

EE6031D - Power Electronic Circuits:-

M210492ee

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Q1

Given dc link voltage = 800V

reference vector = 500V

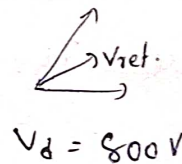
 $f = 50 \text{ Hz}$

Switching frequency = 3000 Hz

$$V_d \cos \theta + j V_d \sin \theta$$

$$V_d (\cos 12.59 + j V_d \sin (60 - 12.59))$$

$$V_d (0.9759 + j(0.736))$$



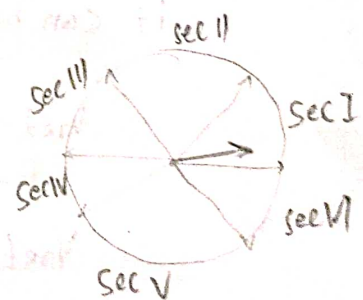
$$V_{ref_{max}} = 977.89$$

1a

given $t_1 = 0.04008 \text{ sec}$

$$\theta = \omega t_1 = 2\pi f t_1$$

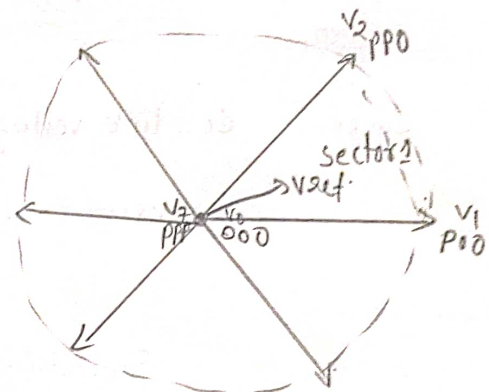
$$\theta = 2 \cdot \pi \cdot 50 \cdot 0.04008 = 12.59^\circ$$

 \therefore it is in Sector 1

(b)

7-segment switching sequence.

		<u>time period</u>
000	\vec{V}_0	$T_0/4$
POO	\vec{V}_1	$T_1/2$
PPO	\vec{V}_2	$T_2/2$
PPP	\vec{V}_7	$T_0/2$
PPO	\vec{V}_2	$T_2/2$
POO	\vec{V}_1	$T_1/2$
000	\vec{V}_0	$T_0/4$



where $T_s = T_0 + T_1 + T_2$

In above we have taken in Sector (1):

⇒ volt-sec balanced equation

$$\vec{V}_{ref} T_s = \vec{V}_1 T_1 + \vec{V}_2 T_2 + \vec{V}_0 T_0$$

it can be represent in real and imaginary

$$V_{ref} T_s \cos \theta = \frac{2}{3} V_d T_1 \cos 0 + \frac{2}{3} V_d T_2 \cos \frac{\pi}{3} + \frac{2}{3} V_d T_0 \cos \frac{\pi}{2}$$

$$V_{ref} T_s \cos \theta = \frac{2}{3} V_d T_1 + \frac{1}{3} V_d T_2$$

let written as. $V_{ref} T_s \cos \theta \times \frac{\sqrt{3}}{2} = \frac{1}{\sqrt{3}} V_d T_1 + \frac{1}{2\sqrt{3}} V_d T_2 \quad \text{--- (1)}$

and $V_{ref} T_s \sin \theta = \frac{2}{3} V_d T_2 \sin \frac{\pi}{3}$

$$V_{ref} T_s \sin \theta \times \frac{1}{2} = \frac{1}{3} V_d T_2 \sin \frac{\pi}{3} = \frac{1}{2\sqrt{3}} V_d T_2 \quad \text{--- (2)}$$

(3)

(1) + (2)

$$V_{ref} T_s \left(\cos \theta \times \frac{\sqrt{3}}{2} + \sin \theta \frac{1}{2} \right) = \frac{1}{\sqrt{3}} V_d T_1$$

$$V_{ref} T_s \sin \left(\frac{\pi}{3} - \theta \right) = \frac{1}{\sqrt{3}} V_d T_1$$

$$T_1 = \sqrt{3} \frac{V_{ref}}{V_d} T_s \sin \left(\frac{\pi}{3} - \theta \right) \quad \text{--- (3)}$$

from eq (2) $T_2 = \sqrt{3} \times \frac{V_{ref}}{V_d} T_s \sin \theta \quad \text{--- (4)}$

$$T_s = T_1 + T_2 + T_0 \Rightarrow T_0 = T_s - T_1 - T_2$$

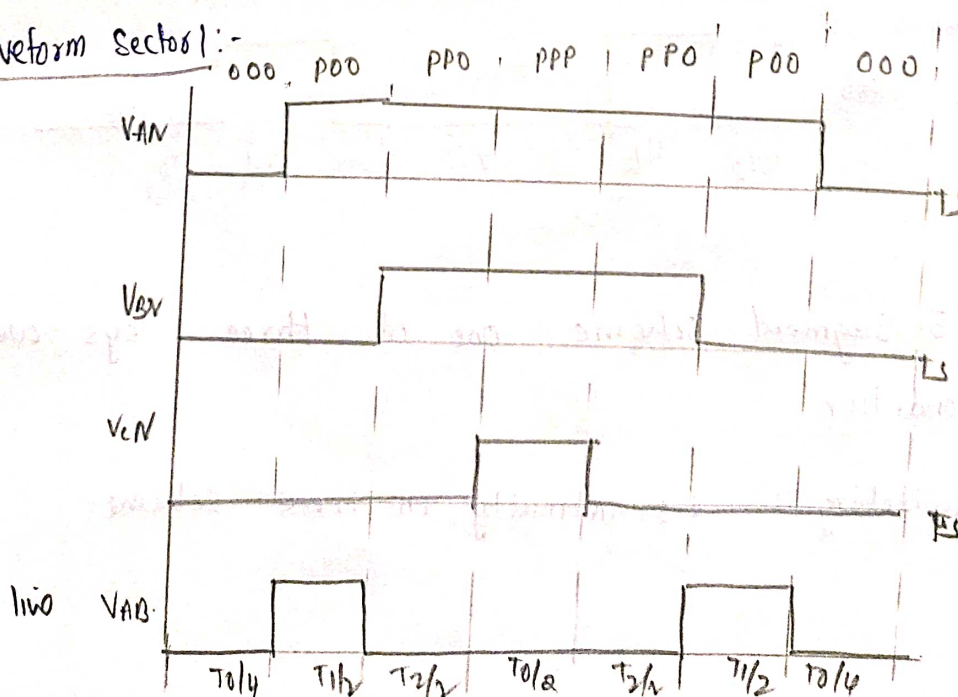
By generating

$$T_1 = \sqrt{3} \cdot \frac{V_{ref}}{V_d} \cdot T_s \cdot \sin \left(\frac{n\pi}{3} - \theta \right)$$

$$T_2 = \sqrt{3} \cdot \frac{V_{ref}}{V_d} T_s \sin \left(\theta - (n-1)\frac{\pi}{3} \right)$$

n = Sector number.

Waveform Sector:-



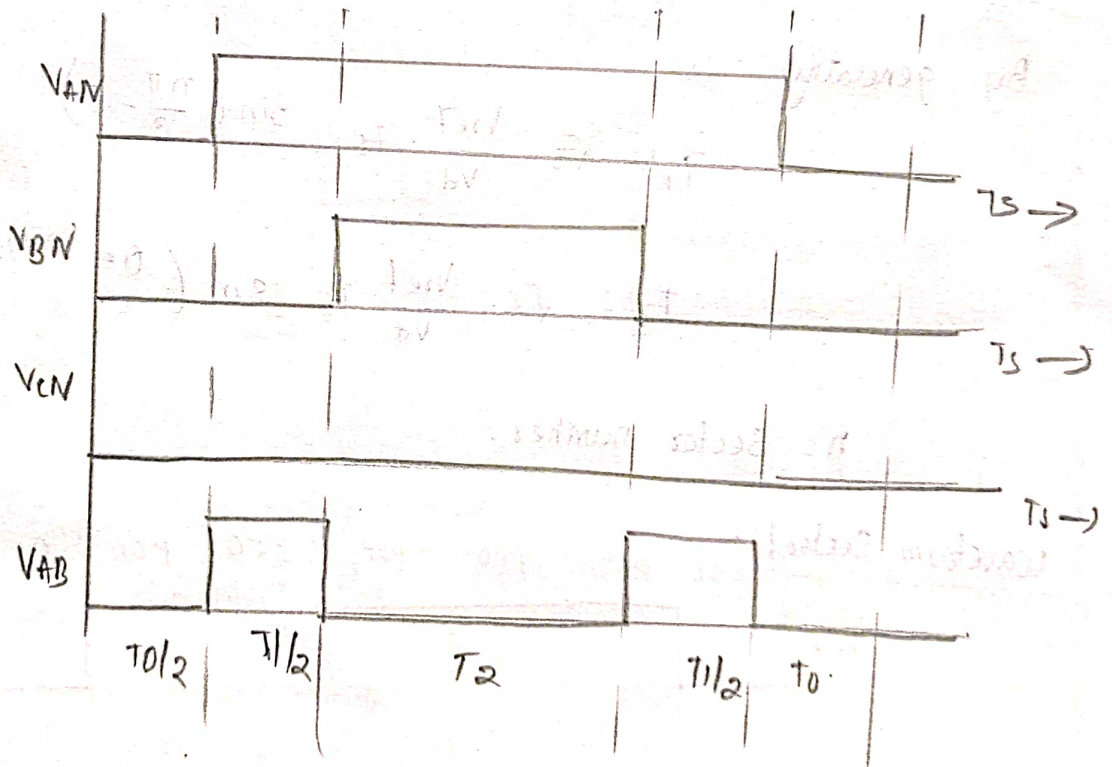
(1C)

(4)

5-segment switching sequence:-

Switching sequence			In sector I :		$T_1 = \text{open}$ $T_2 = \text{close}$	$T_1 = \text{close}$ $T_2 = \text{open}$
	time periods				0	1
000	$T_0/2$	\vec{V}_0				
P00	$T_1/2$	\vec{V}_1	T_1			
PP0	T_2	\vec{V}_2	T_2			
P00	$T_1/2$	\vec{V}_1				
000	$T_0/2$	\vec{V}_0				

wave form:-



→ In 5-segment scheme. one of three legs are off condition.

→ Switching is discontinuity. in these scheme.

(1d)

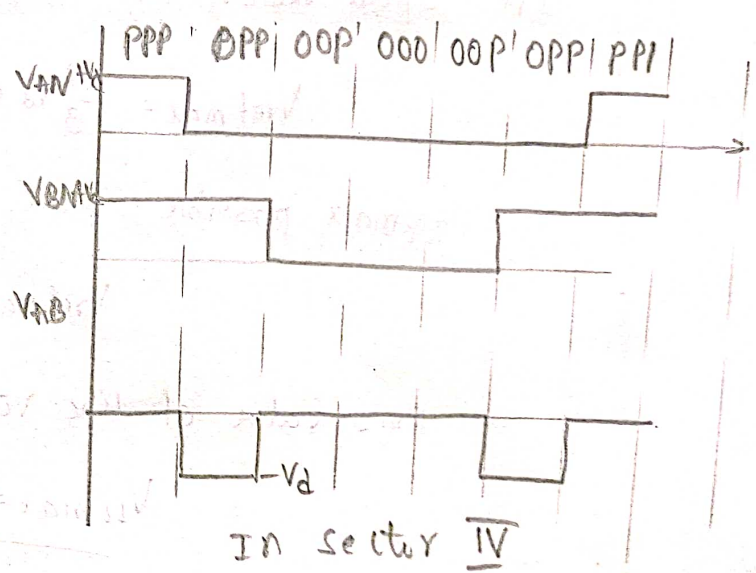
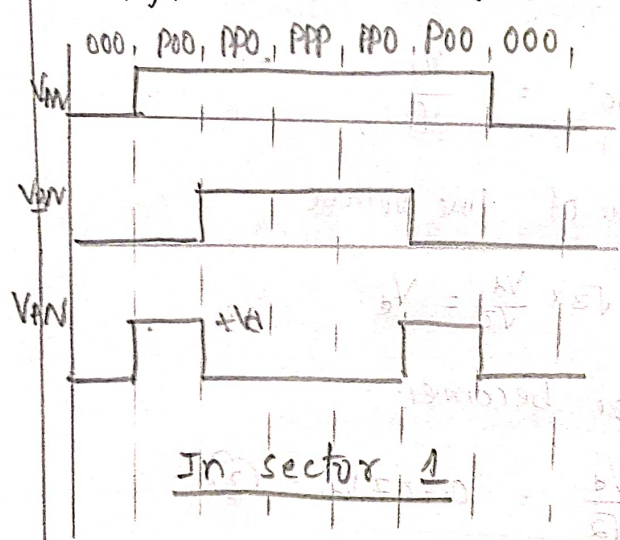
(5)

V_{AB} is not half wave symmetric, \therefore even harmonics are present.

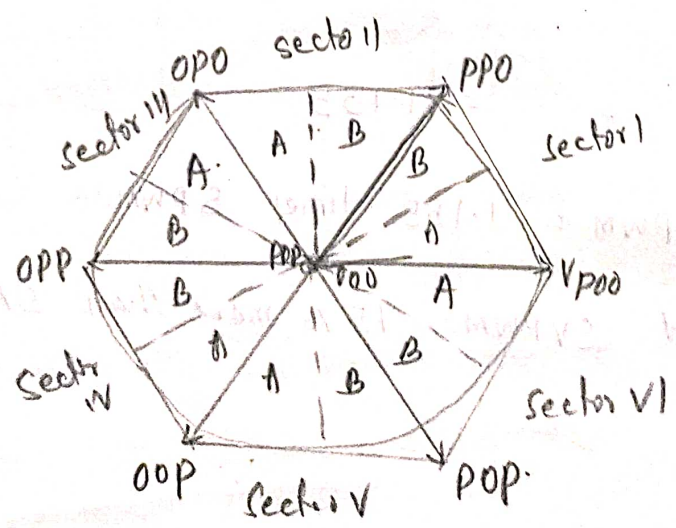
→ To eliminate even order harmonics, we make the line-line voltages are symmetrical.

→ eliminate by using Type A and Type B sequence.

Type A Switching sequence: Type B Switching



→ By using switching sequence A & B alternatively in each sector we eliminate the even order harmonics.



1(c)

In Sinusoidal pulse width Modulation SPWM

Rms value. line-line voltage of fundamental component

$$V_{LL} = \frac{\sqrt{3}}{\sqrt{2}} m_a \frac{V_d}{2}$$

$$V_{LL} = 0.612 m_a V_d \quad \text{for max } m_a = 1$$

$$\underline{V_{LL \max} = 0.612 V_d} \quad \text{--- (1)}$$

In Space vector Pulse width modulation SVPWM

$$V_{ref \max} = \frac{2}{3} V_d \cos 30^\circ = \frac{V_d}{\sqrt{3}}$$

max possible peak value of line voltage

$$V_{ref \max} = \sqrt{3} \times \frac{V_d}{\sqrt{3}} = V_d$$

Rms value of line voltage becomes:

$$\underline{V_{LL \max} = \frac{V_d}{\sqrt{2}} = 0.707 V_d} \quad \text{--- (2)}$$

$$\frac{\text{(2)}}{\text{(1)}} \Rightarrow \frac{\text{SVPWM of Rms value}}{\text{SPWM}} = \frac{0.707 V_d}{0.612 V_d}$$

$$= 1.155$$

$$\text{SVPWM} = 1.155 \text{ times SPWM}$$

Nothing b/w SVPWM = 15% more than SPWM.

Q2

7

a) torque and flux depends on current.

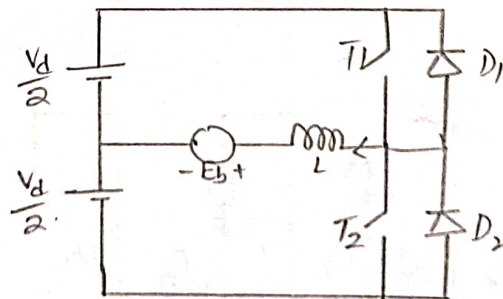
\therefore "Current Mode control scheme"

b)

Advantages of current Mode control Scheme :

- i) ripples currents are reduced
- ii) Reduces the peak current values of device.
- iii) Minimize the cost.
- iv) Avoid the more heating and torque ripples in drive output.
- v) Sinusoidal waveform is generated

c)



T_1 is turn on at positive wave of current. when T_1 is turned off T_2 is turn on. During the positive load current flows through the D_2 and T_1 conduction takes place.

— Here we implemented the hysteresis band PWM

Because when $I_L > I_{ref}$ T_1 Turn on

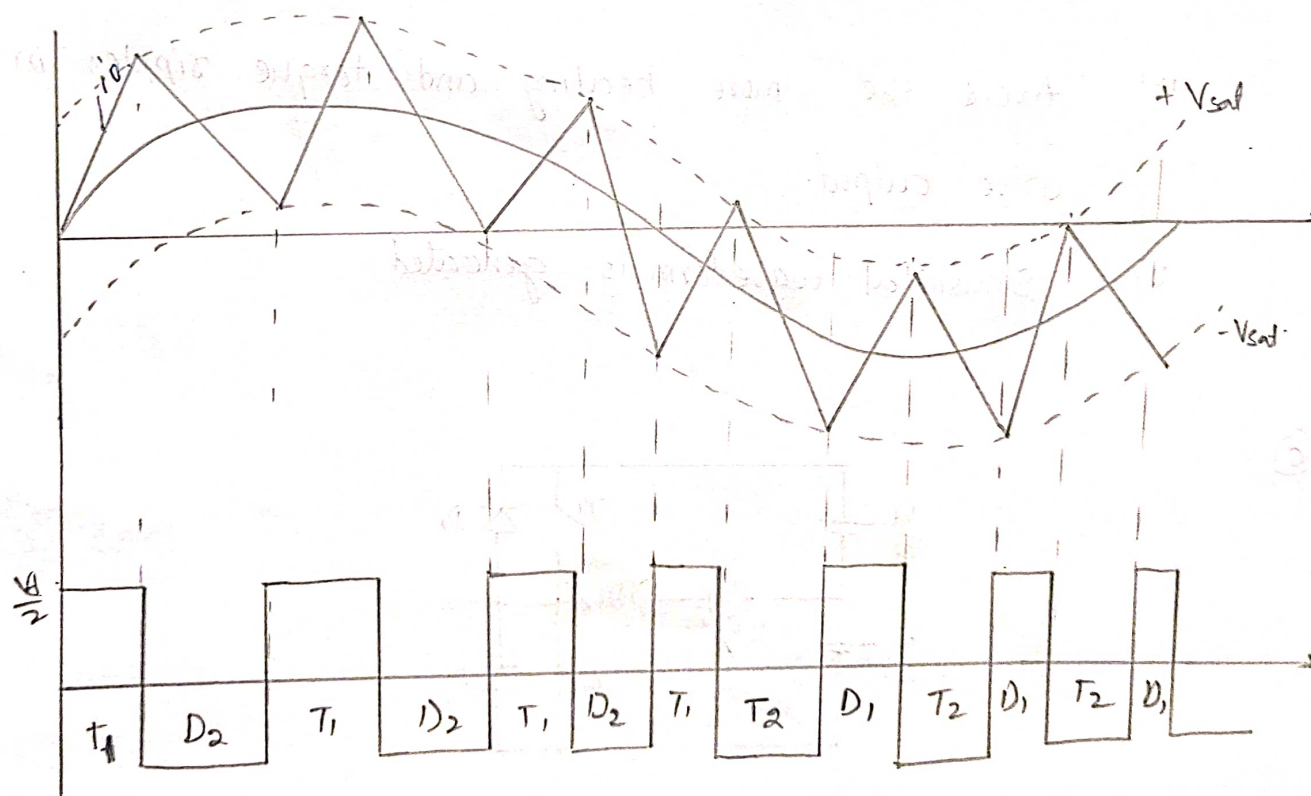
$I_L < I_{ref}$ T_1 turn on.

maximum operating frequency can be obtained in it.

where maximum frequency leads to more losses

in the inverter. To Avoid these we go for

hysteresis band PWM.



i) During positive half cycle of load current i_o , T_1 is conducting and i_o rises. When the current exceeds a hysteresis band then T_1 is turn-OFF and lower switch is turn on. Then D_2 conduction take place.

11) when current crosses the lower band of (9) hysteresis T_2, D_2 - then OFF And T_1 turn ON take place.

During positive half cycle $i_o \geq i_H$ T_1 is turn OFF
 $i_o \leq i_L$ D_2 is turn OFF

During Negative half cycle $i_o > i_H$ D_1 is turn OFF
 $i_o < i_L$ T_2 is turn OFF

\Rightarrow when T_1 is ON:- current rises:-

$$\frac{V_d}{2} - L \frac{di_o}{dt} - E_b = 0$$

$$\frac{di_o}{dt} = \frac{\frac{V_d}{2} - E_b}{L} = \frac{\Delta I}{t_{on}}$$

$$t_{on} = \frac{L \Delta I}{\frac{V_d}{2} - E_b}$$

\Rightarrow When D_2 is ON, T_1 is OFF:

then
$$-\frac{V_d}{2} - E_b + L \frac{di_o}{dt} = 0$$

$$\frac{di_o}{dt} = \frac{\frac{V_d}{2} + E_b}{L} = \frac{\Delta I}{t_{off}}$$

$$t_{off} = \frac{L \Delta I}{\frac{V_d}{2} + E_b}$$

\Rightarrow total time period $t = t_{on} + t_{off} = L \Delta I \left[\frac{2 \cdot \frac{V_d}{2}}{\left(\frac{V_d}{2}\right)^2 - (E_b)^2} \right]$

$$T_s = \frac{L \Delta I}{\frac{V_d}{4}} \times \frac{1}{1 - \left(\frac{E_b}{\frac{V_d}{2}}\right)^2}$$

$$f_s = \frac{1}{T_s} = \frac{V_d/4}{L \Delta I} \left[1 - \left(\frac{E_b}{V_d/2}\right)^2 \right]$$

at $E_b = 0$ $f_s = \max$

$$f_{s\max} = \frac{V_d}{4L \Delta I}$$

$$\therefore f_s = f_{\max} \left[1 - \left(\frac{E_b}{V_d/2}\right)^2 \right]$$

When $E_b = E_m \sin \omega t$ then.

$$f_s = f_{\max} \left[1 - \frac{E_m^2 \sin^2 \omega t}{\left(\frac{V_d}{2}\right)^2} \right]$$

$$f_s = f_{\max} \left[1 - \frac{E_m^2}{\left(\frac{V_d}{2}\right)^2} \left[\frac{1 - \cos 2\omega t}{2} \right] \right]$$

$$f_s = f_{\max} \left[1 - \frac{E_m^2}{\left(\frac{V_d}{\sqrt{2}}\right)^2} [1 - \cos 2\omega t] \right]$$

$$f_s = f_{\max} \left[1 - \left(\frac{E_m}{V_d/\sqrt{2}}\right)^2 + \left(\frac{E_m}{V_d/\sqrt{2}}\right)^2 \cos 2\omega t \right]$$

$$\therefore f_{\max} = \frac{V_d}{4L \Delta I}$$

it is Switching frequency.

④ Factors Affect the switching frequency is

- i) Ripple current (ΔI)
- ii) DC bus voltage (V_d)
- iii) Induced emf ($E_b = E_m \sin \omega t$)

Q. 3
no.

11

given fundamental voltage = 80% of input voltage.

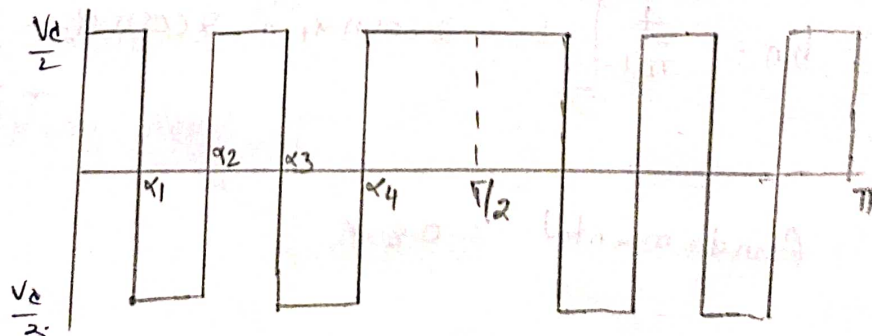
Lower order harmonics of square wave can be eliminated by using the selected harmonic elimination PWM.

→ In these method notches are created on the square wave at predetermined angles

→ If we need to eliminate 'n' no. of harmonics, 'n+1' number of notches be created in the square wave.

→ from given we need to eliminate 3rd, 5th and 9th '3' harmonics we need to eliminate 4 notches are created.

→ let us take $\alpha_1, \alpha_2, \alpha_3, \alpha_4$ are the notches controlled to eliminate three significant harmonic components.



Voltage waveform

- Fourier series of the wave

$$V(t) = \sum_{n=1}^{\infty} a_n \cos n\omega t + b_n \sin n\omega t$$

Sine wave half-wave symmetry $a_n = 0$.

& quarter wave symmetry.

only odd harmonics are present

$$\therefore V(t) = \sum_{n=1}^{\infty} b_n \sin n\omega t$$

$$\therefore b_n = \frac{8}{2\pi} \int_0^{\pi/2} V(t) \sin n\omega t d(\omega t)$$

$$b_n = \frac{4}{\pi} \left[\int_0^{\alpha_1} V_m \sin n\omega t + \int_{\alpha_1}^{\alpha_2} -V_m \sin n\omega t + \int_{\alpha_2}^{\alpha_3} +V_m \sin n\omega t \right. \\ \left. + \int_{\alpha_3}^{\alpha_4} -V_m \sin n\omega t + \int_{\alpha_4}^{\pi/2} V_m \sin n\omega t \right]$$

let us take unit Amplitude $V_m = 1$.

$$\therefore b_n = \frac{4}{n\pi} \left[-\cos n\omega t \Big|_0^{\alpha_1} + \cos n\omega t \Big|_{\alpha_1}^{\alpha_2} - \cos n\omega t \Big|_{\alpha_2}^{\alpha_3} \right. \\ \left. + \cos n\omega t \Big|_{\alpha_3}^{\alpha_4} - \cos n\omega t \Big|_{\alpha_4}^{\pi/2} \right]$$

$$b_n = \frac{4}{n\pi} \left[1 - 2\cos n\alpha_1 + 2\cos n\alpha_2 - 2\cos n\alpha_3 \right. \\ \left. + 2\cos n\alpha_4 \right]$$

Given fundamental $= 0.8 \cdot f$

If $n=1$

$$b_1 = \frac{4}{\pi} [1 - 2\cos\alpha_1 + 2\cos\alpha_2 - 2\cos\alpha_3 + 2\cos\alpha_4] = 0.8$$

3rd harmonic

$$b_3 = \frac{4}{3\pi} [1 - 2\cos 3\alpha_1 + 2\cos 3\alpha_2 - 2\cos 3\alpha_3 + 2\cos 3\alpha_4]$$

5th harmonic

$$b_5 = \frac{4}{5\pi} [1 - 2\cos 5\alpha_1 + 2\cos 5\alpha_2 - 2\cos 5\alpha_3 + 2\cos 5\alpha_4]$$

7th harmonic

$$b_7 = \frac{4}{7\pi} [1 - 2\cos 7\alpha_1 + 2\cos 7\alpha_2 - 2\cos 7\alpha_3 + 2\cos 7\alpha_4]$$

to eliminate 3rd, 5th, 7th

$$b_3 = b_5 = b_7 = 0$$

Solving $b_1 = 0.8$, $b_3 = 0$, $b_5 = 0$, $b_7 = 0$

$$\frac{4}{\pi} [1 - 2\cos\alpha_1 + 2\cos\alpha_2 - 2\cos\alpha_3 + 2\cos\alpha_4] = 0.8$$

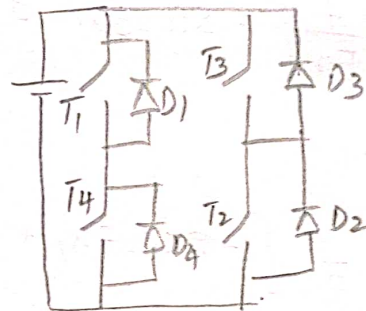
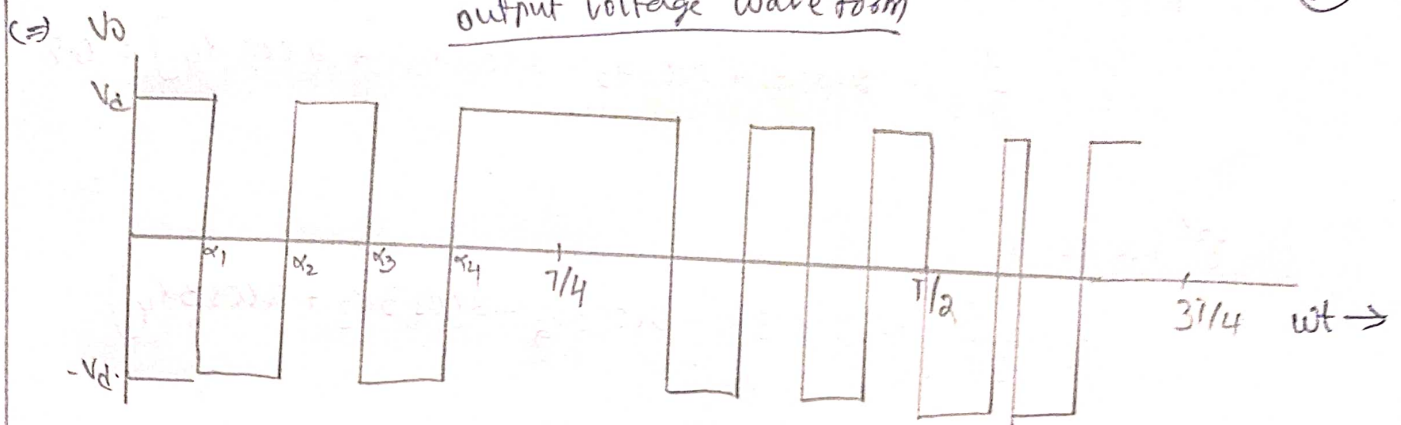
$$1 - 2\cos 3\alpha_1 + 2\cos 3\alpha_2 - 2\cos 3\alpha_3 + 2\cos 3\alpha_4 = 0$$

$$1 - 2\cos 5\alpha_1 + 2\cos 5\alpha_2 - 2\cos 5\alpha_3 + 2\cos 5\alpha_4 = 0$$

$$1 - 2\cos 7\alpha_1 + 2\cos 7\alpha_2 - 2\cos 7\alpha_3 + 2\cos 7\alpha_4 = 0$$

By solving Above we get

$\alpha_1, \alpha_2, \alpha_3, \alpha_4$ Angles.

output voltage waveform

\Rightarrow During the intervals.

$(0 \alpha_1) \rightarrow T_1 \text{ and } T_2 \text{ conduct } V_o = +V_d.$

$(\alpha_1 \alpha_2) \rightarrow T_3 \text{ and } T_4 \text{ conduct } V_o = -V_d$

$(\alpha_2 \alpha_3) \rightarrow T_1 \text{ and } T_2 \text{ conduct } V_o = +V_d$

$(\alpha_3 \alpha_4) \rightarrow T_3 \text{ and } T_4 \text{ conduct } V_o = -V_d.$