

UNIT- III

SQL: QUERIES, CONSTRAINTS, TRIGGERS.

- form of basic SQL query
- UNION, INTERSECT and EXCEPT
- Nested queries, aggregation operators, NULL values
- Complex integrity constraints in SQL
- triggers and active databases.

SCHEMA REFINEMENT:-

- Problems caused by redundancy
- decompositions
- Problems related to decomposition
- reasoning about functional dependency.
- FIRST, SECOND, THIRD normal forms,
- BCNF, (Boyce-Codd Normal form)
- lossless join decomposition
- multi-valued dependencies
- FOURTH Normal form
- FIFTH Normal form.

Form of basic SQL query:-

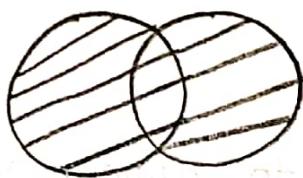
The basic form of SQL query is
 ↳ 3 clauses.

SELECT [DISTINCT] { * / column-name (, column-name, ...) }
 FROM table-name [alias] (, table-name)
 [WHERE condition] { 3 clauses } select A₁, A₂, A₃
 [GROUP BY column-list] [HAVING condition]
 [ORDER BY column-list].

- SELECT \Rightarrow which columns are to appear in the output.
 ↳ corresponds to projection operation.
- DISTINCT \Rightarrow eliminates duplicates
- FROM \Rightarrow specifies the tables to be used.
 ↳ corresponds to cartesian product operation.
- WHERE \Rightarrow filters the rows according to condition.
 ↳ corresponds to select predicate
 The where Condition is a boolean combination
 (using AND, OR and NOT) of conditions of the form
 expression op expression, where op is one of the
 comparison operators. ($<$, \leq , $=$, \geq , $>$)
- GROUP BY forms groups of rows with the same column value.
- HAVING filters the group
- ORDER BY sorts the order of the output.

UNION, INTERSECT, EXCEPT (minus)

UNION: It is used to combine the results of two or more SELECT statements. It will eliminate duplicate rows from its resultset. UNION operation is applied when columns and data type must be same in both the tables.



Example:- Table 1

ID	Name
1	abhi
2	adam

Table 2

ID	Name
2	adam
3	chester

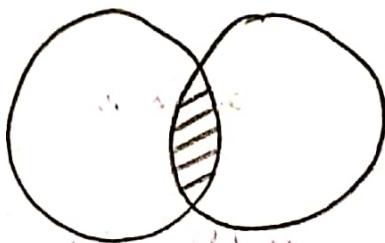
Query:- select * from first UNION select * from second;

Result:-

ID	NAME
1	abhi
2	adam
3	chester

• INTERSECT:-

It is used to combine two SELECT statements, but it only returns the records which are common from both select statements. In case of intersect the number of columns and datatype must be same.



Example:-

ID	Name
1	Abhi
2	adam

ID	Name
2	adam
3	chester

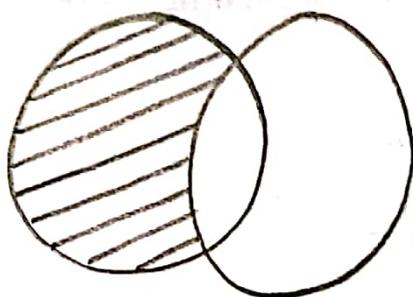
Query:- Select * FROM first INTERSECT select *
From second;

Output:-

ID	Name
2	adam

Except:-

It combines results of two select statements and return only those in final result, which belongs to first set of result.



Example:-

ID	Name
1	abhi
2	adam

ID	Name
2	adam
3	chester

Query:-

Select * From First MINUS select * From Second;

Output:-

ID	Name
1	abhi

Triggers:- A mechanism used to handle < SQL triggers that initiates an action.

A trigger is a SQL procedure that initiates an action.
when an event occurs, event is INSERT, DELETE

and UPDATE.

It has 3 parts.

- ① Event (E)
- ② Condition (C) \Rightarrow optional (whether the trigger should run or not)
- ③ Action (A) \Rightarrow what changes should be made

Syntax:-

```
Create [or Replace] Trigger trigger-name
{Before/ After} trigger event ON table name
[for each row]
[when condition]
```

Trigger Procedure.

Declare

declaration statements;

Begin

executable statements;

exception

exception handling stmt;

END;

Execution (n)

Example:- SQL > select * from customers;

ID	Name	age	address	salary
1	Hari	32	Delhi	20k
2	Priya	35	Hyd	30k
3	Raghu	30	Mumbai	40k
4	Deepu	32	Pune	50k
5	Pinky	37	Madhya	40k

* Update the salary by triggering table. (update)

⇒ Trigger displays the salary difference b/w old values and new values.

Create or replace trigger ^{trigger name} display-salary changes

Before Delete or Insert or Update on customers

for each row

when (New.ID > 0)

DECLARE

sal_diff number;

BEGIN

sal_diff := : New salary - : old salary;

dbms_output.put_line ('old salary');

 ('new salary');

 ('sal difference');

END;

o/p:- Trigger created

Aggregation Operators:-

An aggregate operator in the relational model is an operator that derives a single value from the set of values appearing within some relation.

- Avg - calculates the average of set of values.
- COUNT - counts rows in a specified table or view.
- MIN - Gets the minimum value in a set of values.
- MAX - Gets the maximum value in a set of values.
- SUM - calculates the sum of values.

NULL value:-

It is the term used to represent a missing value. A field with a NULL value is a field with no value.

- It is important to understand that NULL value is different from zero.
- Null value has three different interpretations.
 - > value unknown (value exists but is not known)
 - > value not available (exists but is purposely withheld)
 - > value may not be applicable for that particular attribute.

Eg:-

Fname	Mname	Lname
Amit	NULL	Kumar

- > value may not be applicable for that particular attribute.

Complex integrity Constraints in SQL

Constraints are the rules enforced on the data columns of a table. These are used to limit the type of data that can go into table.

constraint could be either on a column level or a table level.

- ① NOT NULL Constraint - Ensures that a column cannot have NULL value.
- ② DEFAULT constraint - Provides a default value for a column when none is specified.
- ③ UNIQUE constraint - Ensures that all values in a column are different.
- ④ PRIMARY key - Uniquely identifies each row/record in a database table.
- ⑤ FOREIGN key - Uniquely identifies a row/record in any of the given database table.
- ⑥ INDEX :- Used to create and retrieve data from database very quickly.

Complex Integrity Constraints in SQL:

Integrity Constraints

- check
- NOT NULL
- UNIQUE
- Default.

Schema refinement in dbms:

Schema refinement is the process that re-defines the schema of a relation.

- Retinement approach is based on decomposition
- Decomposition can eliminate the redundancy.

Schema-refinement addresses the following problems:

- ① Problems caused by redundancy
- ② Problems caused by decomposition

$$R = (A B C D)$$

student (sid, name, sage)

* TO avoid redundancy.

Decomposition: Let R be a relational schema.

A set of relational schemas $(R_1, R_2, R_3, \dots, R_n)$

is a decomposition of R if

$$R = R_1 \cup R_2 \cup \dots \cup R_n$$

eg:- Relation $R(x, y, z)$

$R_1(x, y) \wedge R_2(y, z)$

Now we get

$$R = R_1 \cup R_2$$

Problem with decomposition:-

R

Model name	Price	category
a ₁₁	100	canon
s ₂₀	200	Nikon
a ₂₀	150	canon

R_1

Modelname	category
a ₁₁	100
s ₂₀	200
a ₂₀	150

R_2

Price	category
100	Canon
200	Nikon
150	Canon

$R_1 \cup R_2$

Modelname	Price	category
a ₁₁	100	canon
a ₁₁	150	canon
s ₂₀	200	Nikon
a ₂₀	100	canon
a ₂₀	150	canon

$$R_1 \cup R_2 \neq R$$

Functional dependency:

The attributes of the table are said to be dependent on each other when an attribute of a table uniquely identifies another attribute of same table.

Eg:- We have student table with attributes : stu-id, stu-name, stu-age. Here stu-id attribute uniquely identifies student name attribute of a student table because if we know stu-id we can say name of the student easily. It can be written as $\underline{\text{stu-id}} \rightarrow \underline{\text{stu-name}}$.

* If column A of table uniquely identifies the column B then it can be represented as $A \rightarrow B$ (B is dependent on A)

symbol \rightarrow

$A \rightarrow B$

↳ dependent

determinant

If $A = 2$ then $B = 1$

If in two tuples

$$t_1 \cdot A = t_2 \cdot B \text{ then } t_1 \cdot B = t_2 \cdot B$$

If repetition is there ✓

A	B
1	1
2	1
3	2
4	3

R.NO	student	Marks	dept	course
1	a	78	CS	C1
2	b	60	EE	C1
3	a	78	CS	C2
4	b	60	EE	C3
5	c	80	IT	C3
6	d	80	EC	C2

$R.NO \rightarrow Name$

$Name \rightarrow R.No X$

$R.No \rightarrow marks ✓$

$Dept \rightarrow course X$

Problems caused by redundancy:-

Redundancy means duplication of data.

Problems caused due to redundancy are

1. Insertion anomaly.

2. Deletion anomaly.

3. Updation anomaly.

Eg:-

emp-id	emp-name	emp-address	emp-dept
101	Rick	Delhi	D001
101	Rick	Delhi	D002
123	Maggie	Agra	D890
166	Glenn	Chennai	D900
166	Glenn	Chennai	D004

Insert anomaly:- Suppose a new employee joins a company who is under training and currently not assigned to any department, then we would not be able to insert the data into table if emp-dept does not allow null value.

Update anomaly:- If I want to update the address of Rick, I need update two tuples i.e. two departments. If I update only in one row, then Rick will have 2 addresses which leads to inconsistency.

Delete anomaly:- Suppose if the company closes the dept D890, then the information of that employee will also be deleted.

* Normalization:

A process of organizing the data in database to avoid data redundancy, insertion anomaly, updation anomaly and deletion anomaly.

It has 6 parts: (1NF, 2NF, ..., 5NF)

* A process of organizing data into tables such a way that the results of using database are always clear.

Types of Normalization:-

- ① First Normal Form (1NF)
- ② Second Normal form (2 NF)
- ③ Third Normal form (3 NF)
- ④ Boyce-codd Normal form (BCNF)
- ⑤ Fourth Normal form (4 NF)
- ⑥ Fifth Normal form (5 NF).

Empid	name	dept	add
1	n ₁	d ₁	a ₁
2	n ₂	d ₂	a ₂
3	n ₃	(d ₄) ^x	a ₃
4	n ₄	d ₂	a ₄
5	t ₁	?	?

↳ trainee - Insertion anomaly.

First Normal form:-

It is a property of a relation in relational database. A relation is in first normal form if and only if the domain of each attribute contains only atomic values, and the value of each attribute contains only single value from that domain.
 atomic values → which can't be divided further.

Rules:-

- * each attribute should contain atomic values.
- * Composite attributes → take more attributes
- * Multivalued → take more tuple.

Eg:- student

cid	sname	s-addr	P.no
1	Jenny	Haryana	P ₁ , P ₂
2	Jiya	Punjab	P ₃
3	Payal	Rajasthan	P ₄ , P ₅

sid	sname	state	country	Phno
1	Jenny	HR	INDIA	P ₁
1	Jenny	HR	INDIA	P ₂
2	Jiya	Punjab		P ₃
3	Payal	Rajasthan		P ₄
3	Payal	Rajasthan		P ₅

- * A column should contain value of same domain.

Int → Integer value

X Shanti 4

String →

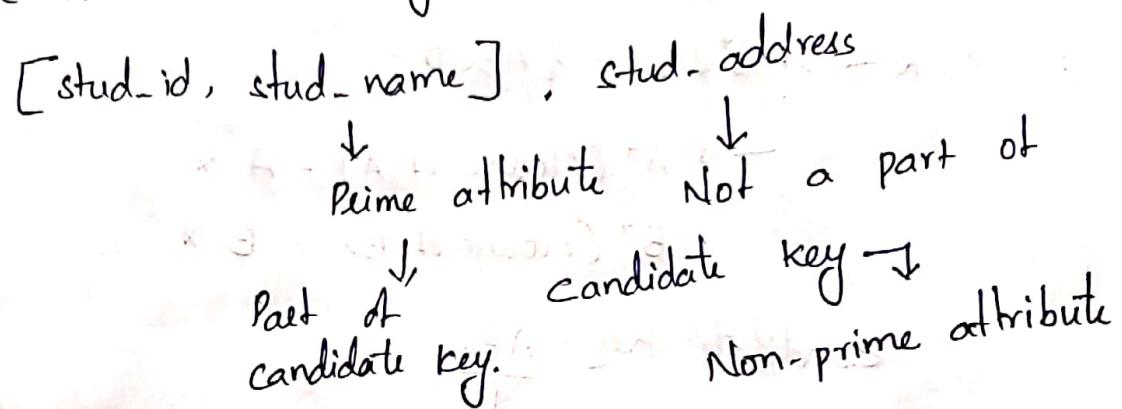
- * each column should have unique name

* No ordering to rows & columns.
 * No duplicate rows.

P.no

Second Normal form (2NF):-

Candidate key:- It is a minimal set of attributes which can uniquely identify a tuple is known as candidate key.
 → The value of candidate key is unique and not null.



* Rules:-

- ① * It should be in 1-NF
- ② * It (relation) must not contain any partial dependency.

Partial dependency:- Proper subset of candidate key → non prime attribute

No partial dependency.

Eg:- R (A, B, C, D, E, F)

Functional dependency = { A → B, B → C, C → D, D → E }

A can determine B so B is discarded
 $AB \not\rightarrow FE = \{ ABCDEF \}$

We can't discard F.

AF = candidate super key.

A, P are primary attributes

Non-prime attributes - B, C, D, E

Partial dependency exist
 so it is not in
 1 NF

Eg - ②

Given R(A, B, C, D)

$$FD = \{AB \rightarrow CD, C \rightarrow A, D \rightarrow B\}$$

Candidate Keys = AB, CD = {AB, CD}

$$S.K \rightarrow AB^+ \cap \emptyset = \{AB, CD\}$$

$$A^+ (\text{closure of } A) = A \times$$

$$B^+ (\text{closure of } B) = B \times$$

Candidate Key = AB.

Replace A with C

CB → AD → replace B with D

Customer

First
table

Eg:-

Customer_id	Store ID	Location
1	1	Delhi
1	3	Mumbai
2	1	Delhi
3	2	Banglore
4	3	Mumbai

cust_id	store_id
1	1
1	3
2	2
3	3
4	

store_id	location
1	Delhi
2	Banglore
3	Mumbai

Candidate keys =

customerID, store ID

Prime attributes =

customerID,

store ID.

Non-prime attribute = location

Location is dependent on
store id.

Example:-

$R(ABCDEF)$ Not in 2NF due to Partial dependency

Functional dependency $\{C \rightarrow F, E \rightarrow A, EC \rightarrow D, A \rightarrow B\}$

Candidate key: $EC = \underline{FADB}$

$$EC^+ = ECFAKB$$

$$1. CK = \{EC\}$$

2. Prime attributes: E, C used to form C.K

3. Non-prime attributes: $\{A, B, D, F\}$

$$FD \{ \underbrace{C \rightarrow F}_{\downarrow PD}, \underbrace{E \rightarrow A}_{\downarrow PD}, \underbrace{EC \rightarrow D}_{\substack{\text{set} \\ \downarrow \\ \text{No subset}}} \downarrow F, A \rightarrow B \}$$

Proper subset

Prime attribute

Condition for Partial dependency

L.H.S should be proper subset of candidate key

R.H.S \rightarrow a non-prime attribute

$\{AB\} \rightarrow$ subset

$A, B \rightarrow$ proper subset

$C \rightarrow F \{PD\}$

$E \rightarrow A \{PD\}$

$EC \rightarrow D \{FD\}$

$A \rightarrow B \{FD\}$

Reflexive Rule:-

$$R(A, B, C, D)$$

$$ABC \rightarrow AB.$$

R

A	B	C
---	---	---

$$R(A, B, C)$$

$$F = \{A \rightarrow B, B \rightarrow C\}$$

Reflexivity.

$$\frac{\begin{matrix} A \rightarrow B \\ A \rightarrow C \end{matrix}}{A \rightarrow BC} \quad \left. \begin{matrix} \\ \end{matrix} \right\} \rightarrow \text{union}$$

Augmentation

$$A \rightarrow B$$

$$CB \rightarrow D$$



$$CA \rightarrow D.$$

Transitivity

$$A \rightarrow BC$$

decomposition

$$R(A, B, C, D, E)$$

$$F \{ A \rightarrow BC, CD \rightarrow E, B \rightarrow D, E \rightarrow A \}$$

Computing F^+ , set of all FD's that are logically implied

from given FD set

$$R(AB) \quad F = \{A \rightarrow B, B \rightarrow A\}^+ \\ x \rightarrow y \text{ func. dep.}$$

F^+ -

A →	A
B →	B
AB →	AB
∅	∅

3NF:-

It should be in 2 NF

There should be no transitive dependency.

Eg:-

Rollno	state	city
1	Punjab	Mohali
2	Haryana	Ambala
3	Punjab	Mohali
4	Haryana	Ambala
5	Bihar	Patna

Candidate key = {Roll No}

Prime attribute = Roll No \rightarrow state

Non-prime attribute = {state \rightarrow city}

Rollno \rightarrow state } Roll no \rightarrow city.
State \rightarrow city }

* Non-prime attribute determines non-prime attributes

This should not be there.

Eg - ①

R (ABCD)

FD : (AB \rightarrow C, C \rightarrow D)

CK = A, B

PA = A, B

NPA = C, D

Eg - ②

R (ABCD)

FD : AB \rightarrow CD, D \rightarrow A

CK : AB \rightarrow ABCD

BCNF:-

Non-trivial functional dependency.

① L.H.S is super key

② R.H.S is prime attribute

Eg - ③

R (A, B, C, D) ————— This is not in 3rd NF. due
FD - $(A \rightarrow B, B \rightarrow C, C \rightarrow D)$ to transitive dependency

^{Transitive dependency TD}
 $PA \rightarrow A, CK = A$

NPA = BCD

$$\boxed{x \rightarrow y \\ y \subseteq x}$$

Trivial
functional dependency

BCNF:- (It is also called as 3.5 NF)

Rules:
Drawbacks in 3rd NF

It should be in 3NF

dependency $A \rightarrow B$ dependency $x \rightarrow y$, x should be superkey & for every functional table.

eg:- Roll No Name voterid age CK = {Roll no, voter id}

1	Ravi	123	20
2	Varun	456	21
3	Ravi	789	23
4	Rahul	1011	21

FD: Roll No \rightarrow name

" \rightarrow voterid

voterid \rightarrow age

voterid \rightarrow RollNo

L.H.S of each functional dependency should be a

candidate key or super key.

eg for BCNF

Std	Course	Teacher
sai	DBMS	Priya
Bhanu	DBMS	Madhu
Deepu	Java	Ramya
shiva	Java	Ramya
Ram	DBMS	Madhu

\Rightarrow key : {std, course}

Non-key attribute = Teacher

\downarrow

is not a super key

Now, we decompose

Std	Course
sai	DBMS
Bhanu	DBMS
Deepu	Java
shiva	Java
Ram	DBMS

$x \rightarrow y$

\downarrow

super key

Course	Teacher
DBMS	Priya
DBMS	Madhu
Java	Ramya.

$x \rightarrow y$

\downarrow

super key.

4-NF

It depends on keys
and

Multi-valued dependencies.

2NF
3NF
BCNF } on keys &
FD's.

Rules:-

4-NF eliminates independent many to one relationships b/w columns.

- * A relation must be in BCNF
- * A given relation may not contain more than one multivalued attribute.

e.g.: stdid subject activity

100 Music Swimming

100 Accounting

100 Music Tennis

100 Account Tennis

150 Maths Tagging.

→ Many student id have same subject

→ Now decompose to convert to 4NF.

schema → {stdid, subject, activity}

New schema → {stdid, subject}

new → {stdid, activity}

(12)

stid	subject
100	Music
100	accounting
150	Maths

stid	activity
100	swimming
100	tennis
150	Jogging

it is in 4NF

4NF:

↳ depends on keys and
Multi valued dependencies.

2NF

3NF

BCNF

} on Keys

&
functional
dependencies

⇒ Rules:

1. Relation must be in BCNF.
2. A given relation may not contain more than one multivalued attribute.

BCNF(✓)

NO Multivalued dependencies

Multivalued dependency

Trivial

Non-trivial

Multivalued
dependency

dependency

$x \rightarrow y$

iff

$y \subseteq x$

subset

(or)

if there is atleast one attribute in
R.H.S that is not a part of L.H.S

Eg: $AB \rightarrow C$

$AB \rightarrow AC$

R.H.S of FD is

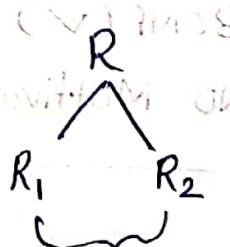
subset of L.H.S of FD

Eg: $AB \rightarrow A$

5NF (fifth Normal form) or Project Join normal form:

Rules:-

1. R should be in 4NF No lossless
 2. It cannot be further non loss decomposed.
- * NO lossless join
Decomposition - Dividing.



If we join these relations we should get same as R

$$R = R_1 + R_2$$

Lossy decomposition: Contains extra tuples.

→ by learning JOIN dependency

→ basic concept of breaking down a table.

* Lossless join decomposition

R (A, B, C)

1 1 1

2 1 2

3 2 1

4 3 2



if AB to ABD

if BC to BCD

if AC to ACD

if A to AD

if B to BD

if C to CD

if D to D

if ABCD to ABCD

if ABD to ABD

if BCD to BCD

if ACD to ACD

if AD to AD

if BD to BD

if CD to CD

if D to D

if ABC to ABC

if BC to BC

if AC to AC

if A to A

if B to B

if C to C

if D to D

if ABCD to ABCD

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

if BADC to BADC

if CBDA to CBDA

if DCBA to DCBA

if ABDC to ABDC

if CADB to CADB

if DABC to DABC

if BCAD to BCAD

if CABD to CABD

if DCAB to DCAB

if ADCB to ADCB

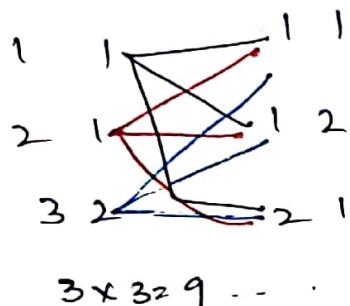
if BADC to BADC

$R_1(A, B)$

1	1
2	1
3	2
4	3

 $R_2(B, C)$

1	1
1	2
2	1
3	2

$$\begin{array}{c} R_1 \times R_2 \\ A \cdot B \quad B \cdot C \\ \diagup \quad \diagdown \\ 1 \quad 1 \quad 1 \quad 1 \\ 1 \quad 1 \quad 1 \quad 2 \\ 1 \quad 1 \quad 2 \quad 1 \\ 1 \quad 1 \quad 2 \quad 2 \end{array}$$
 $R_1(A, B) \quad R_2(B, C)$ 

cartesian product
 $R_1 \times R_2$

$$\begin{matrix} & 1 & 1 \\ = & 1 & 1 \\ & 1 & 2 \\ & 1 & 2 \\ 3 \times 3 = 9 & \dots & 2 & 1 \\ & & & 1 \end{matrix}$$

This is same in
both R_1 & R_2

$$\begin{matrix} & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ 3 & 2 & 2 & 1 \end{matrix}$$

$$R_1 \cdot B = R_2 \cdot B$$

Natural Join

$$R_1 \bowtie R_2$$

A	B	B	C
1	1	1	1
1	1	1	2
2	1	1	1
2	1	1	2
3	2	2	1

remove
jL