

UNIVERSITY OF MISSOURI-COLUMBIA  
COLLEGE OF ENGINEERING  
DEPARTMENT OF ELECTRICAL ENGINEERING AND COMPUTER SCIENCE  
**CS 8050 – DESIGN AND ANALYSIS OF ALGORITHMS II**  
**Fall 2025**

**ASSIGNMENT 5: EXPLORING DIVERSE MACHINE LEARNING ALGORITHMS**

**Due Date: Wednesday Dec 10<sup>th</sup>, 2025, at 5:00 pm**  
**(100 points)**

## Goals

This assignment requires students to examine machine learning algorithms from an algorithmic and complexity-theoretic perspective. Students must analyze selected algorithms focusing on computational structure, time and space complexity, convergence behavior, scalability, and theoretical bounds.

## Key Areas of Investigation:

You must select one algorithm from each of the following five categories.

### 1. Supervised Learning Algorithms:

- Linear Regression (Normal Equation vs. Gradient Descent)
- Decision Trees (ID3, CART)
- Support Vector Machines (primal vs. dual, kernel dependence)
- Feedforward Neural Networks (one-hidden-layer MLP)

### 2. Unsupervised Learning Algorithms:

- k-Means Clustering
- Hierarchical Clustering (agglomerative)
- Principal Component Analysis (SVD-based)

### 3. Reinforcement Learning Algorithms:

- Q-Learning
- SARSA
- Policy Gradient (REINFORCE)
- Deep Q-Networks (DQN)

### 4. Ensemble Learning Algorithms:

- Random Forests
- Gradient Boosting Machines (GBM or XGBoost)
- Bagging or Stacking

### 5. Neural Network Architectures:

- Convolutional Neural Networks (CNN)
- Recurrent Neural Networks (RNN, LSTM)
- Transformer Encoder Block

**Required Analysis for Each Algorithm:**

- Algorithm Description (Theoretical): Definition, pseudocode, data structures.
- Time Complexity: Worst-case, best-case, and average-case; expressed in terms such as;  $n$  (number of training samples),  $d$  (number of features per sample),  $k$  (number of clusters/classes/components/trees, depending on algorithm),  $p$  (number of model parameters (e.g., weights in a neural network)).
- Space Complexity: Memory footprint, model storage, workspace usage.
- Convergence and Termination Analysis: Guarantees, rates, and failure cases.
- Data-Dependent Complexity: Effects of dimensionality, sparsity, depth, kernel selection, etc.
- Algorithmic Strengths and Weaknesses: Scalability, bottlenecks, and computational trade-offs.
- Comparative Analysis Across Algorithms: Efficiency, scalability, and complexity-based trade-offs.

**Submission Format**

File Type	Description
<b>PDF Report (Mandatory)</b>	Your professionally formatted and finalized 12–18-page report (including figures and references).
<b>Code Folder (Optional)</b>	Scripts, notebooks, datasets used.
<b>Any Extra Figures/Diagrams</b>	If not embedded in the report, attach separately.

**Assignment Grading Rubric (Total: 100 Points)**

Category	Criteria	Description of Expectations	Points
<b>A. Literature Review</b>	Coverage of Foundations	Explains theoretical basis, algorithm structure, and key concepts with accuracy and depth.	5
	Use of Academic Sources	Integrates high-quality research papers and authoritative ML/algorithmic references.	5
	Critical Understanding	Demonstrates synthesis, not just description; compares viewpoints where relevant.	5
<b>Subtotal</b>			<b>15</b>
<b>B. Algorithmic &amp; Complexity Analysis</b>	Time Complexity	Correct derivation of worst, best, and average-case time complexities using variables such as $n$ , $d$ , $k$ , $p$ , $T$ .	10
	Space Complexity	Clear understanding of memory usage, model storage, and runtime workspace.	5
	Case-Based Behavior	Discusses how runtime changes with data conditions, dimensionality, initialization, or structure.	10
	Convergence Analysis	Includes mathematical or conceptual discussion of convergence conditions and iteration bounds.	5
	Data-Dependent Complexity	Evaluates how sparsity, feature size, model width, or sampling strategy affects runtime.	5
	Correct Pseudocode	Provides accurate algorithmic pseudocode with appropriate notation.	5
<b>Subtotal</b>			<b>40</b>
<b>C. Experimental / Theoretical Demonstration</b>	Methodology	Clearly explains experimental or theoretical setup used to study computational behavior.	5
	Evidence of Complexity Trends	Provides charts/tables/time measurements or analysis supporting theoretical claims.	5
	Interpretation	Connects empirical results to theoretical complexity and explains discrepancies.	5
<b>Subtotal</b>			<b>15</b>
<b>D. Comparative Analysis</b>	Cross-Algorithm Comparison	Compares algorithms based on complexity, scalability, and computational structure.	6
	Bottleneck Discussion	Identifies which operations dominate runtime and under what data conditions.	6
	Insightful Conclusions	Draws meaningful conclusions about algorithm suitability across scenarios.	3
<b>Subtotal</b>			<b>15</b>
<b>E. Writing, Formatting &amp; Presentation</b>	Organization & Clarity	Logical flow, proper section labeling, readability.	5
	Tables, Figures & Diagrams	Uses visuals to communicate complexity, architecture, or results effectively.	5
	Academic Style & Citation	Proper citation of all sources, no plagiarism, polished grammar.	5
<b>Subtotal</b>			<b>15</b>
		<b>TOTAL</b>	<b>100</b>