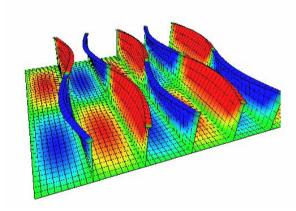
DNV's PULS buckling code Panel Ultimate Limit State

New Computerized Buckling Code

Non-linear plate theory



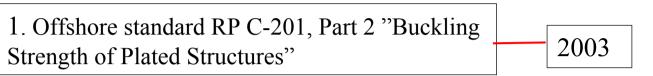
Developed by: DNV Maritime/Section for Hydrodynamics and Structures (mtpno361) Responsible DNV Unit for maintenance/sale: DNV Software

Presentation overview

PULS buckling code

- DNV buckling rules and standards
- Why a new buckling code?
- Theoretical foundation
- PULS element library
- PULS features
- Demonstration of programme
- Practical exercise

PULS implementation in the Rules and Standards



2. Steel Ship Rules, Part 3 Ch.1, (1A1) "Hull Structural design - Ships with length 100 meters and above", Sec.13, D Panel Ultimate strength, ESP additional notation

January 2004

3. LAN (Lloyds/ABS/DNV) common scantlings project for tankers.

2004

PULS in the new Recommended Practice (RP)

Recommended Practice DNV-RP-C201

Buckling Strength of Plated Structures October 2002



Conventional buckling code

Updated CN30.1

Semi-empirical

Part 2:

PULS (Panel Ultimate Limit State)

Computerized buckling code

Semi-analytical | Non-linear light

Recommended Practice RP C-201

- The RP C-201 was released early 2003, and replaces the old Classification Note 30.1 (CN30.1)
- The RP is a supporting document for the DNV Offshore Standards describing two equally acceptable approaches for calculating the buckling capacity of flat plated structures
- The RP contains two separate sections
 - Section one covers updating of the "old" Class Note 30.1 with respect to buckling of plates and girders
 - Section two covers the new buckling code PULS
- The curved shell part from CN 30.1 has been placed in a separate RP, RP C-202

Why a new buckling code?

) Ship Rule formulas predicts buckling imit ..not Ultimate Strength

IACS, DNV, Lloyds, ABS has decided to use Ultimate Limit State Principles in new Unified Requirements and Rules currently up for revision

Time for undeting rules and implement

Present Buckling Rules are "Rule book"

plutions – initial scantling assessment

i) Time for updating rules and implement nodern ULS design principles using irectly recognized buckling and non-

Designers will mostly use PC tools in design
PULS "non-linear light" gives immediate results

near postbuckling theory

OFTWADE

Modern design principles shall be based on Ultimate strength/ULS design principles



ULS design principles are the only feasible concept for estimating safety margins against failure



Present Buckling Rules are not consistent for use towards linear global FE analysis results, combined loads, bi-axial compression, shear etc. ⇒ final scantling assessment



Programming non-linear plate/shell models;

PULS = "Non-linear light"

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Computerized buckling code based on "Non-linear light" theory easily implemented into spreadsheets, etc.

Why new buckling code

PULS approach: Direct application of recognized non-linear plate theory

"Non-linear light theories"

Fast and easy

- Buckling and ULS estimates of panels very complex technical issue for combined load situations
- Direct method gives more realistic buckling estimates Improved safety control
- Buckling Model and Theory Framework "in house"
- Transparent recognized non-linear text book theory as basis
- More data output 3D graphics for improved understanding of buckling failure mechanism

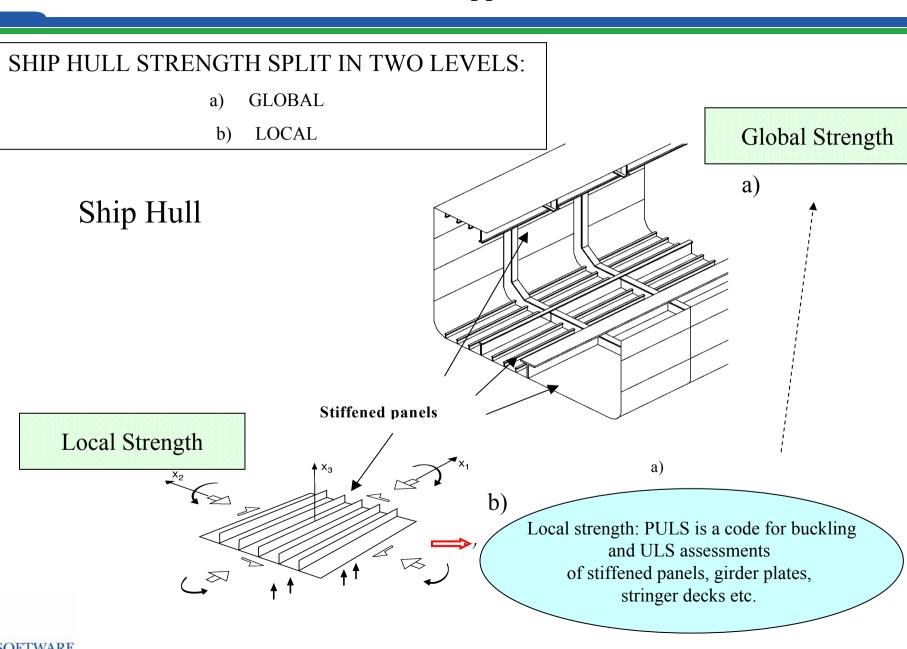


Best approach for optimal use of steel per defined target safety

Robust design

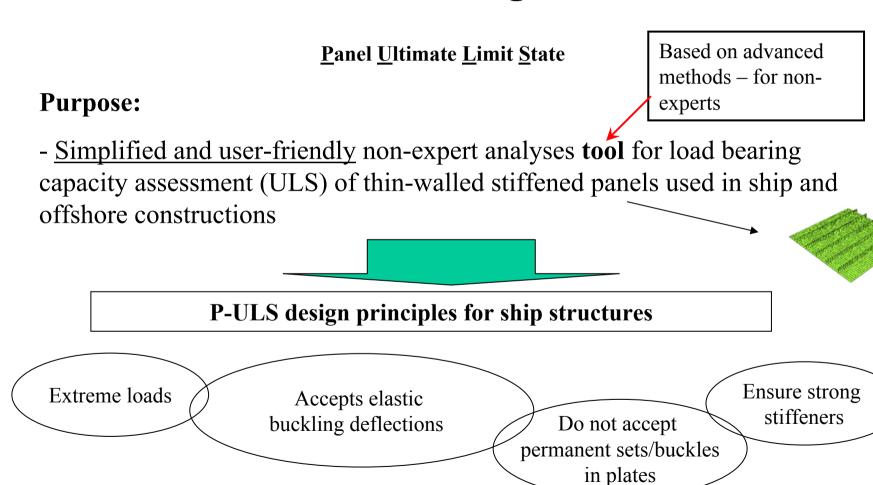
Improved Safety control

PULS: Area of application



PULS code principles

PULS Buckling code



OFTWAD

PULS code principles

PULS Buckling code

- Assessment of <u>ultimate</u> load bearing capacity of stiffened panels as strength measure. Max load capacity nonlinear analysis
- Assessment of buckling limit of stiffened panels to be used in cases where construction elements are not allowed/recommended to buckle elastically: Ensures more steel. Buckling limit also relevant for functional requirements (SLS). Linearized analysis (Eigenvalues)
- Consider all types of load combinations (bi-axial, shear, tension/compression and lateral pressure) as consistent with output from linear FE hull/Nauticus models

PULS code principles

PULS Buckling code

Programme language:

- Fortran 95: All calculations (solving equilibruim equations, incrementation...)
- Visual Basic: User interface
- VB PulsComClasses.dll file for easy plug in different User Interfaces

PULS Stand alone programs: 2 versions – Explorer and Excel

Available from DNV Software Web site download/time limited free lisence

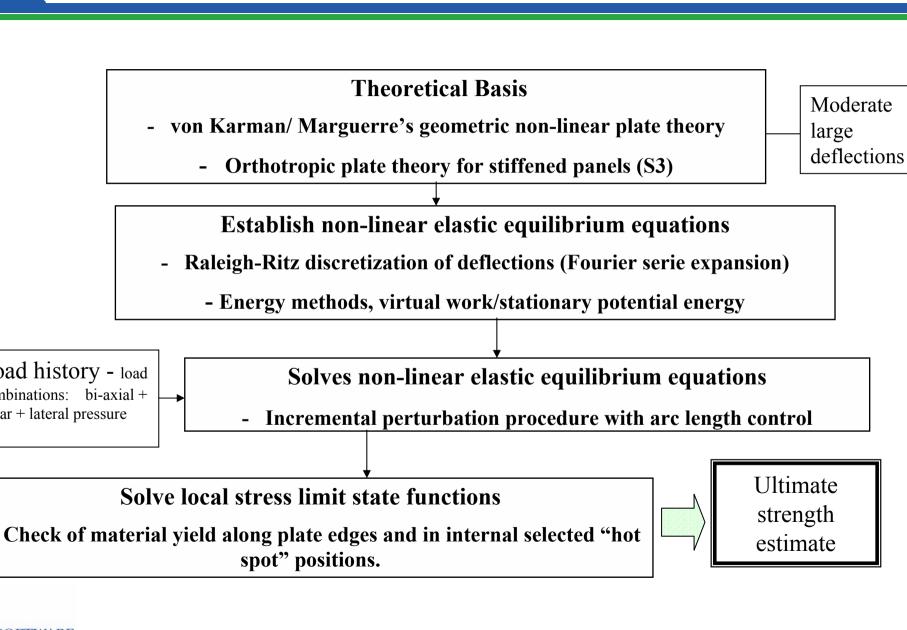
(2 versions: Explorer and Excel versions apply same input file for easy use)

Nauticus Software:

Section
Scantling/different

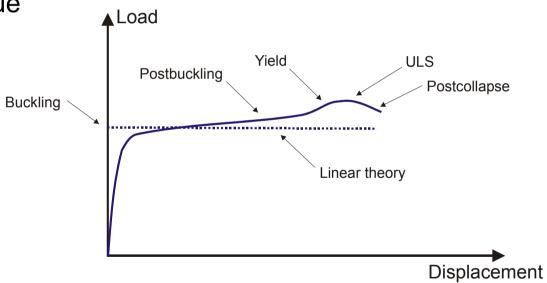
FE Rule Packages

Theoretical foundation: Overview

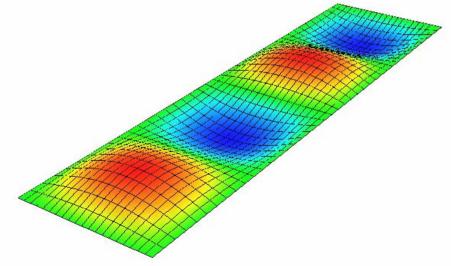


Buckling:

- Linear buckling / Eigenvalue
- Postbuckling, nonlinear
- Ultimate limit state
- Postcollapse



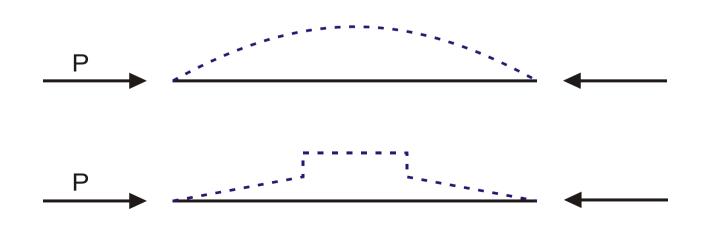
- Deflections represented by trigonometric functions, defined over the entire geometry
 - Buckling deflections tend to be periodic
 - Need very few dof compared to FEM
 - Any shape can be represented by applying sufficiently many terms



Principle of stationary potential energy:

$$\delta\Pi = \delta U + \delta T = 0$$

Intuitively: The structure adjusts itself to the shape that requires the least energy



OFTWAL

Large deflection plate theory, membrane strains (von Karman / Marguerre):

$$\varepsilon_{x} = u_{,x} + \frac{1}{2}w_{,x}^{2} + w_{0,x}w_{,x}$$

$$\varepsilon_{y} = v_{,y} + \frac{1}{2}w_{,y}^{2} + w_{0,y}w_{,y}$$

$$\gamma_{xy} = u_{,y} + v_{,x} + w_{,x}w_{,y} + w_{0,x}w_{,y} + w_{,x}w_{0,y}$$

Total strain found by adding the bending strains according to the Love-Kirchoff assumption:

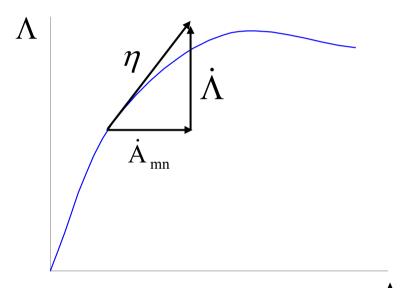
$$\varepsilon_{ij}^{tot} = \varepsilon_{ij} - zw_{,ij}$$

Incremental solution procedure:

- Linearization reduce equation system to 1. order
- Arc-length incrementation

$$\dot{A}_{mn} = \frac{\partial A_{mn}}{\partial n} \qquad \dot{\Lambda} = \frac{\partial \Lambda}{\partial n}$$

$$A_{mn}^{i} = A_{mn}^{i-1} + \eta \dot{A}_{mn}^{i-1}$$
$$\Lambda^{i} = \Lambda^{i-1} + \eta \dot{\Lambda}^{i-1}$$



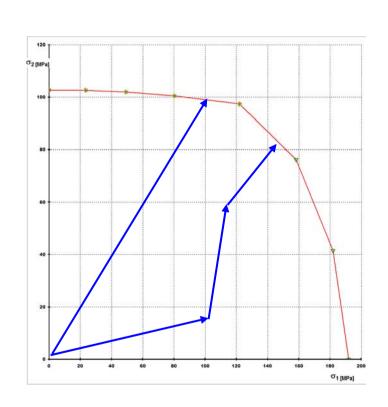
 \mathbf{A}_{mn}

OFTWADE

Staging:

- Assume piecewise linear load path
- Number of load parameters reduced to one

$$P_i(\Lambda) = P_i^{s-1} + \Lambda(P_i^s - P_i^{s-1})$$

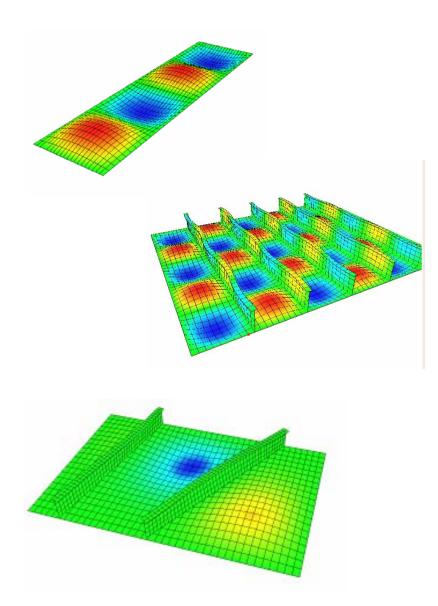


PULS element library: Overview

• U3: Unstiffened plate element

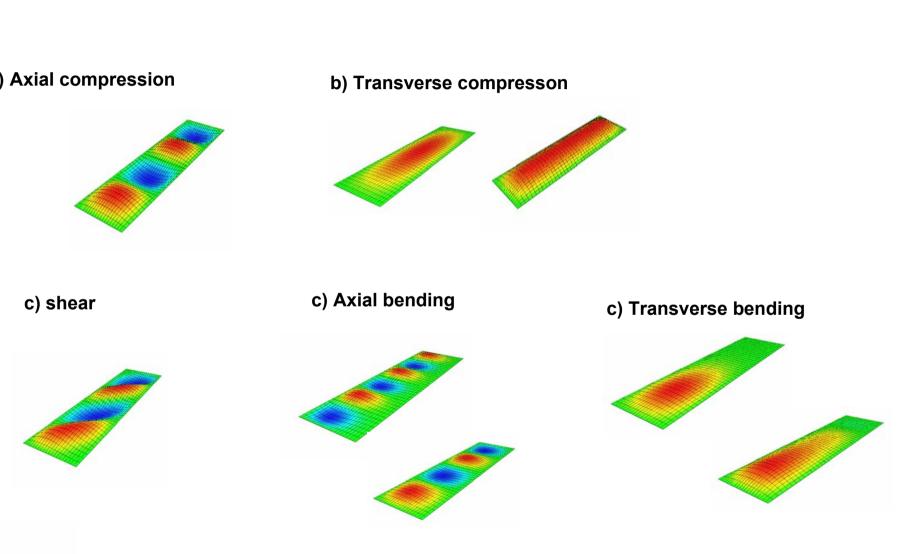
• S3: Stiffened plate element

• T1: Stiffened plate element (non-regular geometry)



Unstiffened plate (U3)

Typical buckling modes in unstiffened plate



OFTWAD

Unstiffened plate: Theoretical model

Buckling mode Deflection:

Raleigh - Ritz discretizations, Fourier expansion

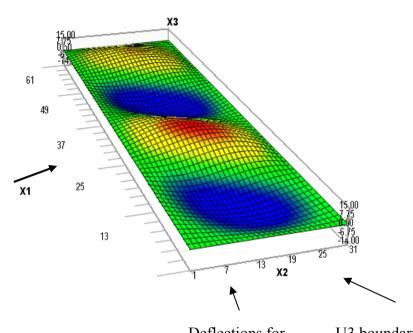
$$w(x,y) = \sum_{m} \sum_{n} A_{mn} \sin(\frac{m\pi x}{a}) \sin(\frac{n\pi y}{b})$$

$$w_0(x,y) = \sum_{m} \sum_{n} B_{mn} \sin(\frac{m\pi x}{a}) \sin(\frac{n\pi y}{b})$$

Von Mises
membrane stress
distribution

x1

25



Deflections for combined load case- bending + shear

- U3 boundary conditions:
- i) simply supported out of plane along all edges
- ii) straight but moveable inplane edges (2D-integrated element)

OTTTALA

Unstiffened plate (U3): Areas of application

- Ultimate Capacity: Integrated elements (deck, ship side, ship bottom, bulkheads etc)
- Buckling Capacity: Other elements such as girders and stringers. Elastic buckling (eigenvalue cut-off) and yield squash are upper limits

Ultimate strength
=
Redistribution of stresses

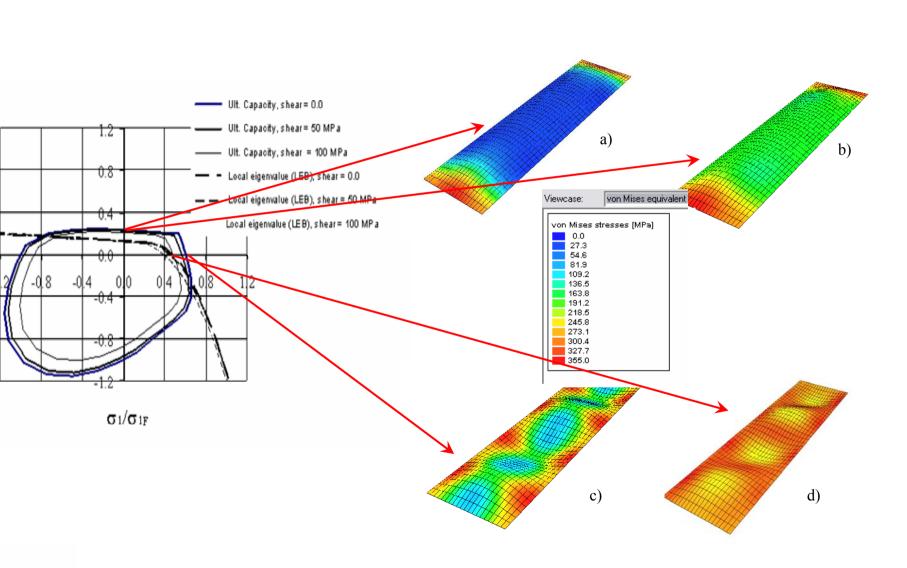
Validity range:

Aspect ratio limit: $L_1/L_2 < 20$ for $L_1 > L_2$ (or equivalent $L_2/L_1 < 20$ for $L_1 < L_2$)

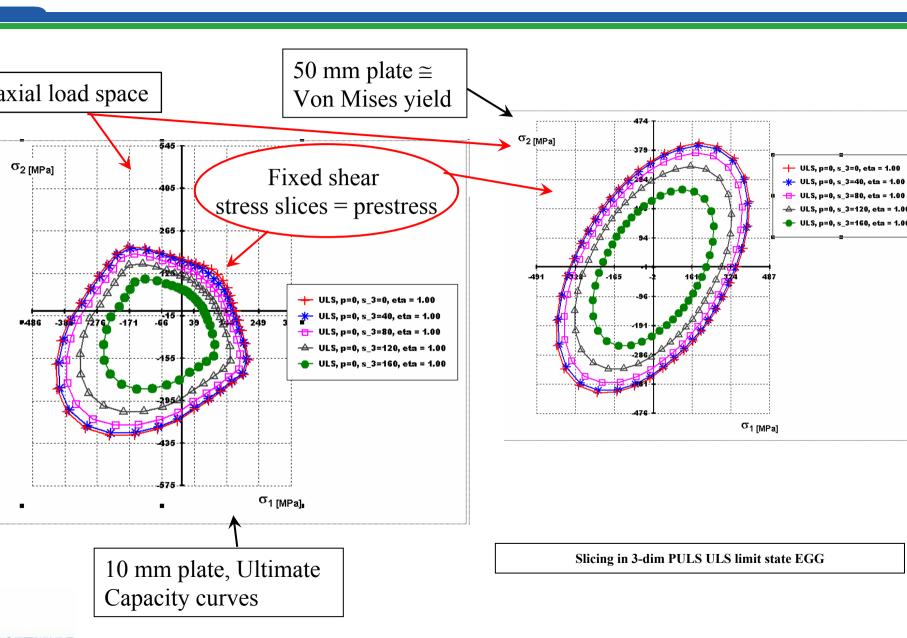
Plate slenderness ratio: $L_i/t_p < 200 (L_i = minimum of L_1 and L_2)$

OFTWAR

Example: Unstiffened plate, combined loads (U3)



Example: Unstiffened plate, Capacity curves for combined loads



Example: Unstiffened plate, axial compression (U3)

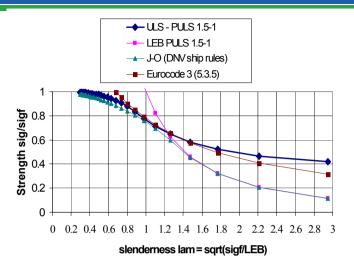
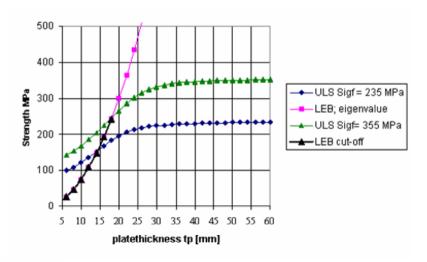
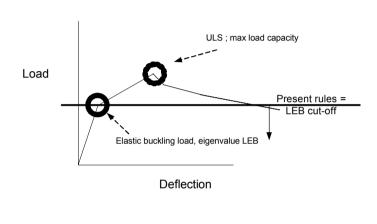
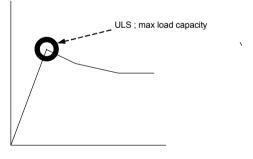


Fig.1 Comparisons between codes: Unstiffened plate in axial compression DNV ship rules, Eurocode 3, PULS 1.5-1 code; U1-unstiffened plate, ULS and elastic eigenvalue LEB Case: Sigf = 235 MPa, E = 208000 Mpa, ny = 0.3, L = 4000 mm, s = 1000 mm, variable platethickness







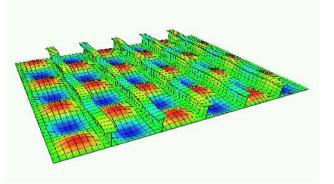
Stiffened panel (S3)

Typical buckling modes in stiffened panels

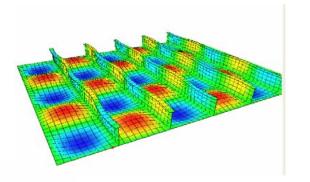
PULS buckling code

) Weak/thin plate - strong stiffener sideways: thin

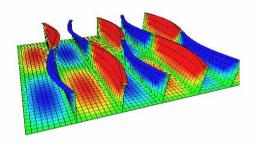
late/wide stiffenerflange



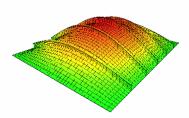
a) + b) effekt interacting



b) Weak stiffener sideways/torsional: High stiffener/small flange

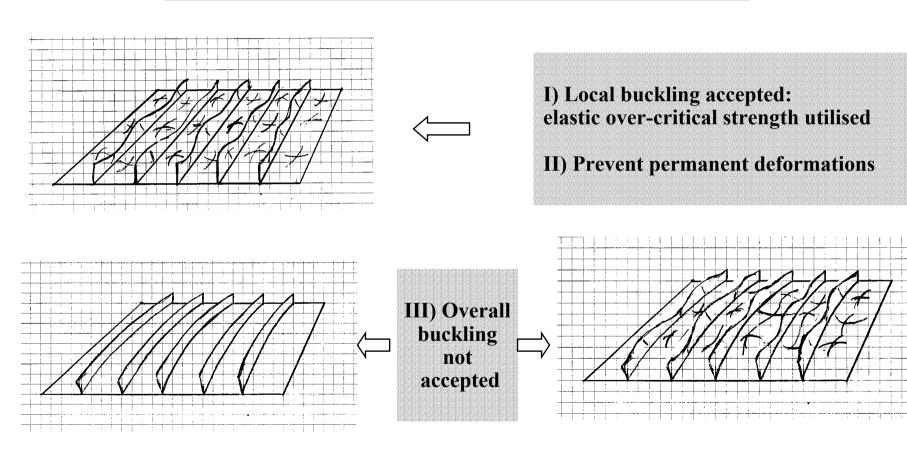


c) Weak stiffener out-of-plane: Low stiffener height/long span/small flange: prevented by PULS design principles



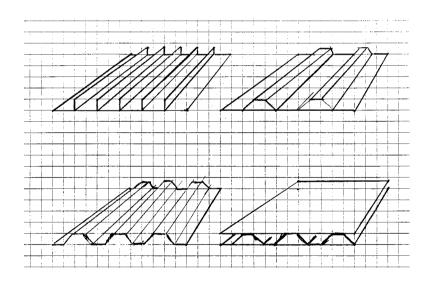
Stiffened panel (S3): Principles

PULS - ULS design principles – S3 element



Stiffened panel (S3): Principles

S3 element Stiffened Panel model = equivalent orthotropic material



Macro material law

$$\begin{bmatrix} \Delta \overline{N}_1 \\ \Delta \overline{N}_2 \\ \Delta \overline{N}_3 \\ \Delta \overline{M}_1 \\ \Delta \overline{M}_2 \\ \Delta \overline{M}_3 \end{bmatrix} = \begin{bmatrix} C_{11} & C_{12} & C_{13} & Q_{11} & Q_{12} & Q_{13} \\ C_{21} & C_{22} & C_{23} & Q_{21} & Q_{22} & Q_{23} \\ C_{31} & C_{32} & C_{33} & Q_{31} & Q_{32} & Q_{33} \\ Q_{11} & Q_{21} & Q_{31} & D_{11} & D_{12} & D_{13} \\ Q_{12} & Q_{22} & Q_{32} & D_{21} & D_{22} & D_{23} \\ Q_{13} & Q_{23} & Q_{33} & D_{31} & D_{32} & D_{33} \end{bmatrix} \begin{bmatrix} \Delta \epsilon_1 \\ \Delta \epsilon_2 \\ \Delta \epsilon_3 \\ \Delta \kappa_1 \\ \Delta \kappa_2 \\ \Delta \kappa_3 \end{bmatrix}$$

$$Q_{11}^{L} = -E \frac{S_s N}{L_2}$$

Coupling bending/membrane

$$D_{11}^{L} = \frac{E t^{3}}{12(1 - v^{2})} \left[1 + 12(1 - v^{2}) \frac{I_{s} N}{L_{2} t^{3}} \right]$$

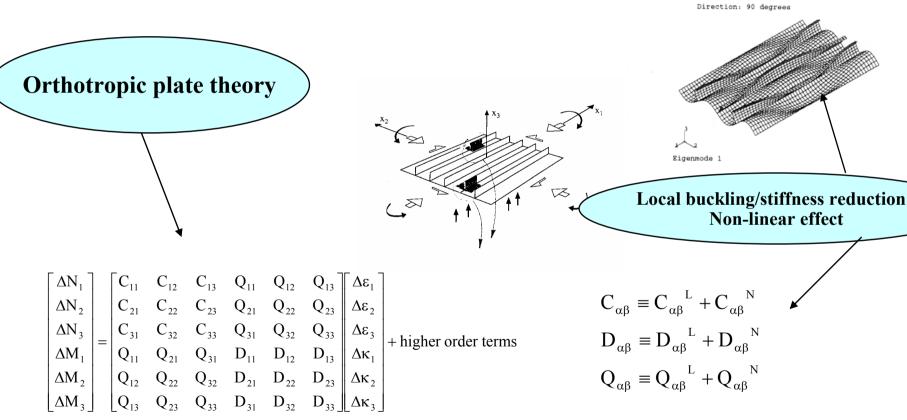
bending

$$D_{11}^{L} = \frac{E t^{3}}{12(1 - v^{2})} \left[1 + 12(1 - v^{2}) \frac{I_{s}N}{L_{2}t^{3}} \right] \qquad C_{11}^{L} = \frac{E t}{1 - v^{2}} \left[1 + (1 - v^{2}) \frac{A_{s}N}{L_{2}t} \right]$$

Stiffened panel (S3): Principles

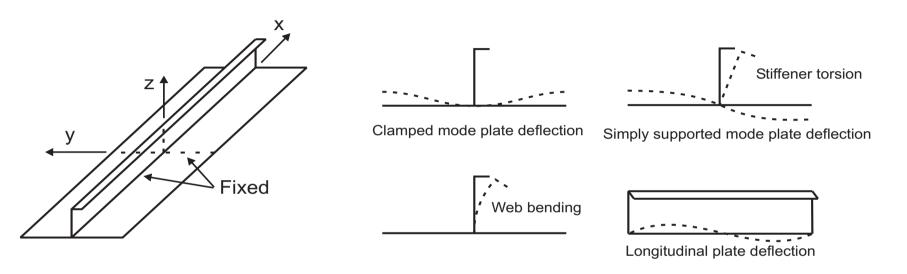
S3 element: Orthotropic Macro Material -

Reduction of stiffness coefficients due to local plate/stiffener buckling



OFTWAD

Stiffened panel (S3): Local buckling modes



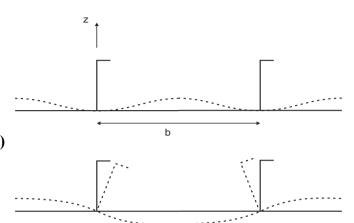
- Local buckling: Assume no vertical deflection of stiffener
- Ship design: Stocky stiffeners, local buckling accepted but global deflection is unwanted

OFTWAR

Stiffened panel (S3): Local buckling modes

Plate deflection:

$$w_{1}(x,y) = \sum_{m=1}^{M_{S}} \sum_{n=1}^{N_{S}} A_{mn}^{s} \sin(\frac{m\pi x}{a}) \sin(\frac{n\pi y}{b}) + \sum_{m=1}^{M_{C}} \sum_{n=1}^{N_{C}} \frac{A_{mn}^{c}}{2} \sin(\frac{m\pi x}{a}) (1 - \cos(\frac{2n\pi y}{b}))$$



Stiffener deflection:

$$v(x) = \frac{z}{h} \sum_{m=1}^{Ms} V_{1m} \sin(\frac{m\pi x}{a}) + (1 - \cos(\frac{\pi z}{2h})) \sum_{m=1}^{Ms} V_{2m} \sin(\frac{m\pi x}{a})$$



Stiffened panel (S3): Local model assumptions

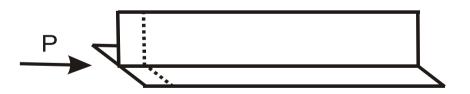
Rotational continuity

$$\frac{\partial \mathbf{v}}{\partial \mathbf{z}}\Big|_{\mathbf{z}=\mathbf{0}} = \frac{\partial \mathbf{w}}{\partial \mathbf{y}}\Big|_{\mathbf{v}=\mathbf{0}}$$



Longitudinal continuity

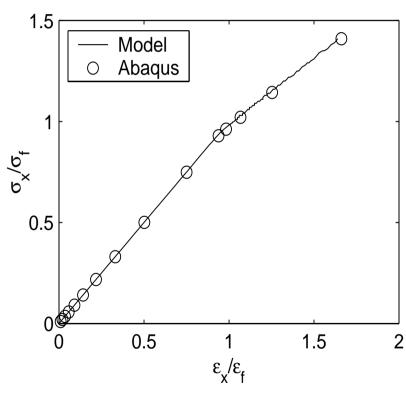
$$\int_{a} u_{,x}^{p} dx = \int_{a} u_{,x}^{s} dx$$

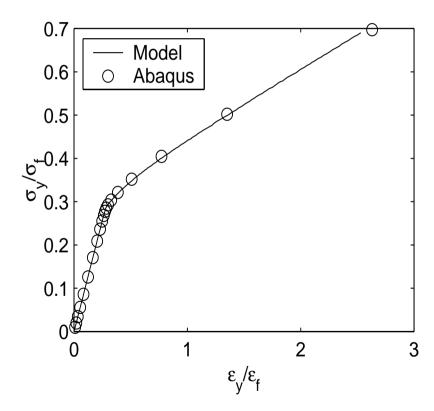


OFTWAL

Stiffened panel (S3): Local model - validation

Angle bar stiffener, from bulk carrier bottom:



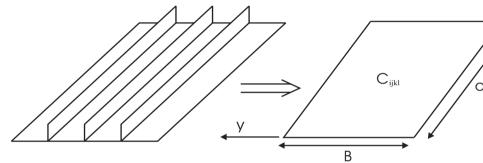


Axial load

Transverse load

Stiffened panel (S3): Global buckling model

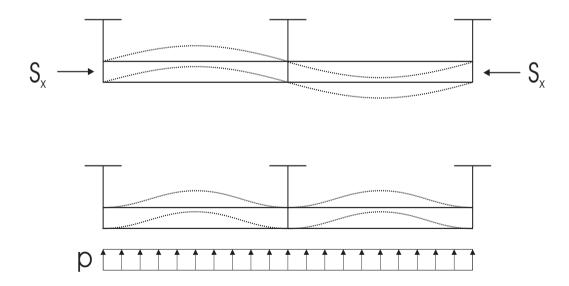
- Anisotropic plate model
 - Structural anisotropic stiffness derived from local analysis
- One-way interaction from local to global



Stiffened panel (S3): Global deflection modes

Deflection shape:
$$W_g(x,y) = \sum_{m=1}^{Ms} \sum_{n=1}^{Ns} A_{mn}^s \sin(\frac{m \pi x}{a}) \sin(\frac{n \pi y}{b}) + \sum_{m=1}^{Mc} \sum_{n=1}^{Nc} \frac{A_{mn}^c}{2} (1 - \cos(\frac{2m \pi x}{a})) \sin(\frac{n \pi y}{B})$$

Clamped mode accounts for lateral pressure



OFTWAL

Stiffness reduction due to local buckling

Global incremental forcedisplacement relation:

$$\Delta N_i = C_{ij} \Delta \varepsilon_j$$

Stiffness coefficients:

$$C_{ij} = \frac{\partial N_i}{\partial \varepsilon_i} = C_{ij}^L + C_{ij}^{NL}$$

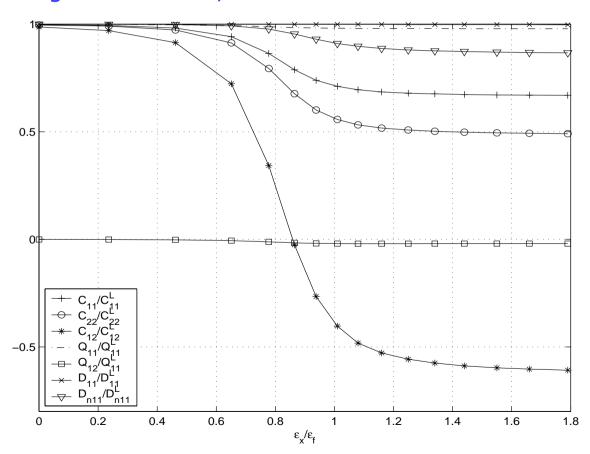
Nonlinear parts derived from local analysis:

$$C_{ij}^{NL} = \frac{\partial N_{i}^{NL}}{\partial \varepsilon_{i}} = \frac{\partial N_{i}^{NL}}{\partial A_{mn}} \frac{\partial A_{mn}}{\partial \varepsilon_{i}}$$

OFTWAI

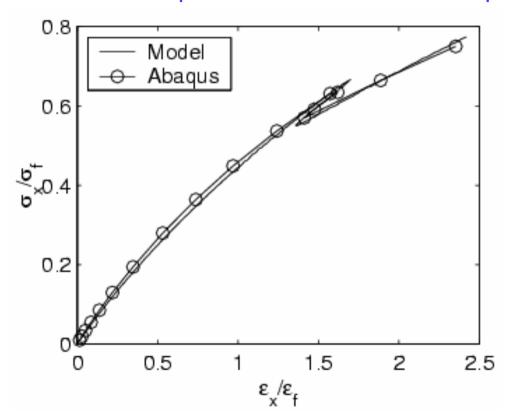
Stiffness reduction due to local buckling

Angle bar stiffener, from bulk carrier bottom:



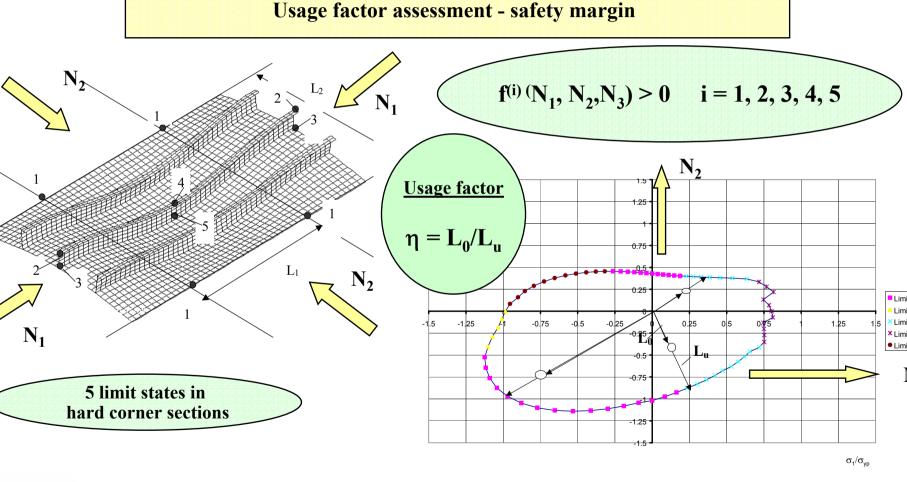
Stiffened panel (S3): Global buckling - validation

Aluminium panel, from passenger vessel Combination of lateral pressure and transverse compression:



Stiffened panel (S3): Limit States

PULS - S3 Ultimate limit states



Stiffened panel (S3): Limit States

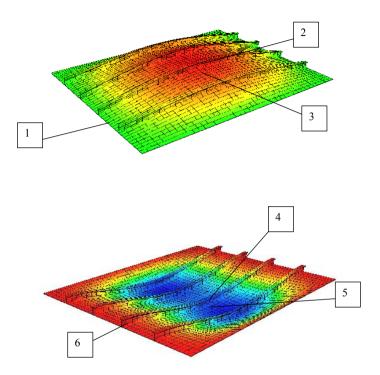


Fig. 9 Stress control points in critical positions in a panel defining the ultimate limit states

The six limit states f_i 's are stress controls in the following positions:

- = 1; Plate criterion: Stress control along plate edges based on max edge stresses along supported edges (typical: transverse load when local buckling dominates)
- = 2; Stiffener tension criterion: Stress control in stiffener; at midspan $x_1 = L_1/2$; in stiffener flange for global panel deflecting towards stiffener flange, tension criterion rare for compressive loads, but kicks in for tension loads (will also kick in for transverse compressive loads for panel with small stiffeners, i.e. large global effects)
- = 3; Plate compression criterion: Stress control in plate; at midspan $x_1 = L_1/2$; in plating for global panel deflecting towards stiffener flange, compression criterion (PI collapse)

- i = 4; **Stiffener compression criterion**: Stiffener criterion Stress control in stiffener; at midspan $x_1 = -L_1/2$: in stiffener flange for global panel deflecting towards plating, compression criterion (SI collapse) (typical for pure axial load)
- i = 5; **Plate tension criterion**: Stress control in plate; at midspan $x_1 = -L_1/2$; in plating for global panel deflecting towards plating, tension criterion rare for compressive least but kicks inn for tension loads

(Note that the limit state criteria i=2.5 is not always evaluated at midspan. Maximum curvature in x_1 – direction, and thereby the highest bending stress, could be closer to ends for certain geometrical proportions of stiffened panels. Typical are cases with statisfieners for which the panel behaves more as a plate than a "column", with a global buckling mode pattern flattening in the mid-regions.)

= 6; Stiffener bending stress criterion at support: Stress and capacity control at support = 0; compressive or tension criterion, kicks in for cases with lateral pressure. This liming state is used to control the bending and shear capacity of the stiffeners under the influence of combined lateral load and in-plane loads. Yielding in the stiffener flange the transverse frames is accepted, since stiffeners have significant strength reserves a first yield when subjected to lateral pressure. The panel is loaded until the plastic capacity of the stiffeners is reached. Two criteria are used for this limit state. The first is the capacity of the top and bottom flanges to carry the combined axial force and bending moment resulting from the applied loads, and the second is the capacity of the web to carry the shear force and axial force due to the applied loads.

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Stiffened plate (S3): Validity range

Validity range for stiffened panel:

- Ultimate Capacity; integrated elements; deck, ship side, ship bottom, bulkheads etc.

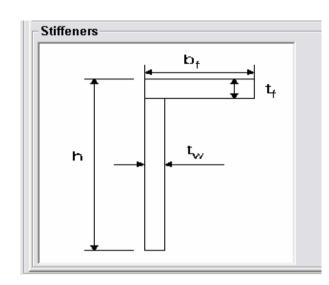
Veb slenderness for flat bar stiffeners: 35

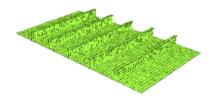
/eb slenderness for L or T profiles: $h_w/t_w < 80$

ree flange for L or T profiles: $f_f/t_f < 10$

ate between stiffeners: s/t < 200

spect ration of plate between stiffeners $0.25 < L_1/s < 10$ *



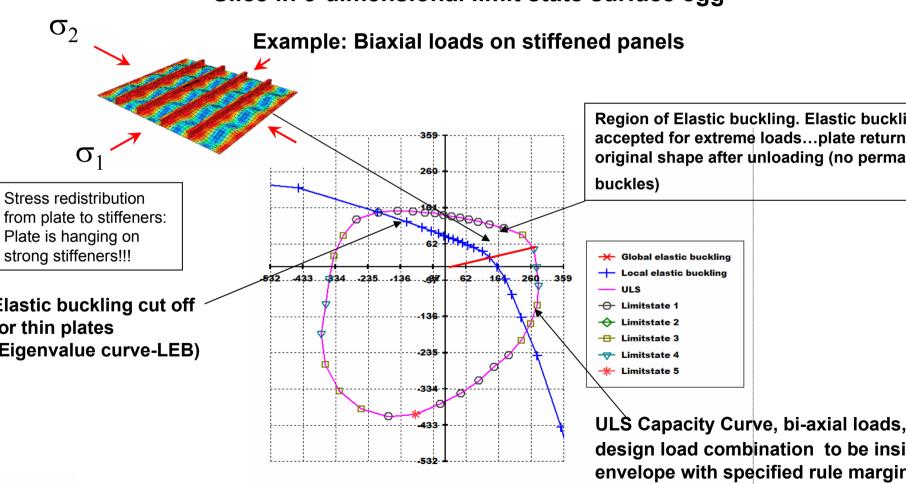


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Example: Stiffened plate, axial compression (S3)

PULS 2D Capacity Curves

Slice in 3-dimensional limit state surface egg



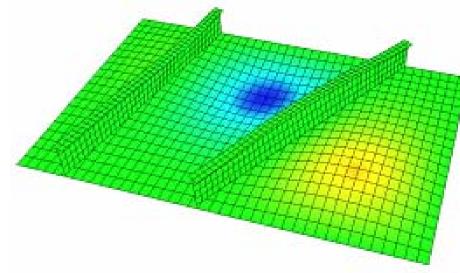
 σ_1

OTTALAT

Stiffened plate, non-regular geometry (T1)

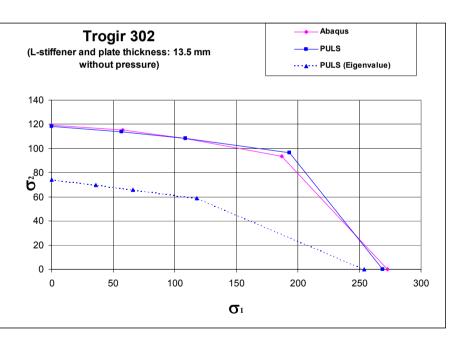
Complex geometry, simplified theory:

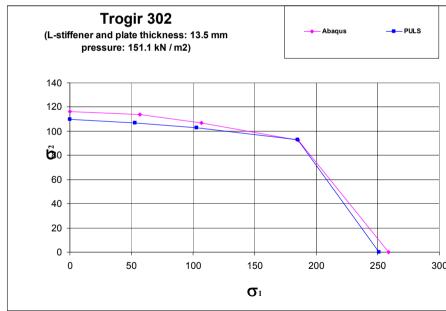
- Analysis of stiffened panels with arbitrary oriented stiffeners
- Based on linear theory
- Ultimate limit state estimates based on hot spot stress control, but limited by linear elastic eigenvalue



PULS validation

PULS validation against non-linear FE/ABAQUS

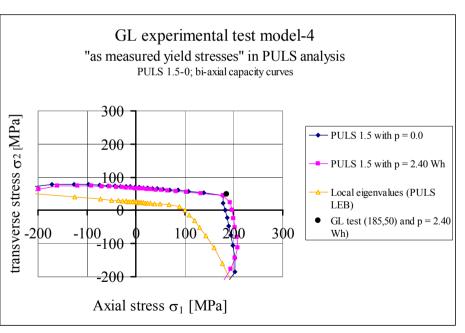


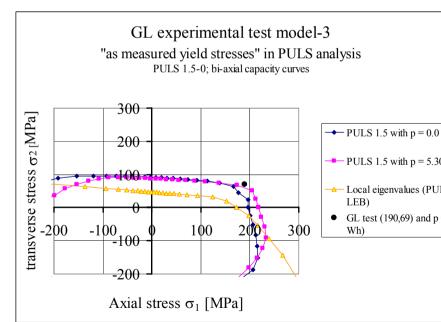


Bottom panel Tanker Lpp = 170 m

PULS validation

PULS validation against GL lab test (Egge/95)





PULS validation

PULS validation

- Extensive comparisons against non-linear FE/ABAQUS
- Limited comparisons against lab tests (Ex: GL/Egge 95)
- Comparisons against against existing rules

Conclusions

Very satisfactory quantiative comparisons ABAQUS and lab tests; mostly within \pm 10%

Same qualitative physical behaviour as seen in ABAQUS and lab tests

PULS: Sound physical models for robust designs

PULS For easy use

Designers, Non-experts etc.

PULS Software

2 different PULS Stand alone programs

PULS General User Interface (GUI) Version, features:

Visual Basic user interface. Very simple and intuitive to use

ingle parameter output for any load combination: Usage factor measured against accept level

rules

ull 3D graphics for illustration of buckling modes, redistributed stress pattern etc.

D capacity curve illustration of ULS and elastic buckling limits for combined loads - slices

3-dimensional limit state surface egg

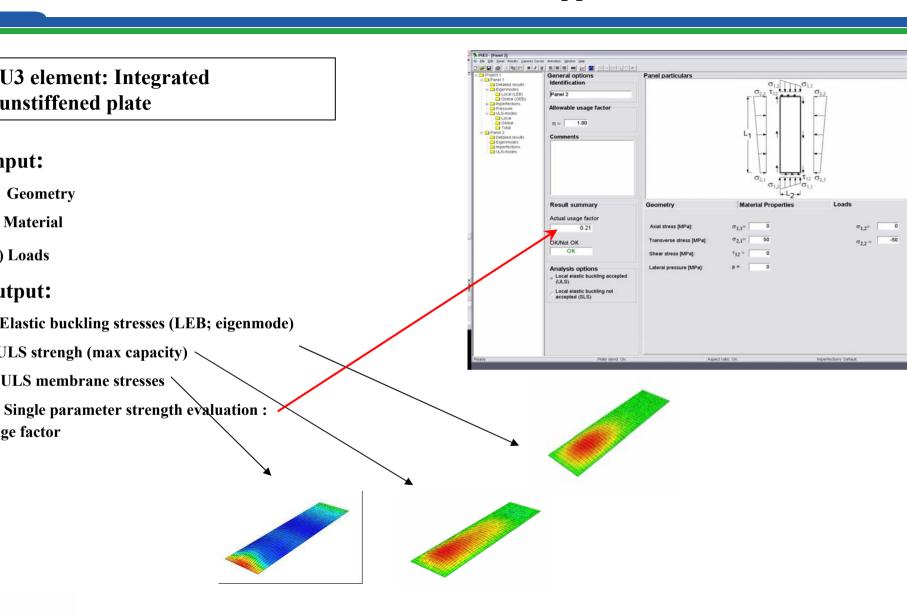
Bulbs, Angles etc

nimation of non-linear buckling process

Same input file

- Profile table; 2. PULS Excel spreadsheet version, features:
 - Material Optimization studies, parameter variasjons

PULS General User Interface Application



OTTTALA

PULS General User Interface Application

S3 element: Integrated stiffened plate

Profile table button

Geometry

or from

Material

Menu: define stiffener

) Loads

Output:

Elastic buckling stresses (LEB and GEB;

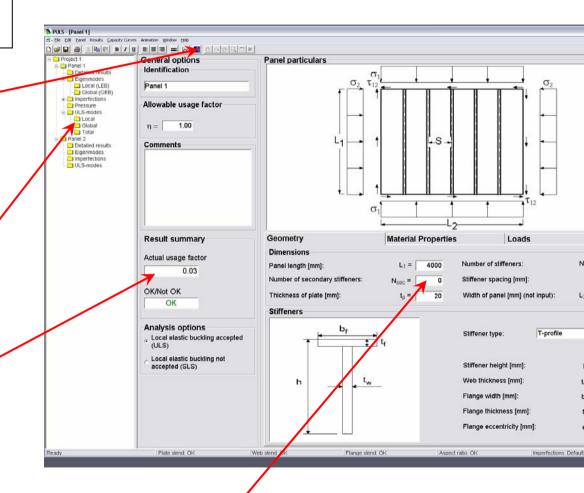
genmodes)

) ULS strengh (max capacity)

i) Local ULS membrane stresses

v) Single parameter strength evaluation :

sage factor



Menu: Panel/Secondary stiffeners

PULS Excel Application

iput:

Material

Profile table button

Geometry

or from

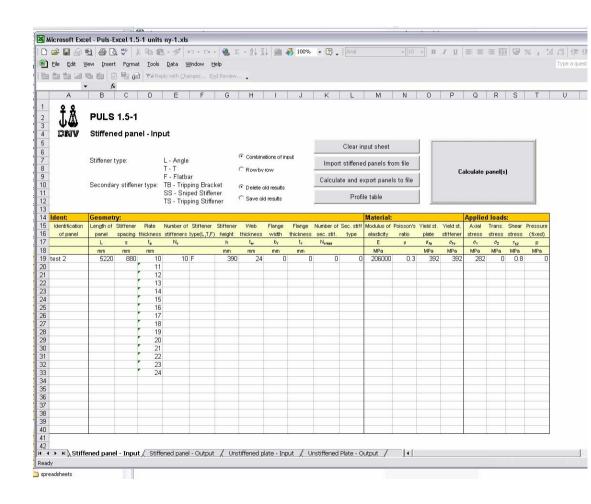
) Loads

Menu: define stiffener

Output:

- Elastic buckling stresses (LEB and GEB; genmodes)
-) ULS strengh (max capacity)
- i) Local ULS membrane stresses

v) Single parameter strength evaluation: sage factor



Menu: Panel/Secondary stiffeners

PULS Excel Application

Parameter study using PULS



PULS 1.5-1

Stiffened panel - Results

C Show all results

· Hide non-essential results

UT:	I:															PULS:						
t.	Geometry:											Material:				Applied loads				ULS:		
cation	Length	Stiffener	Plate	Numbe	Stiffe	Stiff.	Web	Flange	Flange	Number	Second	Modulus of	Poisson'	Yield	Yield	Axial	Trans.	Shear	Pressur	Axial	Trans.	Shear
	of			rof	ner					of sn.	ary			stress	stress				е			
	panel	spacing	thick.	stiffen	type	Height	thick.	width	thick.	stiffene	stiffener	elasticity	s ratio	plate	stiffener	stress	stress	stress	(fixed)	stress	Stress	stress
i	L	s	<u></u>	N _s		h	t _w	b _f	t,	N _{snipe}		E	U	σ_{Fp}	σ_{Fs}	σ ₁	σ_2	7 ₁₂	р	σ_1	σ_2	7 ₁₂
1	5150	900	24	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	236	79	94
2	5150	900	22	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	231	77	92
3	5150	900	20	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	230	77	92
4	5150	900	18	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	223	74	89
5	5150	900	16	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	215	72	86
6	5150	900	14	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	197	66	79
7	5150	900	12	6	Т	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	169	56	67
8	5150	900	10	/ 6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	142	47	57
9	5150	900	8 /	6	T	300	14	150	16	0	0	210000	0.3	355	355	150	50	60	0	119	40	48

ging thickness, all other parameters fixed

Change in usage factor due to thickness chang

PULS 2.0 release, April 2004

PULS 2.0 versus 1.5

Improvements:

- Automatic smoothening routine of Capacity Curves/Surfaces for bi-axial compression (reduce "bumps"
- Modified lateral pressure model, minor changes
- Increased slenderness range of stiffener web and flange (h/ t_w < 90 (80), f_f/ t_f < 15 (10))

New technical features:

- S2 stiffened plate element renamed S3 with new features
- S3: Linearly varying stress perpendicular to primary stiffeners
- S3: Boundary conditions: Option for free to pull in edges (non-linear effect minor interest for normal ship scantlings
- U1 unstiffened plate renamed U3 with new features
- U3: Boundary conditions; Option for clamped or rotational restrained edges
- New element T1: Non-regular stiffening arrangement, triangular plates etc.

PULS 2.0 release, April 2004

PULS 2.0

New software features, Explorer user interface:

- S3: Visualization of secondary stiffeners (run perpendicular to main stiffeners)
- S3, U3: Extra tab strip for boundary conditions
- S3, U3: Improved pressure plot of plate and stiffener deflections
- •S3: Weakest link: identfies max. deflections in plates and stiffeners useful design info
- •S3, U3: New Excel Report generator, summarize input and output results

New software features, Excel user interface:

- S3: Optimisation of stiffener/plate geometry, fixed weight/cross-sectional area
- S3: Weakest link: identfies max. deflections in plates and stiffeners useful design info

PULS 2.0 download and installation

- Go to the internet page:
 - http://www2.dnv.com/software/Products/Nauticus/puls/puls.htm
- Click on "Download PULS"
- Write in name etc., and click "Download PULS"
- Choose "Save", pick a directory for the download, and click "Close" when download is complete
- Go to your PULS directory, and unpack the .zip-file
- Start the installation by double-clicking the setup.exe-file
- Execute PULS from the Start-meny