

Design Analysis of BSU

Problem 1: Determine the beginning - of - life kilowatt hour storage required in a BEV battery pack based on the following requirements : eight years of operation, an average of 18 km of driving per day S_{day} over the 365 days of the year, daily charging, and an average battery output energy per kilometer E_{km} = 180 Wh/km.

Assume L > 1 and N_{100%} = 1000. Assume two parallel battery strings with 96 Li-ion cells per string, with a total number of cells N_{cell} = 192, and a nominal voltage of 3.75 V per cell. Determine the ampere-hours per cell. What are the vehicle range at BOL and EOL?

Solution:

given values

$$S_{\text{day}} = 18 \text{ km}$$

$$E_{\text{km}} = 180 \text{ Wh/km}$$

$$N_{\text{cell}} = 192$$

$$V_{\text{nominal}} = 3.75$$

$$N_{100\%} = 1000, L = 1$$

Calculation

$$\text{No. of cycles } (N) = 365 \times 8 = 2920$$

Average daily output energy (E_{day}) :

$$E_{\text{day}} = S_{\text{day}} \cdot E_{\text{km}}$$

$$= 18 \times 180 = 8640 \text{ Wh}$$

$$E_{\text{day}} = 8640 \text{ Wh}$$

$$\text{DOD} = \left(\frac{N_{100\%}}{N} \right)^{\frac{1}{2}} \times 100\%$$

$$= \left(\frac{4000}{2920} \right)^{\frac{1}{2}} \times 100\% = 34.246\%$$

$$\boxed{\text{DOD} = 34.25\%}$$

$$E_{BOL} = \frac{E_{day}}{\text{DOD}} = \frac{8.64 \text{ kWh}}{0.3425} = 25.226 \text{ kWh}$$

$$\boxed{E_{BOL} = 25.23 \text{ kWh}}$$

$$E_{EOL} = 0.8 \times E_{BOL} = 0.8 \times 25.23 = 20.18 \text{ kWh}$$

$$\boxed{E_{EOL} = 20.18 \text{ kWh}}$$

→ Battery pack voltage (V_{bp}) :

$$V_{bp} = \frac{N_{cell}}{\text{No. of 11el strings}} \times V_n = \frac{192}{2} \times 3.75 = 360 \text{ V}$$

$$\boxed{V_{bp} = 360 \text{ V}}$$

$$Ah_{bp} = \frac{25.23 \times 10^3}{360} = 70.08 \text{ Ah}$$

$$\text{Cell Ah} = Ah_{cell} = \frac{70.08}{\text{No. of 11el String}} = \frac{70.08}{2} = 35.04 \text{ Ah}$$

$$\boxed{Ah_{cell} = 35.04 \text{ Ah}}$$

$$\text{Range BOL} = \frac{E_{BOL}}{E_{km}} = \frac{25.23 \times 10^3}{180} = \boxed{140.2 \text{ km}}$$

$$\text{Range EOL} = \frac{E_{EOL}}{E_{km}} = \frac{20.18 \times 10^3}{180} = \boxed{112.1 \text{ km}}$$

(3)

Problem - 2 : A 24 kWh battery pack can be fast charged from 0% to 80% SOC in 30 min. Determine the approximate charge current and power in order to achieve this charge time.

Solutron :-

24 kWh → given when the Battery is fully charged

$$\therefore 100\% \rightarrow 24 \text{ kWh}$$

$$80\% \rightarrow 24 \times \frac{80}{100} = 19.2 \text{ kWh}$$

$$\text{SOC} \rightarrow 30 \text{ min}$$

0 to 80% → 30 mins are taken

Power = Energy / Time

$$P = \frac{19.2 \text{ kWh} \times 60}{30 \text{ min}} = 38.4 \text{ kW}$$

$$P = 38.4 \text{ kW}$$

If the nominal battery pack voltage is 360V

the approximate charge current = I

$$I = \frac{P}{V}$$

$$I = \frac{38.4 \times 10^3}{360} = 106.67 \text{ A}$$

$$I \approx 107 \text{ A}$$

Problem - 3 : A battery has 96 cells in series with two parallel strings. Each cell has a no-load voltage of 9.18 V and an internal resistance of $2.8 \text{ m}\Omega$.

- Determine the back current and voltage under a 80 kW discharge if the battery is fully charged.
- Determine the discharge efficiency of the battery.

Solution :-

Concept used :-

<u>Current</u>	$+ve \rightarrow$ discharging
	$-ve \rightarrow$ charging

<u>Power</u>	$+ve \rightarrow$ discharging
	$-ve \rightarrow$ charging

Formula Used :-

Current & Voltage

$$\rightarrow I_b = \frac{V_{b(\text{mV})} - \sqrt{V_{b(\text{mV})}^2 - 4 R_b (+P_b)}}{2 R_b} \quad (\text{discharging}) \rightarrow +ve$$

$$\rightarrow I_b = \frac{V_{b(\text{mV})} - \sqrt{V_{b(\text{mV})}^2 - 4 R_b (-P_b)}}{2 R_b} \quad (\text{charging}) \rightarrow -ve$$

$$\rightarrow V_b = V_{b(\text{mV})} - R_b I_b$$

given values

$$N_{\text{series}} = 96$$

$$R_b = 2.8 \text{ m}\Omega = 0.0028 \Omega$$

$$N_{\text{parallel}} = 2$$

$$P_b = +80 \text{ kW}$$

$$V_{b(\text{mV})} = 9.18 \text{ V}$$

$$\text{For 96 cells in series} \rightarrow V_{b(\text{mV})} = 96 \times 9.18 = 901.28 \text{ V}$$

$$\text{iiy } R_b' = 96 \times 2.8 \text{ m}\Omega = 268.8 \text{ m}\Omega$$

$$\text{For two 11th strings - } R_b = \frac{268.8 \times 268.8}{2 \times 268.8} = 134.4$$

$$R_b = 134.4 \text{ m}\Omega$$

Calculating R_b by using formula

$$\boxed{\frac{N_{\text{series}}}{N_{\text{parallel}}} \times R_b}$$

$$\frac{96}{2} \times 2.8 = 134.4 \text{ m}\Omega$$

i) Pack current

$$I_b = \frac{404.28 - \sqrt{404.28^2 - 4 \times 134.4 \times 10^{-3} (80 \times 10^3)}}{2 \times 134.4 \times 10^{-3}}$$

$$= 244.81 \text{ A}$$

$$\boxed{I_b = 244.81 \text{ A}}$$

Voltage

$$V_b = V_{b(\text{max})} - R_b I_b$$

$$= 404.28 - 134.4 \times 10^{-3} \times 244.81$$

$$= 372.4 \text{ V}$$

$$\boxed{V_b = 372.4 \text{ V}}$$

ii) Discharge efficiency

$$\eta_{\text{dis}} = \frac{V_b}{V_{b(\text{max})}} \times 100 = \frac{372.4}{404.28} \times 100 = 92.8\%$$

$$\boxed{\eta_{\text{dis}} = 92.8\%}$$

Problem-4: Determine the pack current and voltage under a 50 kw charge if the battery is fully discharged. The cell voltage drop of 2.5 v when fully discharged. How efficient is the charging of the battery at this power level?

given Values

$$N_{\text{series}} = 96 \quad [\text{Same as } 7^{\text{th}} \text{ Problem}]$$

$$N_{\text{parallel}} = 2$$

$$R_b = 2.8 \text{ m}\Omega$$

$$V_{b(\text{nd})} = 2.5 \text{ V}$$

$$P_b = -50 \text{ kw (charge)}$$

For 96 cells in series and two cells in parallel

$$V_{b(\text{nd})} = 96 \times 2.5 = 240 \text{ V}$$

$$R_b = 134.4 \text{ m}\Omega$$

Formula Used

$$I_b = \frac{V_{b(\text{nd})} - \sqrt{V_{b(\text{nd})}^2 - 4 \times R_b \times (-P_b)}}{2 R_b}$$

$$V_b = V_{b(\text{nd})} - R_b I_b$$

$$\eta_{\text{charging}} = \frac{V_b}{V_{b(\text{nd})}} \times 100$$

Calculations

$$I_b = \frac{240 - \sqrt{240^2 - 4 \times 134.4 \text{ m}\Omega \times (-50 \text{ kw})}}{2 \times 134.4 \times 10^{-3}}$$

$$I_b = -188.49 \text{ A}$$

$$V_b = 210 - (134.4 \times 10^{-3}) (-188.49)$$

$$V_b = 265.32 \text{ V}$$

Charging efficiency

$$\eta_{\text{charging}} = \frac{240}{265.32} \times 100 = 90.5\%$$

$$\eta_{\text{ch}} = 90.5\%$$

Problem-5: The capacity of the cell is approximately 33.3 Ah at C/3 with a rated voltage of 3.75 V. Assume R = 2.8 mΩ. Summarize the following parameters for C/3, 1C and 3C.

Parameters	C/3	1C	3C
χ	1/3	1	3
V	3.75	3.69	3.5
Ah	33.3	33.3	33.3
Wh	124.88	122.8	116.6
Efficiency	99.2	97.5	92.6

Solution :-

given values :- Ah_{rated} = 33.3 Ah

C_{rated} = C/3

$$I_{\text{rated}} = \frac{33 \cdot 3}{3} = 11.1 \text{ A}$$

$$V_{\text{rated}} = 3.75 \text{ V}$$

$$R = 2.8 \text{ m}\Omega = 0.0028 \Omega$$

To calculate : η , V , Ah, wh, Efficiency
for $C/3$, 1C & 3C.

Formula Used

$$1) E_{\text{cell}} = Ah_{\text{rated}} \cdot V_{\text{rated}} + R_b \cdot I_{\text{rated}}^2 \cdot \frac{h}{\text{rated}}$$

$$2) E_{\text{xc}} \approx E_{\text{cell}} - R_b I_{\text{xc}}^2 \cdot \frac{h}{x} \text{ (wh)}$$

$$3) V_{\text{xc}} \approx V_{\text{rated}} - R_b (I_{\text{xc}} - I_{\text{rated}})$$

$$4) \eta_{\text{dis}} = \frac{E_{\text{xc}}}{E_{\text{cell}}} (\%) , \eta_{\text{chang}} = \frac{E_{\text{cell}}}{E_{\text{xc}}} (\%)$$

Calculations

For $C/3$

$$x = \frac{1}{3}$$

$$I_{\text{xc}} = I_{\text{rated}} = 11.1 \text{ A}$$

$$Ah = 33 \cdot 3$$

$$V_{\text{xc}} \approx V_{\text{rated}} = 3.75 \text{ V}$$

$$E_{\text{cell}} = Ah_{\text{rated}} \cdot V_{\text{rated}} + R_b \cdot I_{\text{rated}}^2 \cdot \frac{h}{\text{rated}}$$

$$= \left(33 \cdot 3 \times 3.75 + 0.0028 \times 11.1^2 \times \frac{1}{3} \right) \text{ wh}$$

$$= (33 \cdot 3 \times 3.75 + 0.0028 \times 11.1^2 \times 3) \text{ wh}$$

$$E_{cell} = 125.91 \text{ Wh}$$

$$E_{xc} = E_{cell} - R_b \cdot I_{xc}^2 \cdot \frac{h}{x}$$

$$= (125.91 - 0.0028 \times 11.1^2 \times 3) \text{ Wh}$$

$$E_{xc} = 124.88 \text{ Wh}$$

$$\eta_{dis} = \frac{E_{xc}}{E_{cell}} \times 100 = \frac{124.88}{125.91} \times 100$$

$$\eta_{dis} = 99.18\% = 99.2\%$$

Now, we have

$$x = \frac{1}{3}, V = 3.75V, Ah = 33.3, \text{ Wh} = 124.88$$

$$\eta = 99.2\%$$

For I_{xc}

$$x = 1$$

$$Ah = 33.3$$

$$I_{xc} = 33.3 \text{ A} \quad (33.3 \times 1)$$

$$V_{xc} = V_{rated} - R_b (I_{xc} - I_{rated})$$

$$= 3.75 - 0.0028 (33.3 - 11.1)$$

$$3.687 \text{ V}$$

$$V_{xc} = 3.69 \text{ V}$$

$$E_{cell} = 125.91 \text{ Wh} (\text{Same as } \frac{1}{3})$$

$$\begin{aligned} E_{xc} &= E_{cell} - R_b \cdot I_{xc}^2 \cdot \frac{n}{x} \\ &= (125.91 - 0.0028 \times 33.3^2 \times \frac{1}{1}) \text{ Wh} \end{aligned}$$

$$E_{xc} = 122.8 \text{ Wh}$$

$$\eta_{du} = \frac{122.8}{125.91} \times 100 = 97.5\%$$

$$\eta = 97.5\%$$

Now, we have

$$x = 1, V = 3.69V, Ah = 33.3, \text{Wh} = 122.8, \eta = 97.5\%$$

For 3C

$$x_6 = 3$$

$$Ah = 33.3$$

$$I_{xc} = 33.3 \times 3 = 99.9 A$$

$$V_{xc} = V_{rated} - R_b (I_{xc} - I_{rated})$$

$$= 3.75 - 0.0028 (99.9 - 33.3)$$

$$= 3.50$$

$$V_{xc} = 3.5V$$

$$E_{cell} = 125.91 \text{ Wh} \quad (\text{Same as } S_3)$$

$$E_{xc} = E_{cell} - R_b \cdot I_{xc}^2 \cdot \frac{n}{x}$$

$$E_{xc} = \left(125.91 - 0.0028 \times 99.9^2 \times \frac{1}{3} \right) \text{ Wh}$$

$$= 446.59 \text{ Wh}$$

$$E_{xc} = 446.6 \text{ Wh}$$

$$\eta_{dus} = \frac{446.6}{125.91} \times 100 = 92.6\%$$

$$\eta = 92.6\%$$

Now, we have

$$x = 3, V = 3.5 \text{ V}, Ah = 33.3, \text{ Wh} = 446.6, \eta = 92.6\%$$

Problem - 6: An EV battery has a 100% SOC of 85 kWh. The battery can be charged at high power when the battery DOD is maintained within a range of 20% to 100%. The pack has 96 cells in series per string with 74 parallel strings. Each cell has an average no-load cell voltage during charge of 3.64V and an internal resistance of 65 mΩ.

- i) Determine the battery terminal voltage, current, and efficiency for a 120 kW charge.
- ii) What approximate time is required to charge the battery from a DOD of 100% to 20%?

Solution

Given values :- $N_{\text{series}} = 96$

$$N_{\text{parallel}} = 74$$

$$V_{b(\text{avg})} = 3.64 \text{ V}$$

$$R_b = 65 \text{ m}\Omega = 0.065 \Omega$$

$$P_b = -120 \text{ kW} \quad (\text{charging})$$

For 96 cells in series & 74 cells in parallel

$$V_{b(\text{m.v})} = 96 \times 3.64 = 349.5 \text{ V}$$

$$\underline{V_{b(\text{m.v})} = 349.5 \text{ V}}$$

$$R_b = \frac{N_{\text{series}}}{N_{\text{parallel}}} \times R$$

$$= \frac{96}{74} \times 65 = 84.32 \text{ m}\Omega$$

$$R_b = 0.08432 \Omega$$

To calculate

(i) V_b , I_b , η_{charging}

Calculation of I_b

$$\text{As, we know } I_b = \frac{V_{b(\text{m.v})} - \sqrt{V_{b(\text{m.v})}^2 - 4 R_b (-P_b)}}{2 R_b}$$

$$I_b = \frac{349.5 - \sqrt{349.5^2 - 4 \times 84.32 \times 10^{-3} (-120 \times 10^3)}}{2 R_b}$$

$$= -318.9 \text{ A}$$

$$I_b = -318.9 \text{ A}$$

Calculation of V_b

$$\text{As, we have } V_b = V_{b(\text{m.v})} - R_b I_b$$

$$= 349.5 - (0.08432) \times (-318.9)$$

$$= 376.38 \text{ V}$$

$$V_b = 376.38 \text{ V}$$

$$\eta_{\text{charging}} = \frac{V_b(\text{mV})}{V_b} \times 100 = \frac{349.5}{376.38} \times 100$$

$$\eta_{\text{ch}} = 92.85\%$$

(ii) DOD \rightarrow 100% to 20%

100% \rightarrow 85 kWh till 20%

$$85 \text{ kWh} \times \frac{20}{100} = 17 \text{ kWh}$$

17 kWh \rightarrow tapping the energy from the battery

$$\text{Remaining} \rightarrow (85 - 17) \text{ kWh} = 68 \text{ kWh}$$

68 kWh \rightarrow we are consuming

$$= \frac{68 \text{ kWh}}{120 \text{ kW}} = \frac{68}{120} \text{ h} = \frac{68 \times 60}{120} \text{ min} \\ = 34 \text{ min}$$

$T = 34 \text{ mins}$ \rightarrow approximate time as required to charge the battery

Problem - 7: A lithium cell is rated at 3.6V, 3.9Ah at 0.2C and has an internal resistance of 65 m Ω . Determine the cell wh, Ah, and efficiency for the 1C rate.

Solution

given values :-

$$V_{\text{rated}} = 3.6 \text{ V}$$

$$A_{\text{hrated}} = 3.4$$

$$R_b = 65 \text{ m}\Omega = 0.065 \Omega$$

$$I_{\text{rated}} = 34 \times 0.2 = 0.68 \text{ A}$$

$$C_{\text{rated}} = 0.2 \text{ C}$$

To find :- cell wh, Ah & η

Calculations

For 4C rate

$$\chi = 4$$

$$\boxed{Ah = 3.4}$$

$$I_{xc} = 3.4 \times 4 = 13.6 \text{ A}$$

As we have

$$E_{\text{cell}} = A_{\text{hrated}} \cdot V_{\text{rated}} + R_b \cdot I_{\text{rated}}^2 \cdot \frac{h}{C_{\text{rated}}}$$

$$= \left(3.4 \times 3.6 + 0.065 \times 0.68^2 \times \frac{1}{0.2} \right) \text{ Wh}$$

$$E_{\text{cell}} = 12.4 \text{ Wh}$$

$$E_{xc} = E_{\text{cell}} - R_b \cdot I_{xc}^2 \cdot \frac{h}{\chi}$$

$$= \left(12.4 - 0.065 \times 13.6^2 \times \frac{1}{4} \right) \text{ Wh}$$

$$\boxed{E_{xc} = 9.39 \text{ Wh}}$$

$$\eta = \frac{9.39}{12.4} \times 100 = 75.7\%$$

$$\boxed{\eta = 75.7\%}$$

Problem - 8: A BEV has the following requirements: eight years of operation at an average of 21,000 km per year, averaged out over 365 days per year.

Assume an average battery output of 201 wh/km and a rated cell voltage of 3.6 V, a capacity of 3.1 Ah, and a lifetime index of $L=1$.

- i) Determine the BOL kWh storage.
- ii) How many cells do you need and what is the BOL range.
- iii) What is the BOL storage and how many cells are required for a larger pack in order to increase the BOL range to 425 km?
- iv) How many parallel strings are required if the pack has 96 cells in series?
- v) What is the battery pack mass, assuming a battery with a pack density of 150 wh/kg?
- vi) If the peak power is 325 kW, what is the P/E ratio of the battery for the larger pack?

Solution :-

given values : $V_{\text{rated}} = 3.6 \text{ V}$

$$E_{\text{km}} = 201 \text{ wh/km}$$

$$Ah_{\text{cell}} = 3.1 \text{ Ah}$$

$$L = 1$$

$$\text{Time} = 8 \text{ years}$$

Calculation

- i) The average daily battery output energy.

$$E_{\text{daily}} = S_{\text{daily}} \times E_{\text{km}}$$

$$S_{\text{daily}} = \frac{21000}{365}$$

$$E_{\text{daily}} = \frac{24000}{365} \times 204 \text{ wh}$$

$$= 13413.7 \text{ wh}$$

$$E_{\text{daily}} = 13.4137 \text{ kWh}$$

We have

$$E_{\text{BOL}} = \frac{E_{\text{daily}}}{\text{DOD}}$$

$$\text{DOD} = \left(\frac{N_{100\%}}{N} \right)^{\frac{1}{2}} \times 100\%$$

$$\text{Let } N_{100\%} = 1000, N = 365 \times 8 = 2920$$

$$\text{DOD} = \left(\frac{1000}{2920} \right)^{\frac{1}{2}} \times 100\% = 34.2\%$$

$$\text{DOD} = 0.342465$$

$$E_{\text{BOL}} = \frac{13.4137}{0.342465} = 39.16 \text{ kWh}$$

$$E_{\text{BOL}} = 39.16 \text{ kWh}$$

ii) The cell Ah = 3.4 = $\frac{E_{\text{BOL}}}{V_{bp}}$

Assume that the no. of storing = 1

V_{bp} = battery pack voltage

$$V_{bp} = \frac{E_{\text{BOL}}}{3.4} = \frac{39.16 \times 10^3}{3.4}$$

$$V_{bp} = 11537.64 \text{ V}$$

Also, we have $V_{bp} = N_{cell} \times 3.6$

$$\therefore N_{cell} = \frac{V_{bp}}{3.6} = \frac{44517.647}{3.6} = 3199.346$$

$$N_{cell} \approx 3199.346 \approx 3200$$

$$N_{cell} \approx 3200$$

$$\text{BOL range} = \frac{E_{BOL}}{E_{km}} = \frac{39.46 \times 10^3}{204} = 191.96 \text{ km} \\ \approx 192 \text{ km}$$

$$\text{BOL range} = 192 \text{ km}$$

iii) If BOL range increased to 425 km

then $\frac{E_{BOL}}{E_{km}} = 425 \text{ km}$

$$E_{BOL} = 425 \text{ km} \times 204 \text{ Wh/km} \\ = 86700 \text{ Wh}$$

$$E_{BOL} = 86.7 \text{ kWh}$$

$$\text{No. of cells required} = \frac{E_{BOL}}{A h_{cell} \times V_{cell}}$$

$$= \frac{86.7 \times 10^3}{3.4 \times 3.6}$$

$$= 1083.33$$

$$N_{cell} = 1083$$

iv) Let the no. of parallel strings be N

→ The battery pack voltage (V_{bp}) = $N_{series} \times V_{cell}$

$$V_{bp} = 96 \times 3.6 \quad [\text{given } N_{series} = 96] \\ = 345.6 \text{ V}$$

$$\boxed{V_{bp} = 345.6 \text{ V}}$$

→ The battery pack Ah = $\frac{E_{B01}}{V_{bp}} = Ah_{bp}$

$$Ah_{bp} = \frac{86.7 \times 10^3}{345.6} = 250.86$$

$$\boxed{Ah_{bp} = 250.86 \text{ Ah}}$$

→ The cell Ah (Ah_{cell}) = $\frac{Ah_{bp}}{N}$

$$\frac{Ah_{bp}}{N} = 3.1 \text{ Ah}$$

$$N = \frac{250.86 \text{ Ah}}{3.1 \text{ Ah}} = 73.78$$

$$\boxed{N = 74}$$

v) Battery pack mass (M_{bp}) = $\frac{E_{B01}}{\text{Pack density}}$

$$M_{bp} = \frac{86.7 \times 10^3}{150} = 578 \text{ kg}$$

$$\boxed{M_{bp} = 578 \text{ kg}}$$

vi)

given

$$P = 325 \text{ kW}$$

$$E = 86.7 \text{ kWh} \quad (\text{above calculated})$$

$$\frac{P}{E} = \frac{325}{86.7} = 3.7$$

$$\boxed{P/E = 3.7}$$

Problem - 9: A NiMH HEV battery pack is sized based on the following requirements: 10,000 cycles of 100wh per year for 10 years, a 6.5 Ah cell with a rated voltage of 4.2v and an index of $L = 1.5$.

- what is the BOL battery pack energy storage?
- What is the total number of cells required?
- What is the pack voltage if the cells are all in series?
- If the peak power is 30 kW, what is the P/E ratio of the battery?

Solution :

given values : $N = 10,000$

$$E_{\text{cycle}} = 100 \text{ wh/cycles}$$

$$V_{\text{cell}} = V_{\text{rated}} = 4.2 \text{ V}$$

$$A_{\text{cell}} = 6.5 \text{ Ah}$$

$$L = 1.5$$

Calculation

$$\text{i) No. of cycles per day} = \frac{10,000}{365 \times 10} = 2.739$$

$$E_{\text{day}} = S_{\text{cycle}} \times E_{\text{cycle}} \quad [S_{\text{cycle}} = 2.739]$$

$$E_{day} = 2.739 \times 100 = 273.9 \text{ Wh}$$

$$E_{day} = 273.9 \text{ Wh}$$

Assume $N_{100\%} = 1000$

$$DOD = \left(\frac{N_{100\%}}{N} \right)^{\frac{1}{2}} \times 100\%.$$

$$= \left(\frac{1000}{10,000} \right)^{1/2} \times 100\%.$$

$$DOD = 21.54\%$$

$$E_{BOL} = \frac{E_{day}}{DOD} = \frac{273.9 \text{ Wh}}{0.21} = 1304.2 \text{ Wh}$$

$$E_{BOL} = 1.3 \text{ kWh}$$

$$\text{ii) No. of cell required} = \frac{E_{BOL}}{A_{cell} \times V_{cell}} \quad (\text{Assume no. of strings} = 1)$$

$$= \frac{4.3 \times 10^3}{6.5 \times 1.2} = 166.67$$

$$\text{No. of cells} \approx 167$$

$$\text{i) Pack voltage } (V_{Pack}) = 166 \times 1.2 = 199.2 \text{ V}$$

$$V_{Pack} = 199.2 \text{ V}$$

$$\text{iv) } P = 30 \text{ kW (given)} \quad \text{, } \Sigma = 1.3 \text{ kWh (above cal.)}$$

$$\frac{P}{\Sigma} = \frac{30}{1.3} = 23.07$$

$$\frac{P}{\Sigma} = 23$$

Sizing the EVs drive System

Problem - 1 : 1250 cc capacity of IC engine car having 14 inches of wheel diameter. It can run the maximum speed of 240 kmph with 190 Nm. If it is modified as battery operated vehicle. What is the required motor sizing (BHP) and also estimate the number of batteries to run 8 hrs continuously while driving consistently 60 kmph. Each battery has the rating of 100 Ah for 240V DC.

Solution :-

given values:

$$V = 240 \text{ km/h}$$

$$\text{Diameter} = 14 \text{ inches}$$

$$T = 190 \text{ Nm}$$

$$\text{Time} = 8 \text{ hrs}$$

$$\text{Ahrating} = 100 \text{ for } 240\text{V DC}$$

To calculate : No. of batteries

Calculation :

$$\text{Km/h} \longrightarrow \text{rpm}$$

$$\text{Km/h} = \text{Diameter} \times \text{rpm} \times 1.885 \times 10^{-3}$$

$$1 \text{ inch} = 2.54 \text{ cm}$$

$$\text{rpm} = \frac{\text{Km/h}}{\text{Diameter} \times 1.885 \times 10^{-3}}$$

$$\text{Diameter} = 14 \times 2.54 \text{ cm} = 35.56 \text{ cm}$$

$$\text{rpm} = \frac{240 \text{ km/h}}{35.56 \text{ cm} \times 1.885 \times 10^{-3}}$$

$$3580.15$$

$$N = 3580.15 \text{ rpm}$$

Calculation of Power

$$P = \frac{2\pi NT}{60} \text{ (kW)}$$

$$P = \frac{2\pi \times 3580 \cdot 45 \times 190}{60}$$

$$P = 71.24 \text{ kW}$$

$$P(\text{HP}) = \frac{71.24 \times 10^3}{746} = 95.49$$

$$\boxed{P(\text{HP}) = 95.5 \text{ HP}}$$

Ah rating

$$\text{kWh} \rightarrow 71.24 \times 8 = 569.92 \text{ kWh}$$

570 units

$$\frac{570 \times 10^3 \text{ Wh}}{240 \text{ V}} = \boxed{2375 \text{ Ah}}$$

Number of batteries required to run 8 h

$$= \frac{2375 \text{ Ah}}{100 \text{ Ah}} = 23.75 = 24$$

24 batteries ✓

Problem - 2: Design a medium duty electric vehicle to run 60 kmph with 50 Nm. It should run at least 5 hrs continuously while the wheel diameter of 10 inches. (Ah rating, Motor sizing, suitable motor, power converter circuit for regeneration and power devices rating).

Solution :-

Given values :-

$$V = 60 \text{ km/h}$$

$$T = 50 \text{ Nm}$$

$$\text{Time} = 5 \text{ hrs}$$

$$\text{Diameter} = 10 \text{ inches}$$

$$\text{Assume } V = 240 \text{ V}$$

Calculation

$$\text{Diameter} = 10 \times 2.54 \text{ cm}$$

$$= 25.4 \text{ cm}$$

$$\omega_{\text{pm}} = \frac{60 \text{ km/h}}{10 \times 2.54 \times 1.885 \times 10^{-3}}$$

$$= 1253.16 \text{ rpm}$$

$$N = 1253.16 \text{ rpm}$$

$$P = \frac{2\pi NT}{60}$$

$$= \frac{2\pi \times 1253.16 \times 50}{60} \text{ kW}$$

$$= 6.56 \text{ kW}$$

$$P(\text{HP}) = \frac{6.56 \times 10^3}{746} = 8.79 \text{ HP}$$

$$P = 8.8 \text{ HP}$$

$$\text{KWh} \rightarrow 6.56 \times 5 = 32.8 \text{ KWh}$$

$$\text{Ah} \rightarrow \frac{32.8 \times 10^3}{290} = 136.67 \text{ Ah}$$

$$\boxed{\text{Ah rating} = 136.67 \text{ Ah}}$$

Motor sizing

→ In this case 6.56 kW is the requirement of the mechanical power equivalent to electric power. So, Motor rating has to accept this much maximum power so that our design should be 1.25 to 1.5 times higher than this. One

$$6.56 \times 1.25 = 8.2 \text{ kW}$$

(or)

$$6.56 \times 1.5 = 9.84 \text{ kW}$$

Range of Motor sizing = $(8.2 \rightarrow 9.84) \text{ kW}$

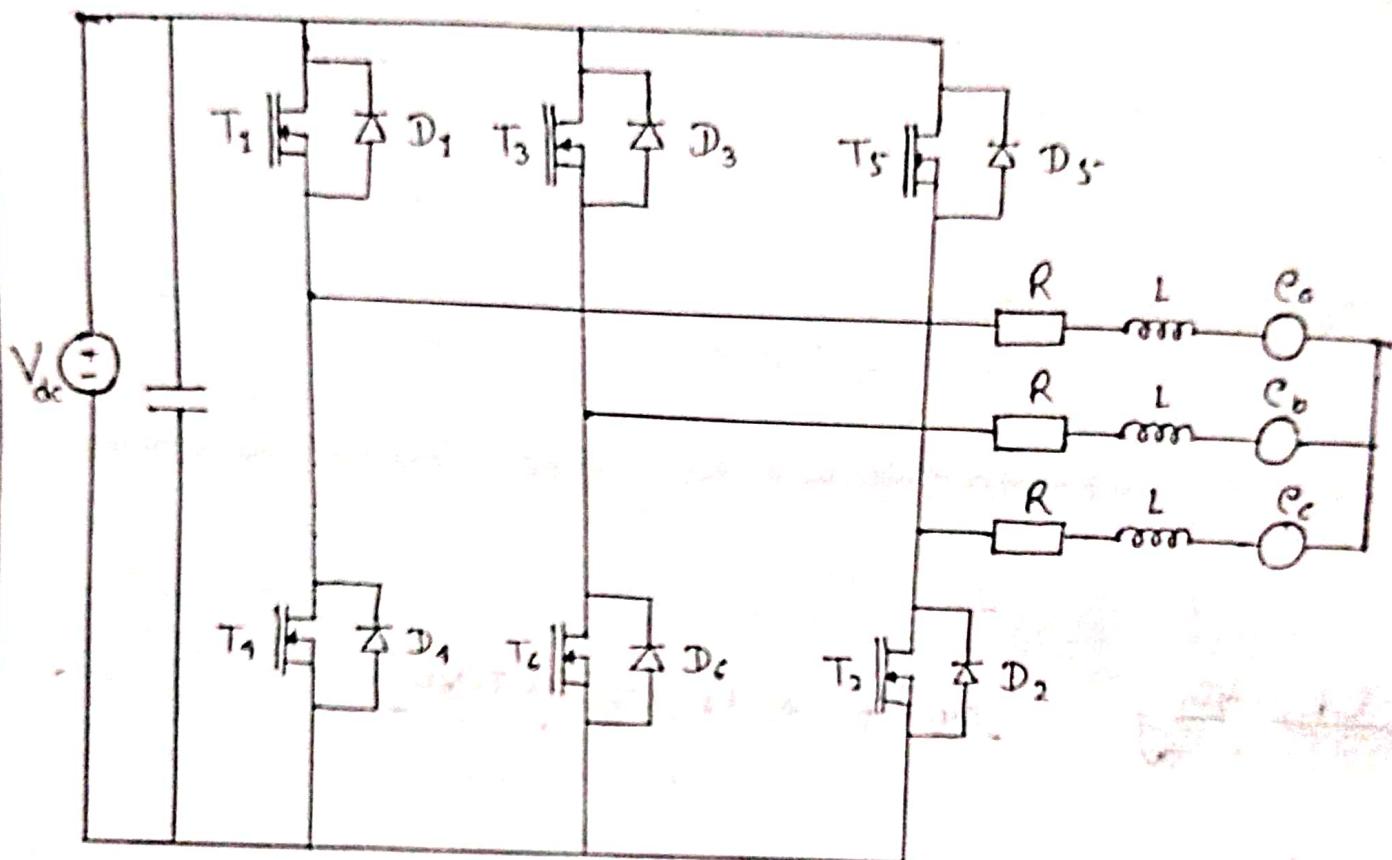
Suitable Motor

→ For Medium duty electric vehicle, BLDC is the best suitable Motor.

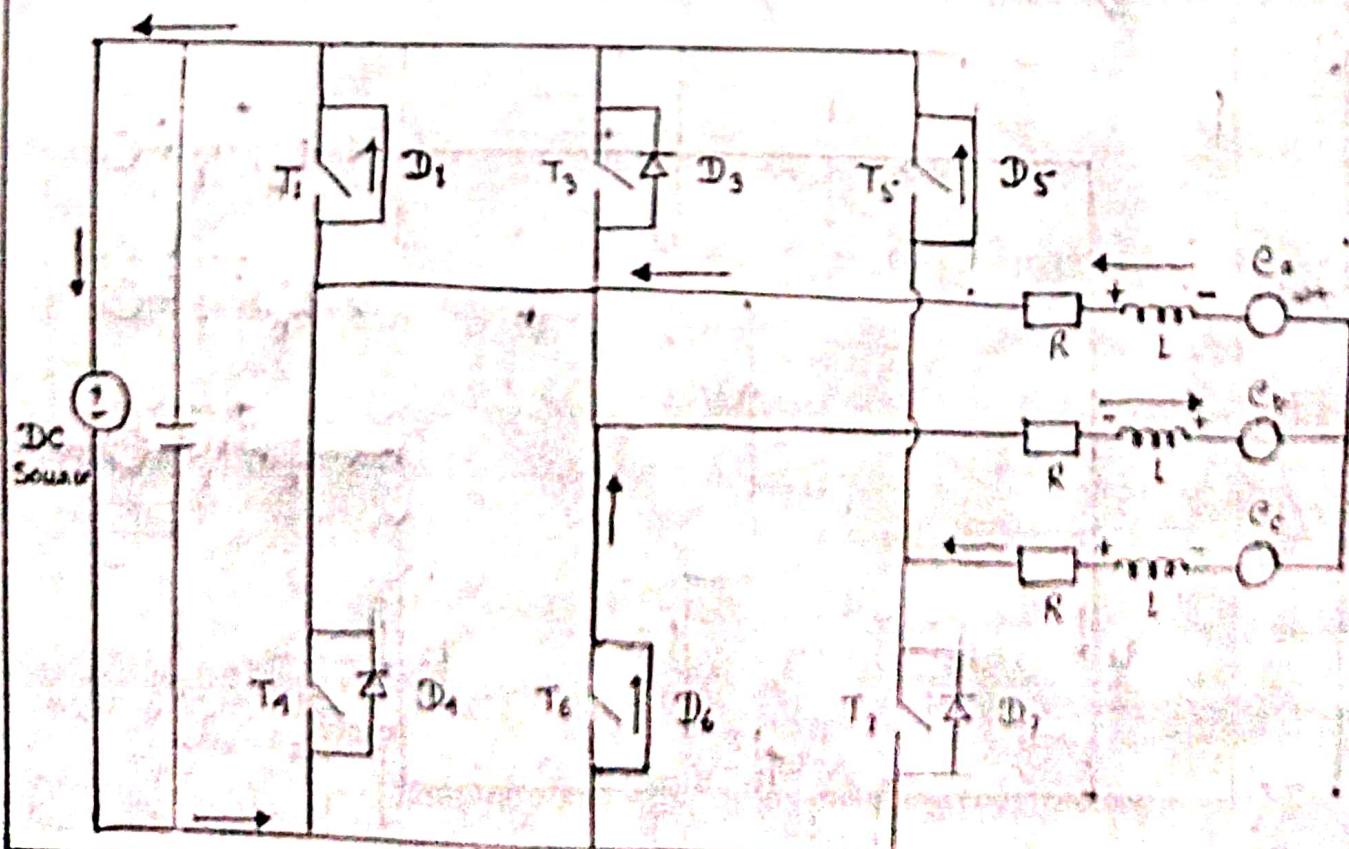
Circuit for regeneration of BLDC:

Regenerative braking

Power Converter circuit for regeneration

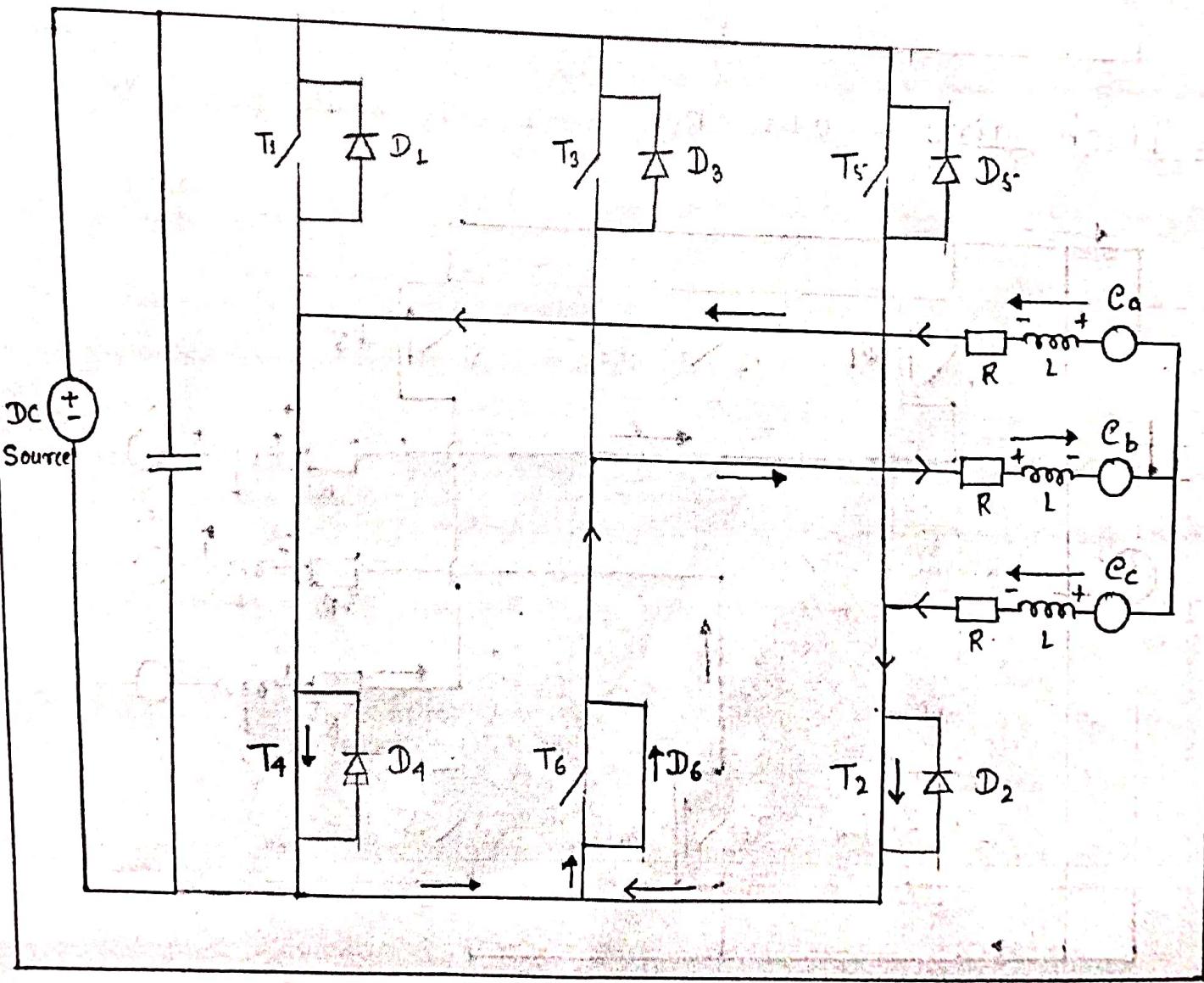


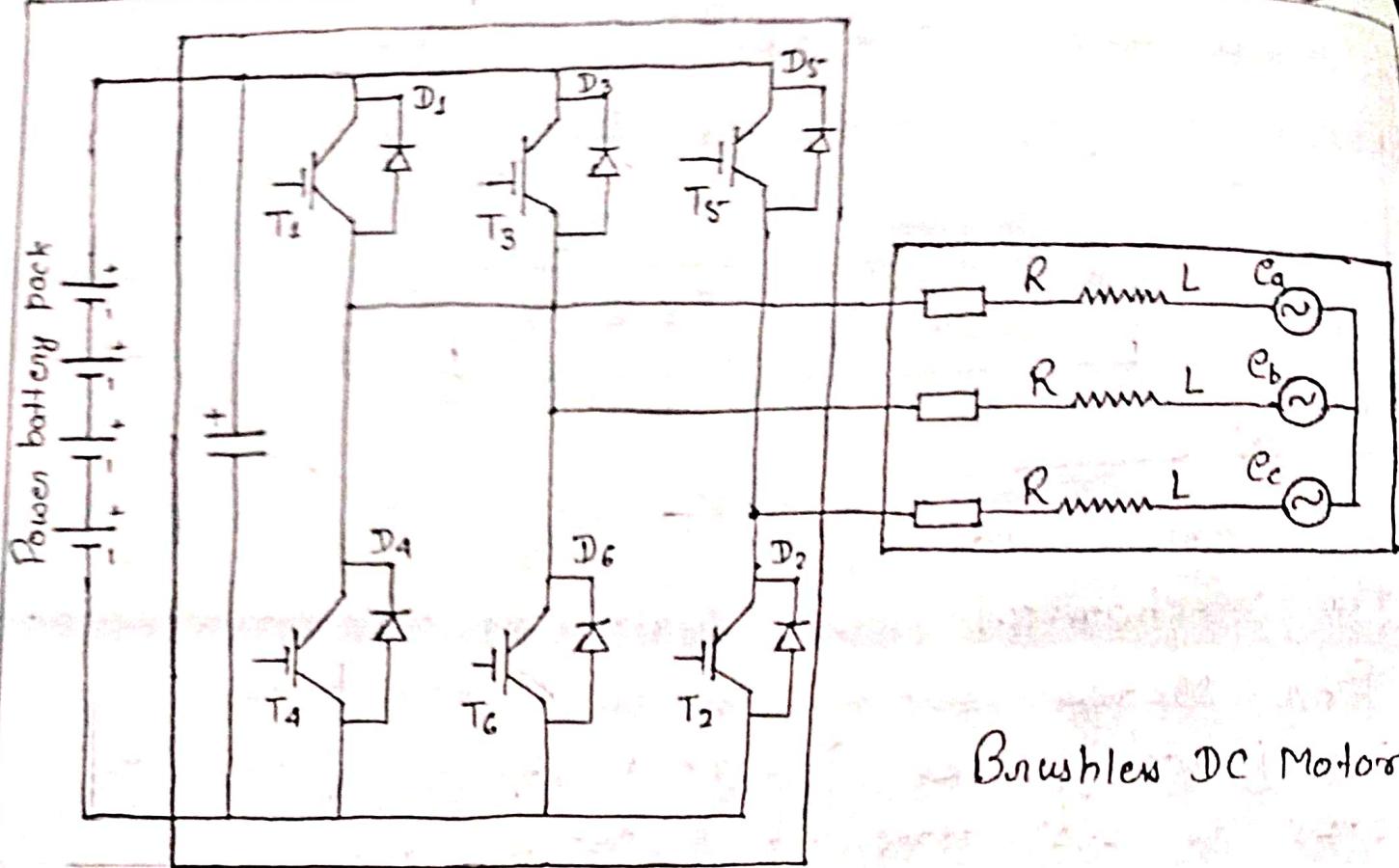
L-Discharging $a + c = b$ $D_1, D_5 \text{ \& } D_6 - \text{active}$



L-Changing

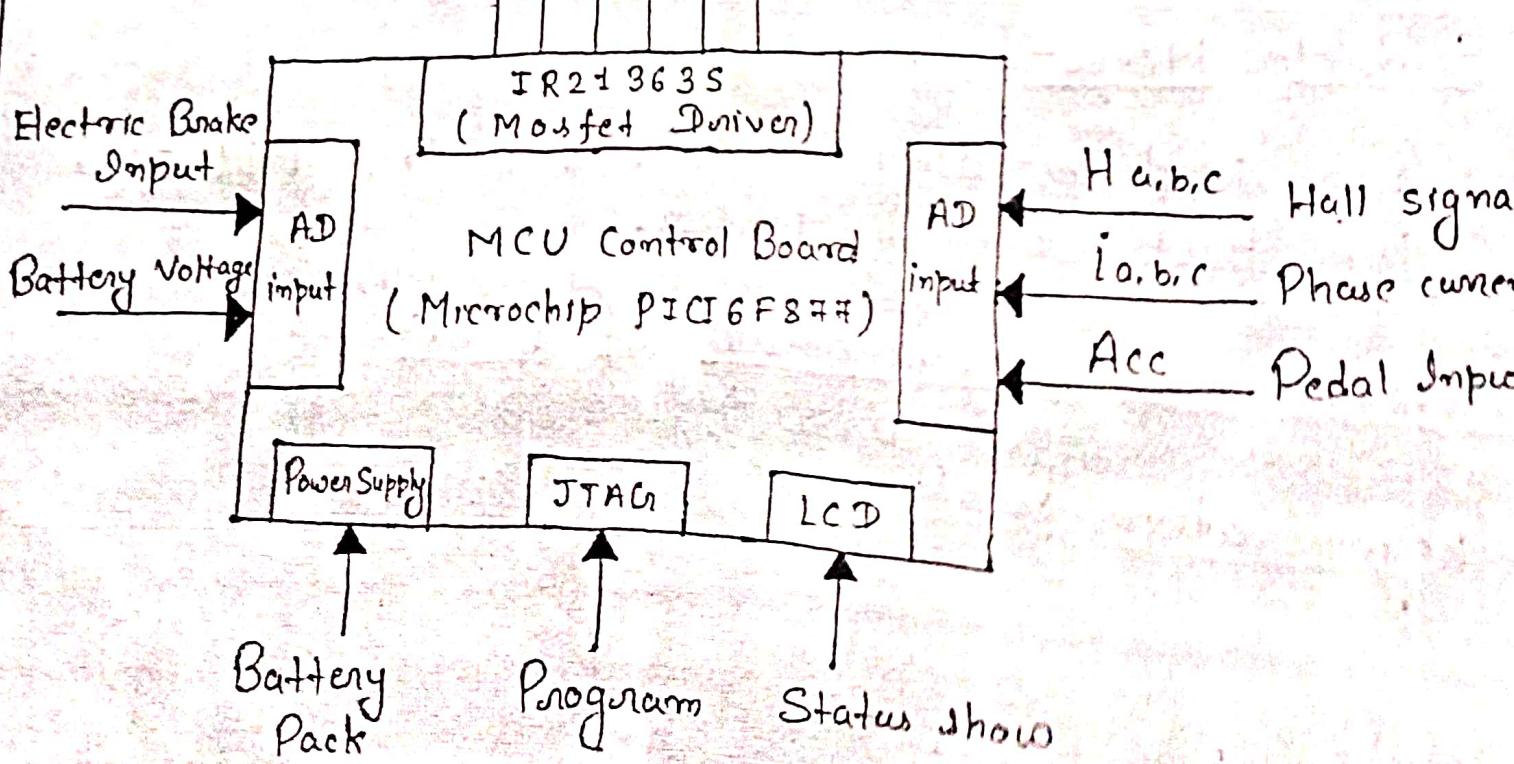
$T_4, D_6 \& T_2$ - active





PWM 1 - 6

P-MOSFET DRIVER
(Communication Block)



Power device rating :

→ Voltage rating = 240V

It is 3-Φ (there are two switches)

240V → connected with upper switch & lower switch.

$$\frac{240}{2} = 120V \rightarrow \text{each switch}$$

∴ Voltage rating for each switch is $\geq 120V$

Current

→ Let us take 1.25 times of power rating

$$6.56 \times 1.25 = 8.2 \text{ kW}$$

DC

→ Normal current is taken whatever we have calculated

→ RMS current is taken
we have calculated peak current so $\sqrt{2}$ times of peak current should be taken

$$I_{\text{rms}} = \sqrt{2} \cdot I_{\text{peak}}$$

In this case, we can take directly because it is DC

$$I = \frac{6.56 \times 1.25 \times 10^3}{240} \text{ A} = 34.367 \text{ A}$$

$$\text{Current rating} = 35 \text{ to } 40 \text{ A}$$

$$I_{\text{rating}} \geq 34.367 \text{ A}$$

Problem - 3 : Design a light duty e-scooter to run 30 kmph with 25 Nm to lift 100 kg of weight (75 kg of body weight) with diameter of 8 inches (It should run at least 100 km for one shot charge when the friction coefficient factor is 0.9.

Solution :

given values :

$$\text{Mass} = (100 + 75) \text{ kg} = 175 \text{ kg}$$

$$V = 30 \text{ Km/h}$$

$$T = 25 \text{ Nm}$$

$$D = 8 \text{ inches}$$

$$\mu = 0.9$$

$$S = 100 \text{ Km}$$

Calculations

$$D = 8 \times 2.54 \text{ cm} = 20.32 \text{ cm}$$

As we know

$$\text{Km/h} = \text{Diameter} \times \text{r.p.m} \times 1.885 \times 10^{-3}$$

$$\text{r.p.m} = \frac{\text{Km/h}}{\text{Diameter} \times 1.885 \times 10^{-3}}$$

$$= \frac{30 \times 1000}{20.32 \times 1.885}$$

$$= 783.2 \text{ r.p.m}$$

$$N = 783.2 \text{ r.p.m}$$

$$P = \frac{2\pi NT}{60}, \quad \frac{2\pi \times 783.2 \times 25}{60} = 2050 \text{ watt}$$

$$P = 2.05 \text{ kW}$$

$$P(\text{HP}) = \frac{2050}{746} = 2.74 \text{ HP}$$

$$P = 2.74 \text{ HP}$$

$$\text{Time} = \frac{\text{Distance}}{\text{Speed}} = \frac{100 \text{ km}}{30 \text{ km/h}} = 3.33 \text{ h}$$

$\text{kWh} \rightarrow$

$$(2.05 \times 3.33) \text{ kWh} = 6.82 \text{ kWh}$$

Assume $V = 24 \text{ V} \rightarrow$ for light duty vehicle

$$\text{Ah} \rightarrow \frac{6.82 \times 10^3}{24 \text{ V}} = 243.57 \text{ Ah}$$

Standard value of Ah for light duty vehicle
is assumed $\rightarrow 45 \text{ Ah}$

$$\text{No. of batteries to run } 3.33 \text{ h} = \frac{243.57 \text{ Ah}}{45 \text{ Ah}}$$

$$= 5.44 \approx 6$$

6 batteries

Motor Sizing

In this case 2.05 kW is the requirement of the mechanical power.

(3)

So, Motor rating has to accept this much maxm power so that our design should be 1.25 to 1.5 times of higher than this one.

$$2.05 \times 1.25 = 2.56 \text{ kW}$$

(approx)

$$2.05 \times 1.5 = 3.075 \text{ kW}$$

Take 1.25,

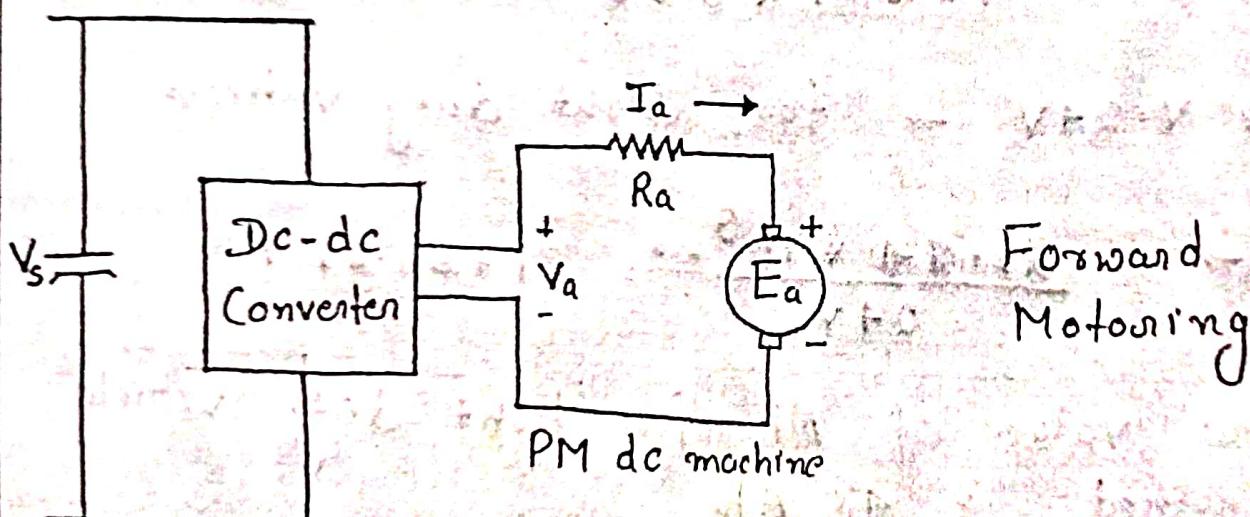
Motor sizing = 2.56 kW

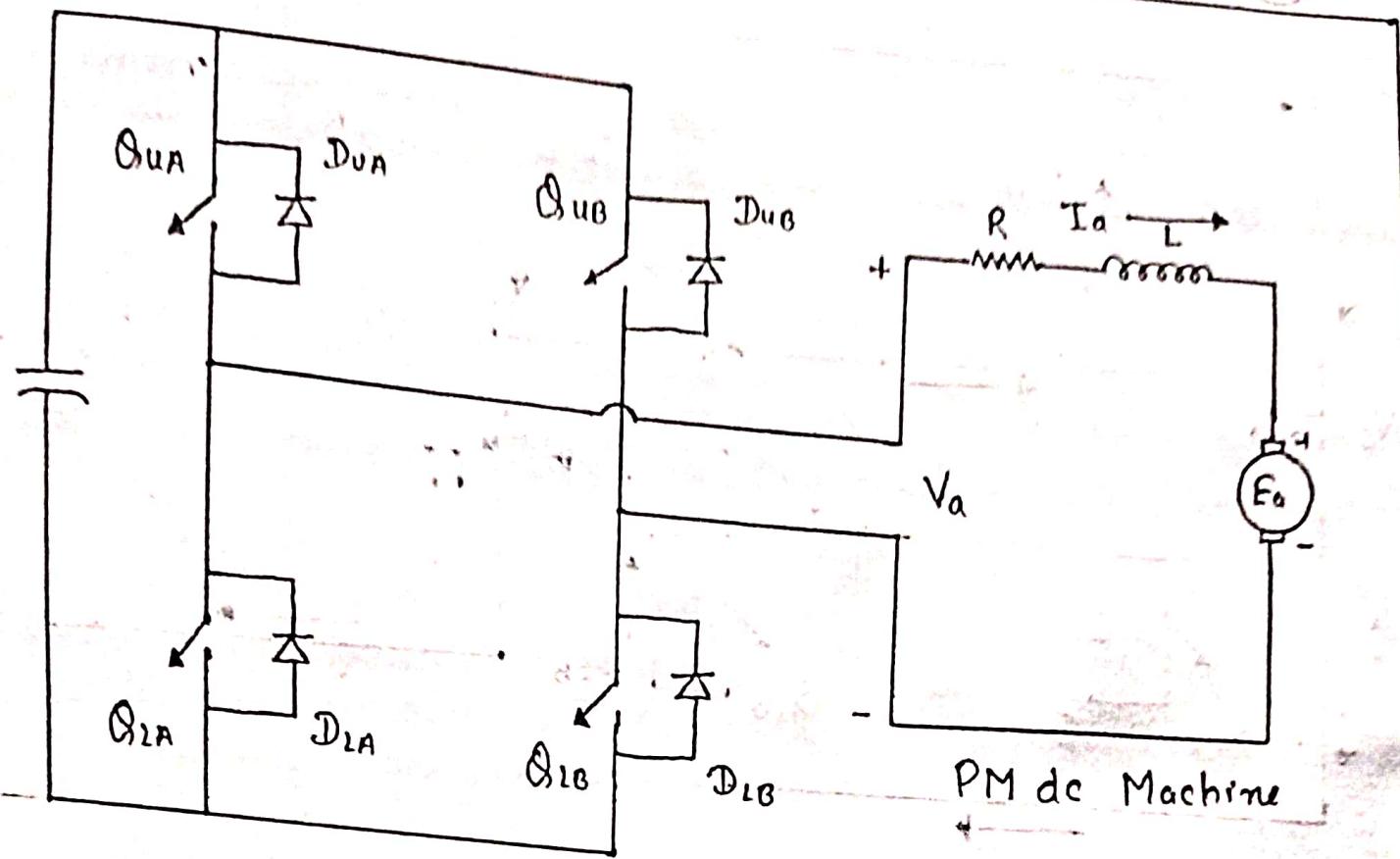
Suitable Motor

→ For light duty electric vehicle, PM DC is the best suitable Motor.

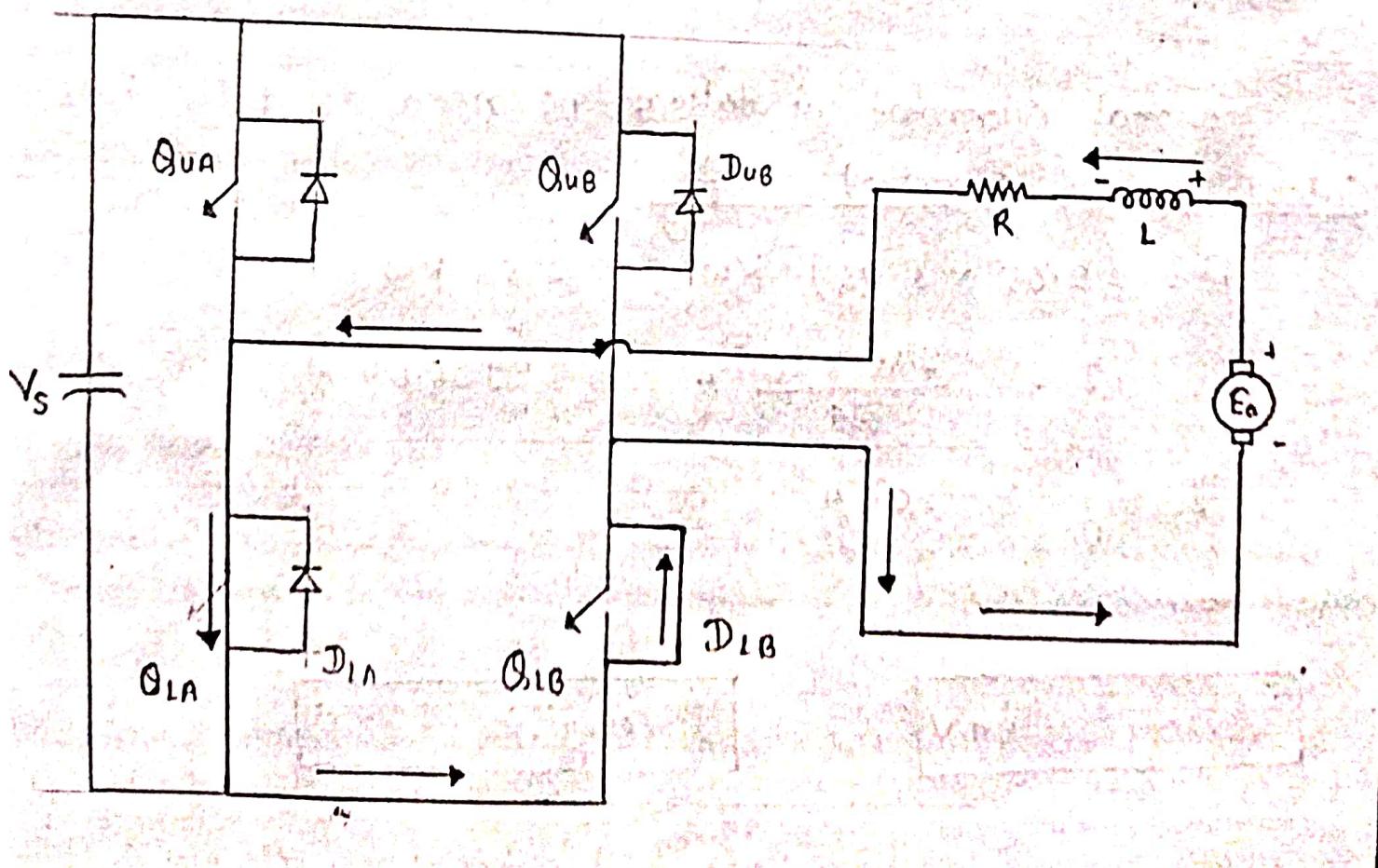
Circuit for regeneration of PMDC

(a)

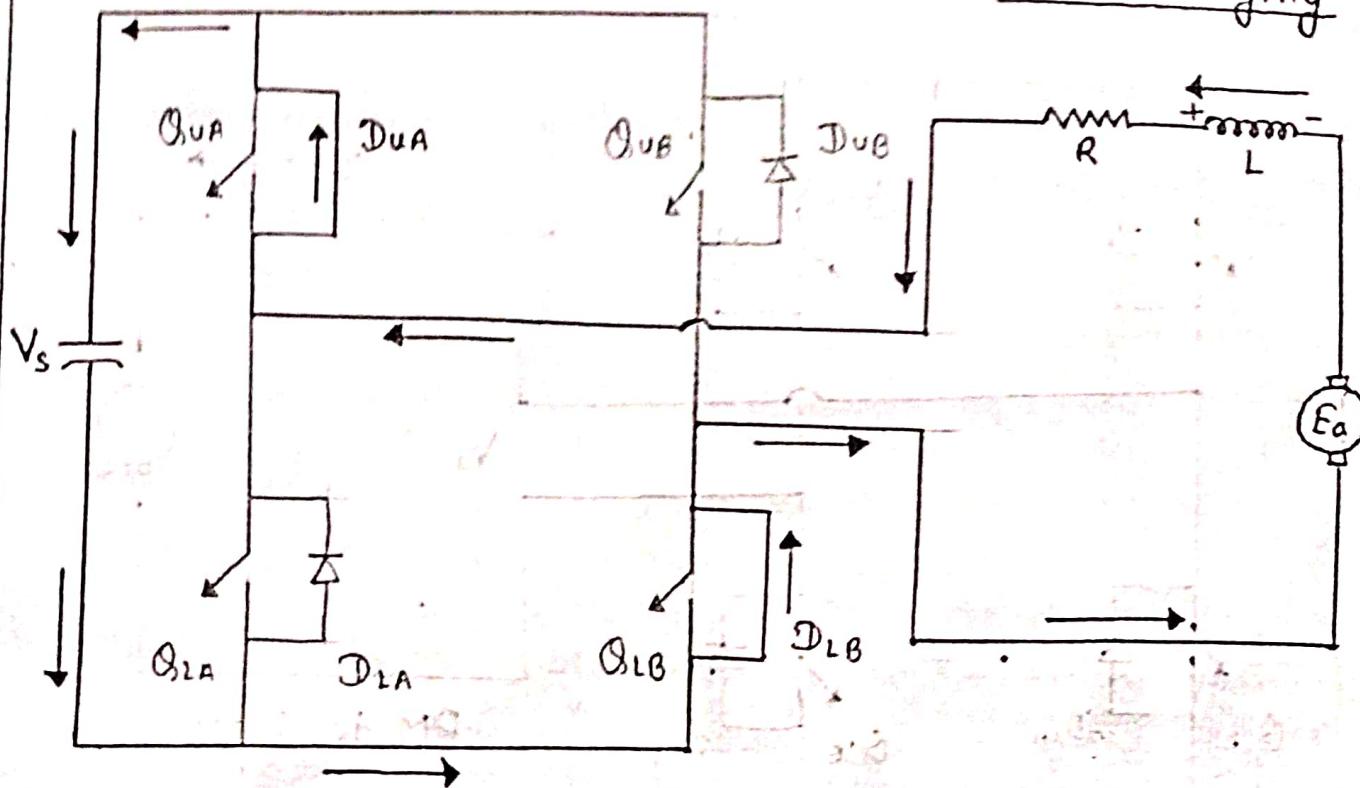




→ L-Charging $Q_{1A}, D_{2B} \rightarrow$ active



Dun, DIB - active

L - Discharging

Power device rating

→ Voltage rating $\geq 24V$ (or) $24V$ to $30V$

Current

DC

So, normal current is taken. no need to take RMS.

Calculation of current rating

$$P = (2.05 \times 1.25) \text{ kW} = 2.56 \text{ kW}$$

$$I = \frac{2.56 \times 10^3}{24} \text{ A} \approx 106.67 \text{ A}$$

$$I_{\text{rating}} \geq 107 \text{ A} \quad (\text{or}) \quad 107 \text{ A to } 310 \text{ A}$$

we have

$$\text{Voltage rating} \geq 24V$$

$$I_{\text{rating}} \geq 107 \text{ A}$$