .....
Correct.
                    Line 390 --> Compute and relinearize encrypted_result
(4(x^2+1)(x+1)^2).
                       + size of encrypted_result: 3 + size of encrypted_result
```

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NOTE: Notice the increase in remaining noise budget.
                                                           Line 407 -->
Decrypt encrypted_result (4(x^2+1)(x+1)^2).
                                                  + decryption of
4(x^2+1)(x+1)^2 = 0x54... Correct.
                                                          Line 425 --> An
example of invalid parameters
                                                           | Encryption
                 scheme: BFV
                                         | poly_modulus_degree: 2048
parameters:
coeff_modulus size: 109 (36 + 36 + 37) bits
                                                   | plain_modulus: 1024
                 Parameter validation (failed): parameters are not compliant with
HomomorphicEncryption.org security standard
  -----+
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                                              | 6_rotation.cpp
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                  | 7 serialization.cpp
                                                18. Performance Test
                               +-----+
8_performance.cpp
                   8 MB] Total allocation from the memory pool
Run example (1 \sim 8) or exit (0): 2
Example: Encoders | +-----+
                                        Example: Encoders / Batch
                        +-----+
Encoder I
| Encryption parameters :
                           | scheme: BFV
                                                    | poly_modulus_degree:
         | coeff_modulus size: 218 (43 + 43 + 44 + 44 + 44) bits
plain_modulus: 1032193
                                                              Batching
enabled: true
                   Plaintext matrix row size: 4096
                                                  Input plaintext matrix:
[ 0, 1, 2, 3, 0, ..., 0, 0, 0, 0, 0]
                                           [4, 5, 6, 7, 0, ..., 0, 0, 0, 0, 0]
Line 124 --> Encode plaintext matrix: + Decode plaintext matrix ..... Correct.
[ 0, 1, 2, 3, 0, ..., 0, 0, 0, 0, 0]
                                           [4, 5, 6, 7, 0, ..., 0, 0, 0, 0, 0]
Line 141 --> Encrypt plain_matrix to encrypted_matrix.
                                                            + Noise budget in
encrypted matrix: 146 bits
                                                      Second input plaintext
matrix:
                             [ 1, 2, 1, 2, 1, ..., 2, 1, 2, 1, 2]
                                                         Line 172 --> Sum,
1, 2, 1, 2, 1, ..., 2, 1, 2, 1, 2]
square, and relinearize. + Noise budget in result: 114 bits Line 187 --> Decrypt and
decode result. + Result plaintext matrix ..... Correct.
[ 1, 9, 9, 25, 1, ..., 4, 1, 4, 1, 4]
                                           [25, 49, 49, 81, 1, ..., 4, 1, 4, 1, 4]
+----+
                                                     Example: Encoders /
CKKS Encoder
                 | Encryption parameters : | scheme: CKKS
```

+ noise budget in encrypted_result: 11 bits

(after relinearization): 2

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poly_modulus_degree: 8192
                               | coeff_modulus size: 200 (40 + 40 + 40 + 40 + 40)
               ١
bits
                                                    Number of slots: 4096
Input vector:
                                            [0.000, 1.100, 2.200, 3.300]
                                   + Decode input vector ..... Correct.
Line 297 --> Encode input vector.
[-0.000, 1.100, 2.200, 3.300, ..., 0.000, -0.000, 0.000, -0.000]
Line 313 --> Encrypt input vector, square, and relinearize.
                                                                 + Scale in
squared input: 1.15292e+18 (60 bits)
                                                Line 333 --> Decrypt and decode.
+ Result vector ..... Correct.
                                                 [0.000, 1.210, 4.840, 10.890, ..., -
                                                  +-----
0.000, -0.000, -0.000, 0.0001
-----+
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                                                       [ 31 MB] Total allocation
                                                     > Run example (1 ~ 8) or exit
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       alpine:~/Projets/Homo<sup>2</sup>rphOS/SEAL/native/examples/build# pwd
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