

Clustering: K-Means

Exercise:

- Consider the 1-dimensional data set with 10 data points  $\{1, 2, 3, \dots, 10\}$ . Show three iterations of the k-means algorithms when  $k = 2$ , and the random seeds are initialized to  $\{1,2\}$ . Repeat the problem with random seeds  $\{2,9\}$ . How did the different choice of the seed set affect the quality of the results?

**Use Manhattan**  $|m_1 - x_i|$   $|m_2 - x_i|$   $i=1$  to  $10$

Solution:

$x_i$	$m_1(1)$	$m_2(2)$	MANHATTAN		
1	0	1			
2	1	0			
3	2	1			
4	3	2			
5	4	3			
6	5	4			
7	6	5			
8	7	6			
9	8	7			
10	9	8			
INITIAL:	$C1=\{1\}$	$C2=\{2,3,4,5,6,7,8,9,10\}$	6		
dp	$m_1(1)$	$m_2(6)$			
1	0	5			
2	1	4			
3	2	3			
4	3	2			
5	4	1			
6	5	0			
7	6	1			
8	7	2			
9	8	3			
10	9	4			
ITERATION 1	$C1=\{1,2,3\}$	$C2=\{4,5,6,7,8,9,10\}$	7		

dp	m1(2)	m2(7)			
1	1	6			
2	0	5			
3	1	4			
4	2	3			
5	3	2			
6	4	1			
7	5	0			
8	6	1			
9	7	2			
10	8	3			
ITERATION 2:	C1={1,2,3,4}	2.5	C2={5,6,7,8,9,10}		7.5
dp	m1(2.5)	m2(7.5)			
1	1.5	6.5			
2	0.5	5.5			
3	0.5	4.5			
4	1.5	3.5			
5	2.5	2.5			
6	3.5	1.5			
7	4.5	0.5			
8	5.5	0.5			
9	6.5	1.5			
10	7.5	2.5			
ITERATION 3: c1={1,2,3,4,5}					
	c2={6,7,8,9,10}				

- √ With the initial seed as {2,9}; the quality of the algorithm is improvised, and the algorithm converges in the first iteration itself.
- √ Initial: C1(m1=2) = {1,2,3,4,5}  
C2(m2=9) = {6,7,8,9,10}
- √ Iteration 1: C1(m1=3) = {1,2,3,4,5}  
C2(m2=8) = {6,7,8,9,10}