

**3** Prove that the problem associated with language  $A_{TM}$  defined below is undecidable. You are given that  $HALT = \{ \langle M, w \rangle : M \text{ is a Turing machine and } M \text{ halts on } w \}$  is undecidable. Use the template provided to perform a mapping reduction. You must give your answer on this exam question sheet.

**EX8** The language  $L_3$  is defined as  $L_3 = \{ \langle M, w \rangle : M \text{ is a TM that does not accept } w \}$ .

**EX9** The language  $L_3$  is defined as  $L_3 = \{ \langle M \rangle : M \text{ is a Turing machine and } M \text{ accepts at most one word} \}$ .

**EX10** The language  $L_3$  is defined as  $L_3 = \{ \langle M, a, b \rangle : M \text{ is a Java program, } a \text{ and } b \text{ are integer variables declared in } M, \text{ and when } M \text{ is run, } a \text{ is never less than } b \}$ .

**EX11** The language  $L_3$  is defined as  $L_3 = \{ \langle M \rangle : M \text{ is a Java program, and when } M \text{ is run it never raises an exception} \}$ .

**EX12** The language  $L_3$  is defined as  $L_3 = \{ \langle M \rangle : M \text{ is a Turing machine and } |L(M)| \text{ does not contain any words of length greater than five symbols} \}$ .

**EX13** The language  $L_3$  is defined as  $L_3 = \{ \langle M \rangle : M \text{ is a Turing machine and } |L(M)| \text{ does not contain any words of length less than five symbols} \}$ .