

Lecture 1: Introduction to DSA with JavaScript

What is DSA?

DSA stands for **Data Structures and Algorithms**. It is the foundation of writing efficient programs. Understanding DSA helps you organize, process, and store data effectively and solve complex problems quickly.

♦ Data Structures

These are ways to store and organize data in computers so it can be used efficiently.





- Examples: Arrays, Objects, Stacks, Queues, Trees, Graphs

♦ Algorithms

These are step-by-step methods or rules to solve a specific problem.

- Examples: Sorting numbers, searching in a list, traversing a tree, optimizing routes
-

Why Learn DSA?

Reason	Description
 Crack Interviews	Top tech companies test your ability to solve DSA problems.
 Write Efficient Code	Learn to solve problems with better time and space complexity.
 Solve Real-World Problems	Understand how Google Maps finds shortest paths, or how search engines rank results.
 Improve Logical Thinking	It enhances your ability to break down and solve complex problems.

Why JavaScript for DSA?

Traditionally, DSA is taught using C++, Java, or Python. But **JavaScript** has grown beyond web development—it's now powerful for backend, app development, and problem-solving.

Advantages of JavaScript:

- Easy syntax — great for beginners
 - Runs in browser or Node.js
 - Good community support
 - Interview platforms like LeetCode, HackerRank now support JavaScript
-

Core Building Blocks of DSA

Data Structure	Description	Real-life Example
Array	Stores elements in linear order	To-do list
Object	Key-value storage	User profile data
Stack	LIFO (Last In, First Out)	Browser back button
Queue	FIFO (First In, First Out)	Print queue
Linked List	Nodes connected via pointers	Playlist (next/prev song)
Tree	Hierarchical data	Folder structure
Graph	Nodes with connections	Social networks

Algorithm Categories

Algorithm Type	Example Problems
Sorting	Sorting students by score
Searching	Finding a name in a contact list

Recursion	Solving a maze
Backtracking	Solving Sudoku
Dynamic Programming	Best way to climb stairs with minimum cost
Greedy	Coin change problems
Graph Algorithms	Finding shortest path (Dijkstra's)

How This Course Will Help You

In this course, you'll:

- Learn and implement each data structure from scratch
 - Solve real-world problems using algorithms
 - Understand time and space complexity
 - Practice problems that appear in coding interviews
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Course Flow

Module 1: JavaScript Fundamentals

We'll start by covering:

- Variables, data types
- Loops, functions
- Control flow

These are prerequisites for writing clean and structured code.

Module 2–4: Core DSA Concepts

You will dive into:

- Arrays, Objects, Linked Lists
- Trees, Graphs, and recursion
- Sorting, searching, and solving problems step-by-step

Module 5: Interview Prep

- Practice most asked problems
 - Get tips to solve them under pressure
 - Learn time complexity analysis using **Big O Notation**
-



Real-Life Example: Google Search

When you type a search query into Google:

1. Google uses **data structures** like graphs to map relationships between web pages.
2. **Algorithms** like PageRank decide which results are most relevant.
3. **Heaps and sorting** help prioritize results based on multiple signals.

Understanding DSA gives you a glimpse into such systems!



Getting Started

Install Node.js (Optional)

You can run JavaScript DSA code either:

- In the browser console (F12 > Console)
- Or using Node.js from your terminal

To install Node.js:

Download from: <https://nodejs.org>

Your First JS Code (Try It!)

javascript

CopyEdit

```
console.log("Hello, DSA world!");
```



Conclusion

DSA is not just about solving problems—it's about solving them **smartly** and **efficiently**. With JavaScript as your tool, you're now ready to explore the world of data structures and algorithms in a modern, flexible way.

Let's dive deeper in the next lecture, where we'll learn about **Variables, Data Types, and Operators** in JavaScript—essential for writing logic.

Lecture 2: Variables, Data Types & Operators in JavaScript

What Are Variables?

A **variable** is like a labeled box that stores information (data) you want to use later. In JavaScript, you can declare a variable using:

- `var` (old, avoid using now)
- `let` (modern, block-scoped)
- `const` (constant, block-scoped)

♦ Example:

```
javascript
CopyEdit
let name = "Alice";
const age = 25;
```

Quick Summary:

Keyword	Can Reassign?	Scope	Use When
<code>var</code>	✓	Function	Legacy code only
<code>let</code>	✓	Block	Default choice
<code>const</code>	✗	Block	For values that don't change

JavaScript Data Types

JavaScript is **dynamically typed**, meaning variables don't have fixed types. A variable can store any type of data.

♦ **Primitive Data Types:**

1. **String** – `"Hello"`
2. **Number** – `42, 3.14`
3. **Boolean** – `true, false`
4. **Undefined** – declared but not assigned
5. **Null** – explicitly "nothing"
6. **BigInt** – large integers
7. **Symbol** – unique identifiers

♦ **Non-Primitive (Reference) Data Types:**

- **Object** – `{ name: "Alice", age: 25 }`
- **Array** – `[1, 2, 3]`
- **Function** – `function greet() { ... }`

Examples:

javascript

CopyEdit

```
let str = "Hello";           // String
let num = 10;                // Number
let isValid = true;         // Boolean
let value;                  // Undefined
let nothing = null;         // Null
let user = { name: "Avi" }; // Object
let list = [1, 2, 3];       // Array
```

Type Checking

Use `typeof` to check a variable's type:

javascript

CopyEdit

```
typeof "hello";    // "string"
typeof 42;         // "number"
typeof true;       // "boolean"
typeof undefined;  // "undefined"
typeof null;       // "object" (quirk in JS)
typeof [1, 2, 3];  // "object"
```

JavaScript Operators

Operators are used to perform actions like calculations, comparisons, and logical operations.

Arithmetic Operators:

Operator	Meaning	Example
+	Addition	$2 + 3 \rightarrow 5$
-	Subtraction	$5 - 2 \rightarrow 3$
*	Multiplication	$4 * 3 \rightarrow 12$
/	Division	$10 / 2 \rightarrow 5$
%	Modulus (remainder)	$7 \% 2 \rightarrow 1$

**	Exponentiation	<code>2 ** 3 → 8</code>
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Assignment Operators:

Operator	Meaning	Example
<code>=</code>	Assign value	<code>x = 5</code>
<code>+=</code>	Add and assign	<code>x += 2 → x = x + 2</code>
<code>-=</code>	Subtract and assign	<code>x -= 2</code>
<code>*=</code>	Multiply and assign	<code>x *= 3</code>
<code>/=</code>	Divide and assign	<code>x /= 2</code>

Comparison Operators:

Used to compare values (returns `true` or `false`):

Operator	Description	Example
<code>==</code>	Equal (loose)	<code>"5" == 5 → true</code>
<code>===</code>	Strict equal (type + value)	<code>"5" === 5 → false</code>
<code>!=</code>	Not equal	<code>3 != 4 → true</code>
<code>!==</code>	Strict not equal	<code>"5" !== 5 → true</code>
<code>></code>	Greater than	<code>10 > 5</code>
<code><</code>	Less than	<code>2 < 4</code>

`>=, <=` Greater or equal / Less or equal `x >= y`

Logical Operators:

Operator	Meaning	Example
<code>&&</code>	AND	<code>true && false → false</code>
<code>!</code>	NOT	<code>!true → false</code>

JavaScript Quirks

`==` vs `===`

javascript
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`"5" == 5 // true → only checks value`
`"5" === 5 // false → checks value & type`

Null vs Undefined

javascript
CopyEdit
`let x; // undefined (no value assigned)`
`let y = null; // explicitly no value`

Mini Project: Variable Playground

Try writing this in your browser console or online editor like [JSFiddle](#) or [CodePen](#):

javascript
CopyEdit
`let name = "John";`
`let age = 30;`

```
let isStudent = true;

console.log("Name:", name);
console.log("Age next year:", age + 1);
console.log("Is a student?", isStudent);
```

Practice Exercises

Try solving:

1. Declare 3 variables: `firstName`, `lastName`, and `fullName`
 2. Store your age and check if you are above 18 using comparison operators
 3. Create a variable and increment it using `+=` operator
-



Conclusion

Understanding variables, data types, and operators is the **core foundation** for any JavaScript or DSA code. Without this, it's impossible to manipulate data or write logic.

In the **next lecture**, we'll explore **Control Flow** in JavaScript—how to use `if`, `else`, and `switch` to make decisions in your code.

Lecture 3: Control Flow (if, else, switch) in JavaScript

What is Control Flow?

Control Flow determines the *order* in which the code runs. In real life, you make decisions like:

If it's raining, carry an umbrella.
Else, wear sunglasses.

In programming, **control flow statements** help us make such decisions using logic.

◆ The **if** Statement

The most basic decision-making structure. If the condition is true, the block runs.

◆ Syntax:

```
javascript
CopyEdit
if (condition) {
  // code to execute if condition is true
}
```

✓ Example:

```
javascript
CopyEdit
let age = 18;

if (age >= 18) {
  console.log("You can vote!");
}
```

◆ The **if...else** Statement

Used when you want to run **one block if true** and **another if false**.

◆ Syntax:

```
javascript
CopyEdit
if (condition) {
    // true block
} else {
    // false block
}
```

✓ Example:

```
javascript
CopyEdit
let isRaining = true;

if (isRaining) {
    console.log("Take an umbrella!");
} else {
    console.log("Wear sunglasses!");
}
```

◆ The **if...else if...else** Ladder

Used to test **multiple conditions** in sequence.

◆ Syntax:

```
javascript
CopyEdit
if (condition1) {
    // block 1
} else if (condition2) {
    // block 2
} else {
```

```
    // fallback block  
}
```

✓ Example:

javascript

CopyEdit

```
let marks = 75;  
  
if (marks >= 90) {  
    console.log("Grade: A");  
} else if (marks >= 75) {  
    console.log("Grade: B");  
} else if (marks >= 60) {  
    console.log("Grade: C");  
} else {  
    console.log("Fail");  
}
```

◆ Comparison Operators Recap

Operator	Meaning
<code>==</code>	Equal (loose)
<code>===</code>	Equal (strict)
<code>!=</code>	Not equal
<code>></code>	Greater than
<code><</code>	Less than
<code>>=</code>	Greater or equal
<code><=</code>	Less or equal

◆ Logical Operators Recap

Operator	Meaning	Example
&&	AND	<code>a > 5 && a < 10</code>
,		,
!	NOT	<code>!isLoggedIn</code>

◆ The **switch** Statement

Used when you have many conditions to check based on a single variable value.

◆ Syntax:

```
javascript
CopyEdit
switch(expression) {
  case value1:
    // code
    break;
  case value2:
    // code
    break;
  default:
    // default code
}
```

✓ Example:

```
javascript
CopyEdit
let day = "Monday";

switch (day) {
  case "Monday":
    console.log("Start of the week!");
    break;
```

```
case "Friday":
  console.log("Almost weekend!");
  break;
default:
  console.log("Regular day.");
}
```

⚠️ Don't Forget **break**

If you skip **break**, the next case will also run — this is called **fall-through**.

```
javascript
CopyEdit
let num = 1;

switch (num) {
  case 1:
    console.log("One");
  case 2:
    console.log("Two");
}
// Output:
// One
// Two    <-- because there's no break!
```



Real-Life Example

```
javascript
CopyEdit
let temperature = 32;

if (temperature >= 30) {
  console.log("It's hot outside!");
} else if (temperature >= 20) {
  console.log("Nice weather!");
} else {
```



```
console.log("Wear a jacket.");  
}
```

Practice Exercises

1. Write a program to check if a number is even or odd.
 2. Create a program that returns a message based on the day of the week using `switch`.
 3. Use `if-else` to check if a student has passed (above 35 marks).
-



Conclusion

Control flow is **essential** for writing smart and interactive programs. You can:

- Use `if` for simple checks
- Use `else if` for multiple branches
- Use `switch` for multi-option cases based on one variable

In the **next lecture**, we'll explore **Loops in JavaScript** — which help you **repeat** actions without writing code multiple times.

Lecture 4: Loops in JavaScript (for, while, do-while)

What Are Loops?

Loops let us **execute a block of code repeatedly** without writing it multiple times. This is extremely useful when:

- Printing a sequence of numbers
- Iterating through arrays
- Repeating tasks until a condition is false

Think of loops as saying:

“Do this thing X times, or until Y is true.”

Types of Loops in JavaScript

1. `for` loop
2. `while` loop
3. `do...while` loop

Let's break down each one.

◆ 1. `for` Loop

Used when you **know exactly how many times** you want to loop.

◆ Syntax:

javascript

CopyEdit

```
for (initialization; condition; increment) {  
    // code block to run  
}
```

✓ Example:

javascript

CopyEdit

```
for (let i = 1; i <= 5; i++) {  
    console.log("Count: " + i);  
}
```

🔍 How It Works:

- **Initialization:** `let i = 1` (start value)
 - **Condition:** `i <= 5` (run while true)
 - **Increment:** `i++` (increase `i` by 1 each time)
-

◆ 2. while Loop

Use this when you're **not sure how many times** the loop should run — only when a condition is true.

◆ Syntax:

javascript

CopyEdit

```
while (condition) {  
    // code block to run  
}
```

✓ Example:

javascript

CopyEdit

```
let i = 1;

while (i <= 5) {
  console.log("While Count: " + i);
  i++;
}
```

⚠ Warning:

Make sure the condition eventually becomes **false**, or you'll create an **infinite loop**.

◆ 3. **do...while** Loop

This loop runs **at least once**, even if the condition is false the first time.

◆ Syntax:

javascript

CopyEdit

```
do {
  // code block to run
} while (condition);
```

✓ Example:

javascript

CopyEdit

```
let i = 1;

do {
  console.log("Do While Count: " + i);
  i++;
} while (i <= 5);
```

Use Case:

When you want to run something **first**, then check if it should repeat.



Real-World Analogy

- **for** loop: “I will do this 5 times.” (You know how many.)
 - **while** loop: “Keep doing this **while** there are customers in the line.”
 - **do...while**: “Do this at least once, and then see if I should do it again.”
-




Infinite Loops

If the condition **never becomes false**, the loop keeps running forever and may crash your program.

javascript

CopyEdit

```
//  Infinite loop example
while (true) {
  console.log("This will never stop!");
}
```



Loop Control Statements

♦ **break**

Stops the loop immediately.

javascript

CopyEdit

```
for (let i = 1; i <= 10; i++) {
  if (i === 5) break;
```

```
    console.log(i);  
}  
// Output: 1 2 3 4
```

♦ continue

Skips the current iteration.

```
javascript  
CopyEdit  
for (let i = 1; i <= 5; i++) {  
    if (i === 3) continue;  
    console.log(i);  
}  
// Output: 1 2 4 5
```

Practice Tasks

1. Print numbers 1 to 10 using `for` loop.
 2. Print even numbers from 1 to 20 using a `while` loop.
 3. Write a `do...while` loop that runs at least once even if the condition is false.
 4. Create a loop that breaks when a number is divisible by both 3 and 5.
 5. Use `continue` to skip printing number 7 from 1 to 10.
-

Summary

Loop Type	Use When
<code>for</code>	You know the number of iterations
<code>while</code>	Repeat while a condition is true

```
do...while Ensure code runs at least once  
le
```

Loops are **fundamental** to programming and power most real-world tasks — like rendering lists, handling users, and managing games or APIs.



Lecture 5: Functions in JavaScript



What is a Function?

A **function** is a reusable block of code designed to perform a particular task.

Think of it as a **recipe**: you define the steps once and call it whenever needed — without rewriting the instructions.



Why Use Functions?

- **Reusability**: Write once, use many times
 - **Organization**: Break large problems into small chunks
 - **Avoid Repetition**: DRY (Don't Repeat Yourself) principle
 - **Better Debugging**: Errors are easier to locate and fix
-



Function Syntax

javascript

CopyEdit

```
function functionName(parameters) {  
    // code block  
}
```

♦ Example:

javascript

CopyEdit

```
function greet(name) {  
    console.log("Hello, " + name + "!");  
}
```



```
}  
greet("Alice"); // Output: Hello, Alice!  
greet("Bob");   // Output: Hello, Bob!
```

Function Components

Part	Description
<code>function</code>	Keyword to declare a function
<code>functionName</code>	Name to identify the function
<code>parameters</code>	Inputs that the function accepts
<code>return</code>	Sends back a result from the function

Function With Return Value

You can return values using `return`.

```
javascript  
CopyEdit  
function add(a, b) {  
    return a + b;  
}  
  
let sum = add(5, 3);  
console.log(sum); // Output: 8
```

Function Without Parameters

```
javascript  
CopyEdit  
function sayHello() {
```

```
    console.log("Hello, world!");  
}  
sayHello(); // Output: Hello, world!
```



Function Expression (Storing Function in Variable)

javascript

CopyEdit

```
const multiply = function(x, y) {  
    return x * y;  
};
```

```
console.log(multiply(4, 5)); // Output: 20
```



Arrow Functions (ES6 Feature)

A shorter way to write functions.

javascript

CopyEdit

```
const square = (n) => {  
    return n * n;  
};
```

```
console.log(square(6)); // Output: 36
```

👉 If it has only one line and one parameter, you can write:

javascript

CopyEdit

```
const double = n => n * 2;
```



Function Calling Another Function

Functions can call each other.

javascript

CopyEdit

```
function greetUser(name) {  
  let message = buildGreeting(name);  
  console.log(message);  
}
```

```
function buildGreeting(name) {  
  return "Hi " + name + ", welcome!";  
}
```

```
greetUser("Alex"); // Output: Hi Alex, welcome!
```

Parameters vs Arguments

- **Parameters:** placeholders in function definition
- **Arguments:** actual values passed when calling the function

javascript

CopyEdit

```
function sayHi(name) { // name is a parameter  
  console.log("Hi, " + name);  
}
```

```
sayHi("Sarah"); // "Sarah" is the argument
```

Scope in Functions

Variables defined **inside** a function are not accessible outside it.

javascript

CopyEdit

```
function testScope() {
```

```
let x = 10;
console.log(x);
}
testScope();      // 10
// console.log(x); // ❌ Error: x is not defined
```

Real-World Analogy

Imagine a coffee machine (function). You give it input (coffee type), press a button (call the function), and it gives you output (coffee) — every time without changing the internals.

Practice Tasks

1. Create a function that returns the square of a number.
 2. Write a function that checks if a number is even or odd.
 3. Build a function to calculate the factorial of a number.
 4. Create a greeting function that returns "Good morning, <name>".
 5. Convert a normal function into an arrow function.
-

Summary

Concept	Description
Function	Block of reusable code
Parameters	Inputs in function definition
Arguments	Actual values passed to the function
return	Sends a value back to the caller
Arrow Function	Concise syntax for writing functions

Functions are the **foundation of structured programming**. They help make your code cleaner, reusable, and easier to debug.



Lecture 6: Arrays and Array Methods



What is an Array?

An **array** is a **collection of items** stored in a single variable. These items can be numbers, strings, objects, or even other arrays.



Think of an array as a **list of items**, like a shopping list.

javascript

CopyEdit

```
let fruits = ["apple", "banana", "orange"];
```



Why Use Arrays?

- To **store multiple values** in a single variable
 - To **organize and group data** logically
 - To **loop and perform actions** on each item
 - To **manipulate lists** easily with built-in methods
-



Array Syntax

javascript

CopyEdit

```
let arr = [item1, item2, item3];
```

Example:

javascript

CopyEdit

```
let numbers = [10, 20, 30, 40];  
console.log(numbers[1]); // Output: 20
```

Accessing Elements

javascript

CopyEdit

```
let colors = ["red", "green", "blue"];  
console.log(colors[0]); // red  
console.log(colors[2]); // blue
```

 Indexing starts from 0.

Looping Through an Array

for loop:

javascript

CopyEdit

```
let nums = [1, 2, 3, 4];  
for (let i = 0; i < nums.length; i++) {  
  console.log(nums[i]);  
}
```

for...of loop:

javascript

CopyEdit

```
for (let num of nums) {  
  console.log(num);  
}
```

Common Array Methods

push() — Adds item to the end

javascript

CopyEdit

```
let fruits = ["apple", "banana"];
fruits.push("orange");
console.log(fruits); // ["apple", "banana", "orange"]
```

pop() — Removes item from the end

javascript

CopyEdit

```
fruits.pop();
console.log(fruits); // ["apple", "banana"]
```

unshift() — Adds item to the start

javascript

CopyEdit

```
fruits.unshift("mango");
console.log(fruits); // ["mango", "apple", "banana"]
```

shift() — Removes item from the start

javascript

CopyEdit

```
fruits.shift();
console.log(fruits); // ["apple", "banana"]
```

indexOf() — Finds index of an item

javascript

CopyEdit

```
let index = fruits.indexOf("banana");
console.log(index); // 1
```

includes() — Checks if item exists

javascript

CopyEdit

```
console.log(fruits.includes("banana")); // true
```

slice() — Extracts a portion of array (non-destructive)

javascript

CopyEdit

```
let nums = [10, 20, 30, 40, 50];  
let part = nums.slice(1, 3); // [20, 30]
```

splice() — Add/Remove items (destructive)

javascript

CopyEdit

```
let items = ["a", "b", "c", "d"];  
items.splice(1, 2); // removes "b" and "c"  
console.log(items); // ["a", "d"]
```

forEach() — Executes a function for each item

javascript

CopyEdit

```
let scores = [100, 200, 300];  
scores.forEach(function(score) {  
  console.log("Score:", score);  
});
```

map() — Transforms each item and returns new array

javascript

CopyEdit

```
let doubled = scores.map(score => score * 2);  
console.log(doubled); // [200, 400, 600]
```

filter() — Filters items based on condition

javascript

CopyEdit

```
let highScores = scores.filter(score => score > 150);  
console.log(highScores); // [200, 300]
```

find() — Returns first item that matches condition

javascript

CopyEdit

```
let firstHigh = scores.find(score => score > 150);  
console.log(firstHigh); // 200
```

Real-Life Analogy

Imagine an **array** like a row of mailboxes (indexes), each holding a letter (value). You can go to a mailbox by number (index) and retrieve or update the contents.

Array Length

Use `.length` to find the number of items:

javascript

CopyEdit

```
let cities = ["Delhi", "Mumbai", "Chennai"];  
console.log(cities.length); // 3
```

Nested Arrays

You can store arrays inside arrays:

```
javascript
CopyEdit
let matrix = [
  [1, 2],
  [3, 4],
];
console.log(matrix[1][0]); // 3
```

Practice Tasks

1. Create an array of 5 colors and print each one.
 2. Add and remove elements using `push`, `pop`, `shift`, and `unshift`.
 3. Create an array of numbers and filter out the even ones.
 4. Map an array of numbers to their squares.
 5. Find the first number greater than 50 from an array.
-

Summary

Concept	Description
Array	List-like object to store multiple values
Index	Position of an item (starts at 0)
<code>push/pop</code>	Add/remove from end
<code>shift/unshift</code>	Add/remove from start
<code>map/filter/find</code>	Array transformation & searching
<code>length</code>	Total number of items in the array

Arrays are the **backbone of data storage** in most JavaScript applications — from lists of users, products, or scores, to building blocks for algorithms.



Lecture 7: Objects and Maps



What is an Object?

In JavaScript, an **object** is a collection of **key-value pairs**. It is used to represent real-world entities with properties and behaviors.



Think of an object as a **dictionary** — you look up a "key" and get its associated "value".

♦ Example:

javascript

CopyEdit

```
let person = {  
  name: "John",  
  age: 25,  
  isStudent: true  
};
```



Why Use Objects?

- To store **structured data**
 - To model **real-world entities**
 - To group **related data and behaviors**
 - To improve **code readability and organization**
-



Object Syntax

javascript

CopyEdit

```
let objectName = {  
  key1: value1,  
  key2: value2,  
  ...  
};
```

Example:

javascript
CopyEdit

```
let car = {  
  brand: "Tesla",  
  model: "Model 3",  
  year: 2022  
};
```

Accessing Object Properties

Using Dot Notation:


javascript
CopyEdit

```
console.log(car.brand); // Tesla
```

Using Bracket Notation:

javascript
CopyEdit

```
console.log(car["model"]); // Model 3
```

 Use bracket notation when the key is stored in a variable.

Modifying Object Properties

javascript
CopyEdit

```
car.year = 2023;
```

```
car["color"] = "white";
```

Deleting Properties

javascript

CopyEdit

```
delete car.color;
```

Looping Through Objects

for...in Loop:

javascript

CopyEdit

```
for (let key in car) {  
  console.log(key + ": " + car[key]);  
}
```

Built-in Object Methods

- ♦ **Object.keys()** — returns array of keys

javascript

CopyEdit

```
console.log(Object.keys(car)); // ["brand", "model", "year"]
```

- ♦ **Object.values()** — returns array of values

javascript

CopyEdit

```
console.log(Object.values(car)); // ["Tesla", "Model 3", 2023]
```

- ♦ **Object.entries()** — returns array of [key, value] pairs

javascript

CopyEdit

```
console.log(Object.entries(car));
```

What is a Map?

A **Map** is a built-in JavaScript object that allows you to store key-value pairs with keys of any type.

Unlike objects:

- **Map keys can be of any type** (objects, functions, etc.)
 - **Preserves insertion order**
 - **Easier iteration and size checking**
-

Creating a Map

javascript

CopyEdit

```
let map = new Map();
```

Adding Values:

javascript

CopyEdit

```
map.set("name", "Alice");  
map.set("age", 30);
```

Getting Values:

javascript

CopyEdit

```
console.log(map.get("name")); // Alice
```

Checking Existence:


```
javascript
CopyEdit
console.log(map.has("age")); // true
```

Removing Values:

```
javascript
CopyEdit
map.delete("age");
```

Looping Through a Map

Using `for...of`:

```
javascript
CopyEdit
for (let [key, value] of map) {
  console.log(key, value);
}
```

Object vs Map: When to Use

Feature	Object	Map
Key Types	Strings and Symbols only	Any type (objects, functions...)
Insertion Order	Not guaranteed	Preserved
Iteration	Requires manual methods	Built-in and easier
Performance	Slower with frequent insertions	Better for frequent additions
Size Property	Not available (<code>Object.keys().length</code>)	Available as <code>map.size</code>

Nested Objects

You can nest one object inside another:

javascript

CopyEdit

```
let user = {  
  name: "Jane",  
  address: {  
    city: "Mumbai",  
    zip: 400001  
  }  
};  
  
console.log(user.address.city); // Mumbai
```



Real-Life Analogy

An **object** is like a **person's profile**:

- name → "Alice"
- age → 25
- isStudent → true

A **map** is like a **contacts app**, where:

- you can look up a person (key) and get their details (value),
 - you can use different types of keys (ID, phone number, object references, etc.)
-



Practice Tasks

1. Create an object for a student with properties: name, rollNo, marks.
2. Update and delete some properties.

3. Loop through the object and print keys and values.
4. Create a Map to store country names as keys and their capitals as values.
5. Iterate through the Map and display key-value pairs.

Summary

Feature	Description
Object	Unordered key-value pairs (keys are strings/symbols)
Map	Ordered key-value pairs (keys can be any type)
Dot/Bracket Notation	Used to access object properties
<code>Object.keys/values/entries()</code>	Methods to extract data from object
<code>map.set/get/has/delete()</code>	Common Map operations

Objects and Maps are **cornerstones of structured data handling** in JavaScript. Mastering them opens the door to better organization and manipulation of data in real-world applications.



Lecture 8: Stacks and Queues



Introduction

Stacks and **Queues** are **linear data structures** used to store and manage data in a specific order. These structures are commonly used in real-life computing tasks such as undo operations, managing tasks in a processor, handling network requests, and more.



1. Stack

A **Stack** follows the **LIFO** (Last In, First Out) principle.

Imagine a stack of plates — you add to the top, and you remove from the top.

♦ Basic Stack Operations:

Operation	Description
<code>push()</code>	Add item to the top
<code>pop()</code>	Remove item from top
<code>peek()</code>	View top item
<code>isEmpty()</code>	Check if stack is empty
<code>length</code>	Number of elements



JavaScript Implementation Using Array:

```
javascript
CopyEdit
let stack = [];

// Push
stack.push(10);
```

```
stack.push(20);
stack.push(30);

// Pop
console.log(stack.pop()); // 30

// Peek
console.log(stack[stack.length - 1]); // 20

// Check if empty
console.log(stack.length === 0); // false
```

Stack Real-Life Use Cases

- Undo/redo functionality in editors
 - Backtracking algorithms (e.g. maze solving, recursion stack)
 - Browser history navigation
 - Syntax parsing in compilers
-

Stack Implementation with Class:

javascript

CopyEdit

```
class Stack {
  constructor() {
    this.items = [];
  }

  push(element) {
    this.items.push(element);
  }

  pop() {
```

```
        if (this.isEmpty()) return "Underflow";
        return this.items.pop();
    }

    peek() {
        return this.items[this.items.length - 1];
    }

    isEmpty() {
        return this.items.length === 0;
    }

    printStack() {
        console.log(this.items.join(" "));
    }
}

let stack = new Stack();
stack.push(5);
stack.push(10);
stack.printStack(); // 5 10
stack.pop();
stack.printStack(); // 5
```

2. Queue

A **Queue** follows the **FIFO** (First In, First Out) principle.

Think of a line at a ticket counter — the first person to get in line is the first served.

◆ Basic Queue Operations:

Operation	Description
-----------	-------------

<code>enqueue()</code>	Add item to the end
------------------------	---------------------

`dequeue()` Remove item from front
`peek()` View front item
`isEmpty()` Check if queue is empty
`length` Number of elements

JavaScript Implementation Using Array:

javascript

CopyEdit

```
let queue = [];  
  
// Enqueue  
queue.push(1);  
queue.push(2);  
queue.push(3);  
  
// Dequeue  
console.log(queue.shift()); // 1  
  
// Peek  
console.log(queue[0]); // 2
```

! `shift()` is less efficient for large queues ($O(n)$ time), so custom implementations are preferred in real-world apps.

Queue Implementation with Class:

javascript

CopyEdit

```
class Queue {  
  constructor() {  
    this.items = [];  
  }  
}
```

```
enqueue(element) {
  this.items.push(element);
}

dequeue() {
  if (this.isEmpty()) return "Underflow";
  return this.items.shift();
}

peek() {
  return this.items[0];
}

isEmpty() {
  return this.items.length === 0;
}

printQueue() {
  console.log(this.items.join(" "));
}
}

let queue = new Queue();
queue.enqueue(100);
queue.enqueue(200);
queue.printQueue(); // 100 200
queue.dequeue();
queue.printQueue(); // 200
```

Queue Real-Life Use Cases

- Printer task queue
- CPU scheduling

- Call center systems
 - Handling asynchronous events
-



Stack vs Queue

Feature	Stack (LIFO)	Queue (FIFO)
Insertion	Top	Rear (end)
Removal	Top	Front (start)
Use Cases	Backtracking, undo	Task scheduling, queues
Operations	push/pop	enqueue/dequeue



Circular Queue (Brief Intro)

In a **circular queue**, the last position connects to the first position to form a circle. This prevents wasted space in a standard queue after many dequeues.

You'll explore this in-depth in more advanced lectures.



Practice Tasks

1. Create a **Stack** class and implement **push**, **pop**, and **peek**.
2. Simulate a stack to reverse a string.
3. Implement a **Queue** class and add basic operations.
4. Simulate a real-life queue (like customer service).
5. Modify queue to reject dequeue operations when empty.

Summary

Concept	Stack	Queue
Principle	Last In First Out (LIFO)	First In First Out (FIFO)
Key Ops	push, pop, peek, isEmpty	enqueue, dequeue, peek, isEmpty
Real Use	Undo, Recursion, History	Scheduling, Buffering, Tasks

Stacks and Queues are **fundamental** for building algorithms and solving real-world problems. They act as **containers for logic** and are often used to control execution flow in programming.



Lecture 8: Stacks and Queues



Introduction

Stacks and **Queues** are **linear data structures** used to store and manage data in a specific order. These structures are commonly used in real-life computing tasks such as undo operations, managing tasks in a processor, handling network requests, and more.



1. Stack

A **Stack** follows the **LIFO** (Last In, First Out) principle.

Imagine a stack of plates — you add to the top, and you remove from the top.

♦ Basic Stack Operations:

Operation	Description
<code>push()</code>	Add item to the top
<code>pop()</code>	Remove item from top
<code>peek()</code>	View top item
<code>isEmpty()</code>	Check if stack is empty
<code>length</code>	Number of elements



JavaScript Implementation Using Array:

```
javascript
CopyEdit
let stack = [];

// Push
stack.push(10);
```

```
stack.push(20);
stack.push(30);

// Pop
console.log(stack.pop()); // 30

// Peek
console.log(stack[stack.length - 1]); // 20

// Check if empty
console.log(stack.length === 0); // false
```

Stack Real-Life Use Cases

- Undo/redo functionality in editors
 - Backtracking algorithms (e.g. maze solving, recursion stack)
 - Browser history navigation
 - Syntax parsing in compilers
-

Stack Implementation with Class:

javascript

CopyEdit

```
class Stack {
  constructor() {
    this.items = [];
  }

  push(element) {
    this.items.push(element);
  }

  pop() {
```

```
        if (this.isEmpty()) return "Underflow";
        return this.items.pop();
    }

    peek() {
        return this.items[this.items.length - 1];
    }

    isEmpty() {
        return this.items.length === 0;
    }

    printStack() {
        console.log(this.items.join(" "));
    }
}

let stack = new Stack();
stack.push(5);
stack.push(10);
stack.printStack(); // 5 10
stack.pop();
stack.printStack(); // 5
```

2. Queue

A **Queue** follows the **FIFO** (First In, First Out) principle.

Think of a line at a ticket counter — the first person to get in line is the first served.

◆ Basic Queue Operations:

Operation	Description
-----------	-------------

<code>enqueue(</code>	Add item to the end
<code>)</code>	

`dequeue()` Remove item from front
`peek()` View front item
`isEmpty()` Check if queue is empty
`length` Number of elements

JavaScript Implementation Using Array:

javascript

CopyEdit

```
let queue = [];  
  
// Enqueue  
queue.push(1);  
queue.push(2);  
queue.push(3);  
  
// Dequeue  
console.log(queue.shift()); // 1  
  
// Peek  
console.log(queue[0]); // 2
```

! `shift()` is less efficient for large queues ($O(n)$ time), so custom implementations are preferred in real-world apps.

Queue Implementation with Class:

javascript

CopyEdit

```
class Queue {  
  constructor() {  
    this.items = [];  
  }  
}
```

```
enqueue(element) {
  this.items.push(element);
}

dequeue() {
  if (this.isEmpty()) return "Underflow";
  return this.items.shift();
}

peek() {
  return this.items[0];
}

isEmpty() {
  return this.items.length === 0;
}

printQueue() {
  console.log(this.items.join(" "));
}
}

let queue = new Queue();
queue.enqueue(100);
queue.enqueue(200);
queue.printQueue(); // 100 200
queue.dequeue();
queue.printQueue(); // 200
```



Queue Real-Life Use Cases

- Printer task queue
- CPU scheduling

- Call center systems
 - Handling asynchronous events
-



Stack vs Queue

Feature	Stack (LIFO)	Queue (FIFO)
Insertion	Top	Rear (end)
Removal	Top	Front (start)
Use Cases	Backtracking, undo	Task scheduling, queues
Operations	push/pop	enqueue/dequeue



Circular Queue (Brief Intro)

In a **circular queue**, the last position connects to the first position to form a circle. This prevents wasted space in a standard queue after many dequeues.

You'll explore this in-depth in more advanced lectures.



Practice Tasks

1. Create a **Stack** class and implement **push**, **pop**, and **peek**.
2. Simulate a stack to reverse a string.
3. Implement a **Queue** class and add basic operations.
4. Simulate a real-life queue (like customer service).
5. Modify queue to reject dequeue operations when empty.

Summary

Concept	Stack	Queue
Principle	Last In First Out (LIFO)	First In First Out (FIFO)
Key Ops	push, pop, peek, isEmpty	enqueue, dequeue, peek, isEmpty
Real Use	Undo, Recursion, History	Scheduling, Buffering, Tasks

Stacks and Queues are **fundamental** for building algorithms and solving real-world problems. They act as **containers for logic** and are often used to control execution flow in programming.

✅ **Next Up:** We'll dive into **Linked Lists**, another powerful structure for dynamic memory allocation and efficient insertions/deletions.

Would you like to continue with **Lecture 9: Linked Lists**?

40

You said:

next

ChatGPT said:

Here's the detailed article for **Lecture 9: Linked Lists** in your JavaScript Data Structures & Algorithms course.

Lecture 9: Linked Lists

What is a Linked List?

A **Linked List** is a linear data structure where elements (called **nodes**) are connected using **pointers** rather than contiguous memory blocks like arrays. Each node contains:

- **Data**
- **Pointer (Reference)** to the next node

Unlike arrays, **linked lists are dynamic** — they can grow and shrink at runtime.

Types of Linked Lists

Type	Description
Singly Linked List	Each node points to the next node only
Doubly Linked List	Each node has two pointers: next and previous
Circular Linked List	Last node points back to the first node

For this lecture, we focus on **Singly Linked List**.

Linked List Node Structure

javascript

CopyEdit

```
class Node {  
  constructor(value) {  
    this.value = value;  
    this.next = null;  
  }  
}
```

Linked List Class Implementation

javascript

CopyEdit

```
class LinkedList {
  constructor() {
    this.head = null;
    this.size = 0;
  }

  // Add at the end
  append(value) {
    const newNode = new Node(value);
    if (!this.head) {
      this.head = newNode;
    } else {
      let current = this.head;
      while (current.next !== null) {
        current = current.next;
      }
      current.next = newNode;
    }
    this.size++;
  }

  // Print the list
  printList() {
    let current = this.head;
    let output = '';
    while (current) {
      output += current.value + ' -> ';
      current = current.next;
    }
    console.log(output + 'null');
  }
}
```

Example

javascript

CopyEdit

```
const list = new LinkedList();
list.append(10);
```

```
list.append(20);
list.append(30);
list.printList(); // 10 -> 20 -> 30 -> null
```

Other Operations

1. Prepend (Insert at Beginning)

javascript

CopyEdit

```
prepend(value) {
  const newNode = new Node(value);
  newNode.next = this.head;
  this.head = newNode;
  this.size++;
}
```

2. Insert at Specific Index

javascript

CopyEdit

```
insertAt(value, index) {
  if (index < 0 || index > this.size) return;
  const newNode = new Node(value);
  if (index === 0) {
    newNode.next = this.head;
    this.head = newNode;
  } else {
    let current = this.head;
    let previous;
    let count = 0;

    while (count < index) {
      previous = current;
      current = current.next;
      count++;
    }
    newNode.next = current;
```

```

        previous.next = newNode;
    }
    this.size++;
}

```

3. Delete by Value

javascript

CopyEdit

```

removeValue(value) {
    if (!this.head) return;

    if (this.head.value === value) {
        this.head = this.head.next;
        this.size--;
        return;
    }

    let current = this.head;
    let previous = null;

    while (current && current.value !== value) {
        previous = current;
        current = current.next;
    }

    if (current) {
        previous.next = current.next;
        this.size--;
    }
}

```



Linked List vs Array

Feature	Linked List	Array
Memory Allocation	Dynamic	Fixed/Contiguous

Insert/Delete	Fast ($O(1)$ at head)	Slow ($O(n)$ due to shift)
Random Access	✗ No	✓ Yes ($O(1)$)
Structure	Nodes with pointers	Indexed elements

Real-Life Use Cases

- Music playlist apps
 - Undo functionality in editors
 - Browser navigation (forward/backward)
 - Memory-efficient storage for large datasets
-

Practice Exercises

1. Create a linked list and add 5 elements using `append`.
 2. Implement a function to search an element in the list.
 3. Add `removeAt(index)` method to delete a node at a specific index.
 4. Create a function to reverse a linked list.
 5. Convert an array into a linked list.
-

Summary

Term	Meaning
Node	Basic unit holding value and next pointer
Head	First node of the list

Tail	Last node (next is null)
Dynamic Size	Can grow/shrink dynamically
No Random Access	Need to traverse for specific element

Key Takeaways

- Linked Lists provide dynamic memory usage and flexible data manipulation.
- They are not suitable for frequent random access but excellent for insertions and deletions.
- Understanding how to manipulate pointers is crucial for mastering linked lists.



Lecture 10: Sets and Hash Tables



Introduction

In this lecture, we will explore **Sets** and **Hash Tables**, two highly efficient data structures used for storing unique elements and enabling fast lookups, insertions, and deletions. They are fundamental in many algorithms and real-world applications where fast access to data is required.

◆ 1. Sets

A **Set** is a collection of **unique** elements, meaning no duplicates are allowed. It is similar to an array but with the restriction that all values must be distinct.

Key Operations on Sets:

- **add(value)**: Adds a new value to the set.
 - **delete(value)**: Removes a value from the set.
 - **has(value)**: Checks if a value exists in the set.
 - **clear()**: Removes all values from the set.
 - **size**: Returns the number of elements in the set.
-



JavaScript Implementation of Set:

In JavaScript, sets are natively supported with the **Set** object.

javascript

CopyEdit

```
let set = new Set();
```



```
// Add elements
set.add(1);
set.add(2);
set.add(3);

// Check if element exists
console.log(set.has(2)); // true
console.log(set.has(4)); // false

// Delete element
set.delete(2);
console.log(set.has(2)); // false

// Size of set
console.log(set.size); // 2

// Clear the set
set.clear();
console.log(set.size); // 0
```

Set Real-Life Use Cases:

- Ensuring uniqueness (e.g., in a list of emails or usernames).
 - Tracking visited nodes in graph traversal algorithms.
 - Filtering out duplicate data from a dataset.
-

◆ 2. Hash Tables (Hash Maps)

A **Hash Table** (or **Hash Map**) is a data structure that allows for **fast access** to values using a **key**. It stores key-value pairs, and the key is hashed to determine the index where the value is stored.

Key Operations on Hash Tables:

- **set(key, value)**: Adds or updates a key-value pair.
 - **get(key)**: Retrieves the value associated with the key.
 - **delete(key)**: Removes the key-value pair.
 - **has(key)**: Checks if a key exists.
 - **clear()**: Clears all key-value pairs.
-

JavaScript Implementation of Hash Table:

javascript

CopyEdit

```
class HashTable {
  constructor() {
    this.table = new Array(137); // Initializing with a fixed size
    array.
  }

  // Hash function to compute index for a given key
  hash(key) {
    let hash = 0;
    for (let i = 0; i < key.length; i++) {
      hash += key.charCodeAt(i);
    }
    return hash % this.table.length;
  }

  // Add or update a key-value pair
  set(key, value) {
    let index = this.hash(key);
    this.table[index] = value;
  }

  // Retrieve a value by its key
  get(key) {
    let index = this.hash(key);
```

```

        return this.table[index];
    }

    // Remove a key-value pair
    delete(key) {
        let index = this.hash(key);
        this.table[index] = undefined;
    }

    // Check if the key exists
    has(key) {
        let index = this.hash(key);
        return this.table[index] !== undefined;
    }

    // Clear all key-value pairs
    clear() {
        this.table = new Array(137);
    }
}

```

✅ Example Usage:

javascript

CopyEdit

```

let hashTable = new HashTable();
hashTable.set("name", "Alice");
hashTable.set("age", 25);
hashTable.set("job", "Developer");

console.log(hashTable.get("name")); // Alice
console.log(hashTable.has("age")); // true

hashTable.delete("age");
console.log(hashTable.get("age")); // undefined

```

🎯 Hash Table Real-Life Use Cases:

- Storing configurations or settings (key-value pairs).
 - Caching, for example, to store the results of expensive function calls.
 - Implementing dictionaries (word lookup in text processing).
 - Optimizing search algorithms (e.g., checking if an item is already in a collection).
-

Sets vs Hash Tables

Feature	Set	Hash Table
Data Storage	Only values (no duplicates)	Key-value pairs
Lookup Time	$O(1)$	$O(1)$
Insertion Time	$O(1)$	$O(1)$
Deletion Time	$O(1)$	$O(1)$
Use Case	Uniqueness, filtering	Fast access to key-value pairs

Hash Collisions

A **hash collision** occurs when two different keys produce the same hash value. Handling collisions is an essential part of hash table design. Common techniques include:

- **Chaining:** Storing multiple key-value pairs at the same index (linked list or array).
- **Open Addressing:** Finding another empty slot for the collided key-value pair.

For simplicity, our earlier implementation does not handle collisions.

Practice Tasks

1. Implement a `HashTable` class with methods for `set`, `get`, `delete`, and `has`.
2. Create a function that counts the occurrences of each element in an array using a hash table.
3. Implement a `Set` class and add methods for `add`, `has`, and `delete`.
4. Use a set to remove duplicates from an array.
5. Design a program that uses a hash table to find the first non-repeating character in a string.

Summary

Data Structure	Set	Hash Table
Purpose	Store unique values	Store key-value pairs
Lookup Time	$O(1)$	$O(1)$
Operations	Add, Delete, Has	Set, Get, Delete, Has, Clear
Ideal Use Case	Uniqueness, filtering duplicates	Fast lookups, key-value storage

Key Takeaways

- **Sets** provide an efficient way to store unique values and check membership.
- **Hash Tables** are excellent for fast key-value lookups and are widely used in real-world applications like caching, databases, and indexing.
- Handling hash collisions efficiently is key to implementing a robust hash table.



Lecture 11: Recursion



Introduction

Recursion is a powerful technique where a function calls itself to solve smaller instances of the same problem. It allows for elegant solutions to problems that are inherently repetitive or have a recursive structure.

In this lecture, we will dive deep into how recursion works, its components, and explore practical examples where recursion can be used effectively.

♦ 1. What is Recursion?

Recursion is a process where a function calls itself directly or indirectly to break down a complex problem into simpler sub-problems. Each recursive call solves a part of the problem, and the results of those sub-problems are combined to give the solution.

For recursion to work correctly, it must have two essential components:

1. **Base Case:** The condition that stops the recursion.
 2. **Recursive Case:** The part where the function calls itself with a simpler or smaller version of the original problem.
-



Basic Example of Recursion:

Here's a simple example of recursion in JavaScript:

javascript

CopyEdit

```
function factorial(n) {  
  if (n === 0) { // Base case  
    return 1;  
  } else {
```

```
        return n * factorial(n - 1); // Recursive case
    }
}

console.log(factorial(5)); // Output: 120
```

Explanation:

- **Base Case:** When `n === 0`, the function returns 1. This prevents infinite recursion.
- **Recursive Case:** The function calls itself with `n - 1` until it reaches the base case.

In this example, the recursion works by breaking down the problem `factorial(n)` into smaller sub-problems like `factorial(n - 1)`, and so on.

♦ 2. How Recursion Works

Recursion works by breaking a problem into smaller instances of the same problem and using the results of those smaller instances to solve the larger problem.

Steps of Recursive Execution:

1. **Start:** The initial function call starts with the original problem.
 2. **Recursive Calls:** Each call works on a smaller sub-problem.
 3. **Base Case:** The base case is eventually reached, which stops further recursive calls.
 4. **Unwinding:** The function returns from the recursive calls, combining the results to solve the original problem.
-

Example: Calculating Factorial

To calculate `factorial(5)`, the recursion happens as follows:

matlab

CopyEdit

```
factorial(5)
= 5 * factorial(4)
= 5 * (4 * factorial(3))
= 5 * (4 * (3 * factorial(2)))
= 5 * (4 * (3 * (2 * factorial(1))))
= 5 * (4 * (3 * (2 * (1 * factorial(0)))))
= 5 * (4 * (3 * (2 * (1 * 1))))
= 120
```

◆ 3. Base Case and Recursive Case

Every recursive function needs both a **base case** and a **recursive case**.

- **Base Case:** This is the condition under which the function stops calling itself. Without a base case, recursion would continue infinitely, leading to a stack overflow error.
 - **Recursive Case:** This part of the function reduces the problem into smaller pieces and calls the function on these smaller sub-problems.
-

Example: Sum of Natural Numbers

Consider the problem of calculating the sum of natural numbers up to n (i.e., $1 + 2 + 3 + \dots + n$).

javascript

CopyEdit

```
function sum(n) {
  if (n === 0) { // Base case
    return 0;
  } else {
    return n + sum(n - 1); // Recursive case
  }
}

console.log(sum(5)); // Output: 15 (1 + 2 + 3 + 4 + 5)
```


- **Base Case:** When $n == 0$, the function returns 0 (the sum of numbers up to 0).
 - **Recursive Case:** The function adds n to the sum of numbers up to $n - 1$.
-

◆ 4. Advantages of Recursion

- **Simplicity:** Recursive solutions often provide a more elegant and easier-to-understand implementation than their iterative counterparts.
 - **Problem-Solving:** Recursion is naturally suited for problems that involve breaking down the problem into smaller sub-problems (e.g., tree traversal, sorting algorithms).
 - **Readability:** Recursion often leads to more readable code for certain types of problems, like tree and graph traversal.
-

◆ 5. Drawbacks of Recursion

- **Memory Usage:** Each recursive call adds a new frame to the call stack, and excessive recursion can lead to a **stack overflow** if the recursion goes too deep.
 - **Performance:** Recursive functions may be slower than their iterative counterparts due to the overhead of function calls and returning values.
 - **Debugging Difficulty:** Recursion can sometimes be more challenging to debug, especially when there are logical errors in the base case or recursive case.
-

Example: Fibonacci Sequence (Recursive)

The Fibonacci sequence is defined as:

r

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$F(0) = 0$
 $F(1) = 1$
 $F(n) = F(n-1) + F(n-2)$ (for $n > 1$)

Here's how you can implement this using recursion:

javascript

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```
function fibonacci(n) {  
  if (n <= 1) { // Base case  
    return n;  
  } else {  
    return fibonacci(n - 1) + fibonacci(n - 2); // Recursive case  
  }  
}
```

```
console.log(fibonacci(6)); // Output: 8 (0, 1, 1, 2, 3, 5, 8)
```

Explanation:

The function calculates the Fibonacci number for a given n by recursively calling itself with smaller values of n until it reaches the base case ($n \leq 1$).

◆ 6. When to Use Recursion

Recursion is particularly useful in scenarios where a problem can be broken down into smaller sub-problems, such as:

- **Tree Traversal:** Recursion is commonly used to traverse hierarchical structures like trees (e.g., binary trees).
- **Graph Traversal:** Recursion is also used in graph traversal algorithms like Depth First Search (DFS).
- **Sorting Algorithms:** Algorithms like Merge Sort and Quick Sort use recursion to divide the problem into smaller sub-problems.

- **Backtracking Problems:** Problems like generating combinations or solving Sudoku puzzles often involve recursion.
-

◆ 7. Tail Recursion

In a **tail recursion**, the recursive call is the last operation in the function, meaning there are no further computations after the function returns. This can optimize performance by allowing the compiler to optimize the call stack.

Example of Tail Recursion:

javascript

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```
function factorialTailRec(n, accumulator = 1) {  
  if (n === 0) {  
    return accumulator;  
  } else {  
    return factorialTailRec(n - 1, n * accumulator);  
  }  
}
```

```
console.log(factorialTailRec(5)); // Output: 120
```

In the tail-recursive version, instead of waiting for the recursion to return a result and then multiplying, the multiplication is done in the recursive call itself, making it more efficient.

Practice Tasks

1. Implement the **factorial function** using recursion and test it with different numbers.
2. Write a recursive function to calculate the **nth Fibonacci number**.
3. Solve the **Tower of Hanoi** problem recursively.
4. Implement a recursive function to **reverse a string**.

5. Write a function to **flatten a nested array** using recursion.
6. Create a recursive solution for **binary search**.

Summary

Concept	Explanation
Recursion	A technique where a function calls itself to solve a problem.
Base Case	The condition that stops the recursion.
Recursive Case	The part where the function calls itself on a smaller sub-problem.
Advantages	Simplicity, readability, and elegance in solving problems like tree and graph traversal.
Drawbacks	High memory usage, potential stack overflow, and performance concerns.
Tail Recursion	A special form of recursion where the recursive call is the last operation, enabling optimization.

Key Takeaways

- Recursion is a powerful problem-solving technique where functions call themselves.
- Always define a base case to prevent infinite recursion.
- Recursive solutions can be more elegant and easier to implement but can have performance issues due to deep recursion.
- Tail recursion is an optimized form of recursion that reduces the overhead.



Lecture 12: Searching Algorithms



Introduction

Searching algorithms are fundamental to many problems in computer science, helping to locate an element within a collection of data. Efficient searching is crucial in optimizing the performance of applications, especially when dealing with large datasets. In this lecture, we will cover two essential searching algorithms:

1. **Linear Search**
 2. **Binary Search**
-

♦ 1. What is Searching?

Searching refers to the process of finding an element or a group of elements that satisfy a specific condition in a collection (such as an array or a list). The goal is to locate the element and return its position or confirm its absence.

Searching Algorithms:

- **Linear Search:** A simple search algorithm that sequentially checks each element until a match is found.
 - **Binary Search:** An efficient search algorithm that works on sorted data by repeatedly dividing the search interval in half.
-

♦ 2. Linear Search

How it Works:

Linear search is the simplest searching algorithm. It starts at the beginning of the list (or array) and compares each element with the target value. If a match is found, the search stops and the index is returned. If no match is found, the algorithm continues until the end of the list.

Steps:

1. Start at the first element of the array.
2. Compare the element with the target value.
3. If the element matches the target, return the index.
4. If the element doesn't match, move to the next element.
5. Repeat steps 2-4 until the target is found or the end of the list is reached.

Time Complexity:

- **Best Case:** $O(1)$ (if the element is the first one).
- **Worst Case:** $O(n)$ (if the element is the last one or not in the array).

Example: Linear Search in JavaScript

javascript

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```
function linearSearch(arr, target) {  
  for (let i = 0; i < arr.length; i++) {  
    if (arr[i] === target) {  
      return i; // Return the index if the target is found  
    }  
  }  
  return -1; // Return -1 if the target is not found  
}
```

```
let arr = [5, 3, 7, 2, 9, 1];  
console.log(linearSearch(arr, 7)); // Output: 2 (index of element 7)  
console.log(linearSearch(arr, 4)); // Output: -1 (element not found)
```

◆ 3. When to Use Linear Search

Linear search is ideal when:

- The dataset is small or unsorted.
 - The array is not sorted, and there is no way to sort the data for better searching.
 - You don't need to worry about performance inefficiencies in small arrays.
-

◆ 4. Binary Search

How it Works:

Binary search is much faster than linear search but requires that the data be sorted. It works by repeatedly dividing the search interval in half. The algorithm compares the target value to the middle element of the array. If the target value is equal to the middle element, the search is complete. If the target value is less than the middle element, the search continues in the lower half of the array; otherwise, it continues in the upper half.

Steps:

1. Start with the entire array and find the middle element.
2. If the middle element equals the target, return the index.
3. If the target is smaller than the middle element, search the left half.
4. If the target is greater than the middle element, search the right half.
5. Repeat steps 1-4 until the target is found or the search interval is empty.

Time Complexity:

- **Best Case:** $O(1)$ (if the middle element is the target).
- **Worst Case:** $O(\log n)$ (each step halves the search space).

Example: Binary Search in JavaScript

javascript

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```
function binarySearch(arr, target) {  
    let low = 0;  
    let high = arr.length - 1;  
  
    while (low <= high) {  
        let mid = Math.floor((low + high) / 2);  
  
        if (arr[mid] === target) {  
            return mid; // Return the index if the target is found  
        } else if (arr[mid] < target) {  
            low = mid + 1; // Search in the right half  
        } else {  
            high = mid - 1; // Search in the left half  
        }  
    }  
  
    return -1; // Return -1 if the target is not found  
}  
  
let arr = [1, 2, 3, 5, 7, 9];  
console.log(binarySearch(arr, 7)); // Output: 4 (index of element 7)  
console.log(binarySearch(arr, 4)); // Output: -1 (element not found)
```

◆ 5. When to Use Binary Search

Binary search is ideal when:

- The dataset is large and sorted.
- You need to find elements quickly, especially when performance is a concern.
- Sorting the data once can save a lot of time if multiple searches are required on the same dataset.

◆ 6. Linear Search vs Binary Search

Aspect	Linear Search	Binary Search
Data Type	Works on unsorted data	Works only on sorted data
Time Complexity	$O(n)$ for the worst case	$O(\log n)$ for the worst case
Space Complexity	$O(1)$	$O(1)$
Use Case	Small or unsorted datasets	Large sorted datasets
Performance	Slower for large datasets	Faster for large datasets

◆ 7. Recap of Searching Algorithms

- **Linear Search:** It works on both sorted and unsorted arrays but is inefficient for large datasets because it checks each element one by one.
 - **Binary Search:** A more efficient algorithm that works on sorted arrays, reducing the time complexity to $O(\log n)$ by halving the search space at each step.
-

Practice Tasks

1. Implement **Linear Search** and test it with unsorted arrays.
2. Implement **Binary Search** and test it with sorted arrays.
3. Compare the performance of both algorithms using a large dataset.
4. Solve a problem where you need to find the position of an element in a **sorted array** using binary search.
5. Modify the binary search algorithm to return the **index of the first occurrence** of the target value if there are duplicate values in the sorted array.

Summary

Concept	Explanation
Linear Search	A simple algorithm that checks each element sequentially.
Binary Search	A fast algorithm that divides the search space in half for sorted data.
Time Complexity	Linear search has $O(n)$, while binary search has $O(\log n)$ for large datasets.
Use Case	Linear search is used for small or unsorted data; binary search is used for large, sorted data.



Lecture 13: Sorting Algorithms



Introduction

Sorting is one of the most fundamental tasks in computer science. The objective of sorting is to arrange elements in a particular order—either ascending or descending. Sorting algorithms are crucial in optimizing data retrieval and processing. A good sorting algorithm can make a significant difference in performance, especially when dealing with large datasets.

In this lecture, we will cover several common sorting algorithms:

1. **Bubble Sort**
 2. **Insertion Sort**
 3. **Merge Sort**
 4. **Quick Sort**
-

◆ 1. What is Sorting?

Sorting is the process of arranging a collection of elements (like numbers or strings) in a specific order. The two most common orders are:

- **Ascending Order:** From smallest to largest (e.g., 1, 2, 3).
- **Descending Order:** From largest to smallest (e.g., 3, 2, 1).

Sorting is important because it helps in:

- Searching (sorted data can be searched faster).
- Organizing data for efficient processing.
- Data visualization.

◆ 2. Bubble Sort

How it Works:

Bubble Sort is a simple comparison-based algorithm. It works by repeatedly stepping through the list, comparing adjacent elements, and swapping them if they are in the wrong order. The process is repeated until the list is sorted.

Steps:

1. Start from the first element and compare it with the next element.
2. If the first element is greater than the second, swap them.
3. Continue to the next pair of elements and repeat until the end of the list.
4. After each pass through the list, the largest element is "bubbled" to the end.
5. Repeat the process for the remaining unsorted elements until no more swaps are needed.

Time Complexity:

- **Best Case:** $O(n)$ (if the array is already sorted).
- **Worst Case:** $O(n^2)$ (if the array is in reverse order).

Example: Bubble Sort in JavaScript

javascript

CopyEdit

```
function bubbleSort(arr) {  
  let n = arr.length;  
  for (let i = 0; i < n - 1; i++) {  
    for (let j = 0; j < n - 1 - i; j++) {  
      if (arr[j] > arr[j + 1]) {  
        // Swap elements if they are in the wrong order  
        let temp = arr[j];  
        arr[j] = arr[j + 1];  
        arr[j + 1] = temp;  
      }  
    }  
  }  
}
```

```
        arr[j + 1] = temp;
    }
}
return arr;
}
```

```
let arr = [5, 3, 8, 4, 2];
console.log(bubbleSort(arr)); // Output: [2, 3, 4, 5, 8]
```

◆ 3. When to Use Bubble Sort

Bubble sort is simple to implement but inefficient for large datasets. It is useful for educational purposes and for small datasets or nearly sorted data. However, for larger arrays, more efficient algorithms should be used.

◆ 4. Insertion Sort

How it Works:

Insertion Sort builds the final sorted array one item at a time. It takes each element from the input and finds its correct position in the sorted portion of the array. It is similar to sorting playing cards in your hands.

Steps:

1. Start with the second element (since the first is trivially sorted).
2. Compare it with the elements before it and insert it in the correct position.
3. Repeat for each subsequent element, shifting larger elements to the right to make space for the current element.

Time Complexity:

- **Best Case:** $O(n)$ (if the array is already sorted).

- **Worst Case:** $O(n^2)$ (if the array is in reverse order).

Example: Insertion Sort in JavaScript

javascript

CopyEdit

```
function insertionSort(arr) {
  for (let i = 1; i < arr.length; i++) {
    let current = arr[i];
    let j = i - 1;

    // Shift elements of arr[0..i-1] that are greater than current
    while (j >= 0 && arr[j] > current) {
      arr[j + 1] = arr[j];
      j = j - 1;
    }
    arr[j + 1] = current;
  }
  return arr;
}

let arr = [5, 3, 8, 4, 2];
console.log(insertionSort(arr)); // Output: [2, 3, 4, 5, 8]
```

◆ 5. When to Use Insertion Sort

Insertion Sort is efficient for small datasets or when the array is partially sorted. It is stable, meaning equal elements maintain their relative order. It is widely used in online sorting applications, where elements are continuously added and need to be sorted incrementally.

◆ 6. Merge Sort

How it Works:

Merge Sort is a **divide and conquer** algorithm. It recursively divides the array into halves until each half contains a single element. Then, it merges the halves back together in sorted order.

Steps:

1. Divide the array into two halves.
2. Recursively divide each half until each subarray contains only one element.
3. Merge the subarrays back together in sorted order.

Time Complexity:

- **Best Case:** $O(n \log n)$.
- **Worst Case:** $O(n \log n)$.

Example: Merge Sort in JavaScript

javascript

CopyEdit

```
function mergeSort(arr) {  
  if (arr.length <= 1) return arr;  
  
  const mid = Math.floor(arr.length / 2);  
  const left = mergeSort(arr.slice(0, mid));  
  const right = mergeSort(arr.slice(mid));  
  
  return merge(left, right);  
}  
  
function merge(left, right) {  
  let result = [];  
  let leftIndex = 0;  
  let rightIndex = 0;  
  
  while (leftIndex < left.length && rightIndex < right.length) {  
    if (left[leftIndex] < right[rightIndex]) {  
      result.push(left[leftIndex]);  
      leftIndex++;  
    } else {  
      result.push(right[rightIndex]);  
      rightIndex++;  
    }  
  }  
  return result;  
}
```

```
    }  
  }  
  
  return  
  result.concat(left.slice(leftIndex)).concat(right.slice(rightIndex));  
}  
  
let arr = [5, 3, 8, 4, 2];  
console.log(mergeSort(arr)); // Output: [2, 3, 4, 5, 8]
```

◆ 7. When to Use Merge Sort

Merge Sort is ideal for large datasets, especially when the data is too large to fit into memory. It is stable, and the time complexity is always $O(n \log n)$, making it one of the most efficient algorithms for large arrays.

◆ 8. Quick Sort

How it Works:

Quick Sort is another **divide and conquer** algorithm. It works by selecting a pivot element and partitioning the array into two subarrays—one with elements smaller than the pivot and one with elements greater than the pivot. It then recursively sorts the subarrays.

Steps:

1. Select a pivot element from the array.
2. Partition the array into two subarrays—one with elements smaller than the pivot, the other with elements larger than the pivot.
3. Recursively apply the same process to the subarrays.

Time Complexity:

- **Best Case:** $O(n \log n)$.

- **Worst Case:** $O(n^2)$ (if the pivot is always the smallest or largest element).

Example: Quick Sort in JavaScript

javascript

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```
function quickSort(arr) {
  if (arr.length <= 1) return arr;

  const pivot = arr[arr.length - 1];
  let left = [], right = [];

  for (let i = 0; i < arr.length - 1; i++) {
    if (arr[i] < pivot) left.push(arr[i]);
    else right.push(arr[i]);
  }

  return [...quickSort(left), pivot, ...quickSort(right)];
}

let arr = [5, 3, 8, 4, 2];
console.log(quickSort(arr)); // Output: [2, 3, 4, 5, 8]
```

◆ 9. When to Use Quick Sort

Quick Sort is one of the fastest algorithms for large datasets. It works well in practice for most scenarios and is used in many built-in sorting functions. However, its worst-case time complexity can be $O(n^2)$, so choosing a good pivot is important.

◆ 10. Sorting Algorithm Comparison

Algorithm	Time Complexity	Space Complexity	Use Case
Bubble Sort	$O(n^2)$	$O(1)$	Small datasets, educational purposes

Insertion Sort	$O(n^2)$	$O(1)$	Small datasets, partially sorted data
Merge Sort	$O(n \log n)$	$O(n)$	Large datasets, stable sort
Quick Sort	$O(n \log n)$ (avg)	$O(\log n)$	Large datasets, fast sorting

Practice Tasks

1. Implement **Bubble Sort**, **Insertion Sort**, **Merge Sort**, and **Quick Sort**.
 2. Compare the performance of these algorithms on various datasets (sorted, reverse sorted, random).
 3. Solve problems where sorting is needed, and choose the most efficient sorting algorithm for the scenario.
 4. Modify **Quick Sort** to use the **median** as the pivot to reduce the likelihood of worst-case performance.
-

Summary

Concept	Explanation
Bubble Sort	Simple but inefficient for large datasets ($O(n^2)$).
Insertion Sort	Builds the sorted array incrementally ($O(n^2)$ worst case).
Merge Sort	Efficient ($O(n \log n)$) and stable; uses additional space.
Quick Sort	Fast for large datasets ($O(n \log n)$ on average).



Lecture 14: Greedy Algorithms



Introduction

Greedy algorithms are a class of algorithms that solve optimization problems by making a series of choices, each of which looks the best at the moment. The idea is to make the locally optimal choice at each step with the hope that these local solutions will lead to a globally optimal solution.

Greedy algorithms are often used in problems where the solution can be constructed by choosing the best option available at each step.

In this lecture, we'll explore:

1. **What Greedy Algorithms Are**
 2. **Greedy Choice Property**
 3. **Optimal Substructure**
 4. **Examples of Greedy Algorithms**
-

◆ 1. What is a Greedy Algorithm?

A greedy algorithm is a straightforward approach for solving problems by making decisions that seem to be the best at the moment. These algorithms don't reconsider their choices after they make them, which makes them faster but potentially less accurate compared to other algorithms like Dynamic Programming.

The general steps for applying a greedy algorithm to a problem are:

1. **Choose:** Make the choice that looks the best at the current step.
2. **Check:** Ensure the choice made does not violate any constraints.
3. **Solve:** Move to the next step and repeat the process until you find a solution.

◆ 2. Greedy Choice Property

The Greedy Choice Property states that a globally optimal solution can be arrived at by selecting a local optimum at each stage of the problem. In simpler terms, making the locally optimal choice at each step can lead to the global optimum.

However, not all problems have this property. It's important to analyze whether or not the problem can be solved optimally with a greedy approach.

◆ 3. Optimal Substructure

Optimal Substructure means that an optimal solution to the problem can be constructed from optimal solutions to its subproblems. This property allows us to solve a problem in a bottom-up manner.

Greedy algorithms generally work when the problem has the **optimal substructure** property because, at each step, we solve smaller subproblems that lead us toward the overall solution.

◆ 4. Examples of Greedy Algorithms

Let's go through some well-known examples of problems that can be solved using a greedy approach:

Example 1: Coin Change Problem

Given a set of coin denominations, you need to make a certain amount of change with the fewest number of coins. The greedy strategy is to always pick the largest coin denomination that is smaller than or equal to the remaining amount.

Greedy Approach:

1. Sort the coins in descending order.
2. Start with the largest coin and subtract it from the total.

3. Continue with the remaining amount using the next largest coin, and so on, until the total is reduced to 0.

Example Code (JavaScript):

javascript

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```
function coinChange(coins, amount) {
    coins.sort((a, b) => b - a); // Sort coins in descending order
    let result = [];
    for (let coin of coins) {
        while (amount >= coin) {
            result.push(coin);
            amount -= coin;
        }
    }
    return amount === 0 ? result : "Not possible to make the change";
}

let coins = [1, 5, 10, 25];
let amount = 63;
console.log(coinChange(coins, amount)); // Output: [25, 25, 10, 1, 1, 1]
```

This algorithm works efficiently when the coin denominations are multiples of each other (like 1, 5, 10, 25 cents). However, in cases where denominations are not multiples of each other, this approach might not always give the optimal solution.

Example 2: Activity Selection Problem

In the Activity Selection Problem, you are given a set of activities, each with a start and finish time. Your goal is to select the maximum number of activities that don't overlap.

Greedy Approach:

1. Sort the activities by their finishing times.
2. Start with the first activity and select it.

3. For each subsequent activity, if its start time is greater than or equal to the finish time of the last selected activity, select it.

Example Code (JavaScript):

javascript

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```
function activitySelection(activities) {
    activities.sort((a, b) => a[1] - b[1]); // Sort by finish time
    let selectedActivities = [activities[0]];
    let lastFinishTime = activities[0][1];

    for (let i = 1; i < activities.length; i++) {
        if (activities[i][0] >= lastFinishTime) {
            selectedActivities.push(activities[i]);
            lastFinishTime = activities[i][1];
        }
    }
    return selectedActivities;
}

let activities = [
    [1, 3], [2, 5], [4, 6], [6, 7], [5, 8]
];
console.log(activitySelection(activities));
// Output: [ [ 1, 3 ], [ 4, 6 ], [ 6, 7 ] ]
```

This algorithm efficiently finds the maximum set of non-overlapping activities by always selecting the activity that finishes the earliest.

Example 3: Fractional Knapsack Problem

In the Fractional Knapsack Problem, you are given items with weights and values, and you need to fill a knapsack of a given capacity to maximize the total value. You can take fractions of items.

Greedy Approach:

1. Calculate the value-to-weight ratio for each item.

2. Sort the items based on this ratio in descending order.
3. Take as much of the highest value-to-weight ratio item as possible, and then proceed with the next item.

Example Code (JavaScript):

javascript

CopyEdit

```
function fractionalKnapsack(items, capacity) {
    items.sort((a, b) => (b.value / b.weight) - (a.value / a.weight));
    // Sort by value-to-weight ratio
    let totalValue = 0;

    for (let item of items) {
        if (capacity === 0) break;

        let takeWeight = Math.min(item.weight, capacity);
        totalValue += takeWeight * (item.value / item.weight);
        capacity -= takeWeight;
    }

    return totalValue;
}

let items = [
    { value: 60, weight: 10 },
    { value: 100, weight: 20 },
    { value: 120, weight: 30 }
];
let capacity = 50;
console.log(fractionalKnapsack(items, capacity)); // Output: 240
```

In this example, the algorithm selects items based on the highest value-to-weight ratio, ensuring the maximum value is achieved for the given capacity.

◆ When to Use Greedy Algorithms?

Greedy algorithms work well when:

- The problem exhibits the **greedy choice property** (locally optimal choices lead to a globally optimal solution).
- The problem has **optimal substructure** (a solution to the problem can be constructed from solutions to subproblems).
- The problem can be solved step-by-step with decisions that do not require revisiting previous choices.

Some problems that are naturally suited for greedy algorithms include:

- Activity Selection Problem
 - Huffman Coding
 - Fractional Knapsack Problem
 - Job Scheduling
-

Practice Tasks

1. Implement a greedy algorithm to solve the **Job Sequencing Problem**.
 2. Solve the **Fractional Knapsack Problem** with a set of random items.
 3. Try to solve the **Coin Change Problem** with different coin denominations and evaluate the performance of the greedy approach.
-

Summary

Concept	Explanation
Greedy Algorithm	Makes the best choice at each step with the hope of finding the global optimum.

Greedy Choice Property	Local optimum choices lead to a globally optimal solution.
Optimal Substructure	An optimal solution can be built from optimal solutions to subproblems.
Examples	Coin Change, Activity Selection, Fractional Knapsack.



Lecture 15: Backtracking Algorithms



Introduction

Backtracking is a general algorithmic technique used to solve problems by trying out all possible solutions and discarding those that fail to meet the conditions. It builds up solutions incrementally, step-by-step, and abandons a solution (backtracks) as soon as it determines that the solution is not feasible.

Backtracking is a refined brute-force approach, and it works well for problems where:

- We need to explore all possible configurations.
- We can prune the search space when we know that certain configurations are not promising.

In this lecture, we'll cover:

1. **What is Backtracking?**
 2. **How Backtracking Works**
 3. **Common Backtracking Problems**
 4. **Implementation Example: N-Queens Problem**
 5. **When to Use Backtracking?**
-

◆ 1. What is Backtracking?

Backtracking is a trial-and-error algorithm that seeks to build a solution to a problem incrementally. The basic idea is to start with an empty solution and try to extend it step by step. If a step leads to a solution that does not meet the problem constraints, the algorithm "backtracks" and tries a different option.

A backtracking algorithm generally explores all possible solutions to find the one that satisfies the problem's constraints. If a certain path leads to an invalid solution, it is abandoned, and the algorithm tries a different path.

◆ 2. How Backtracking Works

Backtracking algorithms follow a systematic method to explore all possible solutions:

1. **Choice:** At each step, the algorithm chooses the next step (or decision) to make.
2. **Constraint Checking:** The algorithm checks whether the current step violates any constraints. If it does, it backtracks to try a different solution.
3. **Goal Check:** The algorithm checks if it has found a valid solution. If yes, it terminates.
4. **Backtrack:** If a partial solution does not lead to a valid solution, the algorithm backtracks to the previous step and tries another option.

This process continues until all possible solutions have been explored, or the algorithm finds the optimal solution.

◆ 3. Common Backtracking Problems

Some common problems that are solved using backtracking include:

1. **N-Queens Problem:** Place N queens on an N×N chessboard such that no two queens threaten each other.
2. **Sudoku Solver:** Solve a partially filled 9x9 grid where the goal is to fill in the grid with digits while adhering to Sudoku rules.
3. **Subset Sum Problem:** Find subsets of a set that add up to a specific sum.
4. **Permutations and Combinations:** Generate all possible permutations or combinations of a given set of items.
5. **Maze Solving:** Find a path through a maze from start to end by trying all possible paths.

◆ 4. Example: N-Queens Problem

The N-Queens problem is a classic example of backtracking. The challenge is to place N queens on an N×N chessboard such that no two queens threaten each other. A queen can attack another queen if they share the same row, column, or diagonal.

Greedy Approach:

1. Start with an empty N×N chessboard.
2. Place a queen in the first column of the first row.
3. Move to the next row, and place a queen in a column where it doesn't conflict with other queens.
4. Continue placing queens row by row.
5. If a queen cannot be placed on any column in the current row without attacking another queen, backtrack to the previous row and move the queen to the next column.

Example Code (JavaScript):

javascript

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```
function solveNQueens(N) {
  let board = Array(N).fill().map(() => Array(N).fill(false));
  let solutions = [];

  function isSafe(row, col) {
    // Check column
    for (let i = 0; i < row; i++) {
      if (board[i][col]) return false;
    }

    // Check diagonal (upper left)
    for (let i = row - 1, j = col - 1; i >= 0 && j >= 0; i--, j--) {
      if (board[i][j]) return false;
    }

    // Check diagonal (upper right)
```

```

    for (let i = row - 1, j = col + 1; i >= 0 && j < N; i--, j++) {
        if (board[i][j]) return false;
    }

    return true;
}

function solve(row) {
    if (row === N) {
        let solution = board.map(r => r.map(c => (c ? 'Q' :
'.'))).join('');
        solutions.push(solution);
        return;
    }

    for (let col = 0; col < N; col++) {
        if (isSafe(row, col)) {
            board[row][col] = true;
            solve(row + 1);
            board[row][col] = false; // Backtrack
        }
    }
}

solve(0);
return solutions;
}

let N = 4;
console.log(solveNQueens(N));

```

Explanation of the Code:

- The `isSafe` function checks if a queen can be placed at the current position (`row`, `col`) by ensuring it doesn't conflict with previously placed queens in the same column or diagonals.

- The `solve` function attempts to place queens row by row, backtracking when it encounters an invalid position.
- The `solveNQueens` function returns all possible solutions by exploring all possibilities recursively.

For $N = 4$, the output will show all possible ways to place the queens on a 4×4 chessboard without any conflicts.

◆ 5. When to Use Backtracking?

Backtracking is suitable for solving problems where:

- The solution space is large, but you can eliminate large sections of it by using constraints.
- You need to explore all possible configurations.
- The solution must satisfy certain conditions, and backtracking helps prune invalid paths early.

It is most effective when the problem is inherently recursive, and each solution can be constructed step-by-step.

Example Use Cases:

- **Combinatorial problems:** Where we need to generate all combinations or permutations of elements.
 - **Optimization problems:** Where we need to find the best solution among many possible solutions.
 - **Puzzles and games:** Solving puzzles like Sudoku, crosswords, and maze-solving.
-

Practice Tasks

1. Implement a backtracking algorithm to solve the **Sudoku Solver** problem.
 2. Solve the **Subset Sum Problem** using backtracking to find subsets that sum up to a given target.
 3. Try implementing the **Permutations and Combinations** problem using backtracking to generate all possible permutations and combinations of a given set.
-

Summary

Concept	Explanation
Backtracking	A trial-and-error technique that explores all possible solutions by incrementally building a solution and backtracking when a constraint is violated.
Recursive Exploration	Backtracking problems are solved recursively by exploring all possible configurations.
Common Problems	N-Queens, Sudoku Solver, Subset Sum, Permutations, Maze Solving.
Optimal for	Combinatorial and optimization problems that require exploring all possibilities while pruning invalid ones.

Lecture 16: Trees (Binary Trees and Binary Search Trees)

Introduction

A tree is a hierarchical data structure consisting of nodes connected by edges. It is a non-linear structure where each node has a value and is connected to other nodes in a parent-child relationship. Trees are essential in many applications, such as representing hierarchical structures (like file systems), building efficient search algorithms, and more.

In this lecture, we'll cover:

What is a Tree?

Types of Trees: Binary Tree and Binary Search Tree

Binary Tree Traversals

Implementation of Binary Tree

Binary Search Tree (BST)

Common Operations on Binary Trees and BSTs

♦ 1. What is a Tree?

A tree is a collection of nodes connected by edges, where:

The root is the topmost node in the tree.

Parent-child relationships exist between nodes.

Each node has zero or more children and exactly one parent (except for the root node, which has no parent).

A leaf node is a node with no children.

Basic Terminology:

Root: The starting node of the tree.

Node: A structure that holds data and references to child nodes.

Edge: A connection between two nodes.

Height of the tree: The length of the longest path from the root to a leaf.

Depth of a node: The number of edges from the root to that node.

♦ 2. Types of Trees: Binary Tree and Binary Search Tree (BST)

Binary Tree:

A binary tree is a tree in which each node has at most two children: a left child and a right child. The tree is organized in a way that allows efficient searching, insertion, and deletion of data.

Properties:

Each node has at most two children.

No order is imposed on the nodes. There is no requirement for values in the left or right subtrees to be smaller or larger.

Example:

markdown

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```
      1
     / \
    2   3
   /\  /\
  4 5 6
```

Binary Search Tree (BST):

A Binary Search Tree (BST) is a binary tree with the following additional properties:

For every node, the value of the left subtree is less than the value of the node.

The value of the right subtree is greater than the value of the node.

This ordering property makes searching for a node more efficient compared to a regular binary tree.

Example:

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```
      8
     / \
    3   10
   /\   \
  1 6   14
 /\  /\
4 7 13
```

♦ 3. Binary Tree Traversals

Traversal refers to the process of visiting all the nodes in a specific order. There are three primary types of tree traversals:

1. Preorder Traversal (Root, Left, Right):
Visit the root node.

Recursively traverse the left subtree.

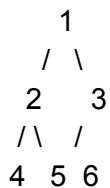
Recursively traverse the right subtree.

Example: For the tree:

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Preorder Traversal: 1, 2, 4, 5, 3, 6

2. Inorder Traversal (Left, Root, Right):
Recursively traverse the left subtree.

Visit the root node.

Recursively traverse the right subtree.

Example:

Inorder Traversal: 4, 2, 5, 1, 3, 6

3. Postorder Traversal (Left, Right, Root):
Recursively traverse the left subtree.

Recursively traverse the right subtree.

Visit the root node.

Example:

Postorder Traversal: 4, 5, 2, 6, 3, 1

♦ 4. Implementation of Binary Tree

To implement a binary tree in JavaScript, we need to define a Node class and a BinaryTree class.

Node Class:

The Node class contains:

A value (data).

Left and right child nodes.

javascript

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```
class Node {  
  constructor(value) {  
    this.value = value;  
    this.left = null;  
    this.right = null;  
  }  
}
```

Binary Tree Class:

The BinaryTree class manages the tree and provides methods for traversal.

javascript

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```
class BinaryTree {  
  constructor(rootValue) {  
    this.root = new Node(rootValue);  
  }  
  
  preorderTraversal(node = this.root) {  
    if (node === null) return;  
    console.log(node.value);  
    this.preorderTraversal(node.left);  
    this.preorderTraversal(node.right);  
  }  
  
  inorderTraversal(node = this.root) {  
    if (node === null) return;  
    this.inorderTraversal(node.left);  
    console.log(node.value);  
    this.inorderTraversal(node.right);  
  }  
  
  postorderTraversal(node = this.root) {  
    if (node === null) return;  
    this.postorderTraversal(node.left);
```

```

        this.postorderTraversal(node.right);
        console.log(node.value);
    }
}

```

```

let tree = new BinaryTree(1);
tree.root.left = new Node(2);
tree.root.right = new Node(3);
tree.root.left.left = new Node(4);
tree.root.left.right = new Node(5);

```

```

console.log("Preorder Traversal:");
tree.preorderTraversal(); // 1, 2, 4, 5, 3

```

```

console.log("Inorder Traversal:");
tree.inorderTraversal(); // 4, 2, 5, 1, 3

```

```

console.log("Postorder Traversal:");
tree.postorderTraversal(); // 4, 5, 2, 3, 1

```

♦ 5. Binary Search Tree (BST)

In a Binary Search Tree (BST), the key property is that for any node:

All values in the left subtree are less than the node's value.

All values in the right subtree are greater than the node's value.

Operations on BST:

Insert: Insert a new node while maintaining the BST property.

Search: Search for a node based on the BST property.

Delete: Delete a node while maintaining the BST property.

Example: Inserting into a BST

javascript

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```

class BinarySearchTree {
    constructor() {
        this.root = null;
    }

```

```

    insert(value) {
        let newNode = new Node(value);

```

```

    if (this.root === null) {
      this.root = newNode;
    } else {
      this._insertNode(this.root, newNode);
    }
  }
}

```

```

_insertNode(node, newNode) {
  if (newNode.value < node.value) {
    if (node.left === null) {
      node.left = newNode;
    } else {
      this._insertNode(node.left, newNode);
    }
  } else {
    if (node.right === null) {
      node.right = newNode;
    } else {
      this._insertNode(node.right, newNode);
    }
  }
}

```

```

search(value) {
  return this._searchNode(this.root, value);
}

```

```

_searchNode(node, value) {
  if (node === null) return null;
  if (value < node.value) return this._searchNode(node.left, value);
  if (value > node.value) return this._searchNode(node.right, value);
  return node;
}

```

```

let bst = new BinarySearchTree();
bst.insert(8);
bst.insert(3);
bst.insert(10);
bst.insert(1);
bst.insert(6);

```

```

console.log(bst.search(6)); // Node { value: 6, left: null, right: null }

```

◆ 6. Common Operations on Trees and BSTs

Traversal:

Preorder, Inorder, Postorder for binary trees and BSTs.

Insertion:

Insert nodes based on their value in BSTs.

Deletion:

For deleting a node in a BST, there are three cases:

Node has no children: Simply remove the node.

Node has one child: Replace the node with its child.

Node has two children: Find the node's in-order successor (or predecessor) and replace the node with it.

✚ Practice Tasks

Implement the Delete operation for a node in a Binary Search Tree.

Create a function to perform a Level Order Traversal (BFS) of a binary tree.

Implement an algorithm to find the Lowest Common Ancestor (LCA) in a Binary Search Tree.

🧠 Summary

Concept	Explanation
---------	-------------

Binary Tree	A tree where each node has at most two children (left and right).
-------------	---

Binary Search Tree (BST)	A binary tree where the left subtree contains values less than the node and the right subtree contains values greater than the node.
--------------------------	--

Tree Traversals	Preorder, Inorder, Postorder (for exploring nodes in a tree).
-----------------	---

Common Operations	Insertion, Search, Deletion (in BST), and Traversals.
-------------------	---

Lecture 17: Tree Traversals (Inorder, Preorder, Postorder)

Introduction

In **Lecture 16**, we introduced trees, focusing on **Binary Trees** and **Binary Search Trees (BSTs)**. In this lecture, we will explore how to traverse trees. **Tree traversal** refers to the process of visiting each node in a tree in a specific order.

There are three main types of tree traversal:

1. **Preorder Traversal**
2. **Inorder Traversal**
3. **Postorder Traversal**

Each traversal method visits the nodes in a different order, and understanding these different approaches is crucial for solving various problems efficiently.

◆ 1. What is Tree Traversal?

Tree traversal refers to the process of visiting every node in a tree exactly once in a specific order. The order can vary depending on the type of traversal.

Traversing a tree is essential for various operations like searching, sorting, and modifying the tree. In the case of **binary trees**, the traversal types are determined by the sequence in which the root, left, and right children are visited.

Traversal Methods:

- **Preorder Traversal**: Visit root first, then left subtree, then right subtree.
- **Inorder Traversal**: Visit left subtree first, then root, then right subtree.

- **Postorder Traversal:** Visit left subtree first, then right subtree, then root.

These methods are typically used for operations like searching for a specific value, printing the tree in a sorted order (for BSTs), or performing a task at each node.

◆ 2. Preorder Traversal (Root, Left, Right)

Preorder Traversal follows the **Root, Left, Right** order. This means:

1. Visit the root node.
2. Traverse the left subtree (in preorder).
3. Traverse the right subtree (in preorder).

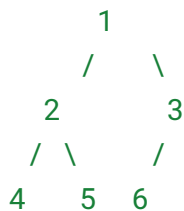
Algorithm:

1. Start at the root node.
2. Visit the node (e.g., print the value).
3. Traverse the left child recursively.
4. Traverse the right child recursively.

Preorder Traversal Example:

Given the following binary tree:

markdown
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The **Preorder Traversal** would be: **1, 2, 4, 5, 3, 6.**

Preorder Implementation:

javascript

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```
class BinaryTree {
  constructor(rootValue) {
    this.root = new Node(rootValue);
  }

  preorderTraversal(node = this.root) {
    if (node === null) return;
    console.log(node.value); // Visit the root
    this.preorderTraversal(node.left); // Traverse left subtree
    this.preorderTraversal(node.right); // Traverse right subtree
  }
}
```

Example:

javascript

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```
let tree = new BinaryTree(1);
tree.root.left = new Node(2);
tree.root.right = new Node(3);
tree.root.left.left = new Node(4);
tree.root.left.right = new Node(5);

console.log("Preorder Traversal:");
tree.preorderTraversal(); // Output: 1, 2, 4, 5, 3
```

◆ 3. Inorder Traversal (Left, Root, Right)

Inorder Traversal follows the **Left, Root, Right** order. This means:

1. Traverse the left subtree.
2. Visit the root node.

3. Traverse the right subtree.

Algorithm:

1. Start at the root node.
2. Traverse the left child recursively.
3. Visit the node (e.g., print the value).
4. Traverse the right child recursively.

Inorder Traversal Example:

Given the same binary tree:

markdown

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The **Inorder Traversal** would be: **4, 2, 5, 1, 3, 6**.

Inorder Implementation:

javascript

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```
class BinaryTree {
  constructor(rootValue) {
    this.root = new Node(rootValue);
  }

  inorderTraversal(node = this.root) {
    if (node === null) return;
    this.inorderTraversal(node.left); // Traverse left subtree
    console.log(node.value); // Visit the root
    this.inorderTraversal(node.right); // Traverse right subtree
  }
}
```

```
}
```

Example:

javascript
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```
let tree = new BinaryTree(1);
tree.root.left = new Node(2);
tree.root.right = new Node(3);
tree.root.left.left = new Node(4);
tree.root.left.right = new Node(5);

console.log("Inorder Traversal:");
tree.inorderTraversal(); // Output: 4, 2, 5, 1, 3
```

In a **Binary Search Tree (BST)**, the inorder traversal yields the values in **sorted order**, which makes it particularly useful for searching or printing the tree in an ordered way.

◆ 4. Postorder Traversal (Left, Right, Root)

Postorder Traversal follows the **Left, Right, Root** order. This means:

1. Traverse the left subtree.
2. Traverse the right subtree.
3. Visit the root node.

Algorithm:

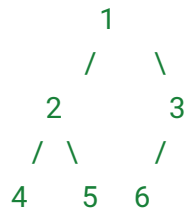
1. Start at the root node.
2. Traverse the left child recursively.
3. Traverse the right child recursively.
4. Visit the node (e.g., print the value).

Postorder Traversal Example:

Given the same binary tree:

markdown

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The **Postorder Traversal** would be: **4, 5, 2, 6, 3, 1**.

Postorder Implementation:

javascript

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```
class BinaryTree {
  constructor(rootValue) {
    this.root = new Node(rootValue);
  }

  postorderTraversal(node = this.root) {
    if (node === null) return;
    this.postorderTraversal(node.left); // Traverse left subtree
    this.postorderTraversal(node.right); // Traverse right subtree
    console.log(node.value); // Visit the root
  }
}
```

Example:

javascript

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```
let tree = new BinaryTree(1);
tree.root.left = new Node(2);
tree.root.right = new Node(3);
tree.root.left.left = new Node(4);
tree.root.left.right = new Node(5);
```

```
console.log("Postorder Traversal:");  
tree.postorderTraversal(); // Output: 4, 5, 2, 6, 3, 1
```

◆ 5. Summary of Tree Traversals

Traversal	Order of Visit	Use Case
Preorder	Root, Left, Right	Used for tree copy or prefix notation.
Inorder	Left, Root, Right	Used for ordered data (BSTs).
Postorder	Left, Right, Root	Used for deleting nodes or post-order processing.

Each traversal serves different purposes in various algorithms, such as searching, sorting, and memory management.

Practice Tasks

1. Implement a function to perform **Level-Order Traversal** (Breadth-First Search).
 2. Modify the tree traversal functions to return the traversal result as an array of node values instead of printing them.
 3. Create a function that counts the number of **leaf nodes** (nodes with no children) in the tree.
-

Summary

- **Preorder Traversal:** Root → Left → Right
- **Inorder Traversal:** Left → Root → Right (commonly used for BSTs to get sorted order)
- **Postorder Traversal:** Left → Right → Root (used for deletion or post-order tasks)

- **Tree Traversals** are crucial for efficient tree operations and help solve various tree-related problems.



Lecture 18: Heaps and Priority Queues



Introduction

In this lecture, we will delve into **Heaps** and **Priority Queues**, two powerful data structures often used in algorithms and system design. Heaps are a type of **binary tree** with special properties, and **Priority Queues** are an abstract data type built on top of heaps. Together, they are used to efficiently manage and retrieve the highest or lowest-priority elements.

♦ 1. What is a Heap?

A **Heap** is a **binary tree** with the following characteristics:

- **Complete Binary Tree**: Every level of the tree is fully filled except possibly the last level, which is filled from left to right.
- **Heap Property**: The value of the parent node must satisfy the heap property:
 - **Max-Heap**: The value of the parent node is greater than or equal to the values of its children.
 - **Min-Heap**: The value of the parent node is less than or equal to the values of its children.

Max-Heap Example:

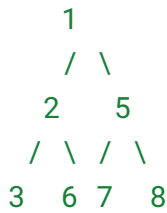
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In this Max-Heap, every parent node is greater than its children.

Min-Heap Example:

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In this Min-Heap, every parent node is smaller than its children.

♦ 2. Operations on Heaps

Heaps support the following primary operations:

1. **Insertion:** Insert a new element into the heap while maintaining the heap property.
2. **Deletion:** Remove the root element (which is either the maximum in a Max-Heap or the minimum in a Min-Heap).
3. **Peek:** Retrieve the root element without removing it (i.e., the maximum or minimum value).
4. **Heapify:** Rearrange the elements in the heap to maintain the heap property. This is done during insertion and deletion.

Insertion in a Heap:

To insert a new element into a heap:

1. Add the element to the bottom of the tree.
2. "Bubble up" or "heapify up" the element to restore the heap property, by comparing it to its parent and swapping if necessary.

Deletion in a Heap:

To delete the root element (the maximum or minimum):

1. Replace the root with the last element in the tree.
 2. "Bubble down" or "heapify down" the new root to restore the heap property by comparing it with its children and swapping if necessary.
-

◆ 3. Priority Queue

A **Priority Queue** is an abstract data type that allows each element to have a **priority**. In a priority queue:

- Elements with higher priority are dequeued before elements with lower priority.
- It can be implemented using a heap, where the root element is always the highest-priority element.

Priority Queue Operations:

1. **Insert**: Insert an element with an associated priority.
2. **Extract Max/Min**: Remove and return the element with the highest or lowest priority (depending on whether it's a Max-Heap or Min-Heap).
3. **Peek**: Retrieve the element with the highest or lowest priority without removing it.

Priority queues are commonly used in algorithms like **Dijkstra's shortest path algorithm**, *A search**, and **Huffman coding**.

◆ 4. Implementation of Heaps in JavaScript

Let's implement a **Max-Heap** in JavaScript to understand how it works.

Max-Heap Class:

javascript

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```
class MaxHeap {  
  constructor() {
```

```

    this.heap = [];
}

// Get the index of the parent node
getParentIndex(index) {
    return Math.floor((index - 1) / 2);
}

// Get the index of the left child
getLeftChildIndex(index) {
    return 2 * index + 1;
}

// Get the index of the right child
getRightChildIndex(index) {
    return 2 * index + 2;
}

// Swap elements at two indices
swap(index1, index2) {
    let temp = this.heap[index1];
    this.heap[index1] = this.heap[index2];
    this.heap[index2] = temp;
}

// Insert a new element into the heap
insert(value) {
    this.heap.push(value);
    this.heapifyUp();
}

// Restore the heap property by moving the new element up
heapifyUp() {
    let index = this.heap.length - 1;

    // Bubble up the new element to its correct position
    while (index > 0 && this.heap[index] >
this.heap[this.getParentIndex(index)]) {

```

```

        this.swap(index, this.getParentIndex(index));
        index = this.getParentIndex(index);
    }
}

// Remove and return the root element (maximum)
extractMax() {
    if (this.heap.length === 0) return null;

    const max = this.heap[0];
    this.heap[0] = this.heap.pop(); // Move the last element to the
root
    this.heapifyDown();
    return max;
}

// Restore the heap property by moving the root element down
heapifyDown() {
    let index = 0;

    while (this.getLeftChildIndex(index) < this.heap.length) {
        let largerChildIndex = this.getLeftChildIndex(index);
        const rightChildIndex = this.getRightChildIndex(index);

        // Find the larger of the two children
        if (rightChildIndex < this.heap.length &&
this.heap[rightChildIndex] > this.heap[largerChildIndex]) {
            largerChildIndex = rightChildIndex;
        }

        // If the current node is greater than or equal to the larger
child, break
        if (this.heap[index] >= this.heap[largerChildIndex]) break;

        // Swap with the larger child
        this.swap(index, largerChildIndex);
        index = largerChildIndex;
    }
}

```

```

    }

    // Peek the root element (maximum)
    peek() {
        return this.heap[0];
    }
}

```

Example Usage:

javascript

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```

const maxHeap = new MaxHeap();

maxHeap.insert(10);
maxHeap.insert(20);
maxHeap.insert(5);
maxHeap.insert(30);
maxHeap.insert(25);

console.log("Max Heap: ", maxHeap.heap); // Output: [30, 25, 10, 5, 20]

console.log("Max Value: ", maxHeap.extractMax()); // Output: 30
console.log("Max Heap After Extract: ", maxHeap.heap); // Output: [25, 20, 10, 5]

```

Heap Operations in Priority Queue:

You can use a Max-Heap or Min-Heap to implement a Priority Queue where:

- **Max-Heap:** The element with the highest priority is dequeued first.
- **Min-Heap:** The element with the lowest priority is dequeued first.

◆ 5. Use Cases of Heaps and Priority Queues

Heap Use Cases:

- **Priority Scheduling:** Operating systems often use heaps to schedule tasks with different priorities.
- **Heap Sort:** A sorting algorithm that uses a heap to sort elements in $O(n \log n)$ time.

Priority Queue Use Cases:

- **Dijkstra's Algorithm:** For finding the shortest path in a graph with weighted edges.
 - **Huffman Coding:** For data compression algorithms.
 - **Task Scheduling:** Managing tasks with different priorities in a system.
-

Practice Tasks

1. Implement a **Min-Heap** class and demonstrate its usage with insertion and extraction.
 2. Create a **Priority Queue** class using a heap, with methods to insert elements with priorities and extract the highest/lowest priority.
 3. Use a heap to implement a **task scheduler** that processes tasks based on priority.
-

Summary

- **Heap:** A special binary tree used to implement priority queues efficiently.
 - **Max-Heap:** The root is the largest element.
 - **Min-Heap:** The root is the smallest element.
- **Priority Queue:** An abstract data type that manages elements with priorities.
- **Operations:** Insert, Extract (Max/Min), Peek, Heapify (Up and Down).

Lecture 19: Graphs (Adjacency List, Matrix)

Introduction

In this lecture, we will explore **Graphs**, one of the most versatile and essential data structures. Graphs are used to represent relationships between objects, and they can be used in many real-world applications such as social networks, routing algorithms, and web page link structures. We'll cover two main ways of representing graphs in memory: **Adjacency Lists** and **Adjacency Matrices**.

◆ 1. What is a Graph?

A **graph** is a collection of **nodes** (also called **vertices**) and **edges** (connections between nodes). Graphs can be:

- **Directed**: The edges have a direction (from one node to another).
- **Undirected**: The edges do not have a direction (the connection is bidirectional).
- **Weighted**: The edges have a weight or cost associated with them.
- **Unweighted**: The edges do not have any weight or cost.

Example:

Consider a graph with nodes **A**, **B**, **C**, and **D** with edges connecting them as follows:

less

CopyEdit

```
A --- B
|     |
C --- D
```

This is an **undirected** graph with **4 nodes** and **4 edges**.

◆ 2. Graph Representation

Graphs can be represented in two primary ways:

1. Adjacency List

An **adjacency list** is a collection of **lists** or **arrays** where each node points to a list of its neighboring nodes. It's the most common and space-efficient way to represent a graph, especially for sparse graphs (graphs with fewer edges).

Example:

For the graph above:

less

CopyEdit

```
A --- B
  |   |
  C --- D
```

The adjacency list representation would look like this:

javascript

CopyEdit

```
const graph = {
  A: ['B', 'C'],
  B: ['A', 'D'],
  C: ['A', 'D'],
  D: ['B', 'C']
};
```

Here, each node (A, B, C, D) is a key, and the value is an array of its neighboring nodes.

Advantages of Adjacency List:

- Space-efficient for sparse graphs, as it only stores edges that exist.

- Insertion and deletion of nodes and edges are fast.

Disadvantages:

- Not as efficient for dense graphs (graphs with many edges), as it may require searching through many neighbors.

2. Adjacency Matrix

An **adjacency matrix** is a **2D array** where each cell (i, j) represents an edge from node i to node j . If there is an edge between nodes, the matrix entry will contain a non-zero value (usually **1** for unweighted graphs, or the weight of the edge for weighted graphs).

Example:

For the same graph:

less

CopyEdit

```
A --- B
 |     |
C --- D
```

The adjacency matrix representation would look like this:

javascript

CopyEdit

```
const graph = [
  // A  B  C  D
  [0, 1, 1, 0], // A
  [1, 0, 0, 1], // B
  [1, 0, 0, 1], // C
  [0, 1, 1, 0]  // D
];
```

In this matrix:

- `graph[0][1] = 1` indicates an edge between node **A** and node **B**.

- `graph[2][3] = 1` indicates an edge between node C and node D.

Advantages of Adjacency Matrix:

- Simple to implement and easy to understand.
- Efficient for dense graphs (graphs with many edges).

Disadvantages:

- Requires more space than an adjacency list for sparse graphs.
 - It can be slow to traverse the neighbors of a node, as you have to check all possible edges (even those that don't exist).
-

◆ 3. Time Complexity of Graph Operations

The time complexity of various operations depends on the representation you choose.

Adjacency List Operations:

1. **Accessing all neighbors of a node:** $O(k)$, where k is the number of neighbors (degree of the node).
2. **Checking if there is an edge between two nodes:** $O(k)$, where k is the number of neighbors of the node.
3. **Adding a node:** $O(1)$.
4. **Adding an edge:** $O(1)$.

Adjacency Matrix Operations:

1. **Accessing all neighbors of a node:** $O(n)$, where n is the number of nodes.
2. **Checking if there is an edge between two nodes:** $O(1)$.

3. **Adding a node:** $O(n^2)$, as we need to expand the matrix.
 4. **Adding an edge:** $O(1)$.
-

◆ 4. Graph Traversals

Once you have a graph, you often need to **traverse** it — that is, visit each node at least once. There are two primary ways to traverse a graph:

1. Depth-First Search (DFS)

In **DFS**, you start at a node and explore as far down a branch as possible before backtracking. It can be implemented using either recursion or a stack.

DFS Example (using recursion):

javascript

CopyEdit

```
function dfs(graph, node, visited = new Set()) {
  if (visited.has(node)) return;

  console.log(node); // Process the node
  visited.add(node);

  for (const neighbor of graph[node]) {
    dfs(graph, neighbor, visited);
  }
}
```

2. Breadth-First Search (BFS)

In **BFS**, you start at a node and explore all of its neighbors at the present depth level before moving on to nodes at the next depth level. It can be implemented using a queue.

BFS Example (using a queue):

javascript

CopyEdit

```
function bfs(graph, start) {
  const queue = [start];
```

```
const visited = new Set();

while (queue.length > 0) {
  const node = queue.shift();
  if (!visited.has(node)) {
    console.log(node); // Process the node
    visited.add(node);
    for (const neighbor of graph[node]) {
      queue.push(neighbor);
    }
  }
}
```

◆ 5. Weighted Graphs and Shortest Path Algorithms

Graphs can be **weighted**, meaning that each edge has a cost associated with it. In such cases, you can use algorithms like **Dijkstra's Algorithm** or **Bellman-Ford Algorithm** to find the shortest path between nodes in a weighted graph.

Practice Tasks

1. Implement an **Adjacency Matrix** representation of a graph and write functions to add nodes and edges.
 2. Implement an **Adjacency List** representation and write functions to add nodes and edges.
 3. Write a program to perform **DFS** and **BFS** on a graph and display the order of traversal.
 4. Implement a function to find the **shortest path** in a weighted graph using **Dijkstra's Algorithm**.
-

Summary

- **Graph:** A data structure consisting of nodes (vertices) and edges connecting them. Can be **directed** or **undirected**, and **weighted** or **unweighted**.
- **Adjacency List:** Efficient for sparse graphs, where each node has a list of its neighbors.
- **Adjacency Matrix:** Simple to implement but less efficient for sparse graphs.
- **Graph Traversals:** **DFS** and **BFS** are the most common algorithms for traversing graphs.
- **Weighted Graphs:** Used in applications where edges have costs, and algorithms like **Dijkstra's** are used to find the shortest paths.

Lecture 20: Graph Traversals (DFS, BFS)

Introduction

In this lecture, we will dive into the **Graph Traversal** techniques: **Depth-First Search (DFS)** and **Breadth-First Search (BFS)**. These algorithms are essential for exploring graphs, and understanding them will help in solving graph-related problems like finding paths, detecting cycles, and exploring connectivity.

◆ 1. What is Graph Traversal?

Graph traversal refers to the process of visiting each node in a graph in a systematic way. Traversal is important for tasks such as searching for a specific node, finding the shortest path, or checking if a graph is connected.

Two Common Types of Graph Traversals:

1. **Depth-First Search (DFS)**: Explores as far down a branch as possible before backtracking.
 2. **Breadth-First Search (BFS)**: Explores all nodes at the present depth level before moving on to nodes at the next depth level.
-

◆ 2. Depth-First Search (DFS)

DFS starts at the root node and explores as far down as possible along each branch before backtracking. DFS can be implemented using recursion or a stack.

DFS Characteristics:

- **Uses a stack** (either explicitly or through recursion).

- **Explores deeply:** DFS goes deep into the graph before visiting other neighboring nodes.
- **Recursive or Stack-based:** It can be implemented either using recursion or an explicit stack.

DFS Algorithm:

1. Start from the initial node, mark it as visited.
2. Explore the first unvisited neighbor of the current node.
3. Repeat the process until there are no unvisited neighbors.
4. Backtrack when there are no more unvisited neighbors, and continue the process for other unvisited nodes.

DFS Implementation (using recursion):

javascript

CopyEdit

```
function dfs(graph, node, visited = new Set()) {
  if (visited.has(node)) return;

  console.log(node); // Process the node
  visited.add(node);

  for (const neighbor of graph[node]) {
    dfs(graph, neighbor, visited);
  }
}
```

DFS Example:

For the graph:

less

CopyEdit

```
A --- B
 |     |
C --- D
```

The **DFS traversal** starting from **A** would visit the nodes in the following order: **A, B, D, C**.

◆ 3. Breadth-First Search (BFS)

BFS starts at the root node and explores all the neighboring nodes at the present depth level before moving on to nodes at the next level. BFS is often used to find the **shortest path** in unweighted graphs and is implemented using a **queue**.

BFS Characteristics:

- **Uses a queue** to keep track of nodes to visit next.
- **Explores level by level:** BFS visits all the nodes at the current level before moving to the next level.
- **Shortest Path:** BFS is guaranteed to find the shortest path in an unweighted graph because it explores all possible paths level by level.

BFS Algorithm:

1. Start from the initial node and add it to a queue.
2. Dequeue the front node and visit it.
3. Add all unvisited neighbors of the current node to the queue.
4. Repeat until all nodes have been visited.

BFS Implementation (using a queue):

javascript

CopyEdit

```
function bfs(graph, start) {  
  const queue = [start];  
  const visited = new Set();  
  
  while (queue.length > 0) {  
    const node = queue.shift();
```



```

    if (!visited.has(node)) {
      console.log(node); // Process the node
      visited.add(node);
      for (const neighbor of graph[node]) {
        queue.push(neighbor);
      }
    }
  }
}

```

BFS Example:

For the graph:

less

CopyEdit

```

A --- B
|     |
C --- D

```

The **BFS traversal** starting from **A** would visit the nodes in the following order: **A**, **B**, **C**, **D**.

◆ 4. Time Complexity of DFS and BFS

The time complexity of both **DFS** and **BFS** is **$O(V + E)$** , where:

- **V** is the number of vertices (nodes) in the graph.
- **E** is the number of edges in the graph.

This is because both algorithms visit each node once and explore each edge once.

DFS:

- **Time Complexity:** $O(V + E)$

- **Space Complexity:** $O(V)$ (due to the recursion stack or explicit stack).

BFS:

- **Time Complexity:** $O(V + E)$
 - **Space Complexity:** $O(V)$ (due to the queue used to store nodes).
-

◆ **5. When to Use DFS and BFS?**

DFS:

- Suitable for tasks where you need to explore deep paths in the graph (e.g., solving mazes, finding connected components).
- Works well for searching paths and detecting cycles.
- Can be used in topological sorting and solving puzzles.

BFS:

- Best for finding the shortest path in an unweighted graph (e.g., shortest path between two nodes in a maze).
 - Often used in applications like web crawlers, level-order traversal of trees, and finding connected components in a graph.
-

◆ **6. Practice Tasks**

1. **DFS:** Implement DFS on a graph and print all nodes in the order they are visited.
2. **BFS:** Implement BFS on a graph and print all nodes in the order they are visited.

3. **Shortest Path:** Use BFS to find the shortest path from a starting node to a target node in an unweighted graph.
 4. **Graph Connectivity:** Write a function to check if a graph is connected using DFS or BFS.
 5. **Cycle Detection:** Detect cycles in an undirected graph using DFS or BFS.
-

Summary

- **DFS** (Depth-First Search): Explores deep into the graph using a stack or recursion, backtracking when necessary.
- **BFS** (Breadth-First Search): Explores level by level using a queue, ensuring the shortest path in unweighted graphs.
- Both DFS and BFS have a time complexity of $O(V + E)$, but their space complexities depend on how the graph is represented and the algorithm's implementation.

Lecture 21: Time and Space Complexity (Big O)

Introduction

In this lecture, we will dive into **Time Complexity** and **Space Complexity**, which are crucial for evaluating the efficiency of algorithms. These two concepts are essential for optimizing algorithms, ensuring that they run within acceptable time limits and use an appropriate amount of memory.

◆ 1. What is Time Complexity?

Time Complexity refers to the amount of time an algorithm takes to run as a function of the size of the input. It gives us an estimate of how the execution time of an algorithm increases as the size of the input grows. Time complexity helps us understand the efficiency of an algorithm in terms of its speed.

Why is Time Complexity Important?

- Helps in predicting how well an algorithm will perform with large inputs.
- Helps compare different algorithms for the same problem to choose the most efficient one.

Common Time Complexities:

- **$O(1)$** : Constant time – The algorithm's run time does not depend on the size of the input.
- **$O(\log n)$** : Logarithmic time – The algorithm reduces the size of the input in each step.
- **$O(n)$** : Linear time – The algorithm's run time is directly proportional to the size of the input.

- **$O(n \log n)$** : Log-linear time – The algorithm runs in linear time, but with a logarithmic factor.
 - **$O(n^2)$** : Quadratic time – The algorithm's run time increases with the square of the input size.
 - **$O(2^n)$** : Exponential time – The algorithm's run time doubles with each additional element in the input.
-

◆ 2. Big O Notation

Big O Notation is used to describe the upper bound of an algorithm's running time. It provides an asymptotic analysis, meaning it looks at how the running time grows as the input size increases. Big O notation helps us understand the worst-case scenario for an algorithm.

Big O Notation Examples:

1. **$O(1)$ – Constant Time:**

- The algorithm takes the same amount of time regardless of the input size.
- Example: Accessing an element in an array by index.

javascript

CopyEdit

```
function getFirstElement(arr) {  
    return arr[0]; // Always takes constant time  
}
```

2.

3. **$O(\log n)$ – Logarithmic Time:**

- The algorithm reduces the size of the problem in each step.
- Example: Binary search in a sorted array.

javascript

CopyEdit

```
function binarySearch(arr, target) {
```

```

let left = 0, right = arr.length - 1;
while (left <= right) {
  const mid = Math.floor((left + right) / 2);
  if (arr[mid] === target) return mid;
  else if (arr[mid] < target) left = mid + 1;
  else right = mid - 1;
}
return -1;
}

```

4.

5. **$O(n)$ – Linear Time:**

- The algorithm's run time is proportional to the size of the input.
- Example: Searching for an element in an unsorted array.

javascript

CopyEdit

```

function linearSearch(arr, target) {
  for (let i = 0; i < arr.length; i++) {
    if (arr[i] === target) return i;
  }
  return -1;
}

```

6.

7. **$O(n^2)$ – Quadratic Time:**

- The algorithm's run time grows quadratically with the input size.
- Example: Bubble sort or selection sort.

javascript

CopyEdit

```

function bubbleSort(arr) {
  for (let i = 0; i < arr.length; i++) {
    for (let j = 0; j < arr.length - i - 1; j++) {
      if (arr[j] > arr[j + 1]) {
        let temp = arr[j];

```

```

        arr[j] = arr[j + 1];
        arr[j + 1] = temp;
    }
}
}
}

```

8.

9. **$O(n \log n)$ – Log-Linear Time:**

- The algorithm combines linear and logarithmic behaviors.
- Example: Merge sort, Quick sort.

javascript

CopyEdit

```

function mergeSort(arr) {
    if (arr.length <= 1) return arr;
    const mid = Math.floor(arr.length / 2);
    const left = mergeSort(arr.slice(0, mid));
    const right = mergeSort(arr.slice(mid));
    return merge(left, right);
}

function merge(left, right) {
    let result = [];
    while (left.length && right.length) {
        if (left[0] < right[0]) result.push(left.shift());
        else result.push(right.shift());
    }
    return result.concat(left, right);
}

```

10.

◆ **3. What is Space Complexity?**

Space Complexity refers to the amount of memory an algorithm uses relative to the size of the input. It measures how the memory usage of an algorithm grows as the input size increases.

Why is Space Complexity Important?

- Helps to optimize the memory usage of algorithms, especially in environments with limited memory.
- Determines how efficiently an algorithm uses the computer's available memory.

Common Space Complexities:

- **O(1)**: Constant space – The algorithm uses the same amount of memory, regardless of the input size.
 - **O(n)**: Linear space – The algorithm's memory usage grows proportionally with the input size.
 - **O(n²)**: Quadratic space – The algorithm's memory usage grows quadratically with the input size.
-

◆ 4. Analyzing Time and Space Complexity

Let's take a few examples to understand both time and space complexities:

Example 1: Linear Search

```
javascript
CopyEdit
function linearSearch(arr, target) {
  for (let i = 0; i < arr.length; i++) {
    if (arr[i] === target) return i;
  }
  return -1;
}
```

1.

- **Time Complexity:** $O(n)$ because we may have to check every element in the array.
- **Space Complexity:** $O(1)$ because we only use a few variables (i and $target$) regardless of the array size.

Example 2: Merge Sort

javascript

CopyEdit

```
function mergeSort(arr) {
  if (arr.length <= 1) return arr;
  const mid = Math.floor(arr.length / 2);
  const left = mergeSort(arr.slice(0, mid));
  const right = mergeSort(arr.slice(mid));
  return merge(left, right);
}

function merge(left, right) {
  let result = [];
  while (left.length && right.length) {
    if (left[0] < right[0]) result.push(left.shift());
    else result.push(right.shift());
  }
  return result.concat(left, right);
}
```

2.

- **Time Complexity:** $O(n \log n)$ because the array is repeatedly divided in half ($\log n$), and each merge operation takes linear time (n).
- **Space Complexity:** $O(n)$ because we create additional arrays (`left`, `right`, and `result`), each of size n .

◆ 5. Best, Worst, and Average Case Complexities

- **Best Case:** The minimum number of steps required to complete the algorithm.
- **Worst Case:** The maximum number of steps required.
- **Average Case:** The expected number of steps on average.

For example, with **Bubble Sort**:

- **Best Case:** $O(n)$ (when the array is already sorted).
 - **Worst Case:** $O(n^2)$ (when the array is in reverse order).
 - **Average Case:** $O(n^2)$ (on average, it will take quadratic time to sort).
-

Summary

- **Time Complexity** measures how an algorithm's run time increases with input size, while **Space Complexity** measures how its memory usage increases with input size.
- **Big O Notation** helps describe the upper bound of an algorithm's performance.
- **Common Time Complexities:** $O(1)$, $O(\log n)$, $O(n)$, $O(n \log n)$, $O(n^2)$, $O(2^n)$.
- **Best, Worst, and Average Case** complexities describe the performance of an algorithm in different scenarios.

Lecture 22: Dynamic Programming

Introduction

Introduction

Dynamic Programming (DP) is a powerful technique for solving problems that involve making a sequence of decisions. It is particularly useful when solving problems that can be broken down into overlapping subproblems. Instead of solving each subproblem repeatedly, DP stores the results of subproblems and reuses them, improving efficiency.

In this lecture, we will cover the fundamentals of dynamic programming, understand how it works, and discuss how it can optimize recursive solutions by avoiding redundant calculations.

◆ 1. What is Dynamic Programming?

Dynamic Programming is a method for solving complex problems by breaking them down into simpler subproblems. It is used when the problem has overlapping subproblems (i.e., the same subproblems are solved multiple times) and optimal substructure (i.e., the solution to the overall problem can be constructed from solutions to the subproblems).

Key Characteristics of Dynamic Programming Problems:

- **Overlapping Subproblems:** The problem can be divided into smaller subproblems that are solved multiple times.
 - **Optimal Substructure:** The optimal solution to the problem can be constructed from the optimal solutions to its subproblems.
-

◆ 2. The Two Approaches to Dynamic Programming

Dynamic programming can be implemented in two main ways:

1. Top-Down Approach (Memoization):

In the top-down approach, the problem is solved recursively, but before solving a subproblem, we check whether its solution has already been computed and stored in a table (usually an array or a hash map). If so, we use the stored result, which saves computation time.

Example: Fibonacci Sequence

The Fibonacci sequence is a classic example to demonstrate both recursion and dynamic programming. Without dynamic programming, a recursive solution recalculates the same Fibonacci values multiple times. With memoization, we store the previously computed results to avoid redundant calculations.

Recursive Solution (Top-Down without Memoization):

```
javascript
CopyEdit
function fib(n) {
  if (n <= 1) return n;
  return fib(n - 1) + fib(n - 2);
}
```

Memoized Solution (Top-Down with Memoization):

```
javascript
CopyEdit
function fibMemo(n, memo = {}) {
  if (n <= 1) return n;
  if (memo[n]) return memo[n]; // Check if the value is already
computed
  memo[n] = fibMemo(n - 1, memo) + fibMemo(n - 2, memo); // Store the
result
  return memo[n];
}
```

Here, `memo` stores the results of previous computations, allowing us to avoid recalculating values for previously encountered `n`.

2. Bottom-Up Approach (Tabulation):

In the bottom-up approach, we solve the problem iteratively, starting from the smallest subproblem and gradually solving larger subproblems. We use a table (usually an array) to store

the solutions to subproblems. This approach eliminates the overhead of recursion and often leads to more efficient solutions.

Example: Fibonacci Sequence (Bottom-Up)

javascript

CopyEdit

```
function fibTab(n) {  
  let dp = [0, 1];  
  for (let i = 2; i <= n; i++) {  
    dp[i] = dp[i - 1] + dp[i - 2]; // Build the solution iteratively  
  }  
  return dp[n];  
}
```

In the bottom-up approach, we avoid recursion and use an iterative loop to fill up the table `dp`.

◆ 3. When to Use Dynamic Programming

Dynamic Programming is ideal for problems that have the following characteristics:

- **Optimal Substructure:** The solution to the problem can be constructed from solutions to its subproblems.
- **Overlapping Subproblems:** The problem can be broken down into subproblems that are solved multiple times.

Common Problems Suitable for Dynamic Programming:

- **Fibonacci Sequence:** Classic example to introduce DP.
- **Knapsack Problem:** Given a set of items with weights and values, determine the maximum value that can be carried with a limited weight capacity.
- **Longest Common Subsequence:** Find the longest subsequence that is common to two sequences.
- **Matrix Chain Multiplication:** Determine the most efficient way to multiply a sequence of matrices.

◆ 4. Steps to Solve a Problem Using Dynamic Programming

To solve a problem using dynamic programming, follow these general steps:

1. **Define the State:** Decide the subproblems that need to be solved. Each subproblem represents a state.
2. **Recurrence Relation:** Express the solution to a subproblem in terms of smaller subproblems.
3. **Base Case:** Identify the base case(s), which are the simplest subproblems that can be solved directly.
4. **Compute and Store the Results:** Compute the solutions to all subproblems and store them to avoid redundant work.
5. **Return the Final Solution:** After computing the subproblems, combine them to solve the original problem.

◆ 5. Example: The 0/1 Knapsack Problem

The **Knapsack Problem** is one of the most famous problems that can be solved using dynamic programming. The problem is as follows:

- You are given n items, each with a weight $w[i]$ and a value $v[i]$.
- You are given a knapsack with a maximum weight capacity W .
- The task is to determine the maximum value you can fit into the knapsack without exceeding the weight limit.

Solution Using Dynamic Programming:

Step 1: Define the State

Define $dp[i][w]$ as the maximum value that can be obtained with the first i items and a knapsack capacity of w .

Step 2: Recurrence Relation

For each item, we have two choices:

1. Include the item in the knapsack.
2. Exclude the item from the knapsack.

The recurrence relation is:

- $dp[i][w] = \max(dp[i-1][w], dp[i-1][w-w[i]] + v[i])$

Step 3: Base Case

- $dp[0][w] = 0$ for all w , because no items mean no value.
- $dp[i][0] = 0$ for all i , because a knapsack with zero capacity can carry no items.

Step 4: Compute and Store Results

javascript

CopyEdit

```
function knapsack(weights, values, W) {
  const n = weights.length;
  let dp = Array(n + 1).fill().map(() => Array(W + 1).fill(0));

  for (let i = 1; i <= n; i++) {
    for (let w = 1; w <= W; w++) {
      if (weights[i - 1] <= w) {
        dp[i][w] = Math.max(dp[i - 1][w], dp[i - 1][w - weights[i - 1]] + values[i - 1]);
      } else {
        dp[i][w] = dp[i - 1][w];
      }
    }
  }
}
```

```
    return dp[n][W]; // Maximum value that can be obtained with full
capacity
}
```

Summary

- **Dynamic Programming (DP)** is a technique used for solving problems with overlapping subproblems and optimal substructure by breaking the problem into smaller subproblems and storing their solutions.
- There are two approaches to implementing DP: **Top-Down (Memoization)** and **Bottom-Up (Tabulation)**.
- DP is ideal for problems that require solving the same subproblems multiple times, such as the **Fibonacci Sequence**, **Knapsack Problem**, and **Longest Common Subsequence**.
- The general steps for solving a DP problem include defining the state, formulating the recurrence relation, identifying base cases, and storing computed results to avoid redundant calculations.

Lecture 23: Top DSA Interview Problems (Part 1)

Introduction

In this lecture, we will focus on some of the most common **Data Structures and Algorithms (DSA)** problems that are frequently asked in technical interviews. These problems test a candidate's problem-solving ability and their knowledge of algorithms and data structures. Mastering these problems will significantly increase your chances of success in coding interviews.

We'll break down each problem with a step-by-step approach, helping you understand how to solve them efficiently. These problems will primarily involve topics like arrays, strings, linked lists, searching and sorting, and dynamic programming.

◆ 1. Two Sum Problem

Problem Statement

Given an array of integers `nums` and an integer `target`, return the indices of the two numbers such that they add up to `target`.

Example:

javascript

CopyEdit

Input: `nums = [2, 7, 11, 15], target = 9`

Output: `[0, 1] // because nums[0] + nums[1] == 9`

Solution Approach

We can use a hash map (or dictionary) to keep track of the numbers we've seen so far and their indices. For each number in the array, we check if `target - current_number` exists in the hash map. If it does, we have found the solution.

Time Complexity: $O(n)$
Space Complexity: $O(n)$

Code Example:

javascript

CopyEdit

```
function twoSum(nums, target) {  
    let map = new Map();  
    for (let i = 0; i < nums.length; i++) {  
        let complement = target - nums[i];  
        if (map.has(complement)) {  
            return [map.get(complement), i];  
        }  
        map.set(nums[i], i);  
    }  
    return [];  
}
```

◆ 2. Reverse Linked List

Problem Statement

Given the head of a singly linked list, reverse the list and return its head.

Example:

javascript

CopyEdit

Input: head = [1, 2, 3, 4, 5]

Output: [5, 4, 3, 2, 1]

Solution Approach

We can reverse the linked list iteratively by changing the direction of each node's pointer. At each step, we'll make the current node's next pointer point to the previous node.

Time Complexity: $O(n)$
Space Complexity: $O(1)$

Code Example:

javascript

CopyEdit

```
function reverseList(head) {  
    let prev = null;  
    let curr = head;  
    while (curr !== null) {  
        let nextTemp = curr.next;  
        curr.next = prev;  
        prev = curr;  
        curr = nextTemp;  
    }  
    return prev;  
}
```

◆ 3. Merge Intervals

Problem Statement

Given a collection of intervals, merge all overlapping intervals.

Example:

javascript

CopyEdit

Input: intervals = [[1, 3], [2, 4], [5, 7], [6, 8]]

Output: [[1, 4], [5, 8]]

Solution Approach

1. Sort the intervals based on their starting times.
2. Iterate through the intervals, merging overlapping ones by checking if the current interval's start time is less than or equal to the end time of the previous interval.

Time Complexity: $O(n \log n)$ due to sorting

Space Complexity: $O(n)$

Code Example:

javascript

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```
function merge(intervals) {
    if (intervals.length === 0) return [];

    intervals.sort((a, b) => a[0] - b[0]);
    let result = [intervals[0]];

    for (let i = 1; i < intervals.length; i++) {
        let last = result[result.length - 1];
        let curr = intervals[i];

        if (last[1] >= curr[0]) {
            last[1] = Math.max(last[1], curr[1]);
        } else {
            result.push(curr);
        }
    }

    return result;
}
```

◆ 4. Valid Parentheses

Problem Statement

Given a string containing just the characters '(', ')', '{', '}', '[', and ']', determine if the input string is valid. An input string is valid if:

1. Open brackets must be closed by the same type of brackets.
2. Open brackets must be closed in the correct order.

Example:

javascript

CopyEdit

Input: `s = "([{}])"`

Output: `true`

Solution Approach

Use a stack data structure to keep track of the opening brackets. As we iterate through the string, we push the opening brackets onto the stack. When we encounter a closing bracket, we check if it matches the top of the stack.

Time Complexity: $O(n)$

Space Complexity: $O(n)$

Code Example:

javascript

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```
function isValid(s) {
    let stack = [];
    let map = { '(': ')', '{': '}', '[': ']' };

    for (let char of s) {
        if (map[char]) {
            stack.push(char);
        } else {
            let top = stack.pop();
            if (map[top] !== char) {
                return false;
            }
        }
    }

    return stack.length === 0;
}
```

◆ 5. Longest Substring Without Repeating Characters

Problem Statement

Given a string, find the length of the longest substring without repeating characters.

Example:

javascript

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Input: `s = "abcabcbb"`

Output: `3 // The answer is "abc", with the length of 3.`

Solution Approach

Use the sliding window technique to track the longest substring. We will maintain a window of characters and a set of seen characters. As we slide through the string, we will adjust the window to ensure that all characters in the window are unique.

Time Complexity: $O(n)$

Space Complexity: $O(\min(n, m))$, where `n` is the length of the string and `m` is the size of the character set.

Code Example:

javascript

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```
function lengthOfLongestSubstring(s) {  
    let set = new Set();  
    let left = 0;  
    let maxLength = 0;  
  
    for (let right = 0; right < s.length; right++) {  
        while (set.has(s[right])) {  
            set.delete(s[left]);  
            left++;  
        }  
        set.add(s[right]);  
        maxLength = Math.max(maxLength, right - left + 1);  
    }  
  
    return maxLength;  
}
```

Summary

In this lecture, we covered several common interview problems:

1. **Two Sum Problem:** Using a hash map to efficiently find two numbers that sum up to the target.
2. **Reverse Linked List:** Reversing a singly linked list with an iterative approach.
3. **Merge Intervals:** Merging overlapping intervals using sorting and a greedy approach.
4. **Valid Parentheses:** Using a stack to validate parentheses in a string.
5. **Longest Substring Without Repeating Characters:** Using the sliding window technique to find the longest unique substring.

These problems are essential for preparing for coding interviews, and they involve fundamental data structures like arrays, stacks, and linked lists.

Lecture 24: Top DSA Interview Problems (Part 2)

Introduction

In this lecture, we continue with some more common **Data Structures and Algorithms (DSA)** problems often encountered in technical interviews. These problems require a solid understanding of advanced data structures, graph algorithms, dynamic programming, and more. The goal is to break down these problems, providing you with a comprehensive understanding and a structured approach to solving them.

◆ 1. Find the Missing Number

Problem Statement

Given an array containing n distinct numbers taken from the range $[1, n+1]$, find the one number that is missing from the array.

Example:

javascript

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Input: `nums = [1, 2, 4, 6, 3, 7, 8]`

Output: `5`

Solution Approach

The sum of the first n natural numbers is given by the formula $n * (n + 1) / 2$. We can compute the sum of the numbers from 1 to $n+1$ and subtract the sum of elements in the array. The difference will be the missing number.

Time Complexity: $O(n)$

Space Complexity: $O(1)$

Code Example:

javascript

CopyEdit

```
function findMissingNumber(nums) {  
  let n = nums.length + 1;  
  let total = (n * (n + 1)) / 2;  
  let sum = nums.reduce((acc, num) => acc + num, 0);  
  return total - sum;  
}
```

◆ 2. Climbing Stairs

Problem Statement

You are climbing a staircase. It takes n steps to reach the top. Each time you can either climb 1 or 2 steps. In how many distinct ways can you climb to the top?

Example:

javascript

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Input: $n = 3$

Output: 3 // There are three ways to climb to the top: 1+1+1, 1+2, 2+1

Solution Approach

This is a classic dynamic programming problem. The number of ways to reach the n th step is the sum of the ways to reach the $(n-1)$ th step and the $(n-2)$ th step.

Time Complexity: $O(n)$

Space Complexity: $O(1)$

Code Example:

javascript

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```
function climbStairs(n) {  
  let a = 1, b = 1;  
  for (let i = 2; i <= n; i++) {  
    let temp = a;  
    a = a + b;  
  }
```

```
    b = temp;
  }
  return a;
}
```

◆ 3. Maximum Subarray Sum (Kadane's Algorithm)

Problem Statement

Given an integer array, find the contiguous subarray (containing at least one number) which has the largest sum.

Example:

javascript

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Input: nums = [-2, 1, -3, 4, -1, 2, 1, -5, 4]

Output: 6 // The subarray [4, -1, 2, 1] has the largest sum

Solution Approach

This is a classical problem solved using **Kadane's Algorithm**. The idea is to iterate through the array and compute the maximum subarray sum ending at each index, updating the global maximum.

Time Complexity: $O(n)$

Space Complexity: $O(1)$

Code Example:

javascript

CopyEdit

```
function maxSubArray(nums) {
  let maxSum = nums[0];
  let currentSum = nums[0];

  for (let i = 1; i < nums.length; i++) {
    currentSum = Math.max(nums[i], currentSum + nums[i]);
    maxSum = Math.max(maxSum, currentSum);
  }
}
```

```
    return maxSum;
}
```

◆ 4. Merge k Sorted Lists

Problem Statement

Merge k sorted linked lists into one sorted list and return it.

Example:

javascript

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Input: lists = [[1, 4, 5], [1, 3, 4], [2, 6]]

Output: [1, 1, 2, 3, 4, 4, 5, 6]

Solution Approach

We can use a **min heap** (priority queue) to keep track of the minimum element among the k lists. The heap will allow us to efficiently get the smallest element, and we can then merge the lists by repeatedly extracting the minimum element.

Time Complexity: $O(n \log k)$, where n is the total number of elements across all lists and k is the number of lists.

Space Complexity: $O(k)$

Code Example:

javascript

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```
function mergeKLists(lists) {
    let heap = new MinHeap();

    // Push the first element of each list into the heap
    for (let i = 0; i < lists.length; i++) {
        if (lists[i]) heap.push(lists[i]);
    }
}
```

```
let dummy = new ListNode(0);
let current = dummy;

while (heap.size() > 0) {
    let node = heap.pop();
    current.next = node;
    current = current.next;

    if (node.next) {
        heap.push(node.next);
    }
}

return dummy.next;
}
```

◆ 5. Course Schedule

Problem Statement

There are n courses labeled from 0 to $n-1$, and some courses have prerequisites. You need to determine if you can finish all courses.

Example:

javascript
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Input: numCourses = 2, prerequisites = [[1, 0]]

Output: true // You can finish the courses

Solution Approach

This problem can be solved using **topological sorting** on a directed graph. We will build the graph using the course dependencies and check if there's a cycle. If there is no cycle, it is possible to finish all courses.

Time Complexity: $O(V + E)$, where V is the number of courses and E is the number of prerequisites (edges).

Space Complexity: $O(V + E)$

Code Example:

javascript

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```
function canFinish(numCourses, prerequisites) {
    let graph = Array.from({ length: numCourses }, () => []);
    let visited = Array(numCourses).fill(false);
    let inStack = Array(numCourses).fill(false);

    // Build the graph
    for (let [course, prereq] of prerequisites) {
        graph[course].push(prereq);
    }

    // DFS to detect cycles
    function dfs(course) {
        if (inStack[course]) return false;
        if (visited[course]) return true;

        inStack[course] = true;
        for (let prereq of graph[course]) {
            if (!dfs(prereq)) return false;
        }
        inStack[course] = false;
        visited[course] = true;

        return true;
    }

    // Check all courses
    for (let i = 0; i < numCourses; i++) {
        if (!dfs(i)) return false;
    }

    return true;
}
```

Summary

In this lecture, we continued with more interview problems:

1. **Find the Missing Number:** Using the sum of the first $n+1$ numbers to find the missing number.
2. **Climbing Stairs:** A dynamic programming approach to count distinct ways to reach the top.
3. **Maximum Subarray Sum:** Solving using Kadane's Algorithm to find the maximum subarray sum.
4. **Merge k Sorted Lists:** Using a min heap to merge k sorted linked lists.
5. **Course Schedule:** Detecting cycles in a directed graph to determine if all courses can be finished.

These problems test important algorithmic concepts such as dynamic programming, graph theory, and greedy algorithms. Mastering these will prepare you for technical interviews.



Lecture 25: Tips for Cracking DSA Rounds



Introduction

In this final lecture, we will discuss essential tips and strategies to successfully crack **Data Structures and Algorithms (DSA)** interview rounds. These tips are aimed at helping you not only to solve problems effectively but also to approach interviews with the right mindset.

◆ 1. Focus on Problem-Solving Skills

Before diving deep into any coding round, it's essential to **improve your problem-solving skills**. Here's how you can enhance them:

Understand the Problem Statement

- Read the problem carefully and break it down into smaller chunks.
- Try to visualize the problem. For example, if it's a graph or tree problem, draw the graph or tree on paper.
- Ask clarifying questions to the interviewer if anything is unclear.

Break It Down

- Start with a brute force solution (if applicable). This will help you understand the problem and give you a baseline to optimize.
- Focus on optimizing the brute force solution step by step.
- Use pseudo-code before writing the actual code to structure your thoughts.

Test with Examples

- After you write the initial code, test it with sample inputs and edge cases. This helps you spot flaws and ensures that your solution works across all scenarios.
-

♦ 2. Master Common Data Structures and Algorithms

Most coding interviews revolve around common **DSA problems**. Having a strong understanding of these topics will give you an edge:

Key Data Structures

- Arrays
- Linked Lists (Singly, Doubly)
- Stacks and Queues
- Hash Tables/Maps
- Heaps (Min/Max heaps)
- Trees (Binary Trees, Binary Search Trees)
- Graphs (Adjacency list, Adjacency matrix)

Key Algorithms

- Sorting (Bubble, Merge, Quick sort, etc.)
- Searching (Binary search, Linear search)
- Recursion and Backtracking
- Dynamic Programming (Knapsack, Fibonacci, etc.)
- Greedy Algorithms
- Graph Traversals (BFS, DFS)
- Divide and Conquer

Understand the Time and Space Complexity

- Be able to analyze and optimize the time complexity of your solution.
 - Always try to reduce both time and space complexity during the optimization phase.
-

◆ 3. Solve Problems Regularly

Practice is key to becoming proficient in DSA. Here's how you can do that effectively:

Start with Easy Problems

- Begin by solving easy problems on platforms like **LeetCode**, **HackerRank**, or **CodeSignal**.
- Master basic problems like reversing an array, finding the maximum/minimum in an array, or calculating the factorial of a number.

Gradually Move to Medium/Hard Problems

- Once you are comfortable with easy problems, move on to more complex ones like dynamic programming problems, graph-based problems, or tree traversal problems.
- Focus on improving both your speed and accuracy.

Track Your Progress

- Maintain a journal or a tracker to note down the problems you solved and the ones you found difficult.
 - If you struggle with a problem, try to understand it deeply. Search for alternate approaches or similar problems.
-

◆ 4. Learn and Use the Right Tools

During the interview, knowing the right **tools and techniques** can be a game-changer:

Coding Platforms

- Use **LeetCode**, **HackerRank**, or **GeeksforGeeks** to practice coding problems.
- Focus on **time-limited contests** or mock interviews on platforms like **Pramp** or **interviewing.io**.

Data Structure Libraries

- Familiarize yourself with built-in data structures available in programming languages like **JavaScript**, **Python**, or **Java**. For instance:
 - **JavaScript**: Arrays, Objects, Sets, Maps, LinkedLists
 - **Python**: Lists, Dictionaries, Sets, Queues (using `collections.deque`)
 - **Java**: Arrays, Lists, HashMap, LinkedList, PriorityQueue

Practice Debugging

- Use **print statements** or **console logs** to track variables and flow.
- Debugging tools like **Chrome DevTools** or **Visual Studio Code's Debugger** can be useful to step through your code and identify bugs.

◆ 5. Communicate Clearly

Effective **communication** is an essential part of coding interviews. Here's how to do it:

Explain Your Thought Process

- Start by explaining the problem to your interviewer. This shows that you understand the requirements.
- Outline your approach before jumping into coding. If you start with a brute-force approach, explain that you'll optimize later.

- Once you write the code, walk the interviewer through it, explaining how it works.

Handle Mistakes Gracefully

- If you realize you made a mistake, acknowledge it. Don't panic.
 - **Iterate** on the solution if needed. Interviewers appreciate candidates who can adapt and improve their solution.
-

◆ 6. Be Prepared for Edge Cases

What are Edge Cases?

Edge cases refer to **boundary conditions** or unusual scenarios that might break your code. Some examples include:

- Empty inputs (e.g., an empty array or null value).
- Inputs that are at the maximum or minimum allowed value.
- Large inputs (e.g., large arrays or numbers).
- Invalid inputs (e.g., negative values where only positive numbers are expected).

How to Handle Them?

- Think of potential edge cases before writing the code.
 - When coding, test your solution on multiple edge cases.
 - Make sure to handle exceptions, such as division by zero or null pointer exceptions.
-

◆ 7. Time Management During Interviews

Break Down the Problem Quickly

- Once you understand the problem, start discussing your approach with the interviewer.
- Don't waste time overthinking; start with a brute-force approach and optimize later.

Optimize Gradually

- Start with a working solution. Don't worry if it's not the most optimal at first.
- Once it works, analyze its time complexity, and try to come up with optimizations to make the solution more efficient.

♦ 8. Stay Calm and Confident

- **Confidence** in solving problems is crucial. Even if you encounter a challenge, **stay calm**.
- If you don't know the answer to a question, it's okay. **Ask for clarification** or suggest how you might go about solving the problem.

Summary

To crack DSA rounds successfully, you need a combination of knowledge, problem-solving skills, and strategic thinking. Key points to remember include:

1. **Mastering Data Structures and Algorithms** will help you tackle a wide range of problems.
2. **Regular practice** on coding platforms will improve your efficiency and problem-solving abilities.
3. **Clear communication** during interviews will showcase your problem-solving process.
4. **Handling edge cases** and analyzing time/space complexities is critical for producing optimal solutions.
5. **Stay calm, confident, and handle mistakes gracefully** during interviews.

With consistent practice and a focused approach, you will be ready to crack any DSA-based interview!