

## Assignment 1 (15 points)

We want to estimate the underlying probability ( $\theta^*$ ) that a coin falls with head up within  $\epsilon$  by tossing the coin  $n$  times. The probability that the estimate ( $\theta$ ) is out of the bound  $\epsilon$  (i.e.,  $P(|\theta - \theta^*| \geq \epsilon)$ , also called the failure probability) is related to both  $n$  and  $\epsilon$  according to the formula  $P(|\theta - \theta^*| \geq \epsilon) \leq 2e^{-2n\epsilon^2}$ .

- (1) Given the relation above, assuming we want the probability that estimate ( $\theta$ ) is within  $\epsilon$  is at least  $1 - \delta$  (i.e.,  $P(|\theta - \theta^*| < \epsilon) \geq 1 - \delta$ ), please prove that the number ( $n$ ) of flips of the coin must satisfy the following inequality (10 points).

$$n \geq \frac{\ln(2/\delta)}{2\epsilon^2}$$

- (2) If  $\epsilon = 0.1$  and  $\delta = 0.05$ , which is the minimum  $n$  that meets the requirement (5 points)