

# Data Structures & Algorithms



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The ML Hub

## Introduction to Stacks

### Definition

A stack is a linear data structure that follows the LIFO (Last-In, First-Out) principle.

### Key Analogy

Like a stack of plates/books — last placed is the first to be removed.

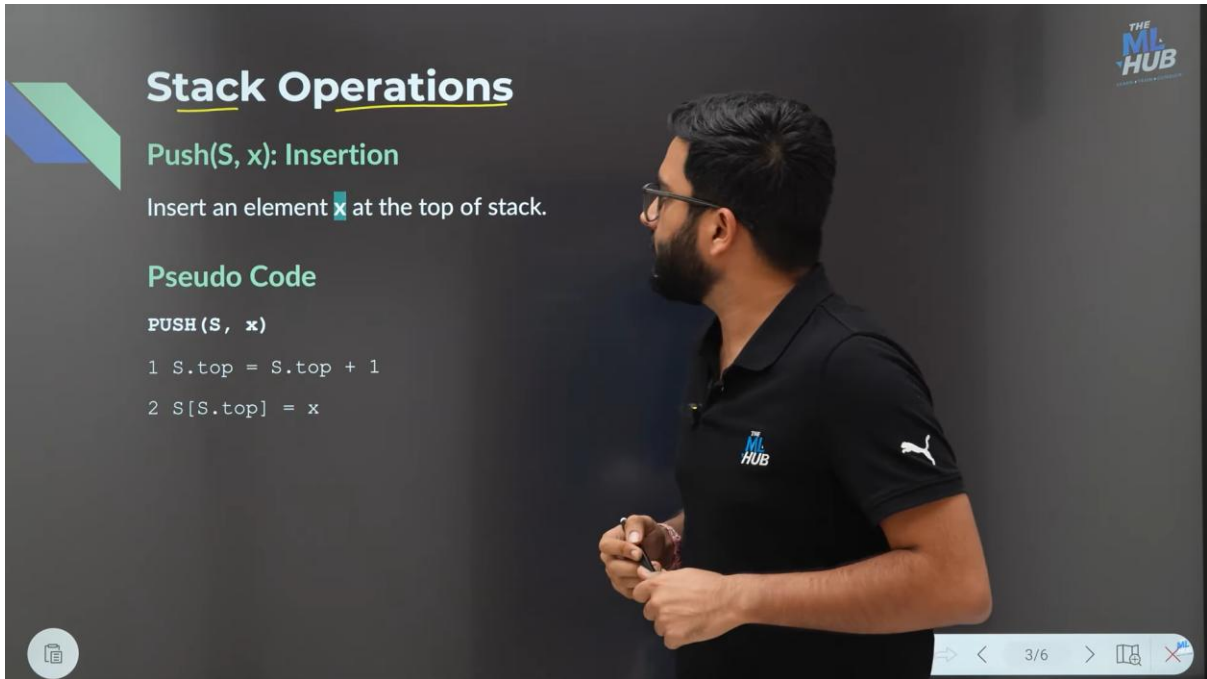
### Parameters

1. S.top: It's the index of the top element in the stack.



	1	2	3	4	5	6	7
S	15	6	2	9			

↑  
S.top = 4



# Stack Operations

## Push(S, x): Insertion

Insert an element  $x$  at the top of stack.

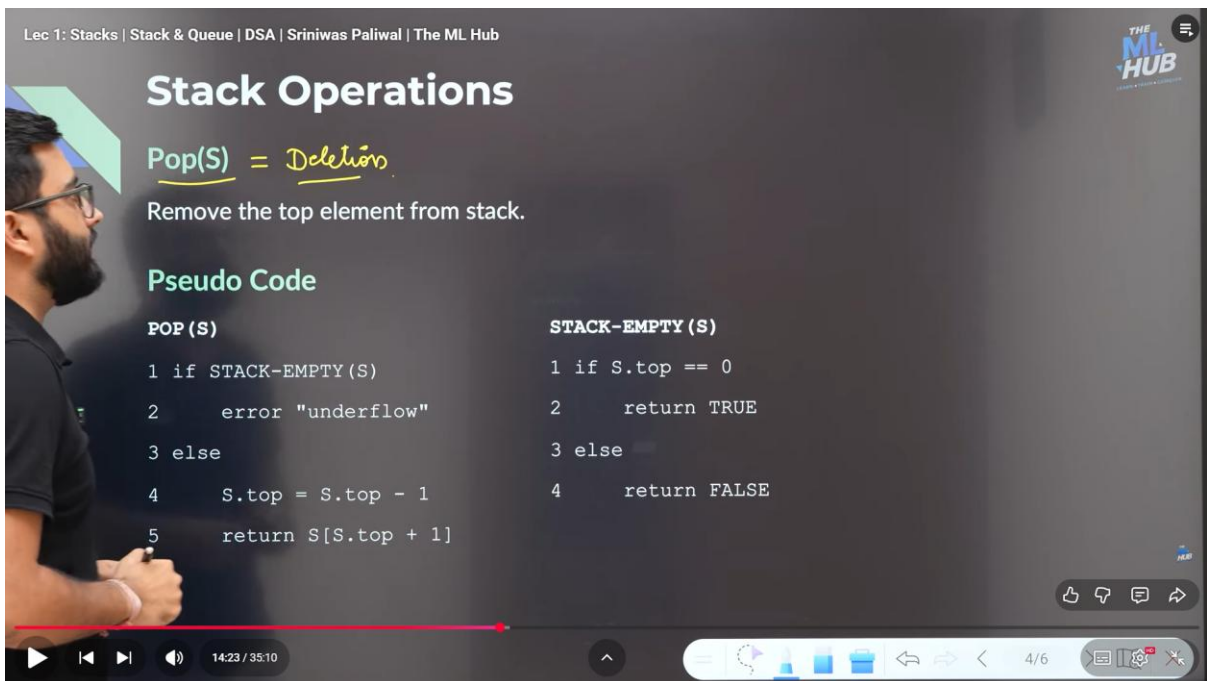
### Pseudo Code

```
PUSH (S, x)
1 S.top = S.top + 1
2 S[S.top] = x
```

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$O(1)$

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# Stack Operations

## Pop(S) = Deletion

Remove the top element from stack.

### Pseudo Code

```
POP (S)
1 if STACK-EMPTY(S)
2   error "underflow"
3 else
4   S.top = S.top - 1
5   return S[S.top + 1]

STACK-EMPTY (S)
1 if S.top == 0
2   return TRUE
3 else
4   return FALSE
```

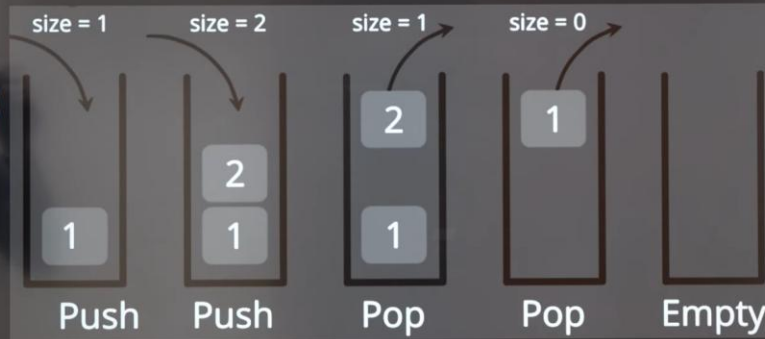
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$O(1)$  -> time complexity

# Stack Operations

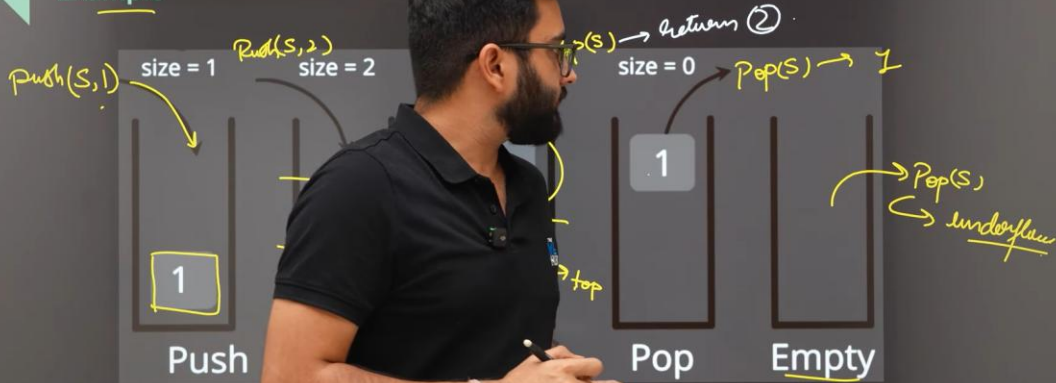
## Example

< - 105



# Stack Operations

## Example



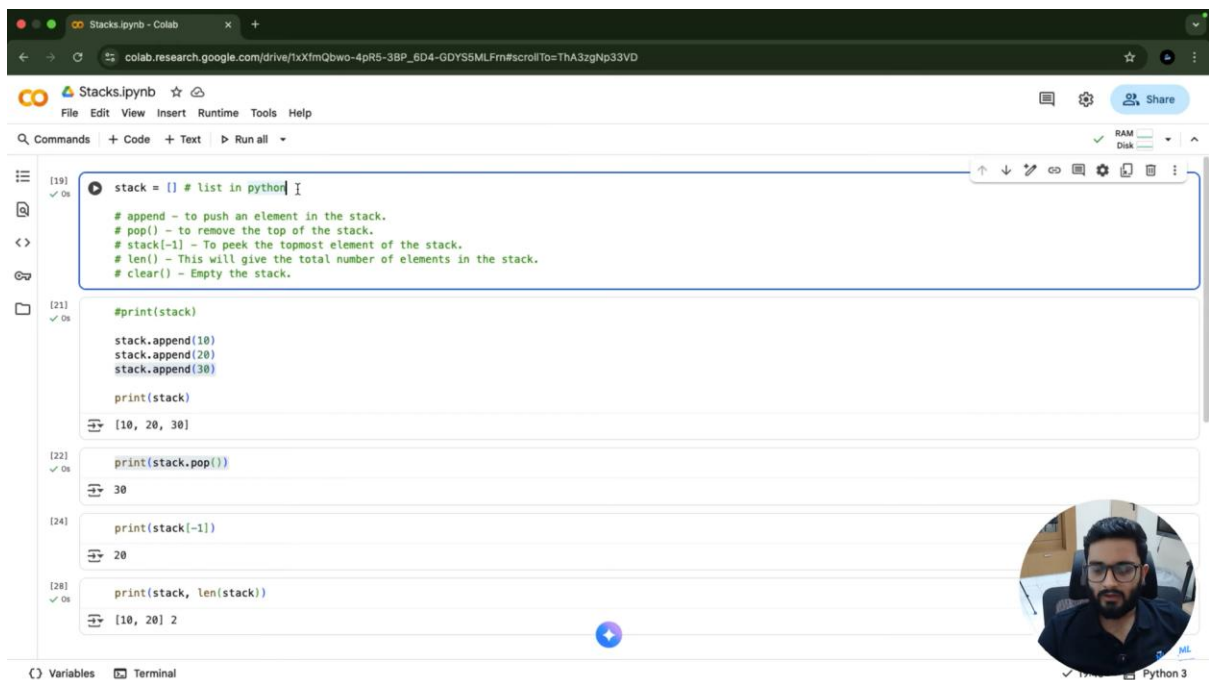
# Stack Representations

## Array-based Implementation

- Uses contiguous memory.
- Operations are fast but fixed size
- Overflow occurs if trying to push beyond capacity.

## Linked List Implementation

- Dynamic size, no overflow.
- More memory per element (extra pointer).



```
[19] ✓ 0s
stack = [] # list in python

# append - to push an element in the stack.
# pop() - to remove the top of the stack.
# stack[-1] - To peek the topmost element of the stack.
# len() - This will give the total number of elements in the stack.
# clear() - Empty the stack.

[21] ✓ 0s
#print(stack)

stack.append(10)
stack.append(20)
stack.append(30)

print(stack)

[22] ✓ 0s
print(stack.pop())

[24] ✓ 0s
print(stack[-1])

[28] ✓ 0s
print(stack, len(stack))
```

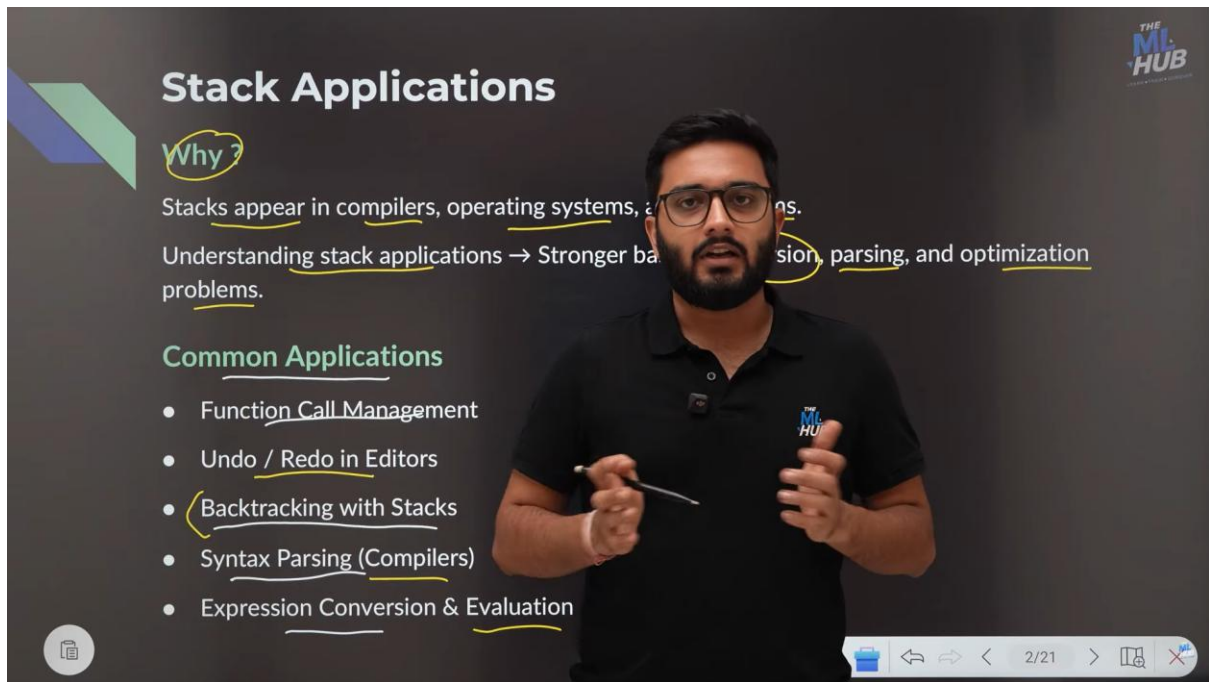
[10, 20, 30]

30

20

[10, 20] 2





# Stack Applications

**Why?**

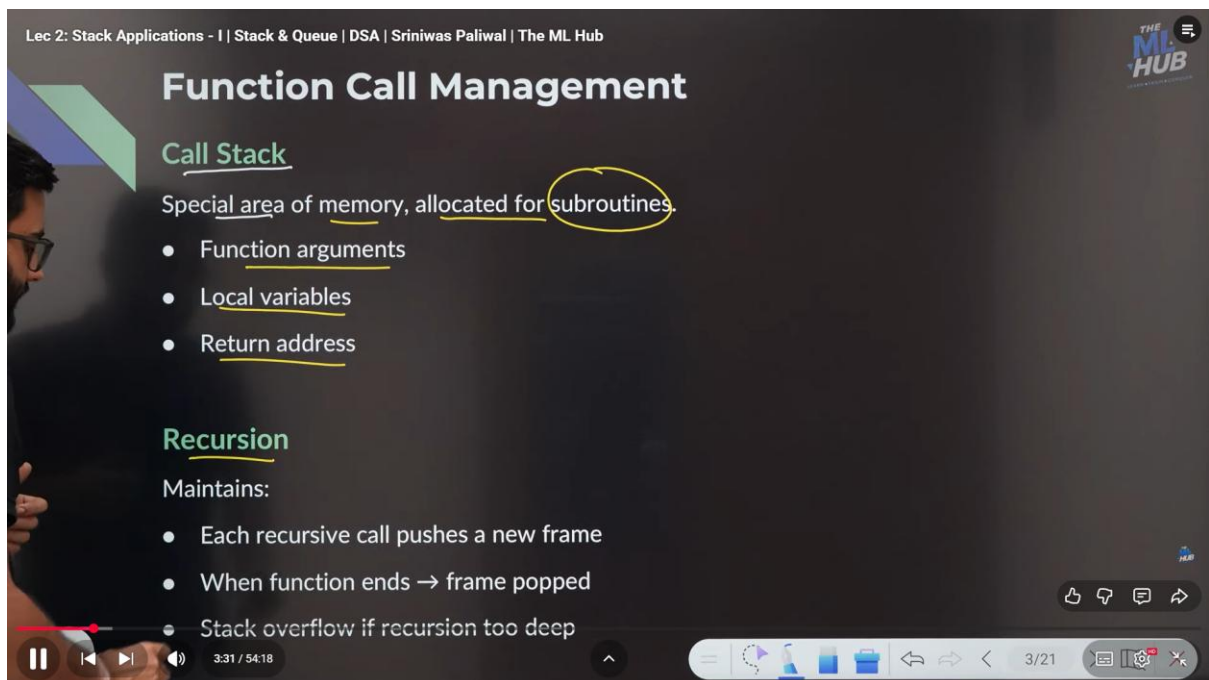
Stacks appear in compilers, operating systems, and applications.

Understanding stack applications → Stronger base understanding, parsing, and optimization problems.

## Common Applications

- Function Call Management
- Undo / Redo in Editors
- Backtracking with Stacks
- Syntax Parsing (Compilers)
- Expression Conversion & Evaluation

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# Function Call Management

## Call Stack

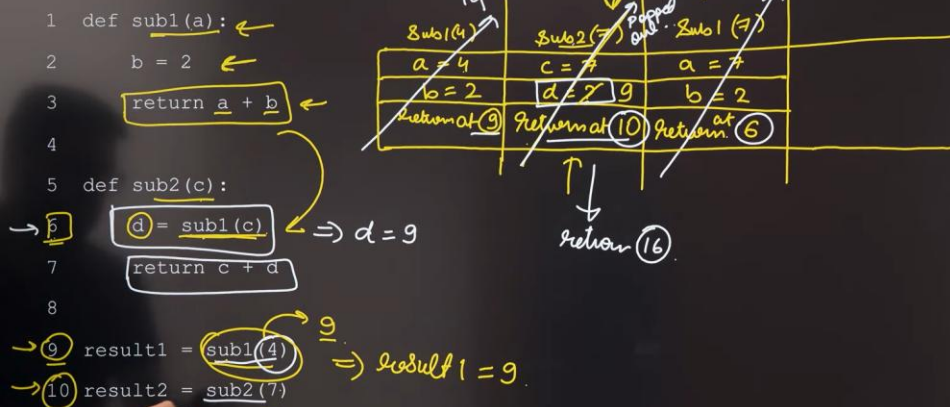
Special area of memory, allocated for subroutines.

- Function arguments
- Local variables
- Return address

## Recursion

Maintains:

- Each recursive call pushes a new frame
- When function ends → frame popped
- Stack overflow if recursion too deep



Q. What will be the output of the following code snippet ?

```

1 def funcA(n):
2     if n > 0:
3         print("A:", n)
4         funcB(n - 1)
5         print("A done:", n)
6
7 def funcB(n):
8     if n > 0:
9         print("B:", n)
10        funcA(n - 2)
11        print("B done:", n)
12
13 funcA(3)

```

```
1 def funcA(n):  
2     if n > 0:  
3         print("A:", n)  
4         funcB(n - 1)  
5         print("A done:", n)  
6  
7     funcB(n):  
8     if n > 0:  
9         print("B:", n)  
10        funcA(n - 2)  
11        print("B done:", n)  
12  
13 funcA(3)
```

funcA(3)
n = 3
returns at line (3)

O/P: A: 3

```
1 def funcA(n):  
2     if n > 0:  
3         print("A:", n)  
4         funcB(n - 1)  
5         print("A done:", n)  
6  
7     funcB(n):  
8     if n > 0:  
9         print("B:", n)  
10        funcA(n - 2)  
11        print("B done:", n)  
12  
13 funcA(3)
```

funcA(3)	funcB(2)
n = 3	n = 2
returns at line (3)	returns at line (4)

O/P: A: 3  
B: 2

+ 45 >

```

1 def funcA(n):
2     if n > 0:
3         print("A:", n)
4         funcB(n - 1)
5         print("A done:", n)
6
7 def funcB(n):
8     if n > 0:
9         print("B:", n)
10        funcA(n - 2)
11        print("B done:", n)

```

funcA(3)	funcB(2)	funcA(0)
n = 3	n = 2	n = 0
returns at line (3)	returns at line (4)	returns at line (10)

O/p: A: 3  
B: 2

funcA(3)

+5 >

```

1 def funcA(n):
2     if n > 0:
3         print("A:", n)
4         funcB(n - 1)
5         print("A done:", n)
6
7 def funcB(n):
8     if n > 0:
9         print("B:", n)
10        funcA(n - 2)
11        print("B done:", n)

```

funcA(3)	funcB(2)	funcA(0)
n = 3	n = 2	n = 0
returns at line (3)	returns at line (4)	returns at line (10)

O/p: A: 3  
B: 2  
B done: 2

funcA(3)

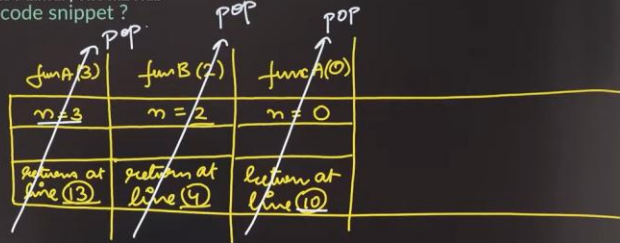
+65 >



```
1 def funcA(n):
2     if n > 0:
3         print("A:", n)
4     → funcB(n - 1)
5     → print("A done:", n)
6
```

```
7 def funcB(n):
8     if n > 0:
9         print("B:", n)
10    → funcA(n - 2)
11    → print("B done:", n)
12
```

```
13 funcA(3)
```



O/p: A: 3  
B: 2  
B done: 2  
A done: 3

+ 25 >

## Undo / Redo in Editors

### Editor Operations

- Undo (Ctrl + Z): Pop last action
- Redo (Ctrl + Y): Use another stack to restore popped actions
- Example: Typing → "A", "AB", "ABC"
  - Undo 1 → "AB"
  - Undo 2 → "A"
  - Redo 1 → "AB"
  - Redo 2 → "ABC"

## Syntax Parsing (Compilers)

### Balanced Parenthesis

- Stack used for balanced parenthesis/bracket
- Example:
  - [[ ( ) ]]
  - { ( [ ] ) }

37:44 / 54:18

8/21

```
[28] print(stack, len(stack))
```

```
[10, 20] 2
```

### Stack Application

```
[33] # str = '({})'
def isBalanced(str):
    stack = []

    for char in str:
        if char == '(':
            stack.append(char)
        elif char == ')':
            stack.pop()

    return len(stack) == 0 # True if len(stack) == 0 or stack is empty, else false.

print(isBalanced('({}))'))
print(isBalanced('({)})'))
print(isBalanced('(){}{}'))

##M: Update the isBalanced function
True
False
True
```

51:19 / 54:18

20%

Python 3

# Expression Evaluation & Conversion

## Expression

- Expressions are combinations of **operands** (variables, constants) and **operator**.
- Examples,
  - $2 + 3 * 5 - 1$
  - $6 * 2 / 3 - 4 * 2 * +$
- Three common notations:
  - Infix:** Operators between operands,  $a + b$
  - Prefix (Polish):** Operators before operands,  $+ a b$
  - Postfix (Reverse Polish):** Operators after operands,  $a b +$

Operator	Precedence
(, )	Highest
^	3
*, /	2
+, -	1

0:20 / 1:33:54

# Expression Evaluation & Conversion

## Expression

- Expressions are combinations (variables, constants) and **operators** (+, -, \*, /).
- Examples,
  - $2 + 3 * 5 - 1$
  - $6 * 2 / 3 - 4 * 2 * +$
- Three common notations:
  - Infix:** Operator
  - Prefix (Polish)**
  - Postfix (Reverse Polish)**

Operator	Precedence	Associativity
(, )	Highest	N/A
^	3	Right
*, /	2	Left
+, -	1	Left

0:27 / 1:33:54

2/16

## Expression Conversion

### Infix $\rightarrow$ Postfix (Shunting Yard Algorithm)

Let's convert,  $(A + B) * (C - D)$ , to postfix expression.

1 for each token in expression:

2 if operand  $\rightarrow$  add to output

3 else if '('  $\rightarrow$  push to stack

4 else if ')'  $\rightarrow$  pop until '('

5 else if operator:

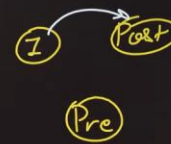
6 while stack not empty and precedence(top)  $\geq$  precedence(token):

7 pop from stack to output

8 push token

9 while stack not empty:

10 pop to output



11:39 / 1:33:54

## Expression Conversion

### Infix $\rightarrow$ Postfix (Shunting Yard Algorithm)

Let's convert,  $(A + B) * (C - D)$ , to postfix expression.

1  $\rightarrow$  for each token in expression:  $\rightarrow$

2  $\rightarrow$  if operand  $\rightarrow$  add to output

3  $\rightarrow$  if '('  $\rightarrow$  push to stack

4  $\rightarrow$  if ')'  $\rightarrow$  pop until '('

5  $\rightarrow$  if operator:

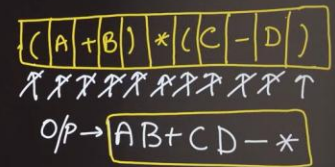
6 while stack not empty and precedence(top)  $\geq$  precedence(token):

7 pop from stack to output

8 push token

9 while stack not empty:

10 pop to output



top is an opening parenthesis

24:31 / 1:33:54



## Expression Conversion

### Infix → Prefix

1. Reverse Infix expression.
2. Convert to Postfix using Shunting Yard Algorithm.
3. Reverse again → This will give the Prefix expression.

Example,

Infix expression =  $(A + B) * (C - D)$

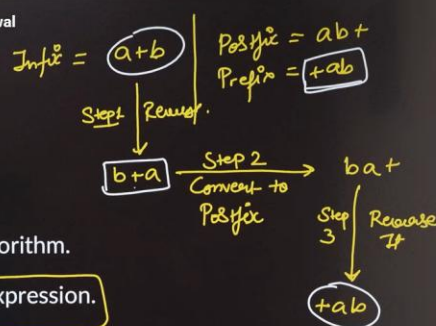
## Expression Conversion

### Infix → Prefix

1. Reverse Infix expression. →  $b+a$
2. Convert to Postfix using Shunting Yard Algorithm.
3. Reverse again → This will give the Prefix expression.

Example,

Infix expression =  $(A + B) * (C - D)$



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**\* Infix =  $(A+B) * (C-D) = I$**   
 Convert it to prefix.

**Step 1: Reverse eg. 1.**  
 $I' = (D-C) * (B+A)$

**Step 2: Convert it to Postfix.**  
 $Postfix(I') = DC-BA+*$

**Step 3: Reverse it again.**  
 $Prefix(I) = *+AB-CD$

token	Stack	O/P
(	(	D
D	(	D
-	(, -	DC
C	(, -, C	DC-
)		DC-
*	*	DC-
(	*, (	DC-
B	*, (, B	DC-B
+	*, (, +	DC-B
A	*, (, +, A	DC-B
)	*, +	DC-BA
	*	DC-BA+
		DC-BA+*

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## Expression Conversion

**Postfix → Infix/Prefix**

Let's convert,  $A B + C *$ , to infix expression.  $(A + B) * (C - D)$

```

1 create empty stack S
2 for each token t in Postfix expression:
3   if t is operand:
4     PUSH(S, t)
5   else if t is operator:
6     op2 = POP(S)
7     op1 = POP(S)
8     expr = "(" + op1 + t + op2 + ")" / expr = t + op1 + op2
9     PUSH(S, expr)
10 return POP(S)
  
```

## Expression Conversion

### Postfix → Infix/Prefix

Let's convert,  $A B + C *$  to infix expression.  $(A + B) * (C / D)$

1 create empty stack S

for each token t in Postfix expression:

if t is operand:

4 PUSH(S, t)

5 → else if t is operator:

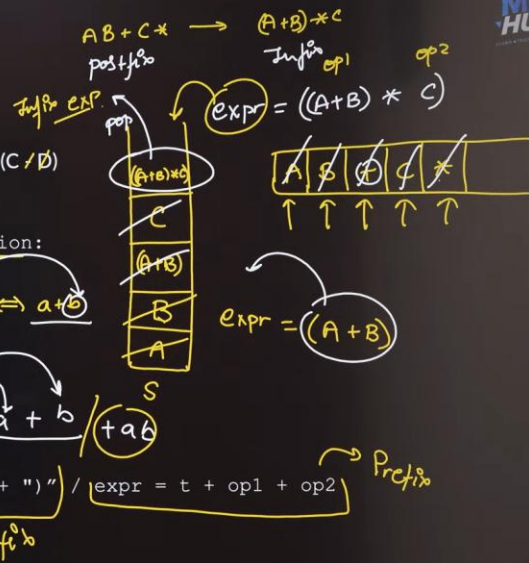
6 op2 = POP(S)

7 op1 = POP(S)

8 expr = "(" + op1 + t + op2 + ")" / expr = t + op1 + op2

9 PUSH(S, expr)

10 return POP(S)



## Expression Conversion

### Prefix → Infix/Postfix

Let's convert,  $* + A B C$ , to infix expression.

1 create empty stack S

2 for each token t in the Prefix expression scanned from right to left:

3 if t is operand:

4 PUSH(S, t)

5 else if t is operator:

6 op1 = POP(S)

7 op2 = POP(S)

8 expr = "(" + op1 + t + op2 + ")" / expr = op1 + op2 + t

9 PUSH(S, expr)

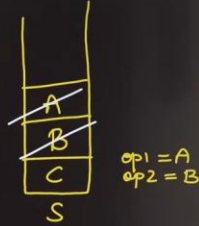
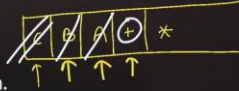
10 return POP(S)

## Expression Conversion

### Prefix → Infix/Postfix

Let's convert  $* + A B C$  to infix expression.

- 1 create empty stack  $S$
- 2 for each token  $t$  in the Prefix expression scanned from **right to left**:
- 3 if  $t$  is operand:
  - $\oplus a b \rightarrow a + b$
- 4  $PUSH(S, t)$
- 5 else if  $t$  is operator:
  - $\text{op1} = POP(S)$
  - $\text{op2} = POP(S)$
  - $\text{expr} = "(" + \text{op1} + t + \text{op2} + ")"$  /  $\text{expr} = \text{op1} + \text{op2} + t$  (Postfix)
  - $PUSH(S, \text{expr})$
- 10 return  $POP(S)$



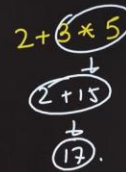
## Expression Evaluation

### Postfix Evaluation

Let's evaluate  $6 2 / 3 - 4 2 * +$

- 1 create empty stack  $S$
- 2 for each token  $t$  in postfix expression:
- 3 if  $t$  is operand:
- 4  $PUSH(S, t)$
- 5 else if  $t$  is operator:
- 6  $\text{op2} = POP(S)$
- 7  $\text{op1} = POP(S)$
- 8  $\text{result} = \text{op1 operator op2}$
- 9  $PUSH(S, \text{result})$
- 10 return  $POP(S)$

a. { Postfix eval.  
b. { Prefix eval.



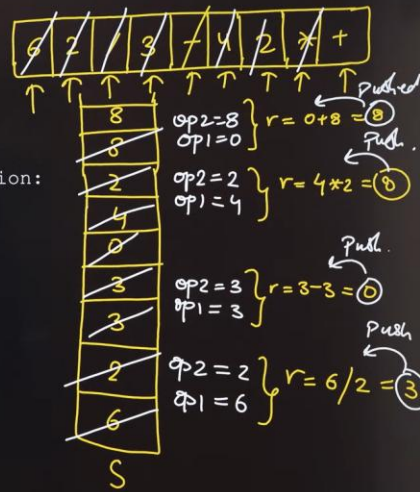


## Expression Evaluation

### Postfix Evaluation

Let's evaluate  $6\ 2\ / \ 3\ - \ 4\ 2\ * \ +$

- 1 create empty stack S
- 2 for each token t in postfix expression:
  - 3 if t is operand:
  - 4  $PUSH(S, t)$
  - 5 else if t is operator:
  - 6  $op2 = POP(S)$
  - 7  $op1 = POP(S)$
  - 8  $result = op1\ operator\ op2$
  - 9  $PUSH(S, result)$
  - 10 return  $POP(S)$



## Expression Evaluation

### Prefix Evaluation

Let's evaluate  $- \ + \ 2 \ 3 \ * \ 5 \ 4 \ 9$

- 1 create empty stack S
- 2 for each token t in prefix exp (scan right to left)
  - 3 if t is operand:
  - 4  $PUSH(S, t)$
  - 5 else if t is operator:
  - 6  $op1 = POP(S)$
  - 7  $op2 = POP(S)$
  - 8  $result = op1\ operator\ op2$
  - 9  $PUSH(S, result)$
  - 10 return  $POP(S)$

