

Newton's Laws

First: Momentum stays the same as long as $F_{\text{net}} = 0$.

Second: $F_{\text{net}} = m\vec{a}$.

Third: Every force occurs as one member of an action/reaction pair of forces.

Conservation

Momentum, energy, and angular momentum are conserved for an isolated system. Mass is conserved in normal situations.

Linear Motion

$$d = v_i t + \frac{1}{2} a t^2 \quad v_f = v_i + a t \quad v_f^2 = v_i^2 + 2 a d \quad v_f^2 = v_i^2 + 2 a d$$

$$K = \frac{1}{2} m v^2 \quad \vec{p} = m \vec{v} \quad J_x = \int_{t_i}^{t_f} F_x(t) dt$$

Springs

$$\text{Hooke's law: } (F_{sp})_s = -k \Delta s \quad U_s = \frac{1}{2} k (\Delta s)^2$$

Rotational Motion

$$\omega_f = \omega_i + \alpha \Delta t \quad \theta_f = \theta_i + \omega_i \Delta t + \frac{1}{2} \alpha (\Delta t)^2 \quad \omega_f^2 = \omega_i^2 + 2 \alpha \Delta \theta$$

$$a_{\text{tangential}} = \alpha r \quad a_{\text{centripetal}} = v^2 / r = \omega^2 r \quad x_{\text{cm}} = \frac{1}{M} \int x dm$$

$$I = \sum_i m_i r_i^2 \quad I = \int r^2 dm$$

$$K_{\text{rot}} = \frac{1}{2} I \omega^2 \quad E_{\text{mech}} = K_{\text{rot}} + U_g = \frac{1}{2} I \omega^2 + M g y_{\text{cm}}$$

$$\text{parallel axis theorem: } I = I_{\text{cm}} + M d^2 \quad \tau \equiv r F \sin \phi \quad \alpha = \frac{\tau_{\text{net}}}{I}$$

$$v_{\text{cm}} = R \omega \quad K_{\text{rolling}} = K_{\text{rot}} + K_{\text{cm}} \quad \vec{\tau} = \vec{r} \times \vec{F} \quad \vec{L} = \vec{r} \times \vec{p}$$

$$d\vec{L}/dt = \vec{\tau}_{\text{net}} \quad \vec{L} = I \vec{\omega}$$

Planets

$$F_{1\text{on}2} = F_{2\text{on}1} = \frac{G m_1 m_2}{r^2} \quad \text{Satellite Speed: } v = \sqrt{\frac{GM}{r}}$$

$$\text{Escape Velocity: } v = \sqrt{\frac{2GM}{r}} \quad \text{On Surface: } g = \frac{GM}{R_L^2}$$

$$U_g = \frac{G m_1 m_2}{r} \quad \text{Kepler's 3rd: } T^2 = \left(\frac{4\pi^2}{GM} \right) r^3$$

$$\text{Kepler's 2nd: } \frac{\Delta A}{\Delta t} = \frac{L}{2m}$$

Simple Harmonic/Circular Motion

Uniform circular motion projected onto one dimension is simple harmonic motion.

Any system with a linear restoring force will undergo simple harmonic motion around the equilibrium position.

$$x(t) = A \cos(\omega t + \phi_0) \quad v_x(t) = -\omega A \sin(\omega t + \phi_0)$$

$$\text{pendulum: } \omega = 2\pi f = \sqrt{\frac{g}{L}}$$

$$\text{damped oscillator: } x(t) = A e^{-bt/2m} \cos(\omega t + \phi_0)$$

$$\text{time constant: } \tau = m/b$$

$$\text{damped system: } E = E_0 e^{-t/\tau}$$

Fluids and Elasticity

Archimedes' principle: The magnitude of the buoyant force equals the weight of the fluid displaced by the object.

Ideal-fluid model: Incompressible. Smooth, laminar flow. Non-viscous.

Bernoulli's is a statement of energy conservation.

$$p = F/A \quad p_g = p - 1 \quad \rho = m/V$$

$$v_1 A_1 = v_2 A_2 \quad \text{Bernoulli's: } p_1 + \frac{1}{2} \rho g y_1 = p_2 + \frac{1}{2} \rho v_2^2 + \rho g y_2$$

$$(F/A) = Y(\Delta L/L) \quad p = -B(\Delta V/V)$$

Matter

Phases: solid, liquid gas. Ideal-gas model. Isochoric process $\rightarrow V$ constant and $W=0$, Isobaric $\rightarrow p=\text{constant}$, Isothermal $\rightarrow T$ constant and $\Delta E_{th} = 0$, Adiabatic $\rightarrow Q=0$. conduction, convection, radiation, evaporation.

Second law: entropy cannot decrease.

$$\text{Ideal Gas Law: } pV = nRT$$

$$\text{First Law of Thermo: } \Delta E_{th} = W + Q \quad W = - \int_{V_i}^{V_f} p dV$$

$$\text{specific heat: } Q = Mc\Delta T \quad \epsilon_{\text{avg}} = \frac{3}{2} k_B T \quad p = \frac{2}{3} \frac{N}{V} \epsilon_{\text{avg}}$$

Waves

Transverse, Longitudinal. Snapshot graph, history graph. Superposition, nodes, and antinodes.

$$v = \lambda f \quad \omega = vk \quad D(x, t) = A \sin(kx - \omega t + \phi_0) \quad I = P/a \quad I \propto A^2$$

$$\text{Doppler: } f_{\pm} = \frac{f_0}{1 \mp v_s/v} \quad \text{Doppler: } f_{\pm} = 1 \pm \frac{v_o}{v} f_0$$

Double slit. angles of bright fringes: $\theta_m = m \frac{\lambda}{d}$ where $m = 0, 1, 2, \dots$, d is slit spacing. $I_{\text{double}} = 4I_1 \cos^2 \frac{\pi d}{\lambda L} y$.

Diffraction grating: angles of bright fringes: $d \sin \theta_m = m\lambda$, $m = 0, 1, 2, \dots$

Single slit: angles of dark fringes $\theta_p = p \frac{\lambda}{a}$, $p = 1, 2, 3, \dots$

$$\text{Circular aperture: } w = 2y_1 = 2L \tan \theta_1 \approx \frac{2.44 \lambda L}{D}$$

New

$$\text{de broglie: } \lambda = \frac{h}{p} = \frac{h}{mv} \quad E_n = n^2 \frac{h^2}{8mL^2}, \quad n = 1, 2, 3, \dots$$

$$\text{snells: } n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$$

Base SI Units length: m, mass: kg, time: s, current: A(ampere),
temp: K, amount: mol, luminous intensity: cd(candela)

Symbols

	Name	Units
A	area	m^2
	amplitude	
a	acceleration	m/s^2
	area	
\vec{B}	magnetic field 1	1 tesla = 1 T \equiv 1 N/A m (flux density)
b	damping constant	kg/s
C	capacitance	1 farad = 1 F \equiv 1 C/V
c	speed of light	299,792,458 m/s
	specific heat	J / kg K
d	distance	m
\vec{E}	electric field	1 N/C = 1 V/m
E	energy	1 joule = 1 J = 1 kg m ² /s ²
e	various	2.71828... , electron, elem. charge.
F	force	1 N = 1 kg m/s ²
f	frequency	frequency (1 Hz = 1/s)
	various	function, friction (N)
G	gravity constant	$6.674 * 10^{-11}$ N m ² /kg ²
g	accel. d.t. gravity	m/s ²
\vec{H}	magnetic field 2	A/m (field strength)
h	height	m
h	planck's constant	$6.626 * 10^{-34}$ J s
\hbar	reduced planck's	$h/2\pi$
I	intensity	W/m ²
	electric current	1 ampere = 1 A = 1 C/s
	mmnt. of inertia	kg m ² – “rotational mass”
i	imaginary unit	$\sqrt{-1}$
\hat{i}	x-axis unit vec	also \hat{j} , \hat{k} for y and z axes
J	impulse	kg m/s – equiv to ΔP
K	kinetic energy	J
k_B	boltzmann const.	$1.381 * 10^{-23}$ J/K = R/N_A
	wave number	rad/m – “spacial freq. of wave”
	spring constant	J/m ²
L	inductance	1 henry = 1 H \equiv 1 Wb/A = 1 T m ² /A
	ang. momentum	kg m ² /s
l	length	m
m	mass	kg
N	various	normal vector, atomic number
N_A	avogadro's num	$6.02 * 10^{23}$ 1/mol
n	ind. of refraction	unitless – n = c/v
	quantum number	$n = 1, 2, 3, \dots$, parameterizes quantum energy state for particle
\vec{p}	momentum	kg m/s – $\vec{p} \equiv m\vec{v}$
p	pressure	1 pascal = 1 Pa \equiv 1 N/m ²
Q	heat	1 joule = 1 J = 0.2389 cal

q	elect. charge	1 coulumb = 1 C = 1 A s – (q or Q)
R	elect. resistance	1 ohm = 1 Ω = 1 V/A
	gas constant	8.314 J/mol K
r	radius	m
S	entropy	
S	entropy	
s	arc length	m
	position	m
T	period	s
	abs. temperature	1 kelvin = 1 K = $T_C + 273$
t	time	s
U	potential energy	1 joule = 1 J
u	atomic mass unit	1 u = $1.66 * 10^{-27}$ kg
V	voltage	1 volt = 1 V = 1 J/C
	volume	m ³
\vec{v}	velocity	m/s
W	work	1 N m = 1 kg m ² /s ² = 1 J
w	width	m
x	displacement	m
Z	elec. impedance	1 ohm = 1 Ω
α	ang. accel	rad/s ²
Δ	change in var.	used to signify change i.e. Δx
ϵ	permittivity	F/m = $\epsilon_r \epsilon_0$
ϵ_0	vac. permittivity	$8.854 * 10^{-12}$ F/m
θ	angle	rad
λ	wavelength	m
μ	mag. moment	A m ²
μ	coeff. friction	unitless
μ	permeability	H/m = N/A ² – $\mu = \mu_0 \mu_r$
μ_0	perm const.	$r\pi * 10^{-7}$ T m/A
π	π	3.14159...
ρ	mass density	kg/m ³ — $\rho = m/V$
	resistivity	Ω m — $\rho = 1/\sigma$
σ	conductivity	1/ Ω m
τ	torque	N m — $\tau = \vec{r} \times \vec{F}$
	time constant	different for circuits, oscillations, etc. . .
	2π	6.28319. . .
Φ	field strength	units vary dep. on context
Φ_m	magnetic flux	1 weber = 1 Wb = 1 T m ²
ϕ	phase	radians — operand to sinusoidal fn.
ψ	wave function	unitless, represents q.m. state
Ω	elec. resistance	1 ohm = 1 Ω = 1 V/A
ω	ang. velocity	rad/s

$$F \rightarrow N = \frac{kg \ m}{s^2} \qquad F \rightarrow N = \frac{kgm}{s^2} \qquad F \rightarrow N = \frac{kgm}{s^2}$$

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Miscellaneous

$\vec{A} \times \vec{B} \equiv AB \sin \alpha$, in the direction given by right-hand rule