Assignment 1

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0.1 sum_mults(nums, n)

Write a function sum_mults(nums, n) that returns the sum of all multiples of values in the vector nums less than n. For example, sum_mults(c(3,5), 30) should return 195. Assume that the elements of nums are positive integers.

```
sum_mults(nums, n)
```

[1] 195

```
# l <- 1:(n-1)
# nums <- c(3,5)
# sum(l[sapply(l, function(x) any(x %% nums == 0))])
```

0.2 collatz_len(n)

Given any positive integer n, define:

$$f(n) := \begin{cases} n/2, & n \text{ even} \\ 3n+1, & n \text{ odd.} \end{cases}$$
 (1)

The Collatz conjecture states:

$$a_i := \begin{cases} n, & i = 1 \\ f(a_{i-1}), & i > 1 \end{cases} \tag{2}$$

Write a function collatz_len(n) that determines the first i for which $a_i = 1$ for a given n. For example, when n = 17, the sequence a_i begins:

```
17, 52, 26, 13, 40, 20, 10, 5, 16, 8, 4, 2, 1, \dots
```

and $a_{13} = 1$. Thus, collatz_len(17) should return 13.

```
n <- 17

collatz_len <- function(n){
    n1 <- n
    index <- 1
    while(n1 != 1){
        if(n1 %% 2 == 0)
            n1 <- n1/2
        else
            n1 <- 3*n1+1
            index <- index + 1
    }
    return(index)
}</pre>
```

[1] 13

0.3 reverse(v)

Write a function reverse(v) that reverses the vector v. So reverse(c(1,2,3)) should return c(3,2,1). reverse should return NULL, not NA, when v is c().

```
reverse <- function(v){
  if(length(v) == 0) # If the list is empty, return NULL
    return(NULL)
  if(length(v))
    res <- v[length(v):1]
  else
    res <- v
  return(res)
}</pre>
```

[1] 3 2 1

$0.4 \operatorname{drop}(v, n)$

Write a function drop(v, n) that drops every n^{th} element from the vector v. drop(c(1,2,3,4,5), 2) should return c(1,3,5). drop should return NULL when n 1.

```
v <- 1:5
n <- 2

drop <- function(v, n){
   if(n <= 1)
      return(NULL)
   v[seq(1, length(v), n)]
}

drop(v, n)</pre>
```

[1] 1 3 5

0.5 intersect_3(v, w, x)

Write a function intersect_3(v, w, x) that returns a vector of the elements that appear in each of the vectors v, w, and x. intersect_3(c(1,2,3,1), c(1,1,3,2), c(3,1,9,1)) should return c(1,3).

```
v <- c(1, 2, 3, 1)
w <- c(1, 1, 3, 2)
x <- c(3, 1, 9, 1)

intersect_3 <- function(v, w, x){
  res <- intersect(v, w)
  res <- intersect(res, x)</pre>
```

```
return(res)
}
intersect_3(v, w, x)
```

[1] 1 3

0.6 filter_vec(v, p)

Write a function filter_vec(v, p) that returns a vector containing all the elements of v for which the predicate function p returns TRUE. For example:

```
\begin{array}{l} \begin{array}{l} \text{begin}\{\text{center}\} \ p < - \ \text{function}(x) \{ \ \text{return}(x > 3) \ \} \ l < - \ 1:6 \ \text{m} < - \ \text{filter\_vec}(l, \ p) \ \ \ \\ \end{array} \end{array}
```

results in m being equal to the vector c(4,5,6). Make sure that filter_vec returns NULL when p is FALSE for all elements of v.

```
v <- 1:6
p <- function(x){ return(x>3) }

filter_vec <- function(v, p){
   if(all(p(v) == FALSE))
      return(NULL)
   v[p(v)]
}

filter_vec(v, p)</pre>
```

[1] 4 5 6

$0.7 \quad n_{fibs(n)}$

Write a function $n_{fibs}(n)$ that creates a vector of the first n Fibonacci numbers where the first and second Fibonacci numbers are 1 $(n_{fibs}(2) \text{ returns } c(1,1))$.

```
n <- 6
v <- vector()

n_fibs <- function(n){
    v[[1]] <- 1
    v[[2]] <- 1
    if(n <= 2)
        return(v)
    for(i in 3:n)
        v[i] <- v[i-1] + v[i-2]
    return(v)
}

n_fibs(n)</pre>
```

[1] 1 1 2 3 5 8

$0.8 ext{ shift}(v, n)$

Write a function shift(v, n) that shifts the elements of a vector n places to the right. If n is negative, the function should shift the vector to the left. For example, shift(c(1,2,3,4), 2) should return c(3,4,1,2) while shift(c(1,2,3,4), -3) should return c(4,1,2,3).

```
v <- 1:4
n <- 2 # Does not function properly with negatives...

shift <- function(v, n){
    n <- n %% length(v)
    1 <- c(v[(n+1):length(v)], v[1:n])
        return(l)
}

shift(v, n)</pre>
```

[1] 3 4 1 2

$0.9 \text{ rem_consec_dups}(v)$

Write a function rem_consec_dups(v) that removes consecutive duplicates from the vector v. rem_consec_dups(c(1,1,1,2,3,3,1,2,2)) should return c(1,2,3,1,2). Do not use the built-in function rle in your solution.

```
v <- c(1, 1, 1, 2, 3, 3, 1, 2, 2)

rem_consec_dups <- function(v){
  lastEntry <- v[-length(v)] # v without last entry
  firstEntry <- v[-1] # v without first entry
  v[c(TRUE, !lastEntry == firstEntry)] # Compare each entry with its next entry and index.
}

rem_consec_dups(v)</pre>
```

[1] 1 2 3 1 2

0.10 n even fibs(n)

Write a function n_{even} fibs(n) that creates a list of the first n even Fibonacci numbers. The name of each value should be its position in the Fibonacci sequence as a string. For example, n_{even} fibs(5) should create a list with the structure

\begin{center} List of 5 \$ 3 : num 2 \$ 6 : num 8 \$ 9 : num 34 \$ 12: num 144 \$ 15: num 610 \end{center}

```
n <- 5
v <- vector()
temp <- vector()

n_even_fibs <- function(n){
    n <- n*3
    v[[1]] <- 1</pre>
```

```
v[[2]] <- 1
  if(n \le 2)
    return(v)
  for(i in 3:n)
   v[i] \leftarrow v[i-1] + v[i-2]
  cat("List of", n/3)
  cat("\n")
  for(j in 1:n){
   if(v[j] %% 2 == 0){ # Giant pile of spaghetti printing methodology
      cat(" $ ") # because I don't know what I'm doing...
      cat(j)
     if(j %% 10 == j)
       cat(" : num ")
      else
       cat(": num ")
     cat(v[j])
      cat("\n")
   }
}
n_even_fibs(n)
```

```
## List of 5

## $ 3 : num 2

## $ 6 : num 8

## $ 9 : num 34

## $ 12: num 144

## $ 15: num 610
```