

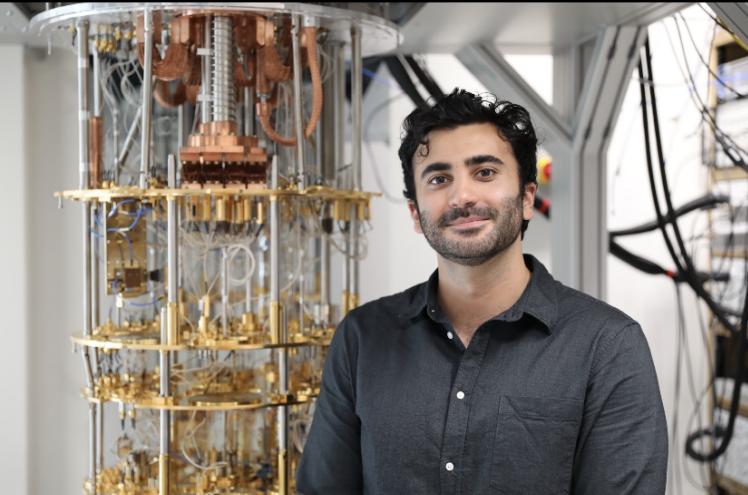


# **Superconducting Circuits for Quantum Computing**

**QEDi Day 1 Lecture 3  
15/09/2025  
Kian Jansépar**

## Outline

- Superconductivity
- Quantum Harmonic Oscillator
- Josephson Junctions
- Transmon Qubit
- Superconducting Qubit Industry



## Kian Jansepar

- Coming from a quantum hardware background, designing and characterizing superconducting circuits for quantum computing.
- 2nd year PhD Student at UCL

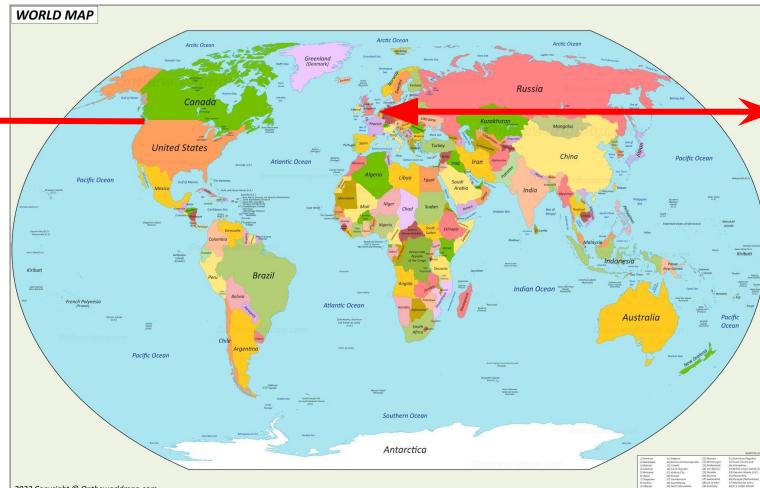
# Berkeley

UNIVERSITY OF CALIFORNIA



deepSight™

Lawrence Livermore  
National Laboratory



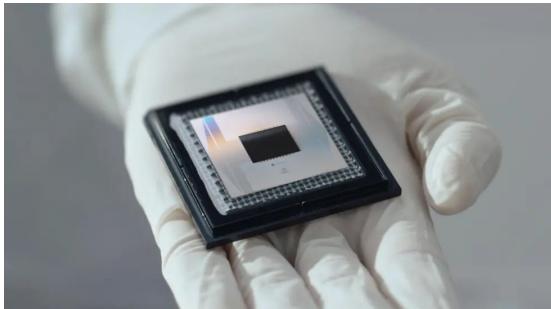
Imperial College  
London

QUANTUM  
MOTION

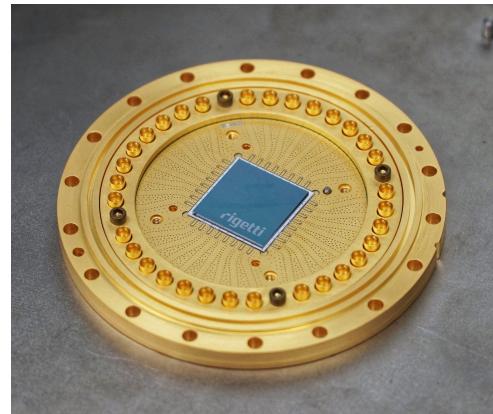
EVOTRACK

# Who uses superconducting quantum qubits?

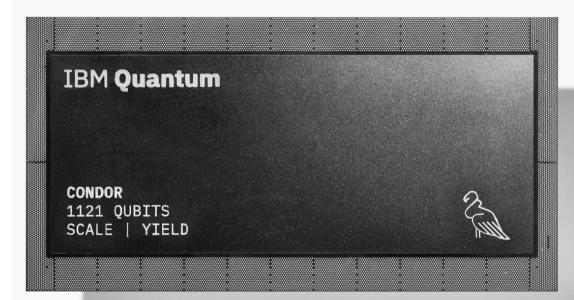
Google



Rigetti



IBM



Most popular platform for qubits at the moment:

- High fidelity operations
- Long coherence times
- Offers degrees of freedom for tunability



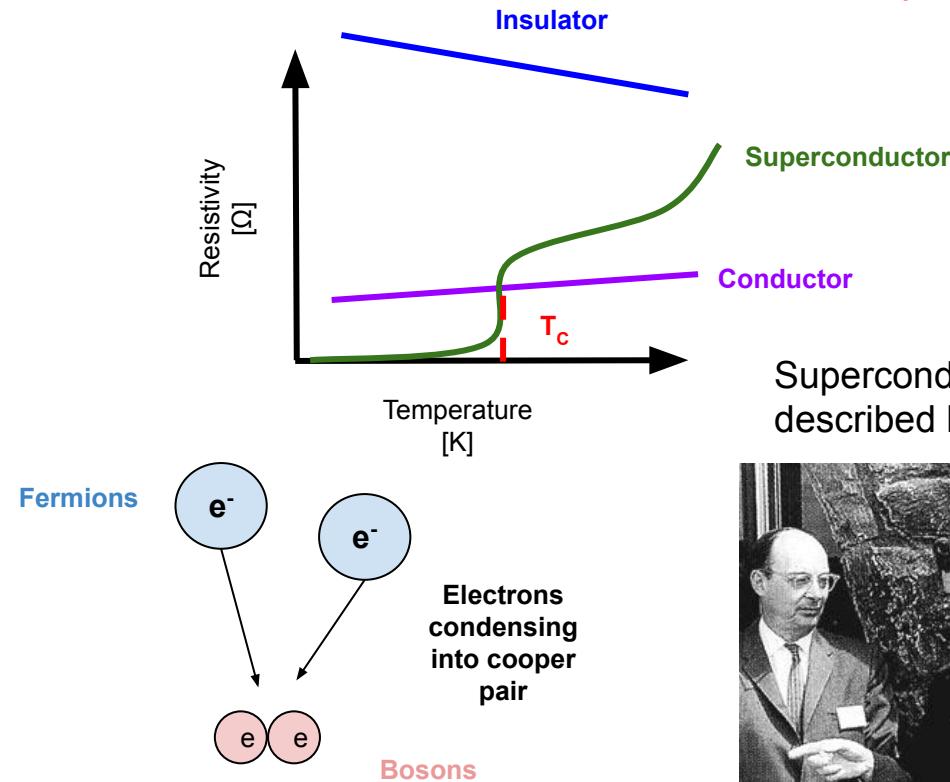
# Superconductivity

## Critical Temperature

$T_c$ : Critical Temperature

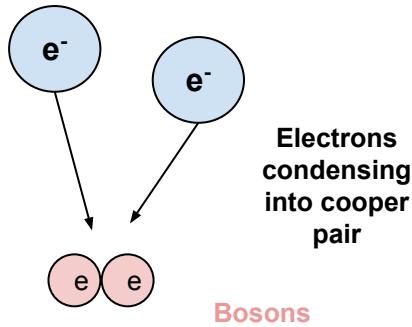
Electrical Conductors	Electrical Insulators
 Silver	 Wood
 Copper	 Rubber
 Sea water	 Oil

<https://ksa.mytutorsource.com/blog/electrical-conductor-electrical-insulator-and-thermal-conductor/>

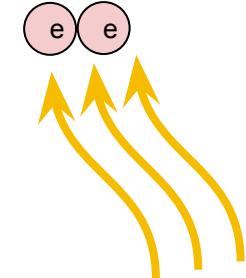


Superconductivity is best described by BCS theory.

# Superconductivity

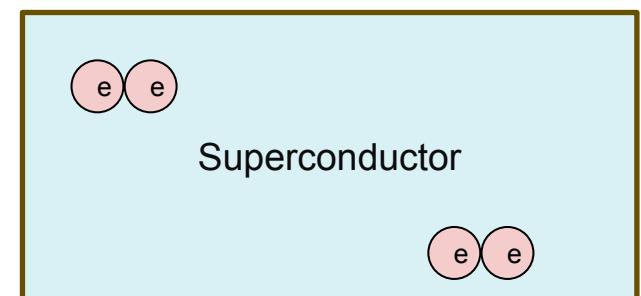
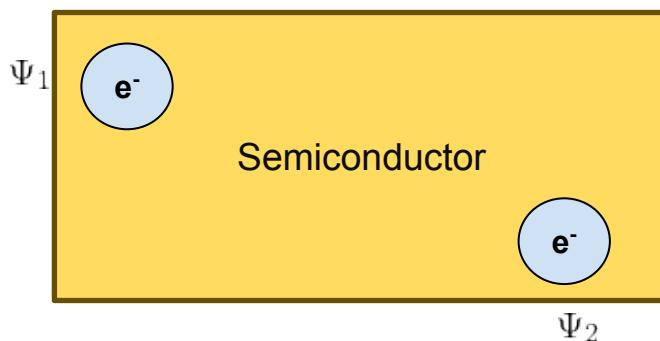


- Cooper pairs in superconductor behave as macroscopic entity with bosonic behavior
- $2\Delta$  is the energy needed to break cooper pair



$$\Psi(r, t) = \Psi_0 e^{i\phi(r, t)}$$

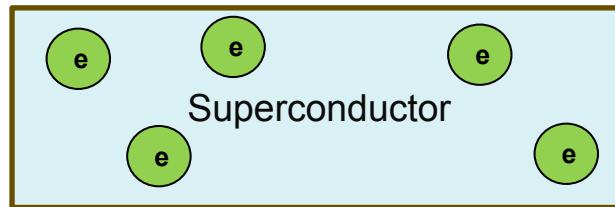
Macroscopic wavefunction (Order Parameter)



# Superconductivity

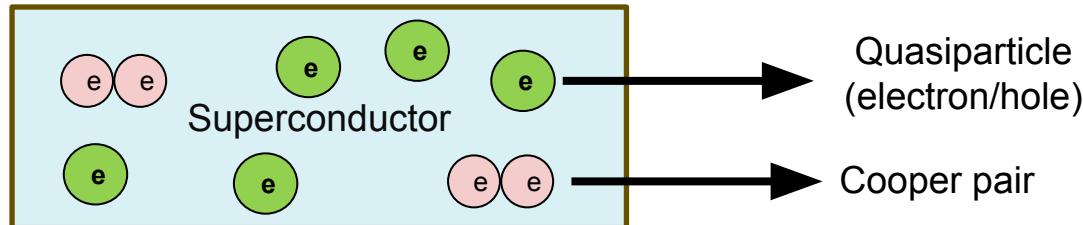
$T > T_c$

As you approach  $T_c$ , the density of quasiparticles increases, and the Cooper pair density goes to zero.



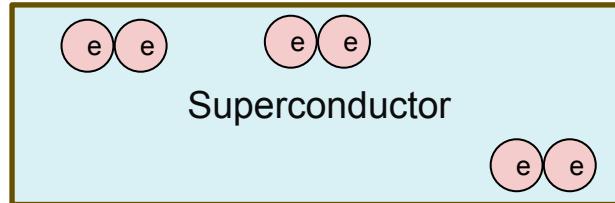
$T < T_c$

**Thermally excited** quasiparticles prevents having a coherent macroscopic wavefunction



$T \ll T_c$

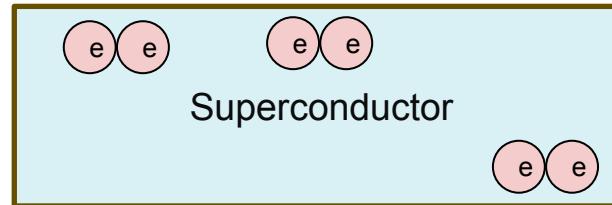
Quasiparticle number is exponentially reduced.



# Superconductivity

$$T \ll T_c$$

Quasiparticle number is exponentially reduced.  
Coherent macroscopic wavefunction is observed.



Below  $T_c$ , a moving Cooper pair condensate cannot dissipate energy through individual scattering, and slowing the entire condensate would require extremely large energy



Well defined macroscopic wavefunction  
describing a **quantum system**.

$$\Psi(r, t) = \Psi_0 e^{i\phi(r, t)}$$

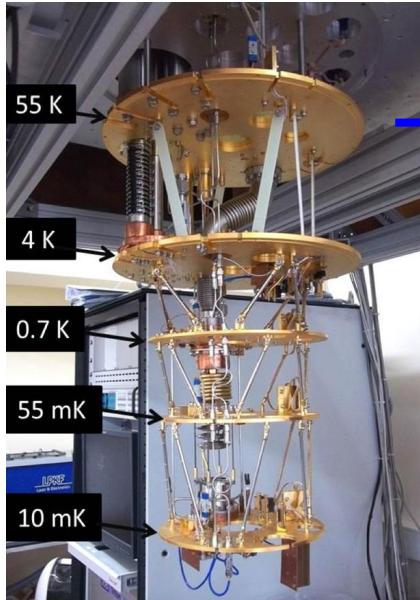
Macroscopic wavefunction (Order Parameter)

# Superconductivity

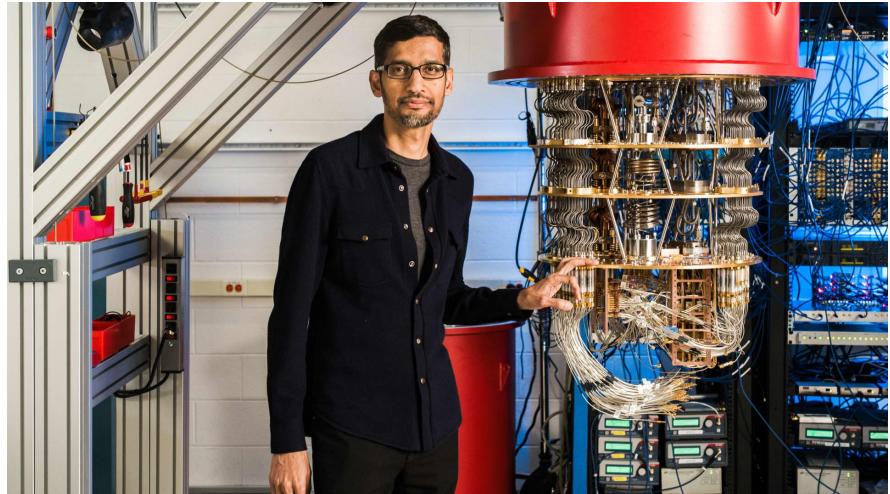
## Critical Temperature

Most widely used superconductors for quantum circuits:

- Nb ( $T_c \sim 9$  K)
- Al ( $T_c \sim 1.2$  K)



Dilution fridge used to  
cool down  
superconducting  
circuits



Google CEO Sundar Pichai stands with a quantum computer a Google laboratory in Santa Barbara, California

*Google*

$$Q(t) = \int I(t)dt$$

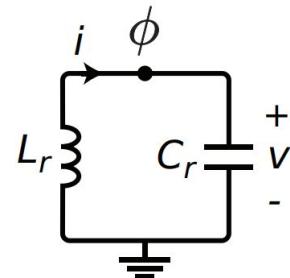
$$\Phi(t) = \int V(t)dt$$

$$E(t) = \int_{-\infty}^t V(\tau)I(\tau)d\tau$$

$$\Phi = LI$$

$$E_{inductor} = \int \dot{\Phi}I(t)dt = \int \dot{\Phi}\frac{\Phi}{L}dt = \int \frac{\Phi}{L}d\Phi = \frac{\Phi^2}{2L}$$

## Quantum Harmonic Oscillator



$$Q = CV$$

$$E_{capacitor} = \int CV(t)dV = C\frac{V^2}{2} = \frac{Q^2}{2C} = \frac{1}{2}CV^2 = \frac{1}{2}C\dot{\Phi}^2$$

$$\mathcal{L} = \frac{1}{2}C\dot{\Phi}^2 - \frac{\Phi^2}{2L}$$

Equations of motion

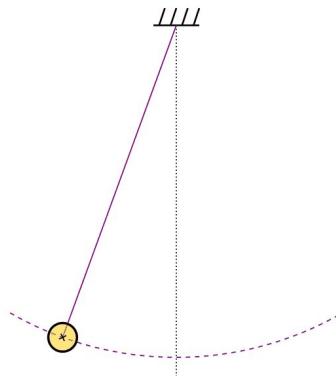
$$\frac{d}{dt} \frac{\delta \mathcal{L}}{\delta \dot{\Phi}} = \frac{\delta \mathcal{L}}{\delta \Phi}$$

$$C\ddot{\Phi} + L^{-1}\Phi = 0$$

Energy in the circuit oscillates between **magnetic field within an inductor** and the **electric field between the capacitor**

# Quantum Harmonic Oscillator

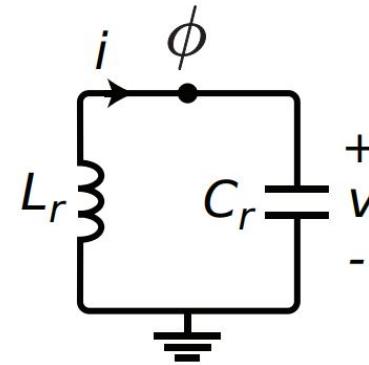
Classical Harmonic Oscillator



<https://commons.wikimedia.org/wiki/File:Pendulum-no-text.gif>

$$\begin{aligned} F &= ma = T \sin(\theta) \approx T\theta \\ T &\approx mg \rightarrow F = ma = mg\theta \\ \theta &\approx \frac{g}{l} \rightarrow F = -m\frac{g}{l} \rightarrow \boxed{F = m\ddot{x} = -kx} \end{aligned}$$

Quantum Harmonic Oscillator



<https://arxiv.org/pdf/1904.06560>

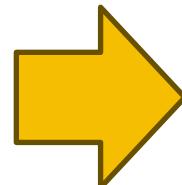
$$\begin{aligned} C\ddot{\Phi} + L^{-1}\Phi &= 0 \\ \boxed{C\ddot{\Phi} = -L^{-1}\Phi} \end{aligned}$$

# Quantum Harmonic Oscillator Hamiltonian

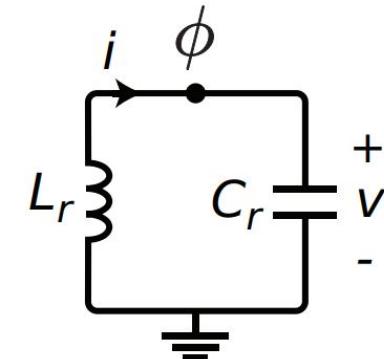
Energy of each component

$$E_{inductor} = \int \dot{\Phi}I(t)dt = \int \dot{\Phi}\frac{\Phi}{L}dt = \int \frac{\Phi}{L}d\Phi = \frac{\Phi^2}{2L}$$

$$E_{capacitor} = \int CV(t)dV = C\frac{V^2}{2} = \frac{Q^2}{2C}$$



$$H_{LC} = \frac{Q^2}{2C} + \frac{\Phi^2}{2L}$$



Defining some new variables:

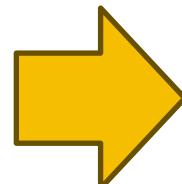
$$n = \frac{Q}{2e} \quad \text{Reduced charge}$$

$$\phi = \frac{2\pi\Phi}{\Phi_0} \quad \text{Reduced flux}$$

$$E_C = \frac{e^2}{2C} \quad \text{Charging energy}$$

$$E_L = (\Phi/2\pi)^2/L \quad \text{Inductive energy}$$

$$\Phi_0 = \frac{h}{2e}$$

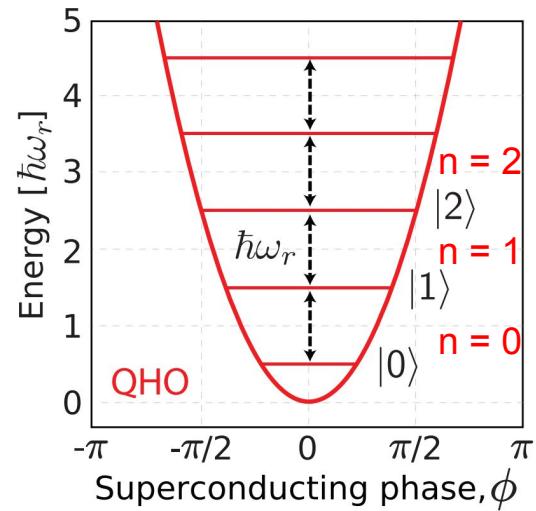


$$H = 4E_C n^2 + \frac{1}{2} E_L \phi^2$$

$$H = \hbar\omega_r(a^\dagger a + \frac{1}{2})$$

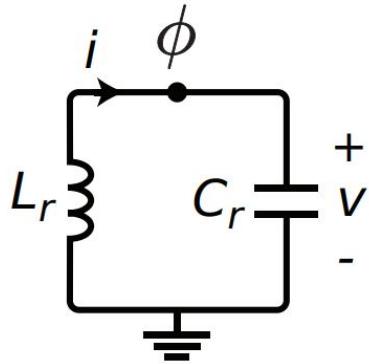
Number of cooper pairs

QHO energy in terms of cooper pair number



# Quantum Harmonic Oscillator

Circuit Diagram



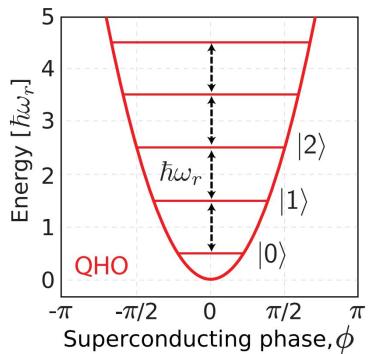
$$n = \frac{Q}{2e} \text{ Reduced charge}$$

$$\phi = \frac{2\pi\Phi}{\Phi_0} \text{ Reduced flux}$$

$$E_C = \frac{e^2}{2C} \text{ Charging energy}$$

$$E_L = (\Phi/2\pi)^2/L \text{ Inductive energy}$$

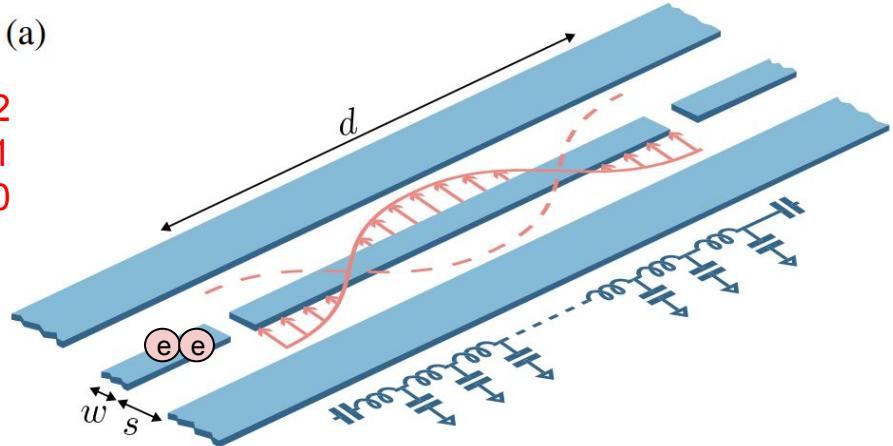
$$\Phi_0 = \frac{\hbar}{2e}$$



Superconducting film  
(Al, Nb, Ta)

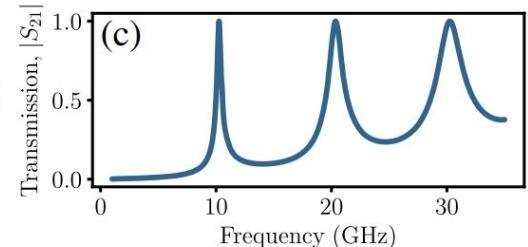
Substrate  
(Si, Sapphire)

Device Design



(b)

(c)



# Quantum Harmonic Oscillator

Schrödinger Equation

$$H |\psi(t)\rangle = i\hbar \frac{\partial}{\partial t} |\psi(t)\rangle$$

Time independent Hamiltonian

$$|\psi(t)\rangle = U(t) |\psi(0)\rangle = e^{-iHt/\hbar} |\psi(0)\rangle$$



Time evolution operator



$$H = 4E_C n^2 + \frac{1}{2} E_L \phi^2$$

QHO Hamiltonian

Do we have everything for a qubit?

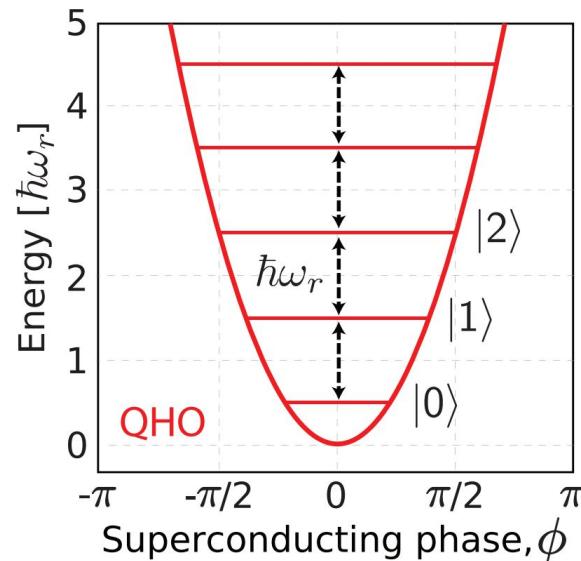
Classical bit  
1 

quantum bit (qubit)  
|0\rangle   
|1\rangle 

At the core of a qubit is a well-defined  
**two-level system**

# Quantum Harmonic Oscillator

At the core of a qubit is a well-defined  
two-level system



Is the QHO a two-level system?

**No! We need Anharmonicity!**

$n = 2$

- **Equally spaced energy levels** → The transition frequency between any two neighboring states is the same, so you can't isolate just two levels without unintentionally exciting higher ones.

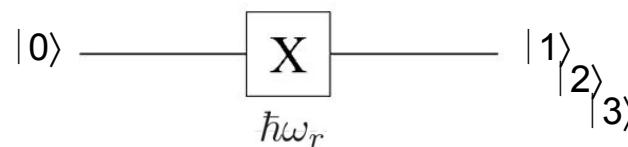
$n = 1$

- **No natural two-level truncation** → QHO doesn't provide a “forbidden” or energetically distinct subspace for a qubit.

$n = 0$

- **Leakage errors** → Driving the  $|0\rangle \leftrightarrow |1\rangle$  transition also couples strongly to  $|1\rangle \leftrightarrow |2\rangle$ , leading to population leakage outside the qubit manifold.

Example of shortcoming

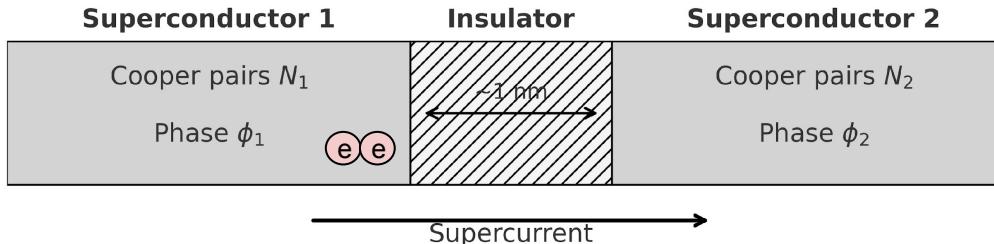


**How can we define a Two-Level System  
with superconducting circuits?**

# Towards Anharominiety Josephson Junctions

$$\Psi(r, t) = \Psi_0 e^{i\phi(r, t)}$$

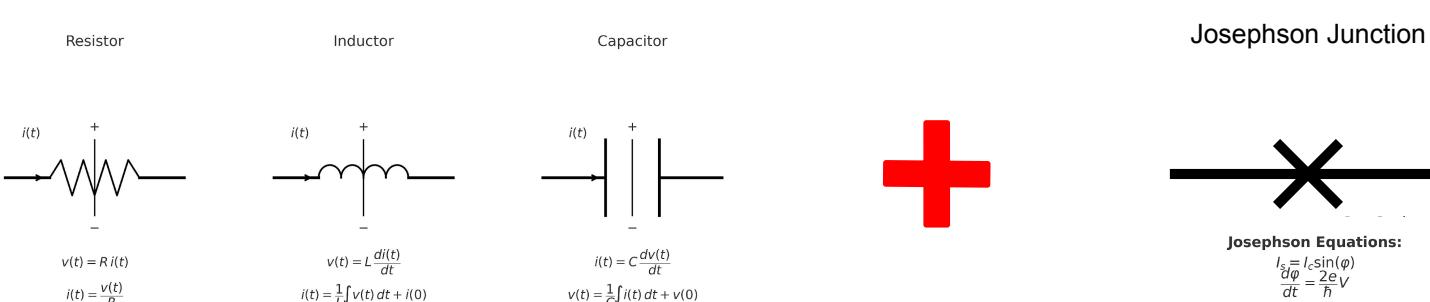
$$\Psi(r, t) = \Psi_0 e^{i\phi(r, t)}$$



Dynamical Variables:  $n = N_1 - N_2$ ,  $\varphi = \phi_1 - \phi_2$

## Josephson Equations:

$$\begin{aligned} I_s &= I_c \sin(\varphi) \\ \frac{d\varphi}{dt} &= \frac{2eV}{\hbar} \end{aligned}$$



$$E(t) = \int_{-\infty}^t V(\tau) I(\tau) d\tau$$

## Towards Anharominiety Josephson Junctions

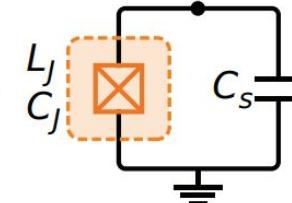
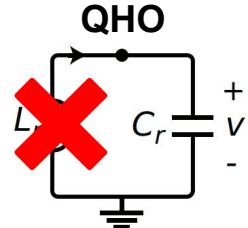
The Josephson Effect is described by 2 equations:

supercurrent,  $I_s = I_c \sin \phi$  (more generally just needs to be  $2\pi$  periodic)

rate of change of phase,  $\frac{d\phi}{dt} = \frac{2e}{\hbar} V$

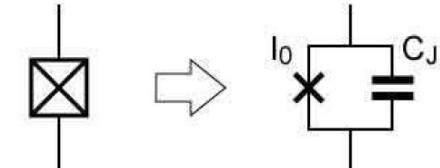
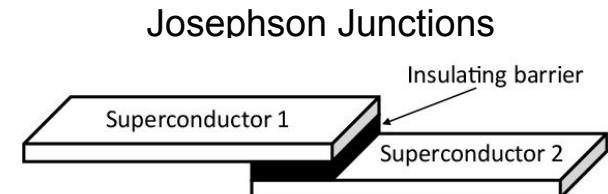
$$E_{JJ} = \int I_C \sin(\phi) \frac{\hbar}{2e} \frac{d\phi}{dt} dt = -\frac{\hbar I_C}{2e} \cos(\phi) = -\frac{\Phi_0 I_C}{2\pi} \cos(\phi) = -E_J \cos(\phi)$$

$E_{JJ} = -E_J \cos(\phi)$  **Josephson Energy**



$$H = 4E_C n^2 + \frac{1}{2} \cancel{\phi}^2$$

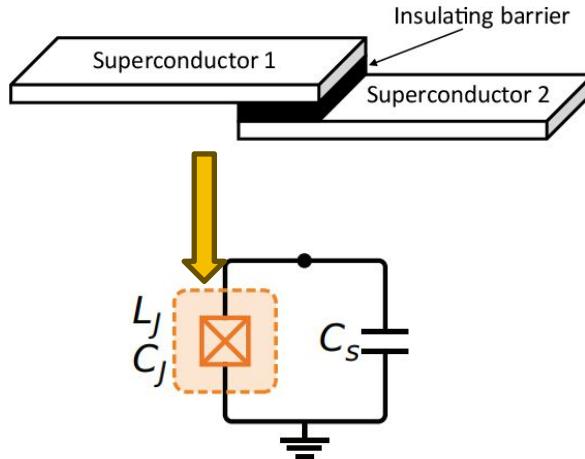
$$H = 4E_C n^2 - E_J \cos(\phi)$$



Josephson Junction have self capacitance

# Towards Anharmonicity

Josephson Junction

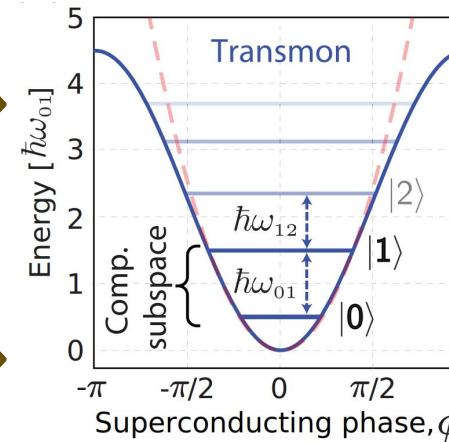


$$H = 4E_C n^2 - E_J \cos(\phi)$$

Josephson Junction have self-capacitance!

$$E_C = \frac{e^2}{2C_\Sigma} = \frac{e^2}{2(C_S + C_J)}$$

- Nonlinear inductance:** Josephson junction provides a tunable, nonlinear inductance that depends on the superconducting phase difference across it.
- Potential energy landscape:** This nonlinearity creates anharmonic energy levels instead of evenly spaced harmonic oscillator states.

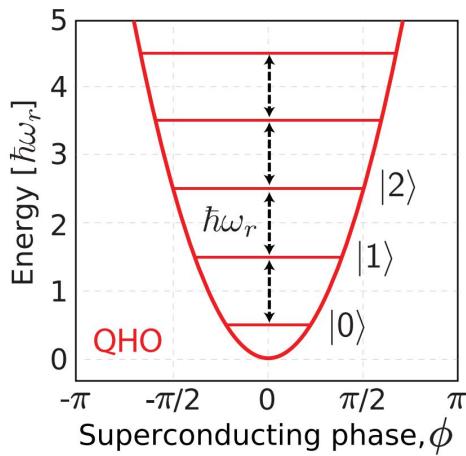
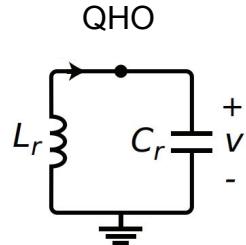


Anharmonic is related to charging energy

$$\alpha \propto E_C$$

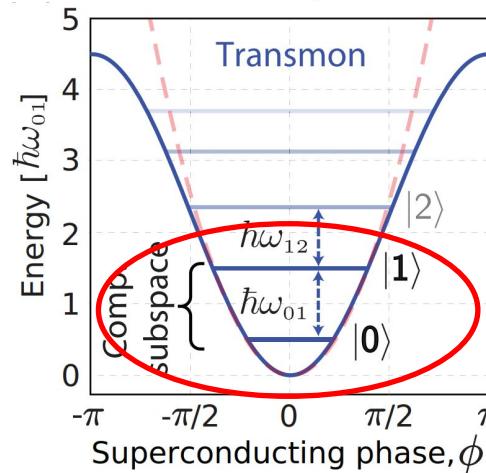
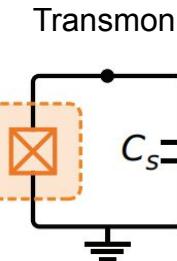
# Transmon

Creating well-defined two-level systems



- Nonlinear energy spacing
- Higher order energy states are removed
- Robust two-level system can be defined (ground & excited state)

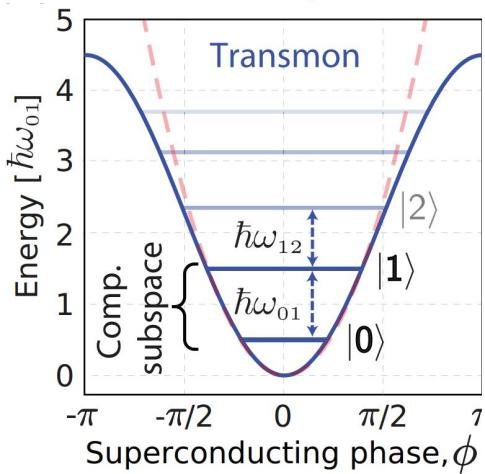
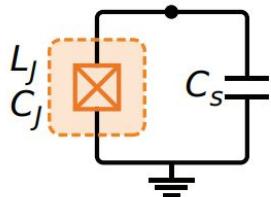
We have a Qubit!  
(aka artificial atom)



# Transmon

Creating well-defined two-level systems

Transmon

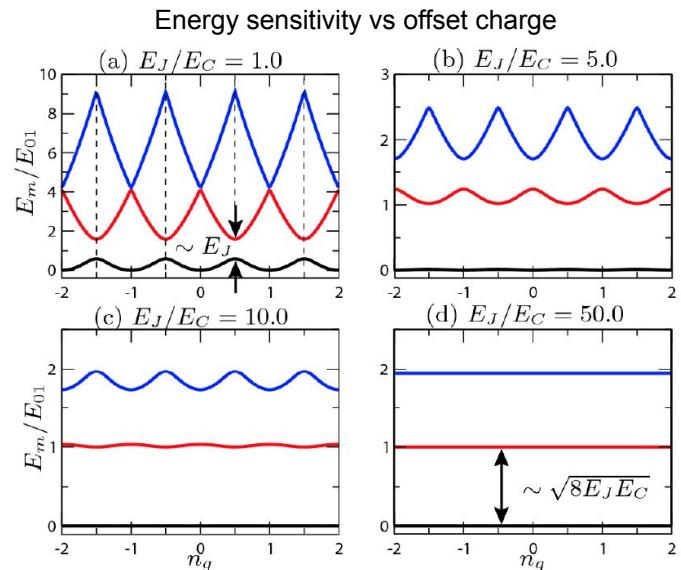


Ideal:  $H = 4E_C n^2 - E_J \cos(\phi)$

Realistic:

$$\hat{H} = 4E_C (\hat{n} - n_g)^2 - E_J \cos \hat{\varphi}$$

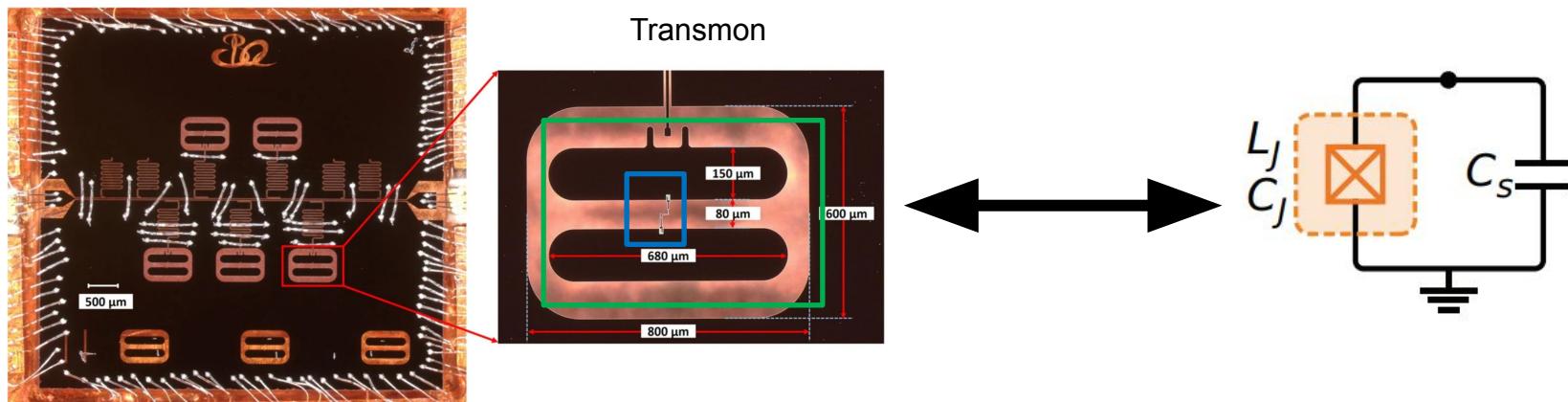
Offset charge



- Qubit dynamics depend on the ratio  $E_J/E_C$ .
- Designs use  $E_J \gg E_C$  for stable, **coherent operation**.
- If  $E_J \leq E_C$ , the qubit becomes very sensitive to **charge noise**.
- Charge noise is harder to mitigate than flux noise → coherence suffers.

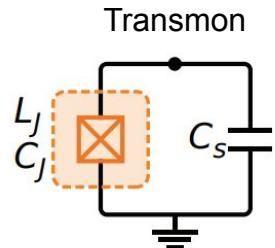
# Transmon Geometry

$$H = 4E_C n^2 - E_J \cos(\phi)$$

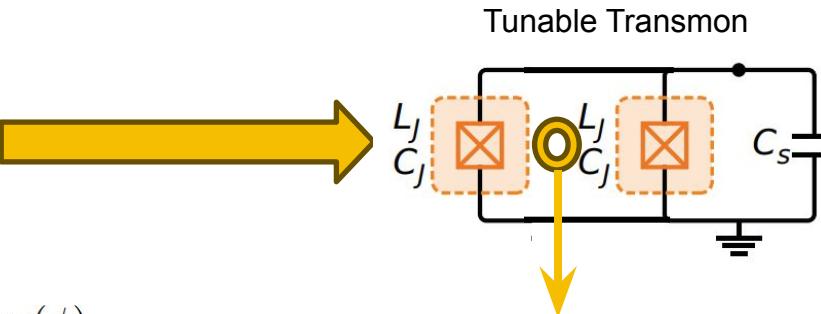


# Superconducting Quantum Interference Device (SQUID)

Can we make a tunable Transmon?



$$H = 4E_C n^2 - E_J \cos(\phi)$$



$$H = 4E_C n^2 - E_J \cos(\phi_1) - E_J \cos(\phi_2)$$

**Caveat: Fluxoid quantization condition**  
states that the total branch flux from all inductive elements in a loop, plus the applied external flux, must equal an integer multiple of the superconducting flux quantum.

$$\varphi_1 - \varphi_2 + 2\varphi_e = 2\pi k$$

$$\varphi_e = \pi\Phi_{\text{ext}}/\Phi_0$$



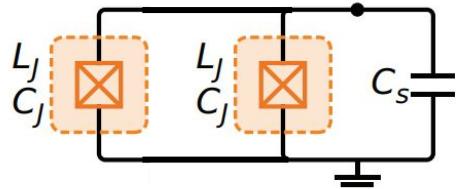
Trig Identities

$$H = 4E_C n^2 - \underbrace{2E_J |\cos(\varphi_e)|}_{E'_J(\varphi_e)} \cos(\phi)$$

The effective Josephson Energy ,  $E_J'$ , can be tuned via externally magnetic field!

# Flux-Tunable Transmon

Tunable Transmon



**Qubit frequency can be tuned!**

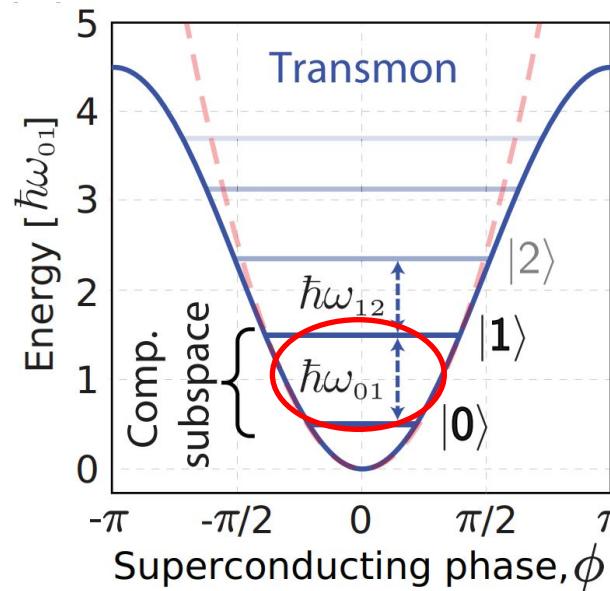
$$H = 4E_C n^2 - \underbrace{2E_J |\cos(\varphi_e)|}_{E'_J(\varphi_e)} \cos(\phi)$$

The effective Josephson Energy , EJ', can be tuned via externally magnetic field!

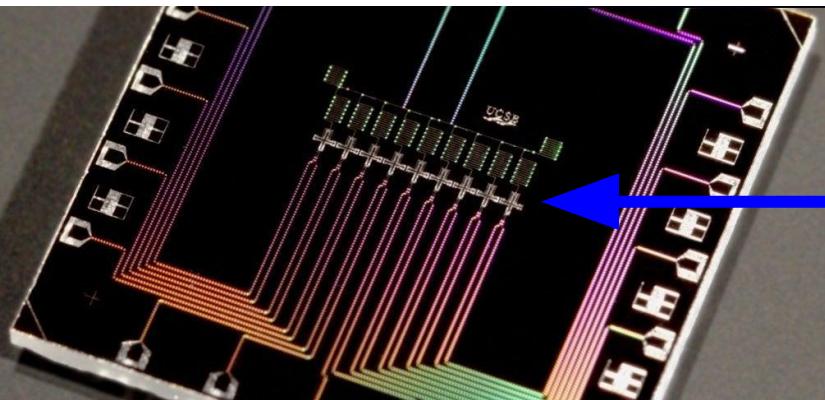
$$\hbar\omega_{qubit} = \sqrt{8E_J E_C} - E_C$$

Energy needed to excite  $|0\rangle \square |1\rangle$

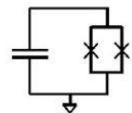
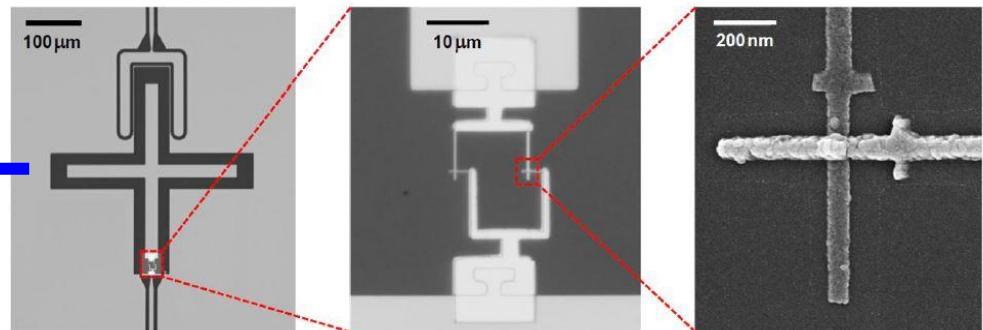
Qubit Frequency (energy) can be tuned!



# Tunable Transmon



Early superconducting qubit chip from UCSB and Google



Transmon qubit

(a)

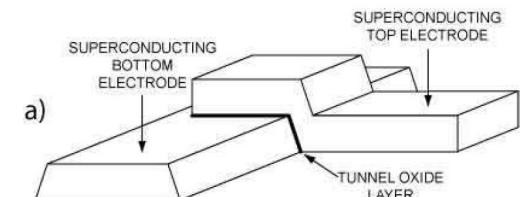


SQUID



Josephson junction

(c)



# DiVincenzo Criteria

## (5 requirements for Quantum Computers)

- Scalable physical system with well-defined qubits**

A system must allow the definition of two-level quantum states (qubits) that can be scaled up.

- Ability to initialize qubits to a known state**

You need a reliable way to prepare qubits in a simple starting state.

- Long decoherence times compared to gate times**

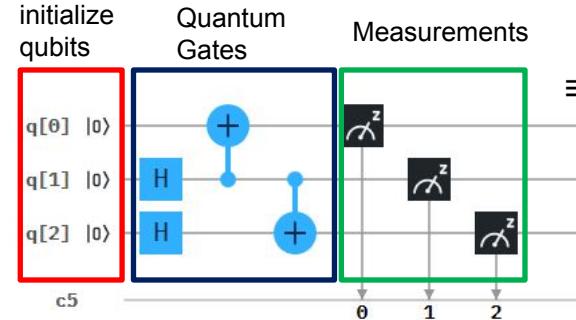
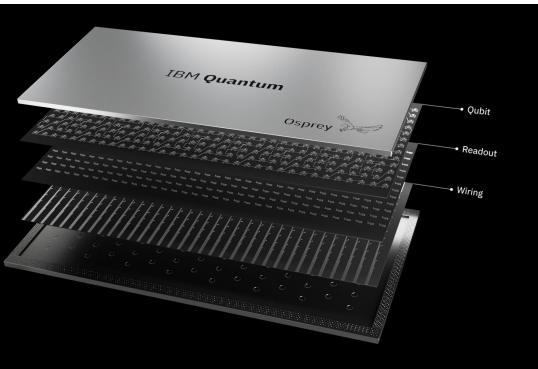
Qubits must maintain coherence long enough to perform operations before errors from the environment dominate.

- A universal set of quantum gates**

There must be physical mechanisms to implement a set of gates.

- Qubit-specific measurement capability**

It must be possible to measure individual qubits with high fidelity without disturbing others unnecessarily.



≡ Prof DiVincenzo at SQA conference in August



# Superconducting Qubit Industry

IQM Quantum Computers Raises over \$300 Million in Series B Funding Round Led by U.S. Investor Ten Eleven Ventures with strong support from Tesi

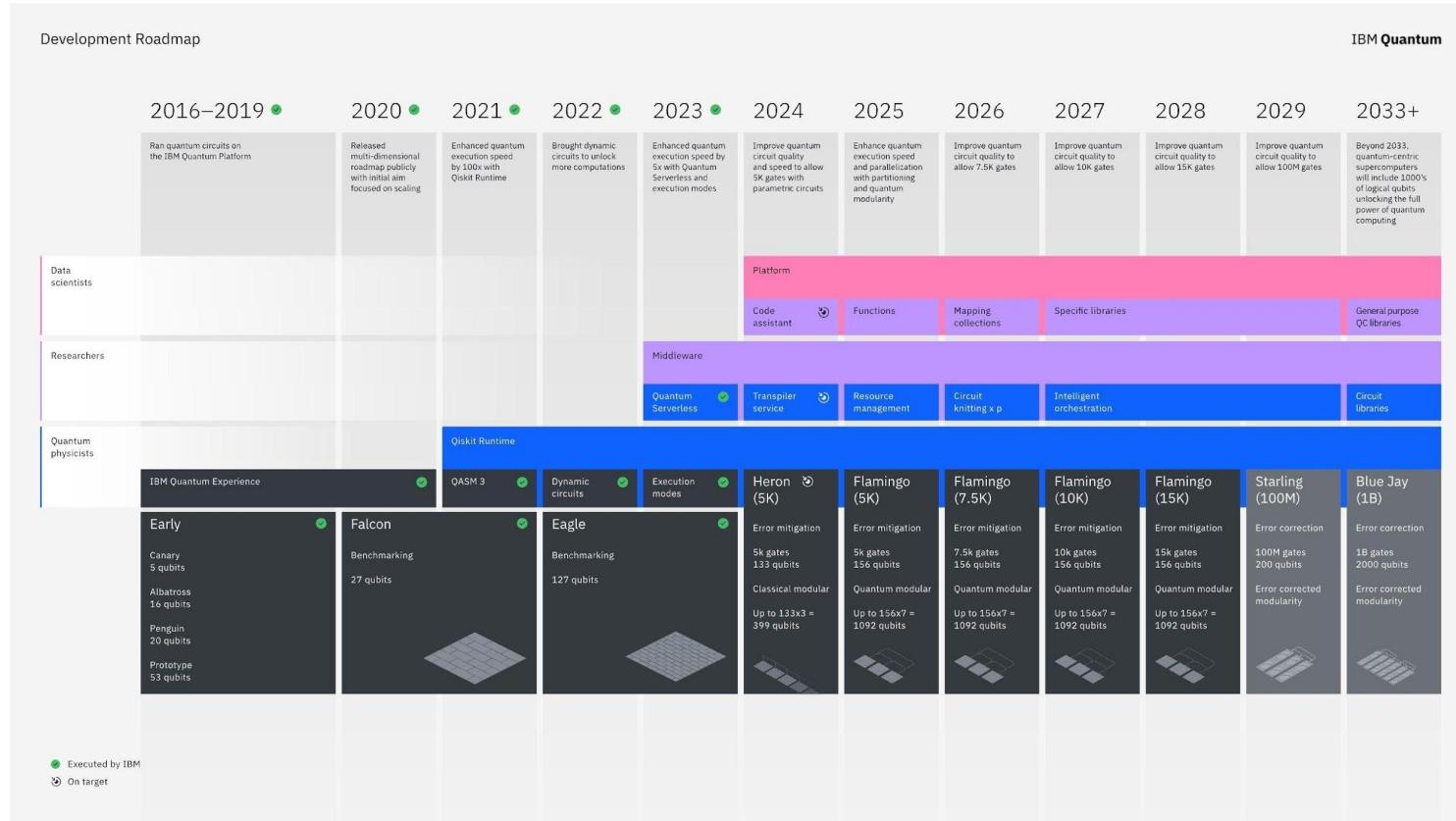
03 Sep 2025



Home > News

Delft's QuantWare extends Series A to €23.3M to unlock the path to million-qubit quantum processors

# Roadmap towards Fault-tolerant Quantum Computing



# Entire Quantum Industry

## Fresh off the press

ZACKS

### Nvidia Just Invested in this Quantum Computing Stock

Ethan Feller  
Thu, September 4, 2025 at 6:32 PM GMT+1 • 3 min read

In this article:

QBTS +4.73% ★ QBTS-WS ★ IONQ +7.29% ★ IONQ-WS ★ NVDA +1.46%

Over the past year, **Nvidia** (NVDA) CEO Jensen Huang has dramatically shifted his view on quantum computing. Once framing the technology as a breakthrough for the distant future, Huang now believes commercialization may be much sooner. Reflecting that conviction, Nvidia has begun actively positioning itself in the quantum space, and this week the company appeared to double down. Reports indicate that Nvidia has invested in **Quantinuum**, a leading quantum computing startup majority-owned by **Honeywell International** (HON).

## Quantum computing company raises a record \$1bn

PsiQuantum backed by BlackRock, Temasek and Baillie Gifford as investment race intensifies

## Maybell Quantum closes \$40m funding round for quantum computing fridges

Company looks to disrupt cryostat industry

September 08, 2025 By: Dan Swinhoe Have your say

## Inflection to go public in SPAC deal valuing quantum computing firm at \$1.8 billion

By Jaspreet Singh

September 8, 2025 9:02 PM GMT+1 • Updated September 8, 2025



## Startups founded in the UK



**river  
Lane**



Universal  
Quantum



QUANTUM  
MOTION



**OQC**

PHASE CRAFT

## UK's Quantum Industry



## Companies with HQs in the UK

**rigetti**



Inflection

$\Psi$  PsiQuantum

**TOSHIBA**

 CLASSIQ

**seeqc**



**Thank you!**

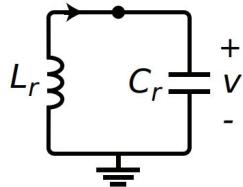


# **Superconducting Circuits for Quantum Computing**

**QEDi Day 2 Lecture 4  
16/09/2025  
Kian Jansépar**

## Recap

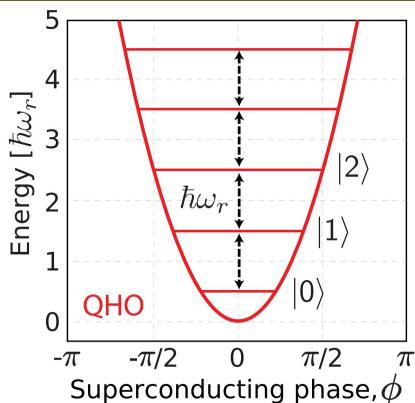
### Quantum Harmonic Oscillator



$$H = 4E_C n^2 + \frac{1}{2} E_L \phi^2$$

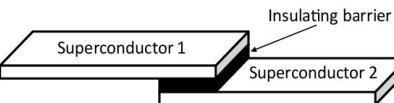
$$H = \hbar\omega_r (a^\dagger a + \frac{1}{2})$$

Number of photons

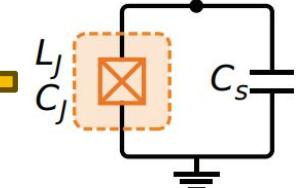


Not a well-defined two-level system for a qubit!

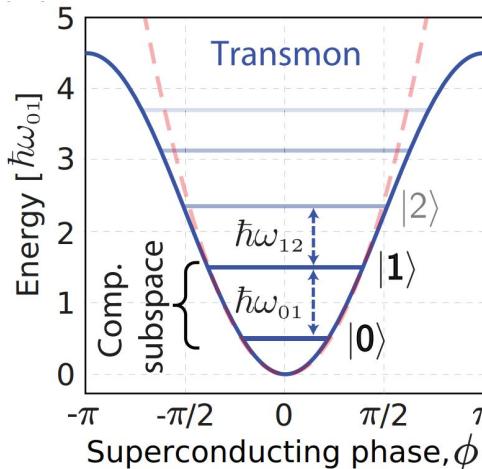
### Josephson Junction



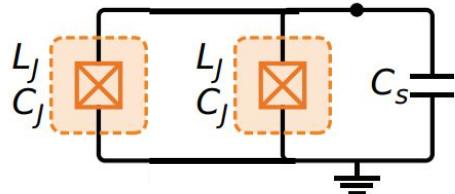
### Transmon



$$\hat{H} = 4E_C (\hat{n} - n_g)^2 - E_J \cos \hat{\varphi}$$

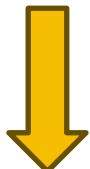


## Tunable Transmon



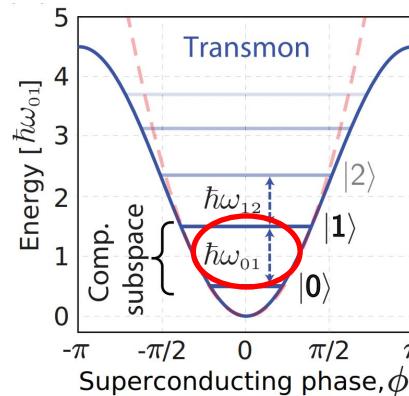
$$H = 4E_C n^2 - \underbrace{2E_J |\cos(\varphi_e)|}_{E'_J(\varphi_e)} \cos(\phi)$$

The effective Josephson Energy,  $E_J'$ , can be tuned via externally magnetic field!



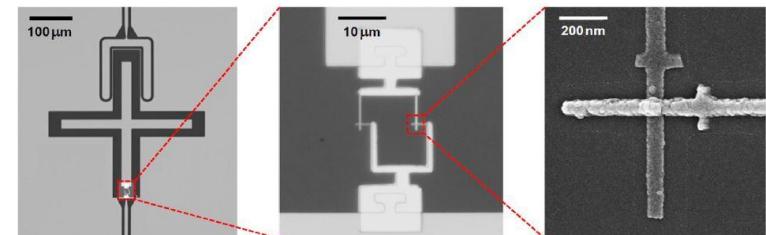
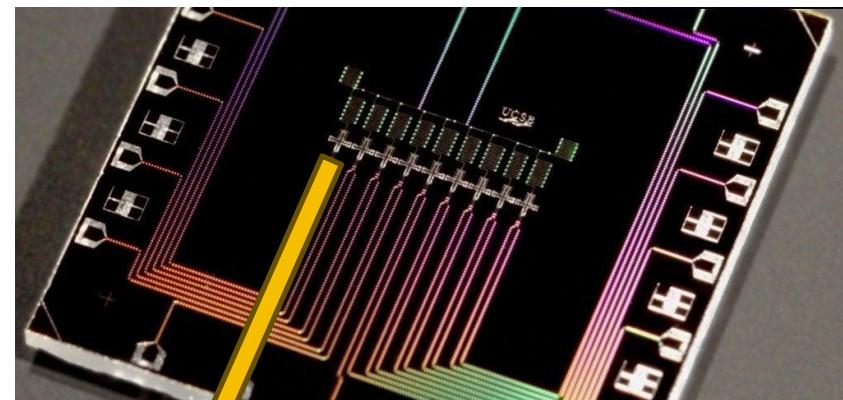
$$\hbar\omega_{qubit} = \sqrt{8E_J E_C} - E_C$$

Energy needed to excite  $|0\rangle \square |1\rangle$



## Recap

### Google 9 qubit chip



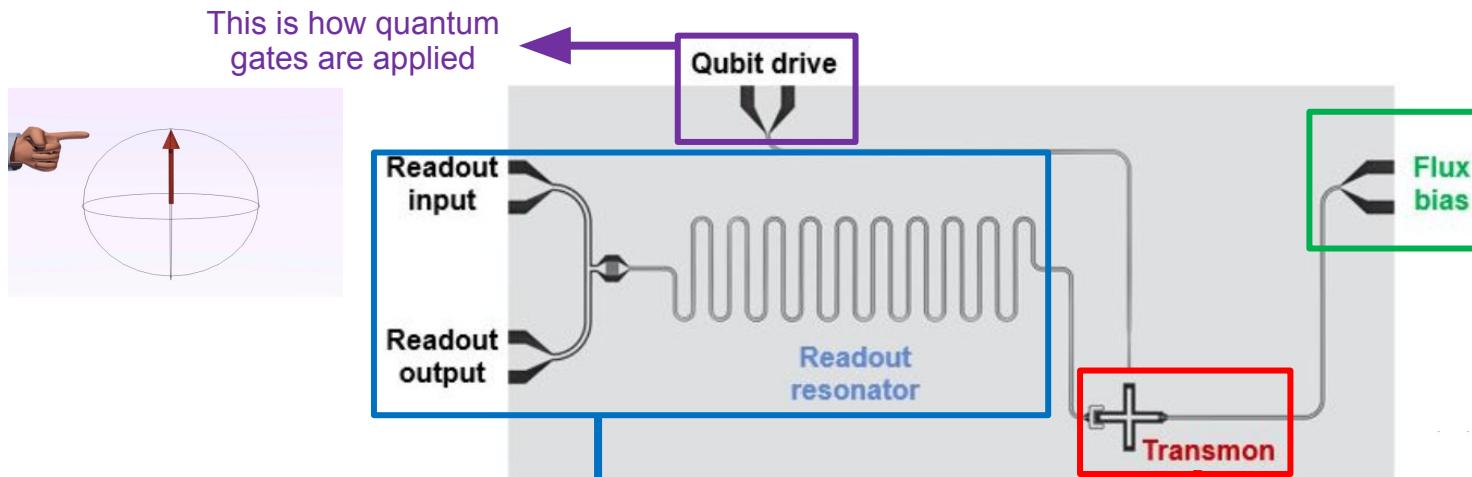
Transmon qubit  
(a)

SQUID  
(b)

Josephson junction  
(c)

**What else do we need for a  
single qubit?**

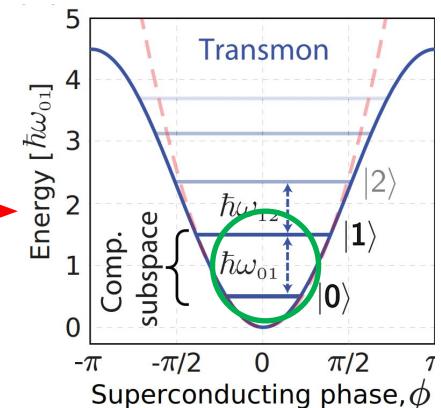
# Controlling a Tunable Transmon



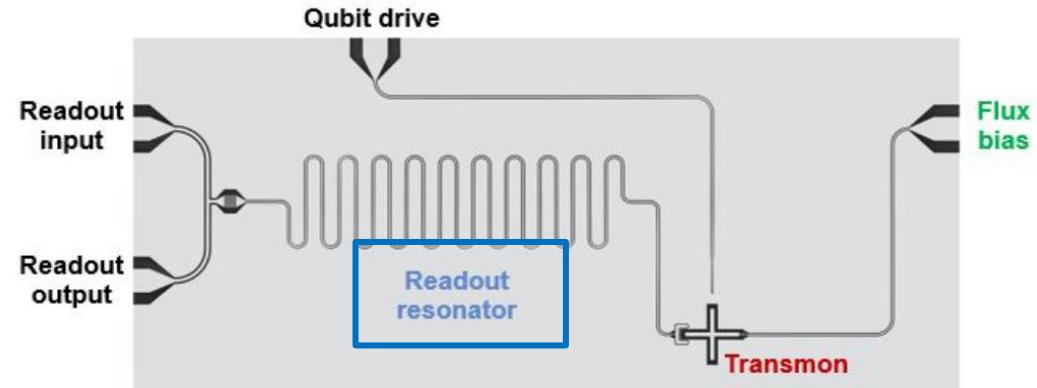
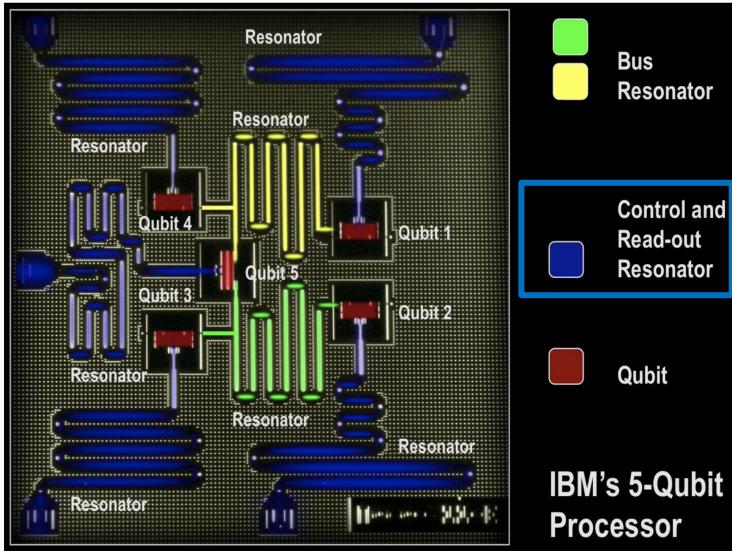
This is what we use to readout the qubit state (measurement)

We have our Quantum Two-Level System:  $|0\rangle, |1\rangle$ , superposition states

We can tune the energy needed to excite the qubit



# Readout Resonator



- Qubit state cannot be probed directly. Various methods are used to readout qubit state
- For superconducting Quantum Processors, qubits are often readout using a resonator
- Qubit and resonator are effectively coupled, and in particular operating points, quantum non-demolition measurements (QND) are taken

## Readout Resonator Hamiltonian

Recall the qubit Hamiltonian:  $H = 4E_C n^2 - E_J \cos(\phi)$

Qubit frequency ( $\sim E_J E_C$ )

$$H_{TLS} \approx \frac{\omega_q \sigma_z}{2}$$

Pauli-Z operator ( $|0\rangle, |1\rangle$   
are its eigenstates)

In the regime where  $E_J \gg E_C$ , system is a two-level system (TLS)  
with states  $|0\rangle, |1\rangle, |2\rangle$ , etc. We truncate the two lowest energy state  
:

Number of photons

Resonator (Quantum Harmonic Oscillator)  $H = \hbar\omega_r (a^\dagger a + \frac{1}{2})$

Jaynes-Cummings Hamiltonian (Light matter interaction)

$$H_{JC} = \underbrace{\omega_r (a^\dagger a + \frac{1}{2})}_{\text{Resonator}} + \underbrace{\frac{\omega_q}{2} \sigma_z}_{\text{Qubit}} + g (\sigma_+ a + \sigma_- a^\dagger)$$

Interaction

## Readout Resonator

### Quantum Non-demolition Measurements (QND)

Jaynes-Cummings Hamiltonian (Light matter interaction)

$$H_{\text{JC}} = \omega_r \left( a^\dagger a + \frac{1}{2} \right) + \frac{\omega_q}{2} \sigma_z + g (\sigma_+ a + \sigma_- a^\dagger)$$

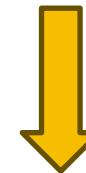


Resonator

Qubit

Interaction

Resonator Frequency Shifts



Dispersive limit:  $\Delta = |\omega_q - \omega_r| \gg g$

$$H_{\text{disp}} = \left( \omega_r + \chi \sigma_z \right) \left( a^\dagger a + \frac{1}{2} \right) + \frac{\tilde{\omega}_q}{2} \sigma_z$$

Dispersive shift

$\chi = g^2 / \Delta$

Dispersive shift

$$\chi = g^2 / \Delta$$

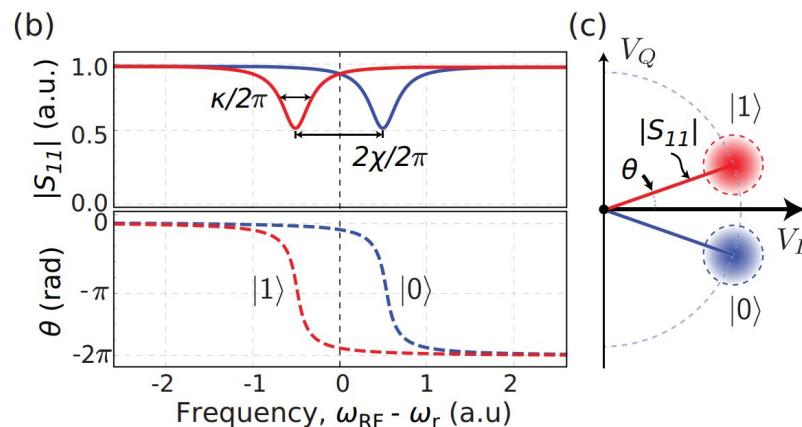
## Readout Resonator

### Dispersive Readout

$$H_{\text{disp}} = \left( \omega_r + \chi \sigma_z \right) \left( a^\dagger a + \frac{1}{2} \right) + \frac{\tilde{\omega}_q}{2} \sigma_z$$

Resonator Frequency Shift

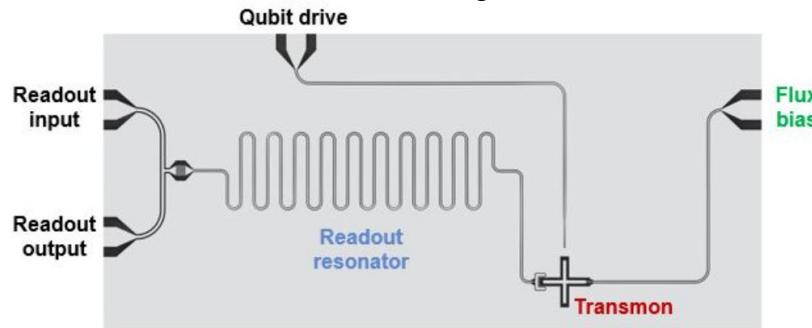
Allows you to do quantum non-demolition measurements on qubit!



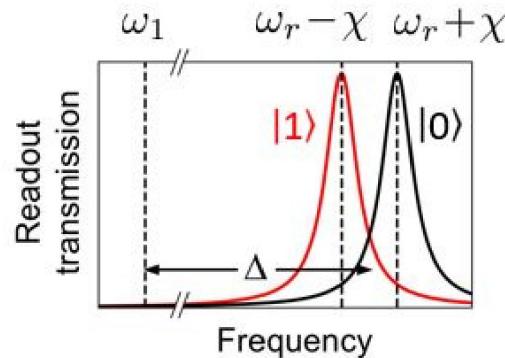
Readout of qubit states using  $S_{11}$  measurement.

# Readout Resonator (Circuit)

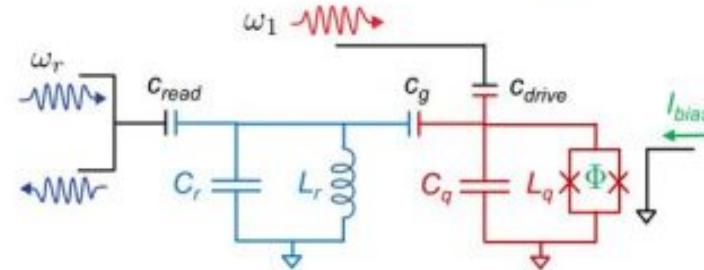
Actual Design



Dispersive Readout



Circuit Design



Resonator

$$H_{JC} = \omega_r \left( a^\dagger a + \frac{1}{2} \right) + \frac{\omega_q}{2} \sigma_z + g ( \sigma_+ a + \sigma_- a^\dagger )$$

Qubit

$$\frac{\omega_q}{2} \sigma_z$$

Interaction

$$g ( \sigma_+ a + \sigma_- a^\dagger )$$

Dispersive Limit

$$H_{\text{disp}} = \left( \omega_r + \chi \sigma_z \right) \left( a^\dagger a + \frac{1}{2} \right) + \frac{\tilde{\omega}_q}{2} \sigma_z$$

$$\chi = g^2 / \Delta$$

*g: Qubit-resonator coupling strength*

# Next Steps

## Quantum chip design flow

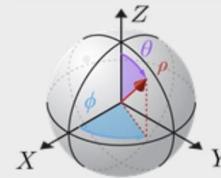
Complexity, Information, Accuracy

Risk, Cost, Time, Resources

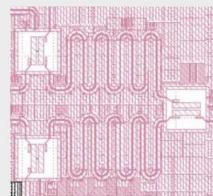
Concept



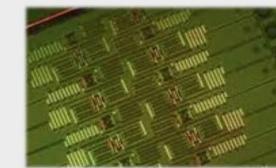
Hamiltonian



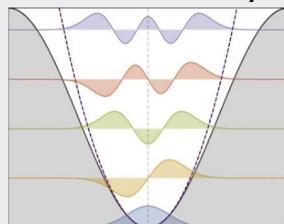
Layout



Fabrication

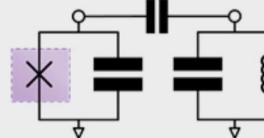


Quantum Analysis



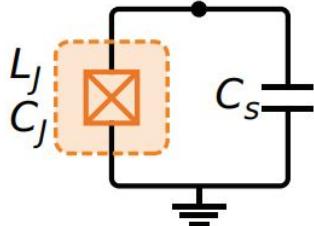
Project  
**Metal**

Electromagnetic  
Analysis



# Quantum Circuit Design

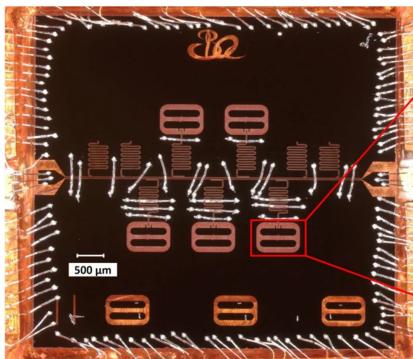
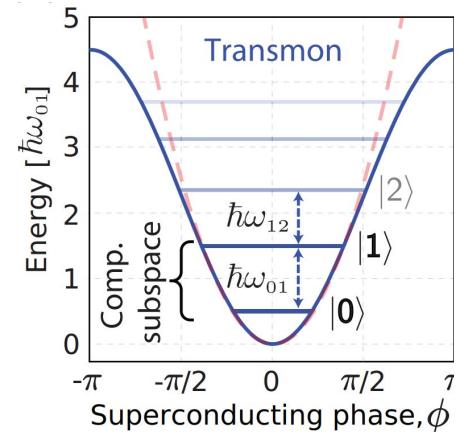
## Starting point



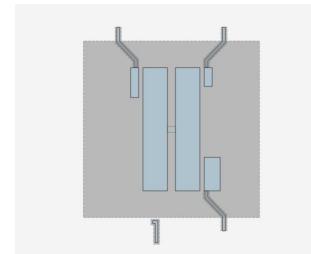
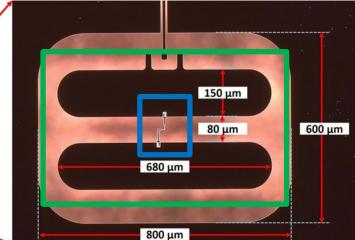
$$H = 4E_C n^2 - E_J \cos(\phi)$$

Transmon

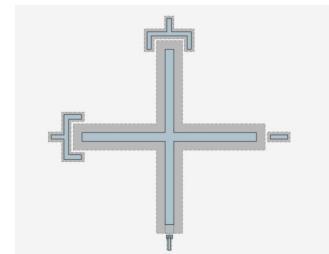
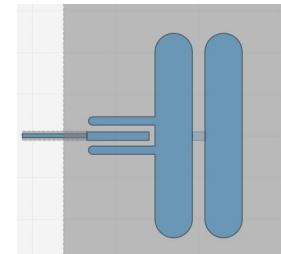
**Transmon designs can look very different!**



Transmon



Also Transmons



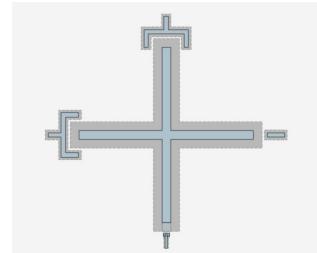
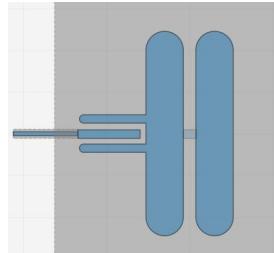
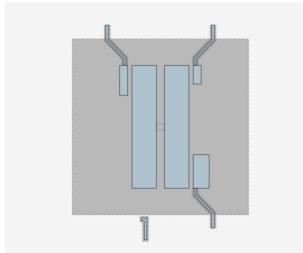
# Quantum Circuit Design

## Fabrication

Fabricating this will be time/resource consuming!  
**How can we make sure our design is giving the correct Hamiltonian values?**

Fabrication (£££)

Transmons Designs



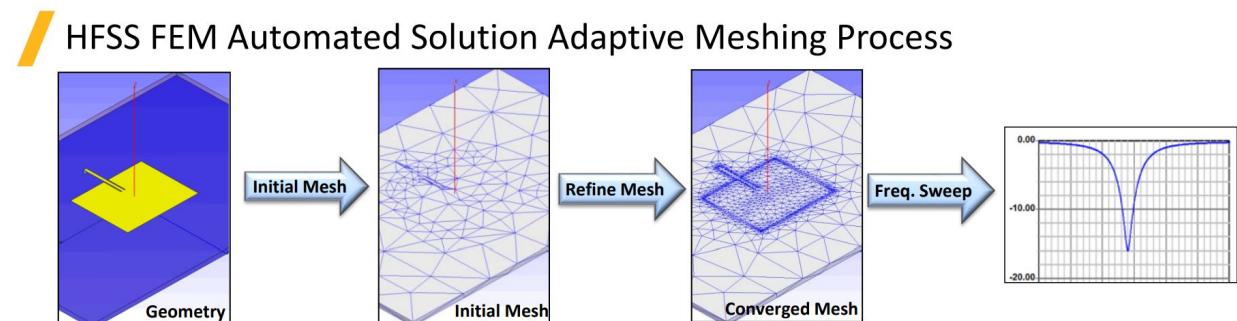
# Electromagnetic (EM) Simulations!

# EM Simulations

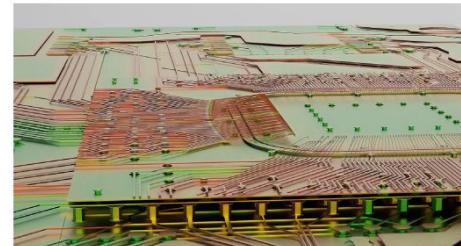
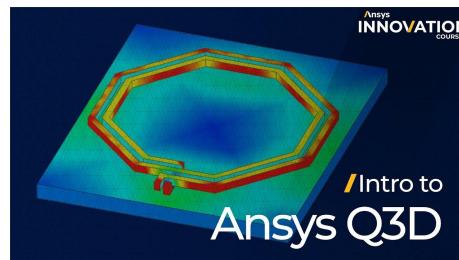
EM Simulations are a valuable approach for analyzing your chip design (classical and quantum) before fabricating it

**What can QPU properties can we extract using EM solvers?**

- 1) Frequencies (qubit frequency, resonator frequency)

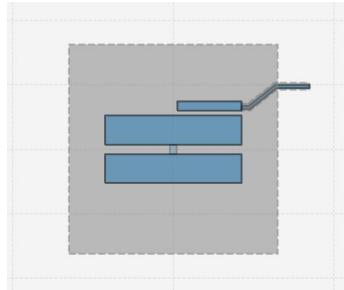


- 2) Capacitance, Inductance, Resistance, Conductance



Fast, Accurate 3D Parasitic Extraction with Q3D

## Transmon Design



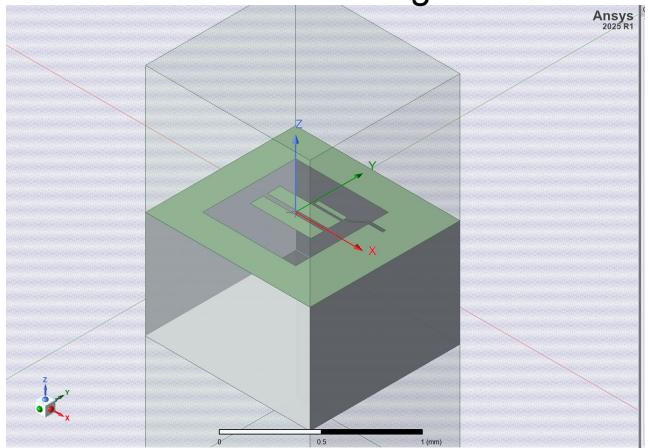
Import design

## EM Simulations

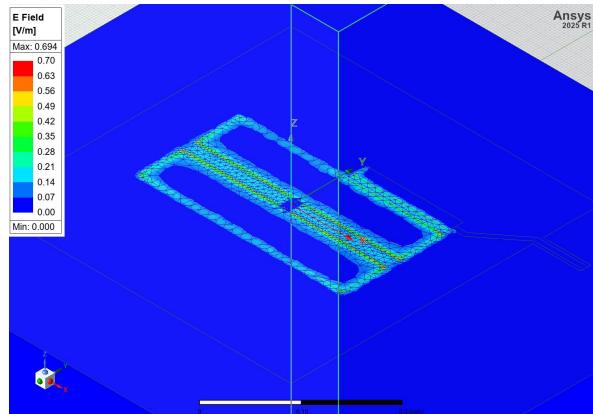
EM Simulation Software

Define materials

## Create 3D Design

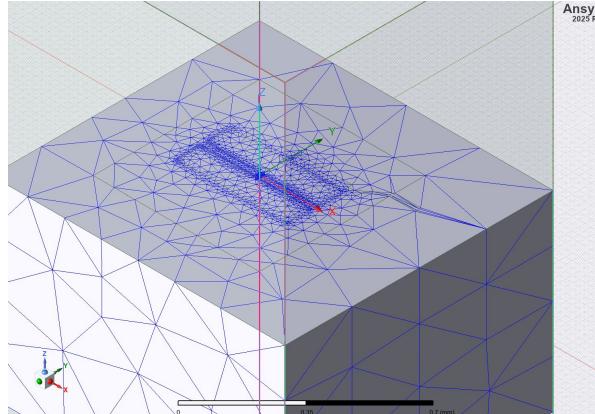


## Plot Electric Field



Solve Maxwell's equations for each segment (FEM)

## Create Mesh

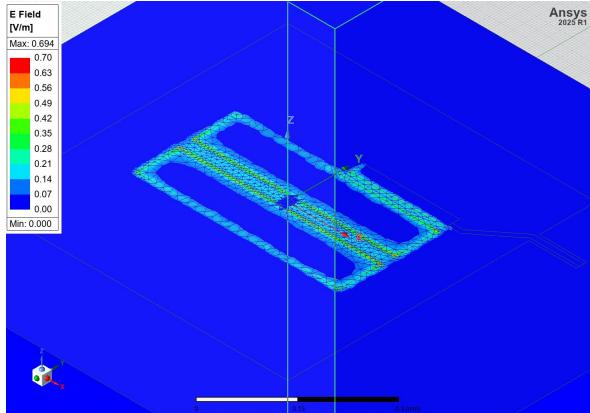


Break up design into small segments

# EM Simulations

## Frequency

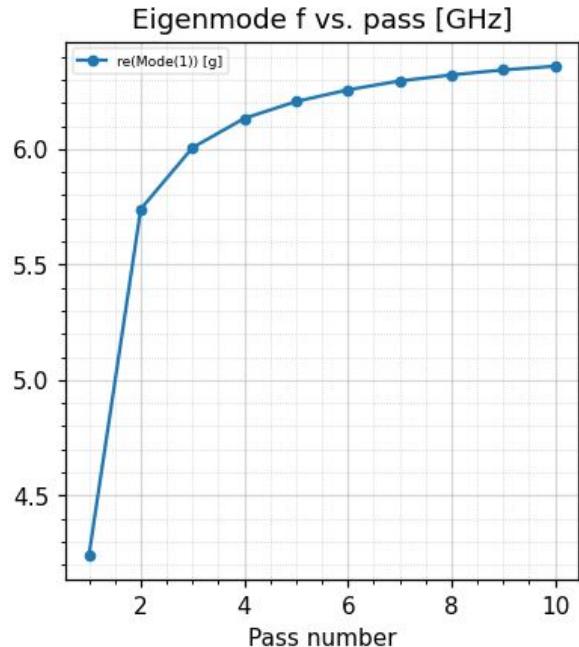
Electric field



Solve EM fields at various frequencies until converging to solution



Found Transmon frequency!



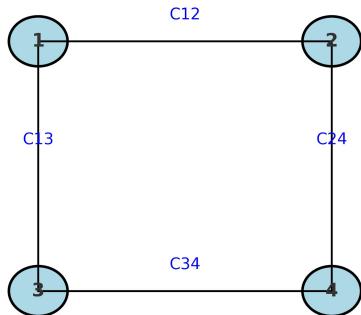
$$H_{\text{JC}} = \omega_r \left( a^\dagger a + \frac{1}{2} \right) + \frac{\omega_q}{2} \sigma_z + g (\sigma_+ a + \sigma_- a^\dagger)$$

Resonator
Qubit
Interaction

# EM Simulations

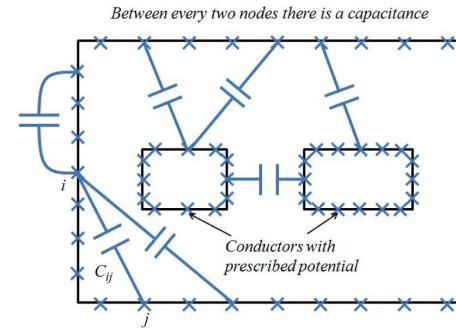
## Capacitance Matrix

Example 4-Capacitor Configuration



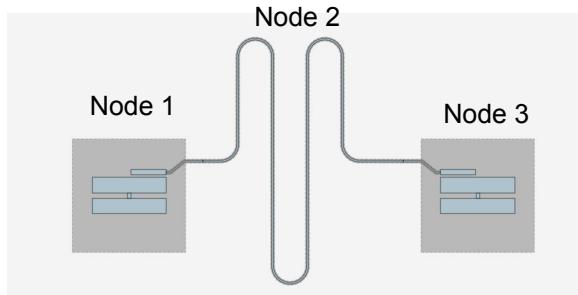
Generalize to N nodes

$$\begin{bmatrix} C_{11} & C_{12} & \dots & C_{1N} \\ C_{21} & C_{22} & \dots & C_{2N} \\ \vdots & \vdots & \ddots & \vdots \\ C_{N1} & C_{N2} & \dots & C_{NN} \end{bmatrix}$$



Capacitance Matrix for QPU

2 Qubit Design

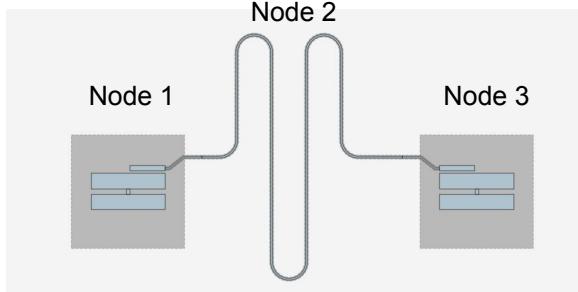


$C_{11}$	$C_{12}$	$C_{12}$
$C_{21}$	$C_{22}$	$C_{22}$
$C_{31}$	$C_{32}$	$C_{32}$

# EM Simulations

## Capacitance Matrix

2 Qubit Design



$C_{11}$	$C_{12}$	$C_{12}$
$C_{21}$	$C_{22}$	$C_{22}$
$C_{31}$	$C_{32}$	$C_{32}$

Transmon  $\hat{H} = 4E_C(\hat{n} - \boxed{n_g})^2 - \boxed{E_J} \cos \hat{\varphi}$

Qubit + Resonator  $H_{\text{JC}} = \omega_r \left( a^\dagger a + \frac{1}{2} \right) + \frac{\omega_q}{2} \sigma_z + \boxed{g} (\sigma_+ a + \sigma_- a^\dagger)$

Resonator
Qubit
Interaction

## EM Simulations

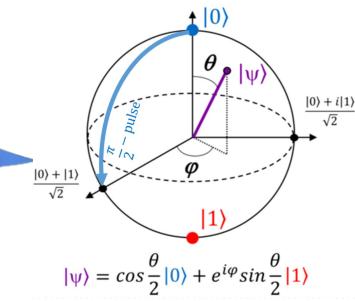
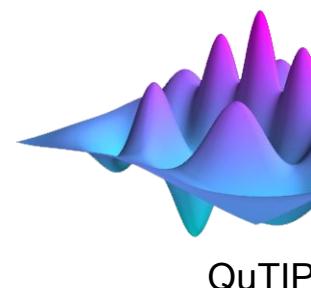
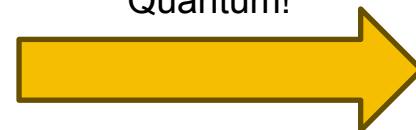
With EM simulations, we can extract all the quantum circuit parameters needed to analyze the Hamiltonian of a quantum system.

Transmon       $\hat{H} = 4E_C(\hat{n} - \boxed{n_g})^2 - \boxed{E_J} \cos \hat{\varphi}$

Qubit + Resonator       $H_{JC} = \boxed{\omega_r} \left( a^\dagger a + \frac{1}{2} \right) + \boxed{\frac{\omega_q}{2}} \sigma_z + \boxed{g} (\sigma_+ a + \sigma_- a^\dagger)$

- Charging Energy  $E_C$
- Josephson Energy  $E_J$
- Offset Charge  $n_g$
- Resonator frequency  $\omega_r$
- Qubit frequency  $\omega_q$
- Coupling coefficient  $g$

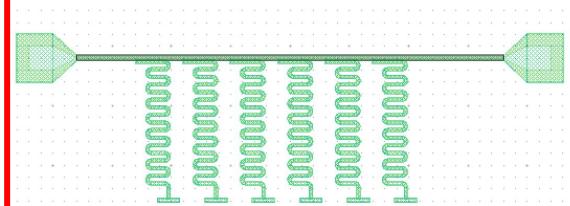
Back to  
Quantum!



# Testing Superconducting Circuits

Upcoming workshop focuses on these parts

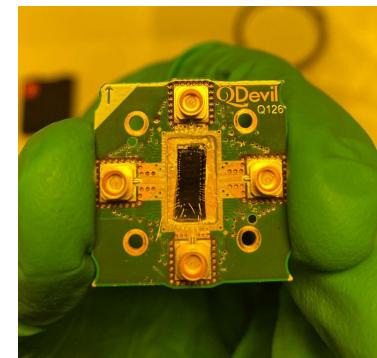
Design



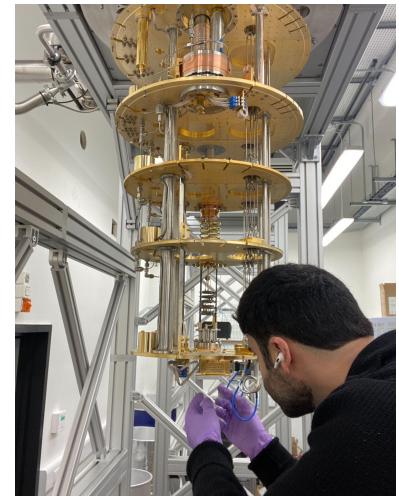
Simulation



Fabrication

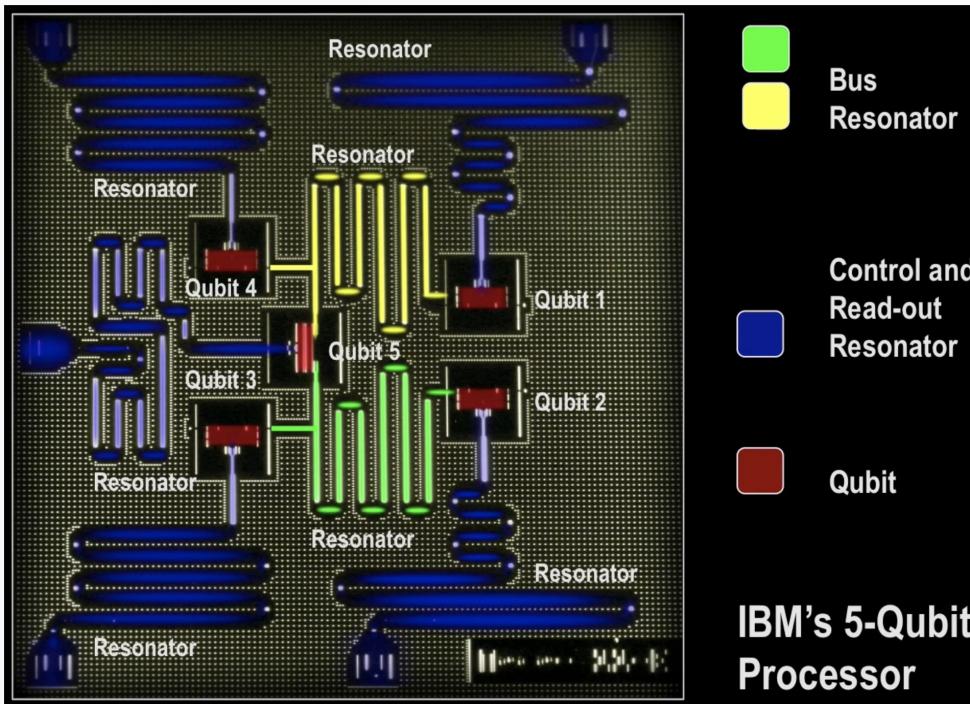


Measurement



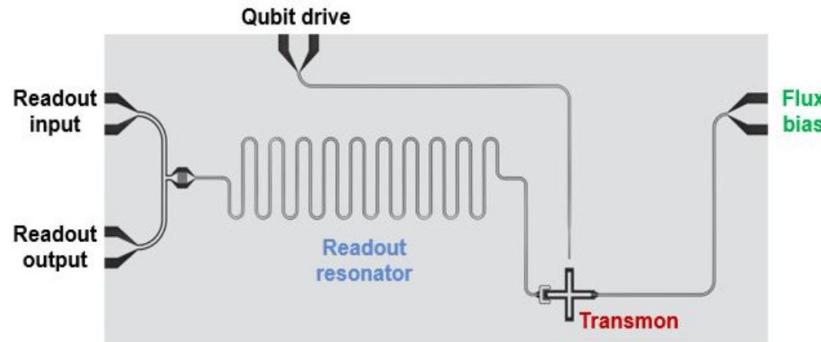
# Superconducting Quantum Processors

Operating Frequency: 4 GHz - 7 GHz



[https://www.researchgate.net/figure/An-image-of-IBMs-five-qubit-processor-with-its-main-elements-highlighted-including-the\\_fig4\\_358153899](https://www.researchgate.net/figure/An-image-of-IBMs-five-qubit-processor-with-its-main-elements-highlighted-including-the_fig4_358153899)

## Recap



Jaynes-Cummings Hamiltonian (Light matter interaction)

$$H_{\text{JC}} = \omega_r \left( a^\dagger a + \frac{1}{2} \right) + \frac{\omega_q}{2} \sigma_z + g (\sigma_+ a + \sigma_- a^\dagger)$$

Resonator      Qubit      Interaction

Dispersive limit:  $\Delta = |\omega_q - \omega_r| \gg g$

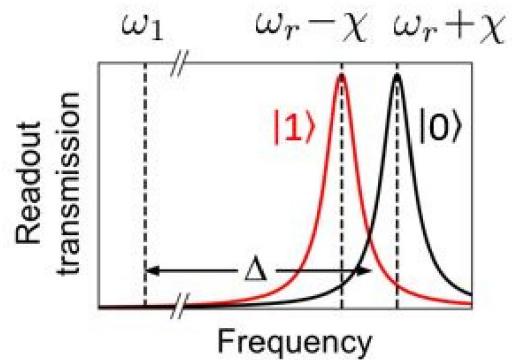
Resonator Frequency Shifts

$$H_{\text{disp}} = \left( \omega_r + \chi \sigma_z \right) \left( a^\dagger a + \frac{1}{2} \right) + \frac{\tilde{\omega}_q}{2} \sigma_z$$

Dispersive shift

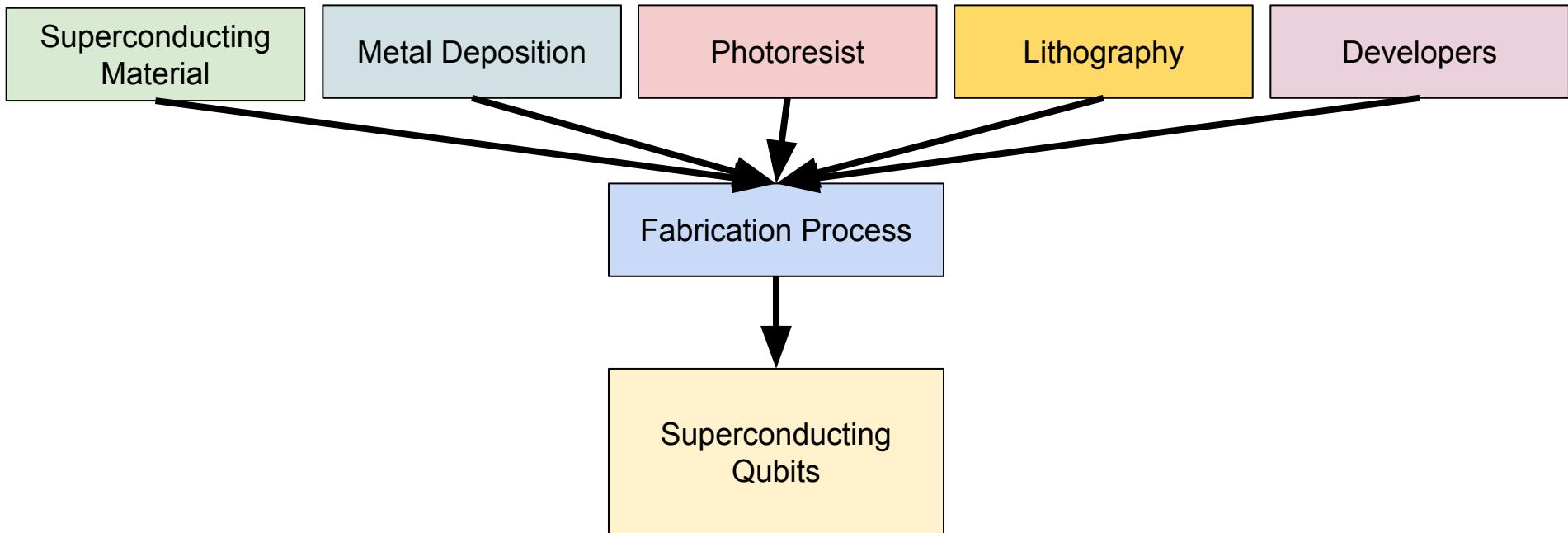
$$\chi = g^2 / \Delta$$

Dispersive Readout



**Thank you!**

# In-House Fabrication of Superconducting Circuits



# Preparing quantum chips/devices

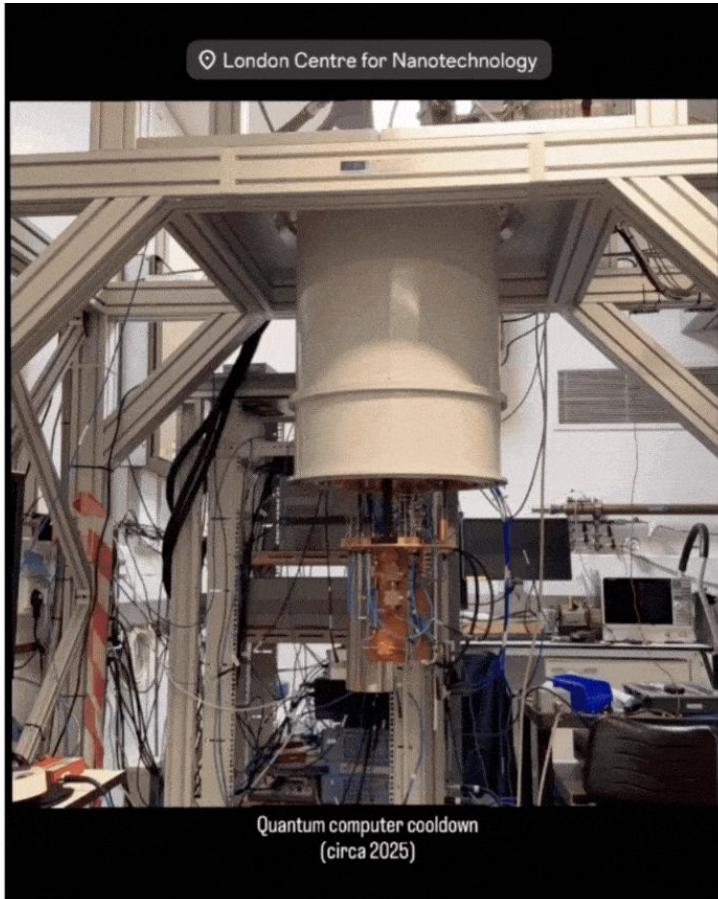
Expectation



Reality

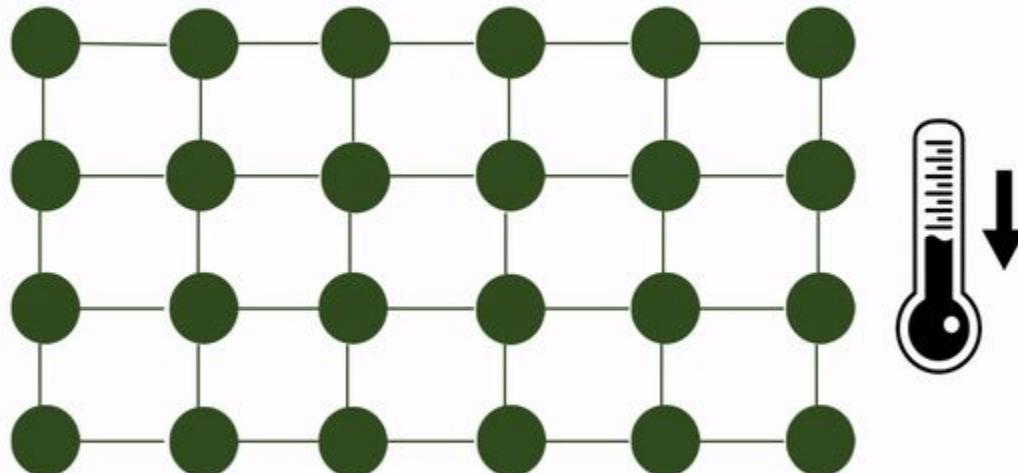


# Fridge Cooldown

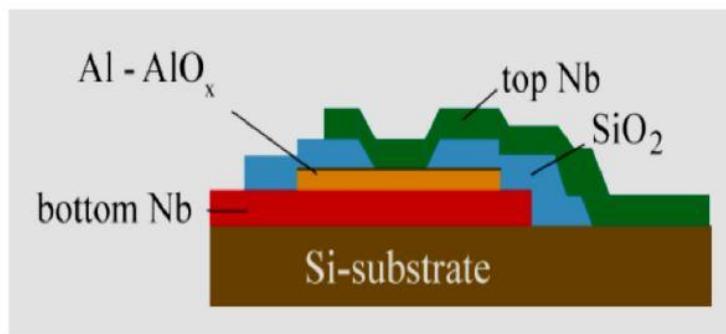


# Supplementary Information

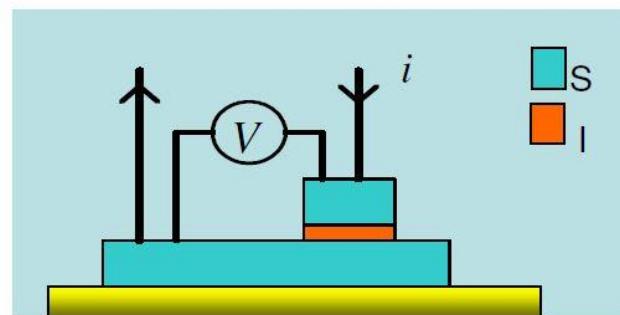
AT THE CRITICAL TEMPERATURE THERMAL VIBRATIONS BECOME NEGLECTABLE



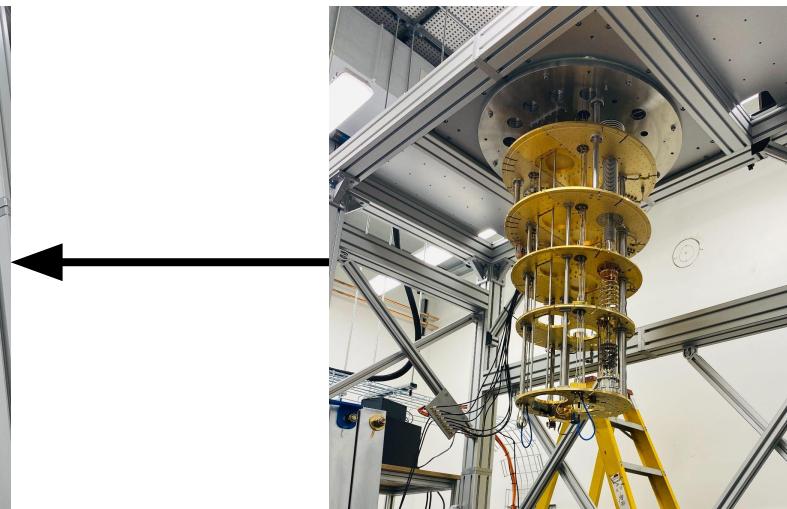
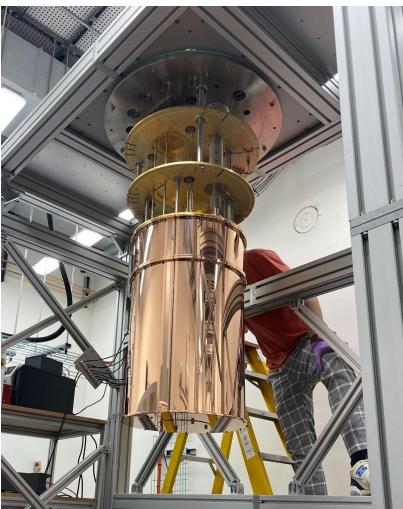
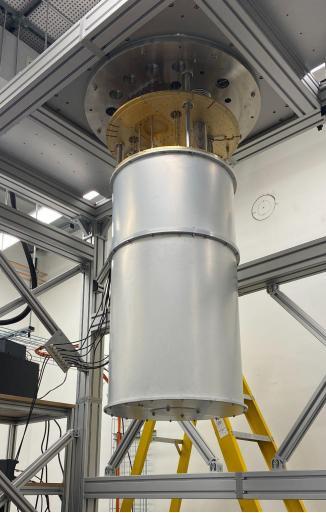
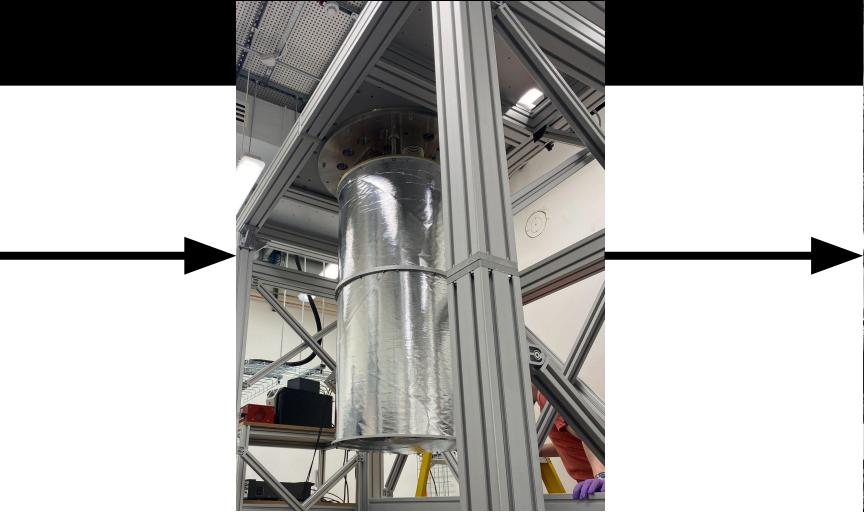
## Supplementary Information



Typical junction cross-section

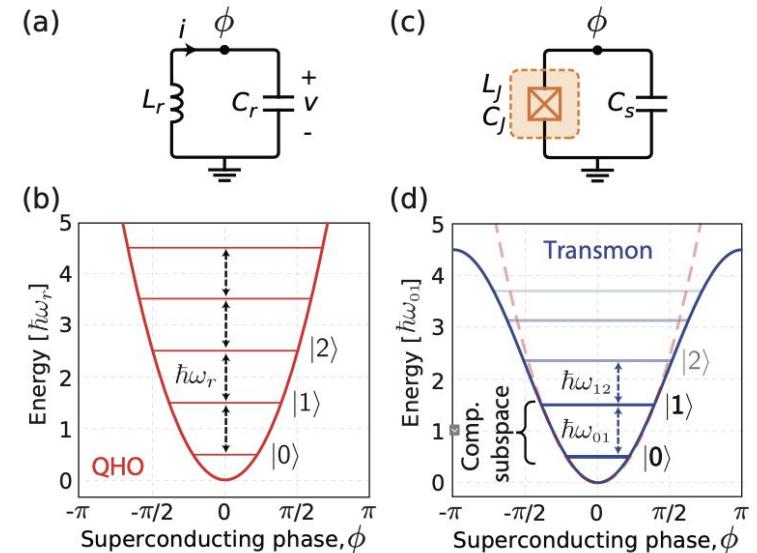


I-V Measurement Principle



# Transmon Qubit I

- Two level system with quantum mechanical properties (superposition, entanglement)
- Tunable qubit transition frequency via electromagnetic flux biasing
- Long coherence times (milliseconds)
- Qubit states being represented by the number of Cooper pairs on the island



$$H = Q\dot{\Phi} - \mathcal{L} = \frac{Q^2}{2C} + \frac{\Phi^2}{2L} \equiv \frac{1}{2}CV^2 + \frac{1}{2}LI^2$$

$$H = 4E_Cn^2 - E_J \cos(\phi)$$

$$H = \hbar\omega_r \left( a^\dagger a + \frac{1}{2} \right)$$

# Transmon Qubit II

## Transmon Hamiltonian

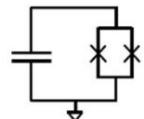
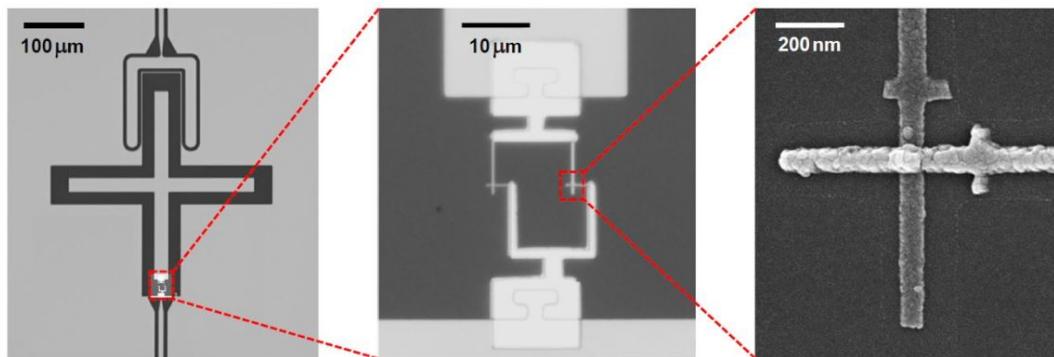
$$H = 4E_C n^2 - E_J \cos(\phi)$$

Excess number of cooper pairs on island      Reduced flux

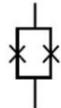
Energy required to add each electron of cooper-pair to island      Josephson energy

- Dynamics of quantum system are governed by  $E_J/E_C$  ratio
- $E_C$  can be decreased by using shunt capacitor ( $E_C \sim 1/C_{\text{Total}}$ )
- In  $E_J \gg E_C$  regime, system is less sensitive to noise

# SEM Images of Transmon



Transmon qubit  
(a)



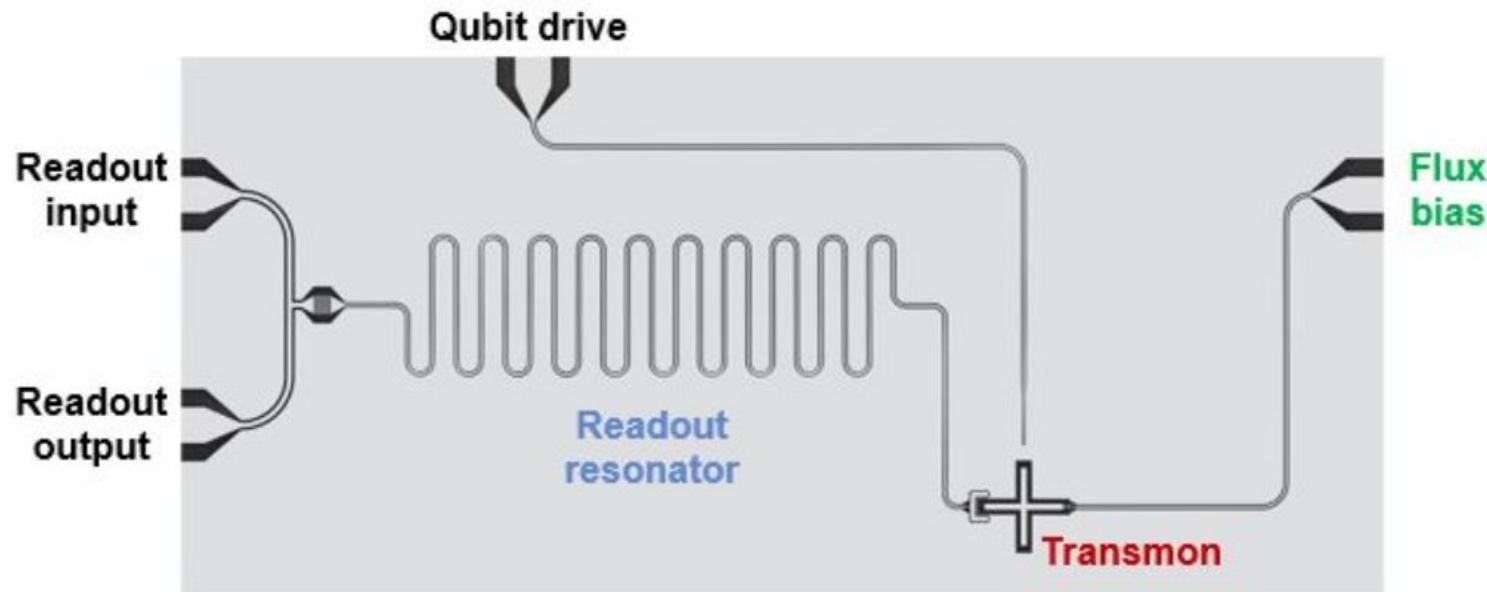
SQUID  
(b)



Josephson junction  
(c)

Roth, Thomas E. and Ma, Ruichao and Chew, Weng C. An Introduction to the Transmon Qubit for Electromagnetic Engineers (2021)

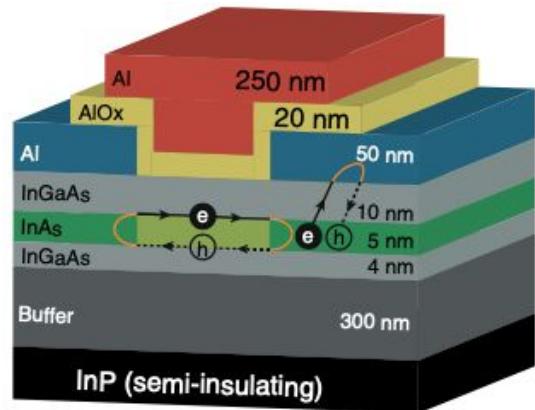
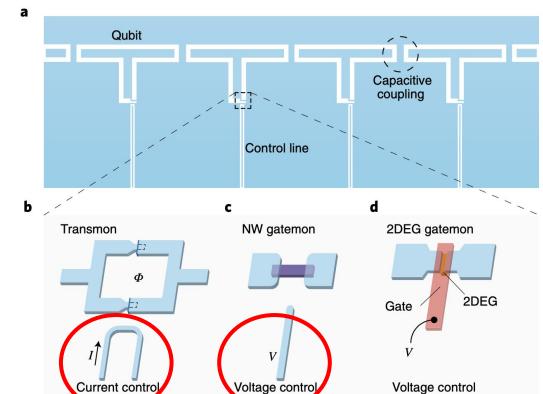
# Resonator + Qubit



Roth, Thomas E. and Ma, Ruichao and Chew, Weng C. An Introduction to the Transmon Qubit for Electromagnetic Engineers (2021)

# Gatemon Qubit

- Derived from Transmons, Superconducting gate tunable qubits based on Josephson Junction
- High fidelity two qubit measurements rely on qubit frequency
- Unlike flux inducing current reliance of transmon, gatemon relies on  $V_g$  to tune qubit
- Eliminates heating through wires caused by current as well as crosstalk



[1] Weber, S.J. Gatemons get serious. *Nature Nanotech* 13, 877–878 (2018).

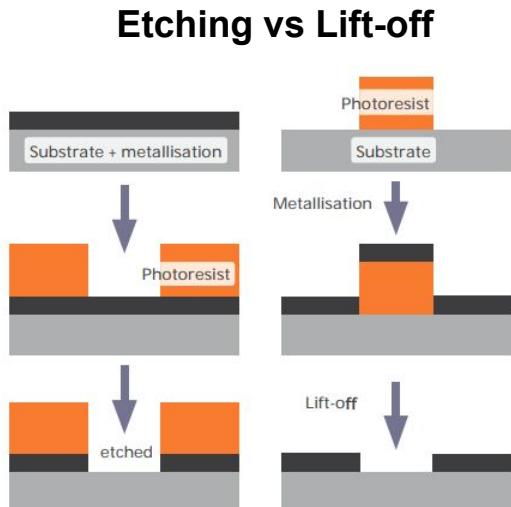
[2] P. Krantz and M. Kjaergaard and F. Yan and T. P. Orlando and S. Gustavsson and W. D. Oliver. A quantum engineer's guide to superconducting qubits (2019)

[3] Casparis, L., Connolly, M.R., Kjaergaard, M. *et al.* Superconducting gatemon qubit based on a proximitized two-dimensional electron gas.(2018)

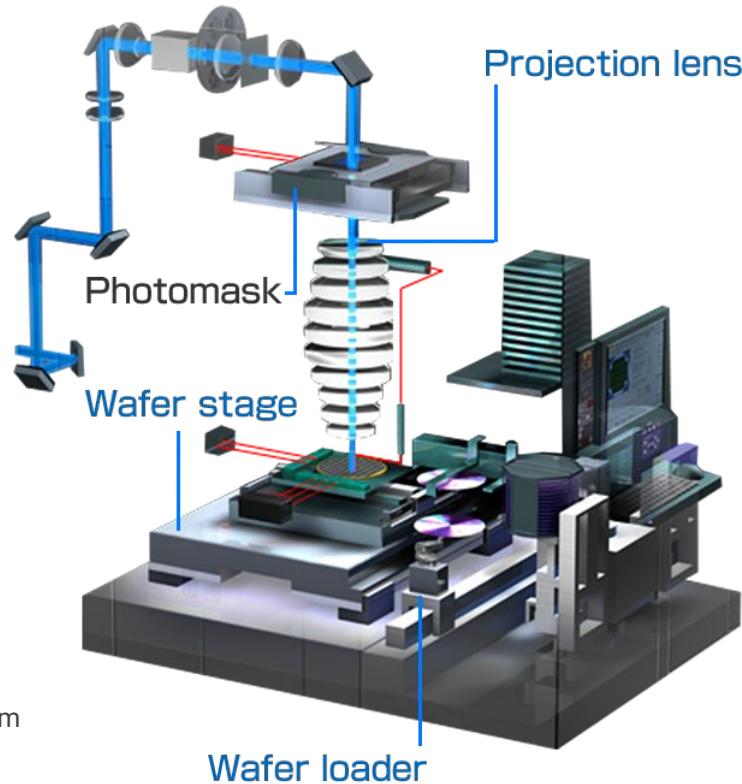
# Photolithography

## Parameters:

- Intensity of light [%]
- Laser Power [mW]

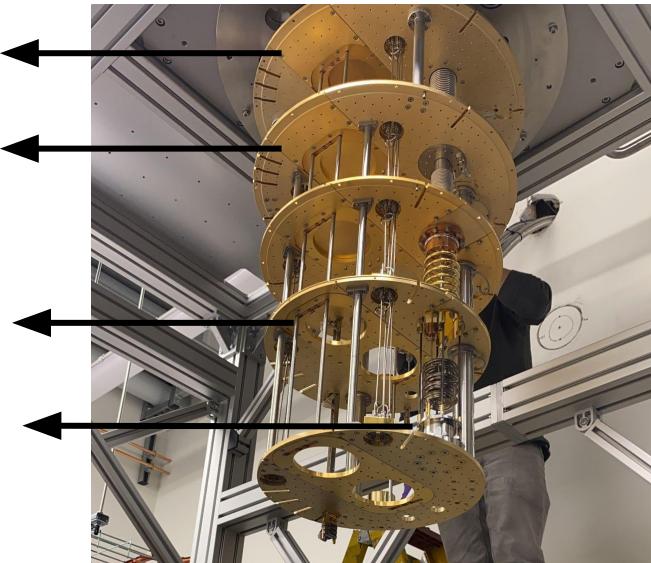
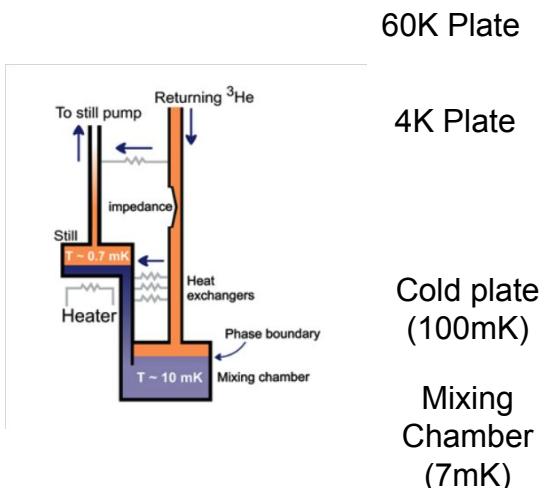


[https://www.microchemicals.com/technical\\_information/lift\\_off\\_photoresist.pdf](https://www.microchemicals.com/technical_information/lift_off_photoresist.pdf)



# Dilution Fridge I

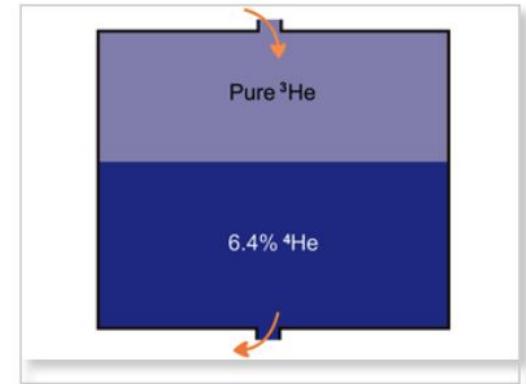
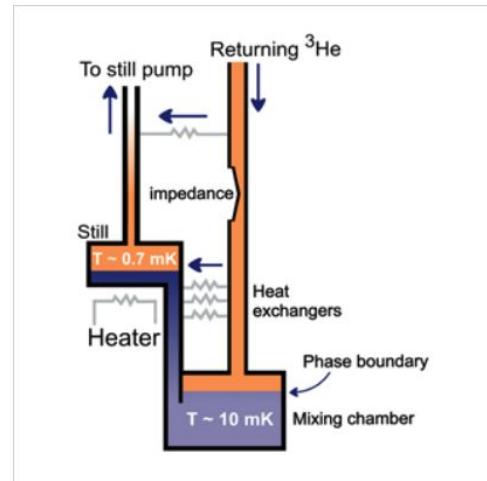
- Dry dilution fridge using Pulse Tubes
- Uses mixture of He3 and He4
- Cooling power is generated by pumping heat out of the mixing chamber and into the surrounding stages
- Distilling He3 out of He4 is absorbing heat (Taking pure phase atoms into dilute phase, increasing entropy)



[https://nanoscience.oxinst.com/assets/uploads/NanoScience/Brochures/Principles%20of%20dilution%20refrigeration\\_Sept15.pdf](https://nanoscience.oxinst.com/assets/uploads/NanoScience/Brochures/Principles%20of%20dilution%20refrigeration_Sept15.pdf)

# Dilution Fridge II

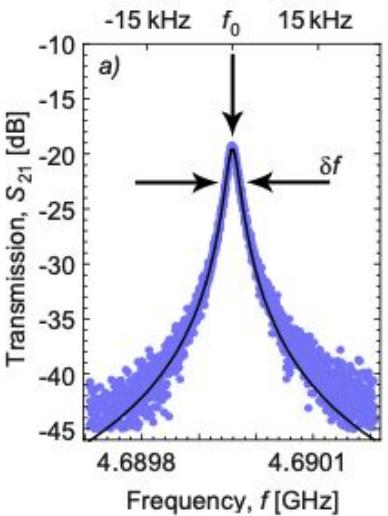
- Pulse tubes offer low vibrations
- Copper braids are used to couple first two stages (avoids vibrations)
- He3 has lower latent heat of evaporation, higher vapour pressure
- He3 atom attracted to He4 due to Van der Waals
- Osmotic pressure pulls Helium up
- Pressure of chamber can be adjusted to change temperature



[https://nanoscience.oxinst.com/assets/uploads/NanoScience/Brochures/Principles%20of%20dilution%20refrigeration\\_Sept15.pdf](https://nanoscience.oxinst.com/assets/uploads/NanoScience/Brochures/Principles%20of%20dilution%20refrigeration_Sept15.pdf)

# RF Measurements

## Single Tone Frequency Sweep



```
class singleToneFreqSweep(spectroscopyMeas):
    name = 'singleToneFreqSweep'

    def __init__(self, parent_dir, date, vna=None, vna_settings=None, fridge=None):
        super().__init__(parent_dir, date, vna, vna_settings, fridge)

    ## Retrieving data
    def get_mag(self, path=None, counter=None):
        return self.grab_file('mag.txt', path, counter)

    def get_phase(self, path=None, counter=None):
        return self.grab_file('phase.txt', path, counter)

    def get_freq(self, path=None, counter=None):
        return self.grab_file('freqs.txt', path, counter)

    def meas(self, vna_settings=None, plot=True, save=True, reduce_bg=False, style=None):
        channel = self.vna.channels.S21
        self.write_vna_settings(vna_settings)

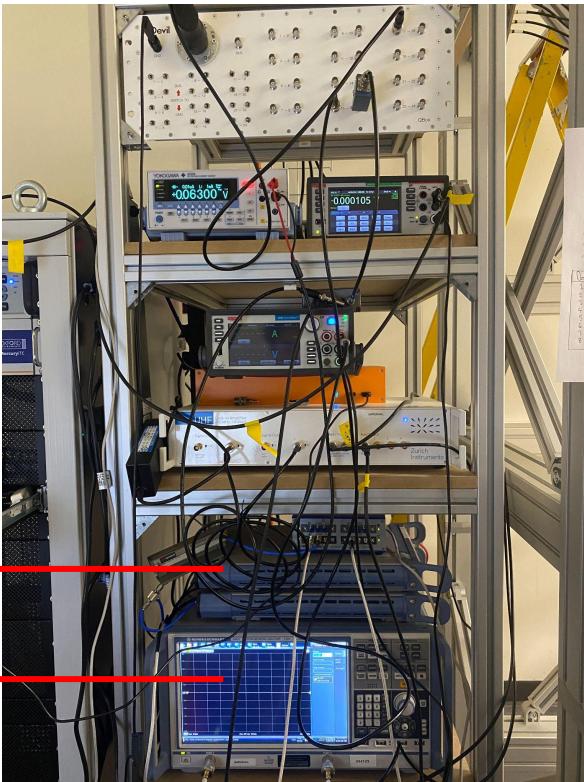
        self.prepare_meas()

        ## Start Measurement
        amp, phase = channel.trace_mag_phase()
        #mag = 10*np.log10(mag)
        mag = util.mag2dB(amp)

        if reduce_bg:
            channel.power(-80)
            mag_bg, phase_bg = channel.trace_mag_phase()
            mag = mag - util.mag2dB(mag_bg)
            phase = phase - phase_bg

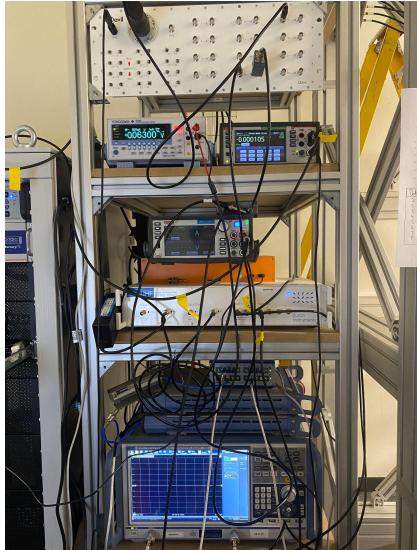
        ## Plot and save data
        freqs = util.sweep(self.vna_settings['center'], self.vna_settings['span'], self.vna_settings['npts'])
        freqs = util.freq2GHz(freqs)
```

M. Göppel and A. Fragner and M. Baur and R. Bianchetti and A. Wallraff. Coplanar waveguide resonators for circuit quantum electrodynamics (2008)



# Noise & Dissipation

- Caused by fluctuations in the temperature of the environment, generating fluctuations in electrical properties of the quantum system.
- Electromagnetic interference (EMI): This is caused by electromagnetic fields (external sources, power cables, electrical devices, environment)
- Noise from electrical components and instruments
- Lossy Resonators lead to dissipation of energy

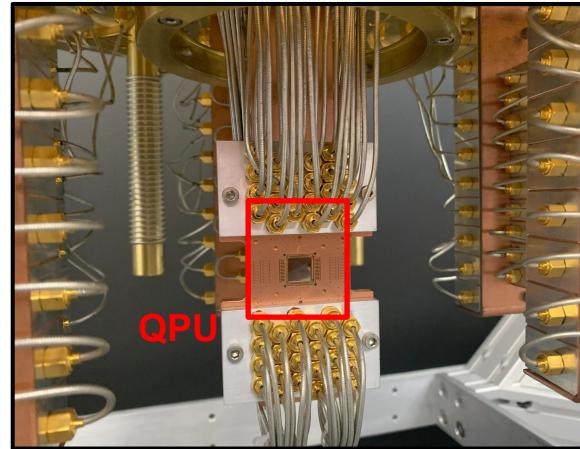
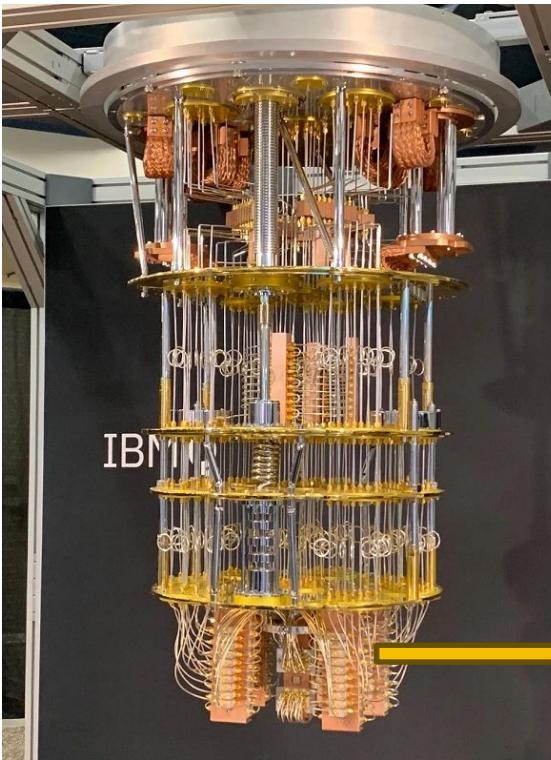


# Various Quantum Computing Architectures

Qubit Type	Pros/Cons	Select Players
Superconducting	<p><b>Pros:</b> High gate speeds and fidelities. Can leverage standard lithographic processes. Among first qubit modalities so has a head start.</p> <p><b>Cons:</b> Requires cryogenic cooling; short coherence times; microwave interconnect frequencies still not well understood.</p>	       
Trapped Ions	<p><b>Pros:</b> Extremely high gate fidelities and long coherence times. Extreme cryogenic cooling not required. Ions are perfect and consistent.</p> <p><b>Cons:</b> Slow gate times/operations and low connectivity between qubits. Lasers hard to align and scale. Ultra-high vacuum required. Ion charges may restrict scalability.</p>	    
Photonics	<p><b>Pros:</b> Extremely fast gate speeds and promising fidelities. No cryogenics or vacuums required. Small overall footprint. Can leverage existing CMOS fabs.</p> <p><b>Cons:</b> Noise from photon loss; each program requires its own chip. Photons don't naturally interact so 2Q gate challenges.</p>	   
Neutral Atoms	<p><b>Pros:</b> Long coherence times. Atoms are perfect and consistent. Strong connectivity, including more than 2Q. External cryogenics not required.</p> <p><b>Cons:</b> Requires ultra-high vacuums. Laser scaling challenging.</p>	   
Silicon Spin/Quantum Dots	<p><b>Pros:</b> Leverages existing semiconductor technology. Strong gate fidelities and speeds.</p> <p><b>Cons:</b> Requires cryogenics. Only a few entangled gates to date with low coherence times. Interference/cross-talk challenges.</p>	    

<https://quantumtech.blog/2022/10/20/quantum-computing-modalities-a-qubit-primer-revisited/>

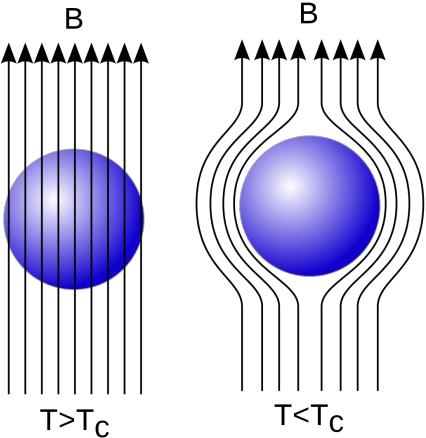
# Superconducting Quantum Computers



# Superconductivity

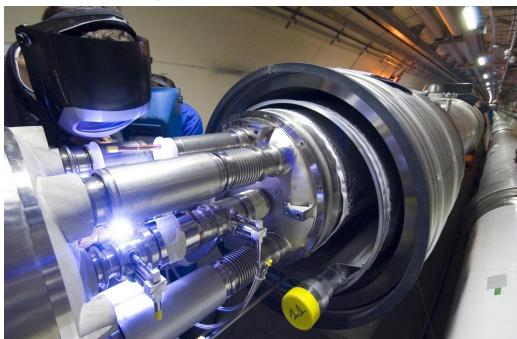
## Meissner effect

Meissner effect



Expulsion of magnetic fields from the superconductor

Magnetic field shielding used at CERN



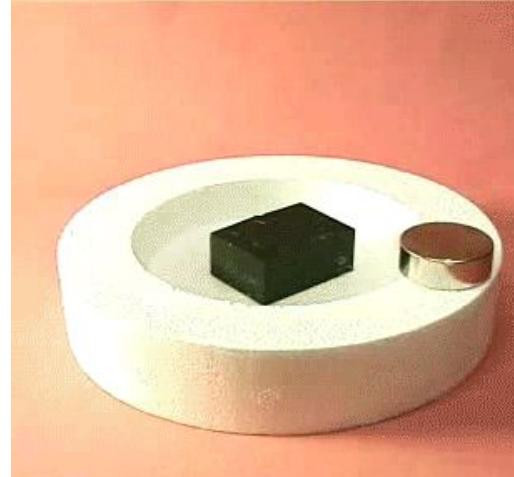
<https://home.cern/news/news/knowledge-sharing/exchanging-knowledge-industry-superconducting-tech>

MRI



<https://www.medimaging.net/mri/articles/294795607/use-of-high-temperature-superconductors-to-make-mr-imaging-more-affordable-accessible-and-sustainable.html>

<https://www.pinterest.co.uk/pin/431571576761730279/>



# Superconductivity

## Back to Quantum

### Why are superconductors good for quantum?

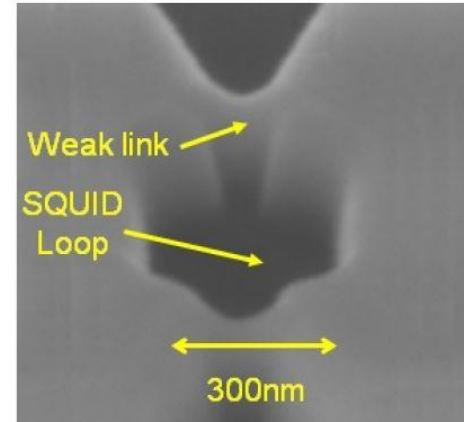
- Ability to control quantum effects
- Advancements in Semiconductor industry are transferable to superconducting chips
- Minimal energy dissipation

### SQUID

(Superconducting Quantum Interference Device)



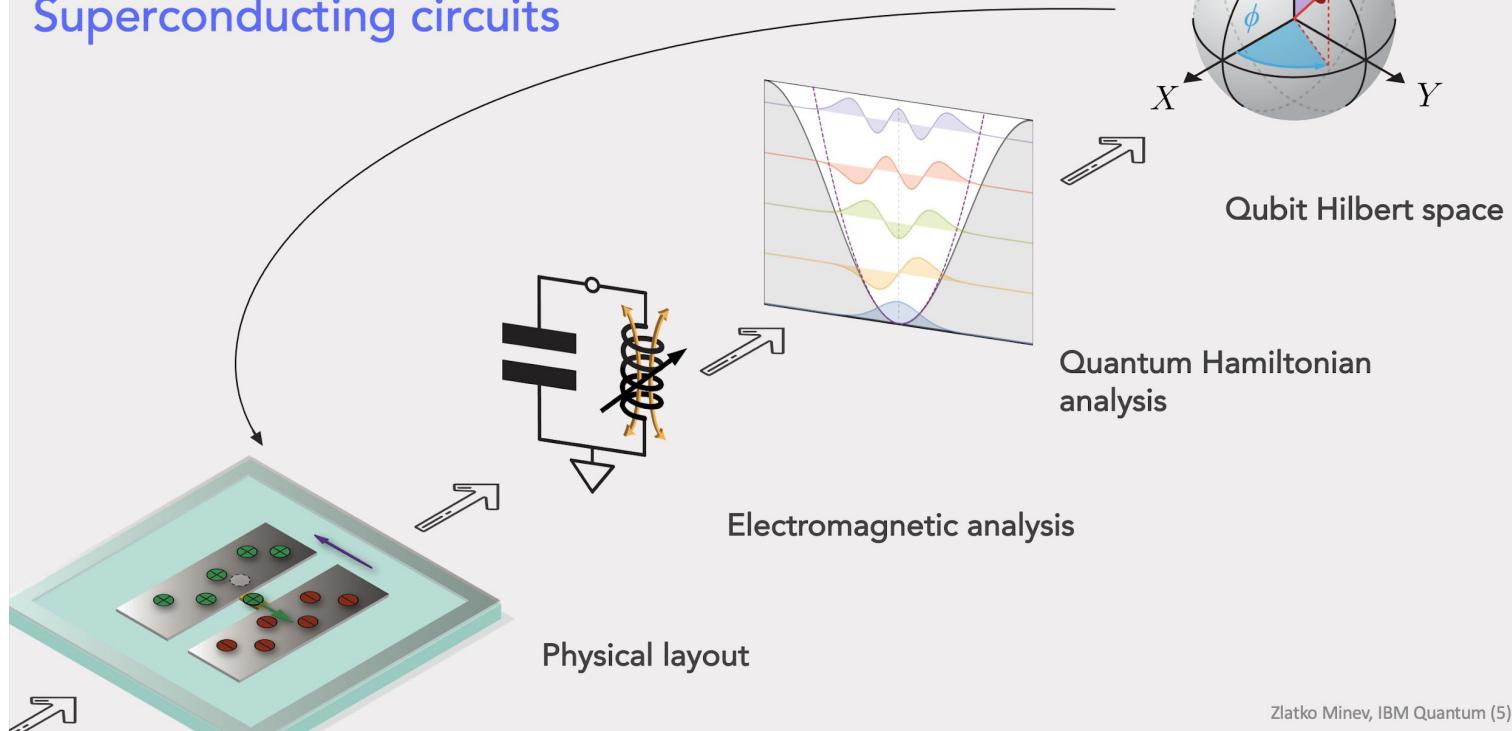
Giant SQUID



Nano SQUID

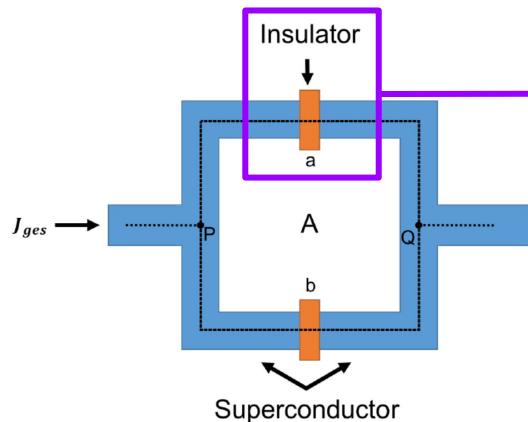
# Quantum Device Design

Superconducting circuits

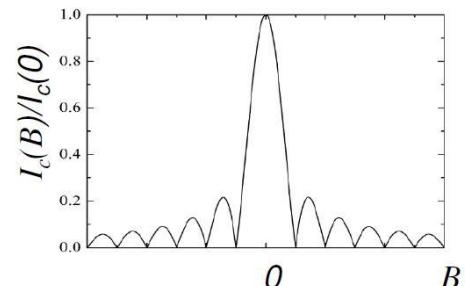
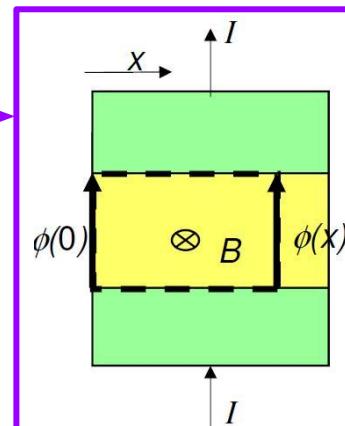


# Superconducting Quantum Interference Device (SQUID)

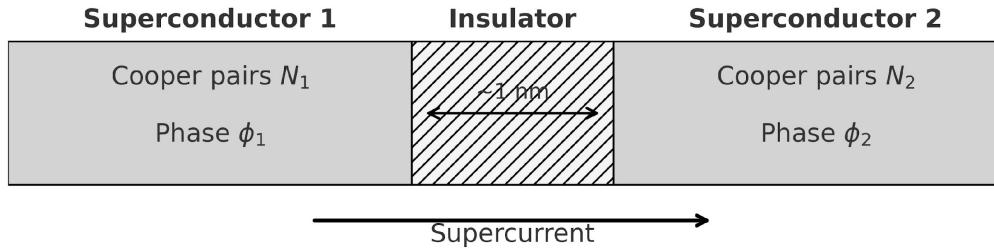
SQUID diagram



Macroscopic quantum interference



When a magnetic field is applied perpendicular to the junction, the critical current  $I_c$  changes in a way that resembles the diffraction intensity of light diffracted through a single slit (Fraunhofer Diffraction).



Dynamical Variables:  $n = N_1 - N_2$ ,  $\varphi = \phi_1 - \phi_2$

### Josephson Relations

$$I_s = I_c \sin(\varphi)$$

$$\frac{d\varphi}{dt} = \frac{2e}{\hbar} V$$

Differentiate  $I_s$  with respect to time:

$$\frac{dI_s}{dt} = I_c \cos(\varphi) \frac{d\varphi}{dt}$$

Substitute  $\frac{d\varphi}{dt} = \frac{2e}{\hbar} V$ :

$$\frac{dI_s}{dt} = I_c \cos(\varphi) \frac{2e}{\hbar} V$$

Compare to  $V = L \frac{dl}{dt}$ :

$$L_J(\varphi) = \frac{\Phi_0}{2\pi I_c \cos(\varphi)}$$

where  $\Phi_0 = \frac{\hbar}{2e}$  is the flux quantum