

This Mathcad sheet will calculate the longitudinal (surge) force, lateral (sway) force and turning moment (yaw), based on Wang's paper. Below please input the ship particulars as required:

Length of Moored vessel (LBP), in feet:	$L \equiv 950$
Midship cross-sectional area of moored ship, in ft ² :	$A1 \equiv 3192$
Length of passing vessel (LBP), in feet:	$L_2 \equiv .5 \cdot L$
Midship cross-sectional area of passing ship, in ft ² :	$A2 \equiv 6413$
Water density, in slug/ft ³ :	$\rho \equiv 1.9905$
Passing ship velocity (incl. current), in feet/second:	$U \equiv 11.2$
Separation distance (from centerline to centerline), in feet:	$SEP_DIST \equiv .2 \cdot L$
Stagger distance (negative when passing ship behind moored ship), in feet:	$STA_DIST \equiv 0 \cdot L$
Water depth, in feet:	$D \equiv .1 \cdot L$

Results:

$$\begin{aligned}
 \textit{SurgeForce} &= 1.016 \times 10^{-11} \text{ in lbf} \\
 \textit{SwayForce} &= 7.644 \times 10^4 \text{ in lbf} \\
 \textit{YawMoment} &= 7.851 \times 10^{-9} \text{ in ft-lbf}
 \end{aligned}$$

Sectional area curves as functions of length, for both moored and passing ship (from Wang's paper):

$$S_1(x_1) \equiv \left(1 - \frac{4 \cdot x_1^2}{L^2}\right) \cdot A_1 \quad dS_1(x_1) \equiv \frac{d}{dx_1} S_1(x_1) \quad S_2(x_2) \equiv \left(1 - \frac{4 \cdot x_2^2}{L_2^2}\right) \cdot A_2 \quad dS_2(x_2) \equiv \frac{d}{dx_2} S_2(x_2)$$

$$F(x_1, \xi, \eta) \equiv \int_{-\frac{L_2}{2}}^{\frac{L_2}{2}} \frac{dS_2(x_2) \cdot (x_2 - x_1 + \xi)}{\left[(x_2 - x_1 + \xi)^2 + \eta^2\right]^{\frac{3}{2}}} dx_2$$

$$G(x_1, \xi, \eta) \equiv \int_{-\frac{L_2}{2}}^{\frac{L_2}{2}} \frac{dS_2(x_2)}{\left[(x_2 - x_1 + \xi)^2 + \eta^2\right]^{\frac{3}{2}}} dx_2$$

$$\text{Wang_Surge}(\xi, \eta) \equiv \frac{\rho \cdot U^2}{2 \cdot \pi} \cdot \int_{-\frac{L}{2}}^{\frac{L}{2}} dS_1(x_1) \cdot F(x_1, \xi, \eta) dx_1 \quad \text{surge force formulation for infinite depth}$$

$$\text{Wang_Sway}(\xi, \eta) \equiv \frac{\rho \cdot U^2 \cdot \eta}{\pi} \cdot \int_{-\frac{L}{2}}^{\frac{L}{2}} dS_1(x_1) \cdot G(x_1, \xi, \eta) dx_1 \quad \text{sway force formulation for infinite depth}$$

$$\text{Wang_Yaw}(\xi, \eta) \equiv \frac{\rho \cdot U^2 \cdot \eta}{\pi} \cdot \int_{-\frac{L}{2}}^{\frac{L}{2}} \left[(dS_1(x_1) \cdot x_1 + S_1(x_1)) \cdot G(x_1, \xi, \eta) \right] dx_1 \quad \text{yaw moment formulation for infinite depth}$$

$$\eta(\eta, h, n) \equiv \sqrt{\eta^2 + 4 \cdot n^2 \cdot h^2} \quad \text{separation distance parameter as a function of finite depth}$$

$$\text{Wang_Surge_Depth}(\xi, \eta, h) \equiv \sum_{n=-10}^{10} \text{Wang_Surge}(\xi, \eta(\eta, h, n))$$

surge force as a function of
finite depth

$$\text{Wang_Sway_Depth}(\xi, \eta, h) \equiv \eta \cdot \sum_{n=-10}^{10} \frac{\text{Wang_Sway}(\xi, \eta(\eta, h, n))}{\eta(\eta, h, n)}$$

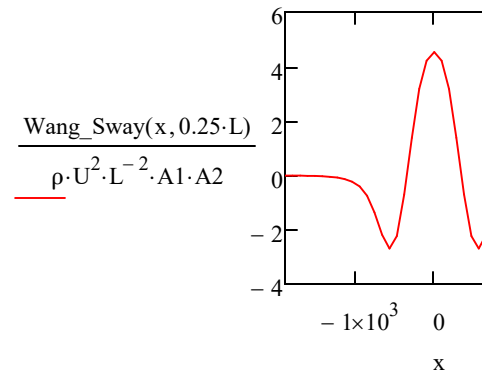
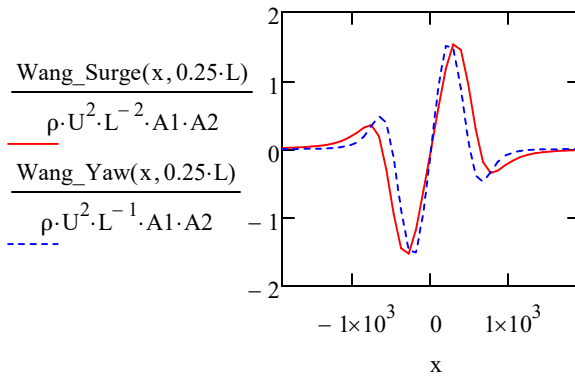
sway force as a function of
finite depth

$$\text{Wang_Yaw_Depth}(\xi, \eta, h) \equiv \eta \cdot \sum_{n=-10}^{10} \frac{\text{Wang_Yaw}(\xi, \eta(\eta, h, n))}{\eta(\eta, h, n)}$$

yaw moment as a function of
finite depth

Plots of Surge, Sway and Yaw forces and moments for separation distance of 0.25xL for infinite water depth:

$$x := -2 \cdot L, -1.9 \cdot L \dots 2 \cdot L$$



$$\frac{\text{Wang_Sway}(0, 0.25 \cdot L)}{\rho \cdot U^2 \cdot L^{-2} \cdot A1 \cdot A2} = 4.534$$

$$\text{SurgeForce} \equiv \text{Wang_Surge_Depth}(\text{STA_DIST}, \text{SEP_DIST}, D)$$

$$\text{SwayForce} \equiv \text{Wang_Sway_Depth}(\text{STA_DIST}, \text{SEP_DIST}, D)$$

$$\text{YawMoment} \equiv \text{Wang_Yaw_Depth}(\text{STA_DIST}, \text{SEP_DIST}, D)$$

