#### Problem Set 1

QTM 200: Applied Regression Analysis January 29, 2020

#### Instructions

- Please show your work! You may lose points by simply writing in the answer. If the problem requires you to execute commands in R, please include the code you used to get your answers. Please also include the .R file that contains your code. If you are not sure if work needs to be shown for a particular problem, please ask.
- Your homework should be submitted electronically on the course GitHub page in .pdf form.
- This problem set is due at the beginning of class on Wednesday, January 22, 2020. No late assignments will be accepted.
- Total available points for this homework is 100.

# Question 1 (25 points)

A private school counselor was curious about the average of IQ of the students in her school and took a random sample of 25 students' IQ scores. The following is the data set:

```
\begin{array}{l} 1 \ y \longleftarrow c(105,\ 69,\ 86,\ 100,\ 82,\ 111,\ 104,\ 110,\ 87,\ 108,\ 87,\ 90,\ 94,\ 113,\ 112,\ 98,\\ 80,\ 97,\ 95,\ 111,\ 114,\ 89,\ 95,\ 126,\ 98) \end{array}
```

Find a 90% confidence interval for the student IQ in the school assuming the population of IQ from which our random sample has been selected is normally distributed.

- ANSWER: The 90% confidence interval is (94.1, 102.7).
- INTERPRETATION: We are 90% confident that true average IQ of students at her school lies between 94.1 and 102.7.

```
1 z90 <- qnorm((1-.90)/2, lower.tail = FALSE)
2 n <- length(y)
3 mean(y)
4 sample_mean <- mean(y)
5 sample_sd <- sd(y)
6 lower_90 <- sample_mean - (z90 * (sample_sd/sqrt(n)))
7 upper_90 <- sample_mean + (z90 * (sample_sd/sqrt(n)))
8 confint90 <- c(lower_90, upper_90)
9 # ANSWER: 90% confidence interval is (94.1, 102.7)
10 # INTERPRETATION: We are 90% confident that that true average IQ of students at her school lies between 94.1 and 102.7.</pre>
```

## Question 2 (25 points)

A private school counselor was curious whether the average of IQ of the students in her school is higher than the average IQ score 100 among all the schools in the country. She took a random sample of 25 students' IQ scores. The following is the data set:

```
y \leftarrow c(105, 69, 86, 100, 82, 111, 104, 110, 87, 108, 87, 90, 94, 113, 112, 98, 80, 97, 95, 111, 114, 89, 95, 126, 98)
```

Conduct a test with 0.05 significance level assuming the population of IQ from which our random sample has been selected is normally distributed.

ANSWER: p-value = 0.7216 greater than 0.05, therefore sample mean is not significantly greater than 100

```
#null hypothesis: xbar = 100
2 #alternative hypothesis: xbar > 100
3 #calculate test statistic and p-value
4 mean(y)
5 #mean of sample is 98.44
6 sd (y)
7 #sample size
s n \leftarrow length(y)
9 #standard deviation of sample is 13.09
teststata < (98.44-100)
teststatb < 13.09/(sqrt(n))
teststatistic <- ((teststata)/(teststatb))
13 #test statistic = -0.596
_{14} \# n=25 therefore df = 24
_{15} #test statistic = -0.119
pt(abs(-0.596), df=24)
_{17} \# p-value = 0.7216
_{18} # ANSWER/INTERPRETATION: p-value = 0.7216 > 0.05 therefore sample mean is not
  significantly greater than 100
```

## Question 3 (50 points)

Assume y is variable with values 1,2,3,4 standing for "Freshman", "Sophomore", "Junior", and "Senior", convert y from numbers to characters in  $\mathbb{R}$ :

#### ANSWER:

```
highschool [y==1] <- "Freshman"
highschool [y==2] <- "Sophomore"
highschool [y==3] <- "Junior"
highschool [y==4] <- "Senior"
str(highschool)
highschool [1:10]
highschool
#Recode numerical vector y so that values are assigned to corresponding categories

######
```

Researchers are curious about what affects the education expenditure on public education. The following is available variables in a data set about the education expenditure.

```
State | 50 states in US | y | per capita expenditure on public education | X1 | per capita personal income | X2 | Number of residents per thousand under 18 years of age | X3 | Number of people per thousand residing in urban areas | Region | 1=Northeast, 2= North Central, 3= South, 4=West |
```

Explore the expenditure data set and import data into R.

```
expenditure <- read.table("expenditure.txt", header=T)
```

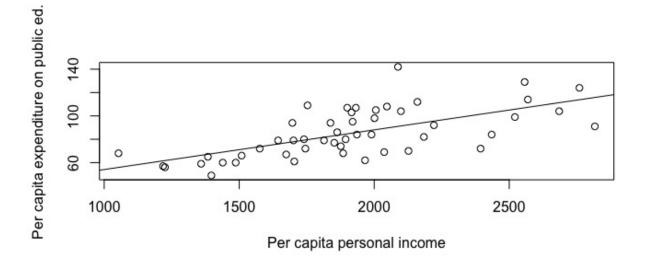


Figure 1: Y and X1: Moderate, linear, positive correlation

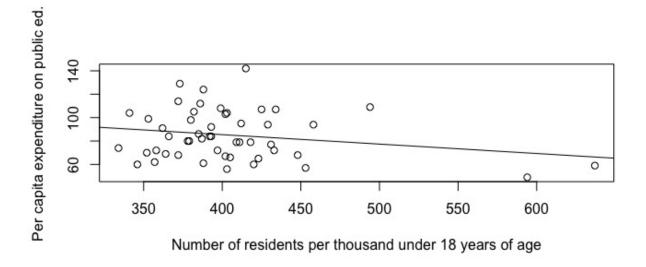


Figure 2: Y and X2: Weak, negative, non-linear correlation

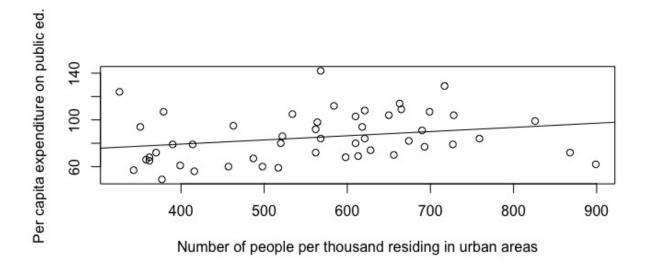


Figure 3: Y and X3: Weak positive correlation

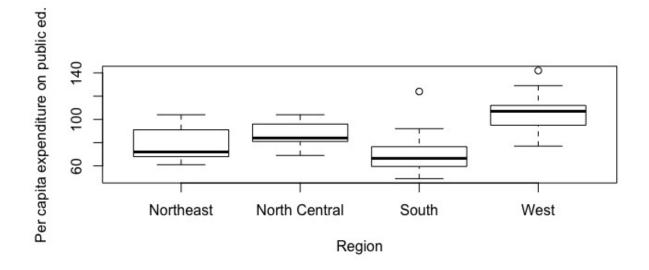


Figure 4: On average, the Western region has the highest per capita expenditure on public education

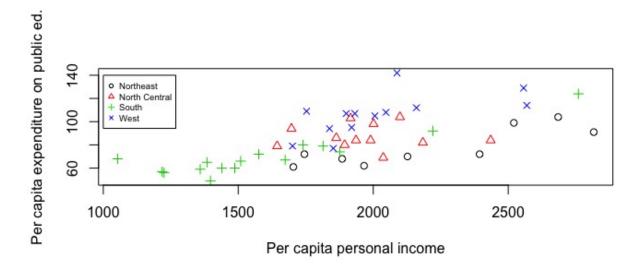


Figure 5: Moderate, linear, positive correlation between per capita expenditure on public education and per capita personal income

```
7 # PLOT 2
8 plot (expenditure$X2, expenditure$Y,
       xlab="Number of residents per thousand under 18 years of age", ylab=
     "Per capita expenditure on public ed.")
abline (lm (expenditure $Y ~ expenditure $X2))
11 #Weak negative correlation
12
13 # PLOT 3
plot (expenditure $X3, expenditure $Y,
       xlab="Number of people per thousand residing in urban areas", ylab="
     Per capita expenditure on public ed.")
abline (lm (expenditure $Y ~ expenditure $X3))
17 #Weak positive correlation
18
20 # PLOT 4
  expenditure four regions <- NA
  expenditure $ four regions <- factor (NA, levels=c("Northeast", "North
     Central", "South", "West"))
23 expenditure $ fourregions [expenditure $ Region == 1] <- "Northeast"
  expenditure $fourregions [expenditure $Region == 2] <- "North Central"
25 expenditure fourregions expenditure Region == 3 <- "South"
26 expenditure $fourregions [expenditure $Region==4] <- "West"
  boxplot(expenditure$Y ~ expenditure$fourregions,
27
          xlab= "Region".
28
          ylab= "Per capita expenditure on public ed.")
29
31 # On average, the Western region has the highest per capita expenditure
     on public education
```