






Machine Learning

GO Classes



Host

Bias-Variance Tradeoff

www.goclasses.in




00:43 -1:19:32



Machine Learning


GO Classes

Host

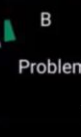


Guessing

underfitting
(simple model)




A



B

Mr. know it all


overfitting







C

Problem solving approach:


just right



Professor




02:02 -1:18:13




Machine Learning

GO Classes




Host



A
under fit


B
Just Right

C
overfit




03:09

1:17:06

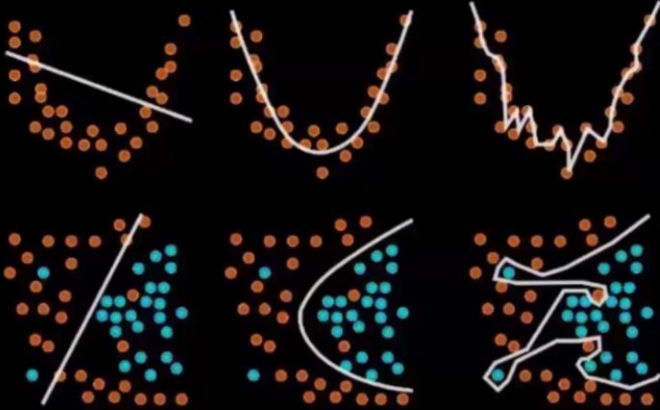



Machine Learning

GO Classes



Host





04:37

1:15:38

GO CLASSES

Machine Learning

GO Classes

Host

	Under-fitting	Optimal-fitting	Over-fitting
Regression			
Classification			

www.goclasses.in

05:03
-1:15:12

GO CLASSES

Machine Learning


GO Classes

Host

	Under-fitting	Optimal-fitting	Over-fitting
Regression			

these both can not generalise but for separate reasons

www.goclasses.in




Machine Learning


GO Classes

Generalization error Components


- Bias: Component of generalization error due to model is less expressive
- Variance: Component of generalization error due to model is too much expressive and data is less.



Host



09:42 -1:10:33




Machine Learning

GO Classes


Generalization error Components

- ✗ • Bias: Component of generalization error due to model is less expressive
- γ • Variance: Component of generalization error due to model is too much expressive and data is less.

Test error = $\underbrace{x}_{\text{Bias}} + \underbrace{y}_{\text{Variance}}$



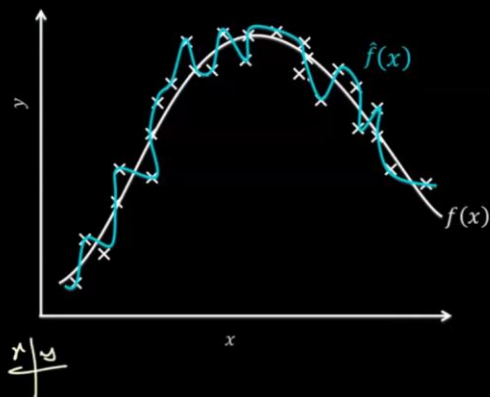
Host



11:11 -1:09:04

Bias → underfitting

Variance → overfitting

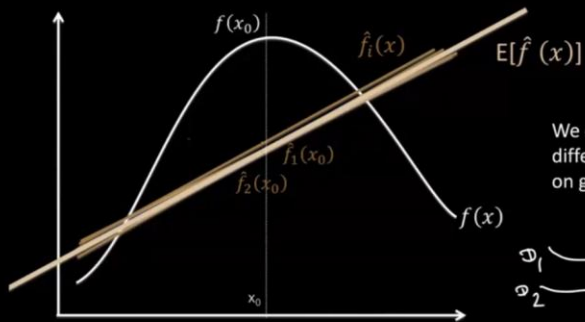


- Let $f(x)$ be the true model (usually unknown)

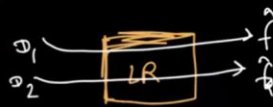
- $MSE = \sum_i (y_i - \hat{y}_i)^2$

- $\hat{y} = \hat{f}(x)$ \hat{f} could be simple or complex model

$\hat{f}(x)$ is complex model in this case.



We can keep on taking different datasets and keep on getting new models.



$$\text{Bias} = E[\hat{f}(x)] - f(x) \quad \left\{ \begin{array}{l} \text{won't this term} \\ \text{will be higher} \\ \text{for simple model?} \end{array} \right.$$

GO CLASSES
Machine Learning
GO Classes

$f(x)$
 $f_1(x)$
 $f_2(x)$
 $f_i(x)$
 $E[f(x_0)]$
 x_0
 x
 y

$Bias = E[\hat{f}(x)] - f(x)$
 $E[\hat{f}(x)]$

Ajay Sreenivas to Everyone 10:39 AM

average model is closer to $f(x)$ in this case

D44_sumaya to Everyone 10:40 AM

Less

Sriyash to Everyone 10:40 AM

less

www.goclasses.in

29:57 -50:18

GO CLASSES
Machine Learning
GO Classes

$f(x_0)$
 $\hat{f}_i(x)$
 $E[\hat{f}(x)]$
 $f_1(x_0)$
 $f_2(x_0)$
 $f(x)$
 x_0
 x
 y

Simple Model

Bias is more


Complex Model

Bias is less

www.goclasses.in

31:24 -48:51

GO CLASSES
Machine Learning
GO Classes




Bias

- Let $f(x)$ be the true model and $\hat{f}(x)$ be our estimate of the model.


$$\text{Bias}(\hat{f}(x)) = E[\hat{f}(x)] - f(x)$$

Mathematically, this means that the simple model has a high bias


www.goclasses.in

E → estimated

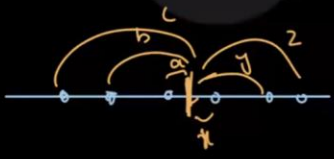
GO CLASSES
Machine Learning
GO Classes




Variance

- Let $f(x)$ be the true model and $\hat{f}(x)$ be our estimate of the model.

$$\text{Variance}(\hat{f}(x)) = E[(\hat{f}(x) - E[\hat{f}(x)])^2]$$



$$\frac{a^2 + b^2 + c^2 + x^2 + y^2 + z^2}{6}$$

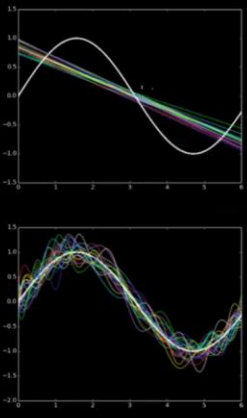

www.goclasses.in

36:11
||
-44:04


GO CLASSES


Machine Learning

GO Classes



- In summary (informally)
- Simple model: high bias, low variance
- Complex model: low bias, high variance
- There is always a trade-off between the bias and variance
- Both bias and variance contribute to the mean square error.




www.goclasses.in

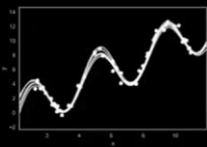
Bias → how far it is from true function

GO CLASSES

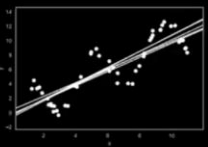
Machine Learning

GO Classes

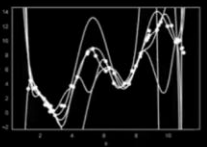
[1 Pt] Which of the following plots depicts models with the highest model variance?



(a)





(b)



(c)

☐ (a)
 ☐ (b)
 ☒ (c)




www.goclasses.in

41:43
38:32

Machine Learning

GO Classes

Host

[2 Pts] Which of the following depicts models with the largest bias?

www.goclasses.in

42:05 -38:10

Machine Learning

GO Classes

Host

Test Error

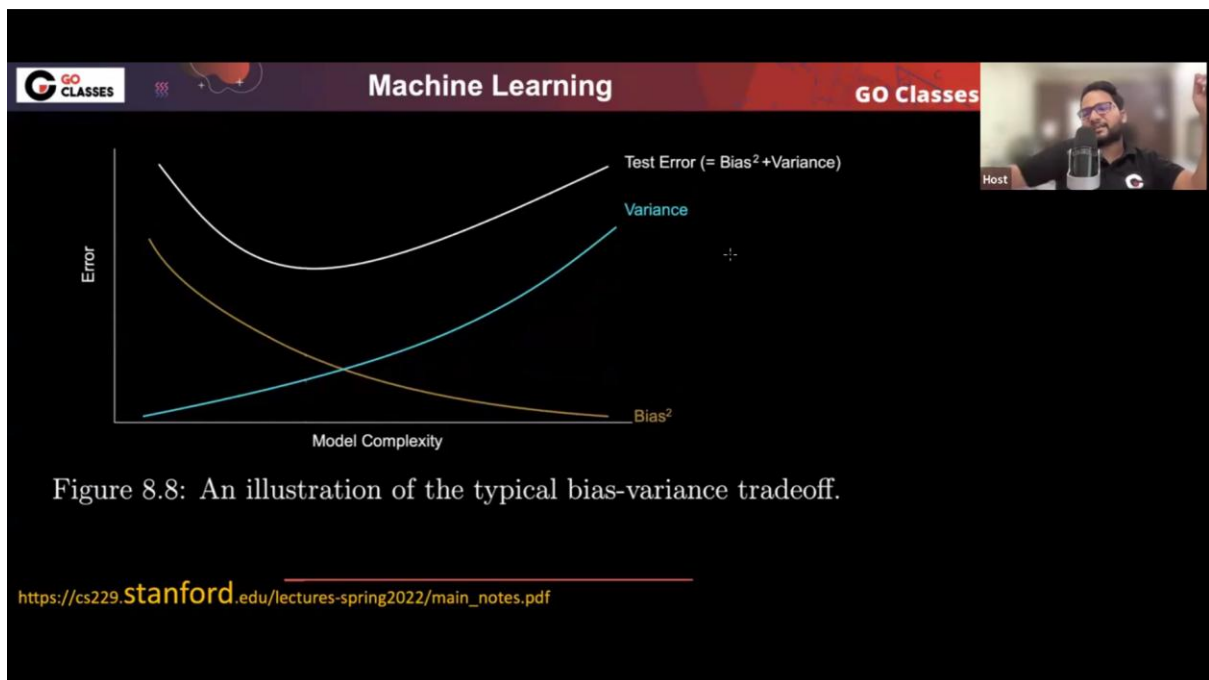
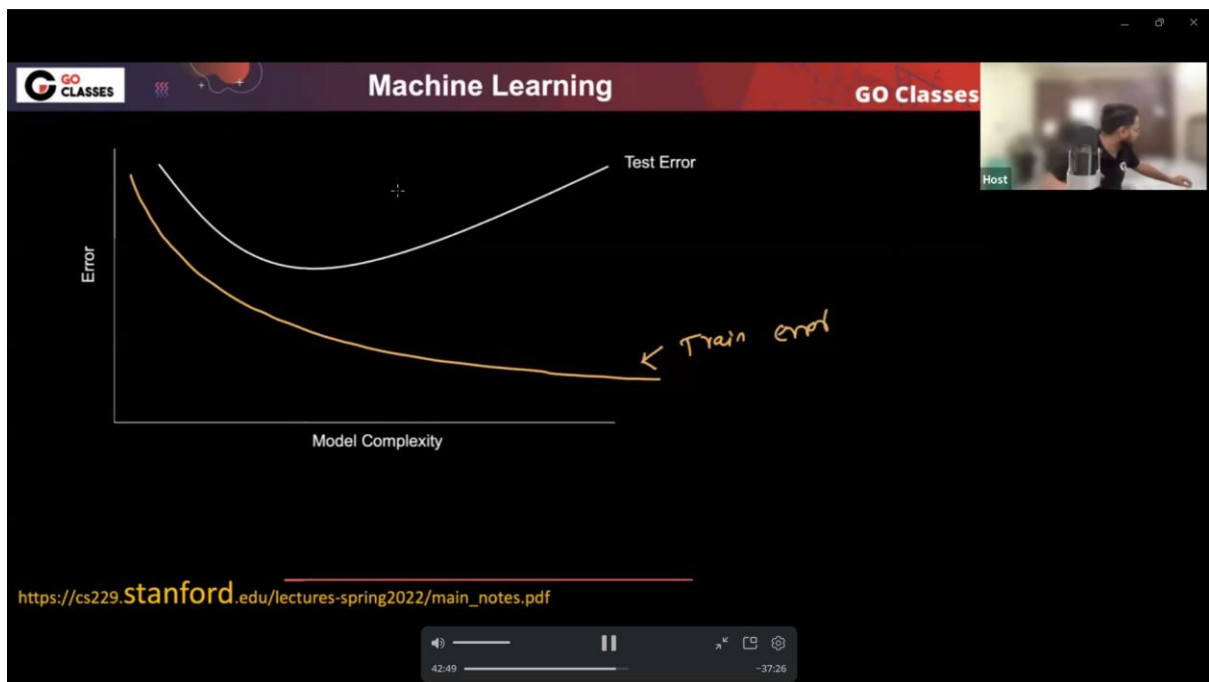
Error

Model Complexity


https://cs229.stanford.edu/lectures-spring2022/main_notes.pdf

42:18 -37:57


If we keep on increasing the complexity at some point the test error will also increase..



Predictions distance less → less variance



Machine Learning





Low Bias


High Bias

Low Variance


High Variance


www.goclasses.in




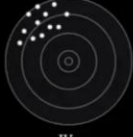




Machine Learning



Question:


I. II. III. IV.


Figure 1: The following graphic will be used as a representation of bias and variance. Imagine that a true/correct model is one that always predicts a location at the center of each target (being farther away from the center of the target indicates that a model's predictions are worse). We retrain a model multiple times, and make a prediction with each trained model. For each of the targets, determine whether the bias and variance is low or high with respect to the true model.

In Figure 1, subplot I, how are bias and variance related to the true model?

- (A) High bias, High variance
- (B) High bias, Low variance
- (C) Low bias, High variance
- ✓ (D) Low bias, Low variance





<https://courses.o.washington.edu/courses/cs446/23su/notes/pd08sum/22low-midterm-solutions.pdf>





GO CLASSES
Machine Learning
GO Classes

Question:







I. II. III. IV.

Figure 1: The following graphic will be used as a representation of bias and variance. Imagine that a true/correct model is one that always predicts a location at the center of each target (being farther away from the center of the target indicates that a model's predictions are worse). We retrain a model multiple times, and make a prediction with each trained model. For each of the targets, determine whether the bias and variance is low or high with respect to the true model.

In Figure 1, subplot II, how are bias and variance related to the true model?

(A) High bias, High variance
 (B) High bias, Low variance
 (C) Low bias, High variance
 (D) Low bias, Low variance



Host




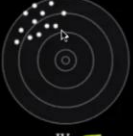
<https://courses.washington.edu/courses/cse441/23su/teams/pastexams/22su-midterm-solutions.pdf>

51:55

🔊
⏸
-28:20

GO CLASSES
Machine Learning
GO Classes

Question:







I. II. III. = B IV. =

Figure 1: The following graphic will be used as a representation of bias and variance. Imagine that a true/correct model is one that always predicts a location at the center of each target (being farther away from the center of the target indicates that a model's predictions are worse). We retrain a model multiple times, and make a prediction with each trained model. For each of the targets, determine whether the bias and variance is low or high with respect to the true model.

In Figure 1, subplot II, how are bias and variance related to the true model?

(A) High bias, High variance
 (B) High bias, Low variance
 (C) Low bias, High variance
 (D) Low bias, Low variance



Host

<https://courses.washington.edu/courses/cse441/23su/teams/pastexams/22su-midterm-solutions.pdf>

52:07

🔊
⏸
-28:08

Question:



Figure 1: The following graphic will be used as a representation of bias and variance. Imagine that a true/correct model is one that always predicts a location at the center of each target (being farther away from the center of the target indicates that a model's predictions are worse). We retrain a model multiple times, and make a prediction with each trained model. For each of the targets, determine whether the bias and variance is low or high with respect to the true model.

In Figure 1, subplot II, how are bias and variance related to the true model?

- (A) High bias, High variance
- (B) High bias, Low variance
- ☒ (C) Low bias, High variance
- (D) Low bias, Low variance

https://courses.cs.washington.edu/courses/cs446/23au/exams/pastexams/22au_midterm_solutions.pdf



Question:



[1 points] What best defines the relationship between a model's fit and its bias and variance

- (a) A model with low bias and high variance is underfitting
- (b) A model with high bias and high variance is underfitting
- (c) A model with low bias and low variance is underfitting
- (d) A model with high bias and low variance is underfitting


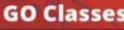


https://www.seas.upenn.edu/~cis520/exams/midterm2022_solutions.pdf





Machine Learning







[1 points] What best defines the relationship between a model's fit and its bias and variance



- (a) A model with low bias and high variance is underfitting
- (b) A model with high bias and high variance is underfitting
- (c) A model with low bias and low variance is underfitting
- (d) A model with high bias and low variance is underfitting

★ SOLUTION: D



https://www.seas.upenn.edu/~cis520/exams/midterm2022_solutions.pdf



54:02 -26:13



Machine Learning




How will regularizing the weights in a linear regression model change the bias and variance (relative to the same model with no regularization)?





- (A) Increase bias, increase variance
- (B) Increase bias, decrease variance
- (C) Decrease bias, increase variance
- (D) Decrease bias, decrease variance

Solution:

The solution is (B).



www.goclasses.in



56:02 -24:13



Question:

How will regularizing the weights in a linear regression model change the bias and variance (relative to the same model with no regularization)?

- (A) Increase bias, increase variance
- (B) Increase bias, decrease variance
- (C) Decrease bias, increase variance
- (D) Decrease bias, decrease variance

Regularization



reduce overfitting



reduce variance

<https://courses.cs.washington.edu/courses/cse446/23wi/assignments/midterm/midterm-solutions.pdf>





(1 point) Peanut wants to train a model to accurately classify different types of animals from images. After training and testing his model, he observes that the model has high training error and high test error. What can we most confidently say about the bias/variance characteristics of Peanut's model?

- A. High bias. ✓ → model is simple
- B. Low bias.
- C. High variance.
- D. Low variance. ✓ (because high training error is given)

Solution: A. High bias because the model has high training error.


High training error ⇒ Simple model

⇒ High bias
Low variance



Machine Learning

GO Classes


Host


Question: MSQ





Which of the following can impact our model variance? Select all that apply.



- ☐ The regularization coefficient λ . ✓
- ☐ The choice of features to include in our design matrix. ✓
- ☐ The learning rate α in gradient descent. ✗
- ☐ The size of the training set. ✓

↳ Variance is reduced if
Size of training set increases

↳ complicated features
↓
complex model
↓
Variance is high


www.goclasses.in


1:06:41 -13:34




Machine Learning





GO Classes


Host


Which of the following are indications that you should regularize? Select all that apply.

- ☐ A. Our training loss is 0.
- ☐ B. Our model bias is too high.
- ☐ C. Our model variance is too high.
- ☐ D. Our weights are too large.

www.goclasses.in


1:09:16 -10:59


GO CLASSES
Machine Learning
GO Classes



Reducing the regularization of a model would typically . . .


- (a) Decrease its bias and increase its variance
- (b) Decrease its bias and decrease its variance
- (c) Increase its bias and decrease its variance
- (d) Increase its bias and increase its variance

Correct answers: (a) ✓


www.goclasses.in

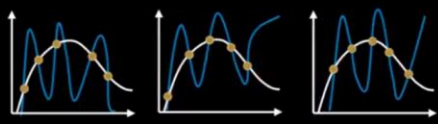
1:16:46
||
-03:29

GO CLASSES
Machine Learning
GO Classes



Variance

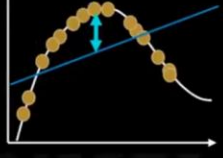
Regardless of what the true function is, how much does our prediction change with dataset?




Variance reduces if we increase data

Bias²

This error doesn't go away no matter how much data we have!



Bias = $E(\hat{f}(x)) - f(x)$


www.goclasses.in

Machine Learning

Consider a quintic (degree 5) model $\hat{y} = \hat{\theta}_0 + \hat{\theta}_1 x + \dots + \hat{\theta}_5 x^5$, where $\hat{\theta}_j$ is the MSE parameter estimate for feature j of this quintic model. You first fit this model to Training Set #1; then, you fit this model again to Training Set #2.

Training Set #1

Training Set #2

(i) The primary contributor to this model's risk is: ☐ High bias ☒ **High variance**

(ii) This contributor to model risk can be addressed by the following (select all that apply):

- ☒ **Reducing model complexity**
- ☐ Adding additional features to the model
- ☐ Reducing the regularization hyperparameter λ
- ☒ **Increasing the regularization hyperparameter λ**

Host

https://ds100.org/sp24/resources/assets/exams/sp23/sp23_final_sol.pdf

16:16
1:42:54

Machine Learning

(b) [1 Pt] Suppose we control the complexity of the linear models using a Ridge penalty term $\lambda \sum \beta_i^2$. Which of the following is true?

☐ The left side of the graph represents small λ .

☒ **The right side of the graph represents small λ .**

Solution: A smaller λ value means higher model complexity. Remember that a zero λ value means a model with no regularization.

(c) [3 Pts] Which of the following can impact our model variance? Select all that apply.

- ☒ **The regularization coefficient λ .**
- ☒ **The choice of features to include in our design matrix.**
- ☐ The learning rate α in gradient descent.
- ☒ **The size of the training set.**

Host

www.goclasses.in

21:03
1:38:07