

1. Given $g_1 = f_1 + h_2 * f_2$, $g_2 = h_1 * f_1 + f_2$
 g_1, g_2, h_1, h_2 are known.

$$F(g_1) = F(f_1 + h_2 * f_2)$$

$$\rightarrow G_1 = F_1 + H_2 F_2 \quad \text{--- (1)}$$

$$\text{Similarly } G_2 = H_1 F_1 + F_2 \quad \text{--- (2)}$$

from above equations, we can write,

$$F_1 (1 - H_1 H_2) = G_1 - H_2 G_2$$

$$F_2 (1 - H_1 H_2) = G_2 - H_1 G_1$$

$$\text{if } H_1 H_2 \neq 0 \text{ then } f_1 = \frac{G_1 - H_2 G_2}{1 - H_1 H_2} \text{ and } f_2 = \frac{G_2 - H_1 G_1}{1 - H_1 H_2}$$

$$f_1 = F^{-1} \left(f_1 \right) = F^{-1} \left(\frac{G_1 - H_2 G_2}{1 - H_1 H_2} \right)$$

$$f_2 = F^{-1} \left(f_2 \right) = F^{-1} \left(\frac{G_2 - H_1 G_1}{1 - H_1 H_2} \right)$$

\rightarrow We might not be able to recover ~~few~~ the higher frequency components as H_1 and H_2 are lowpass (blue) filters, as ~~and~~ the corresponding f_1 and f_2 will blow up.