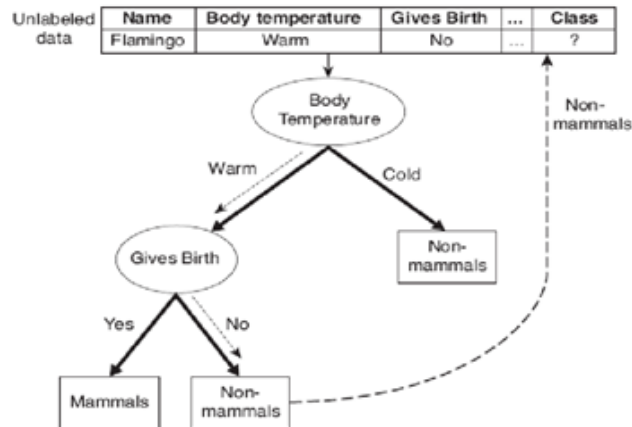


**DEPARTMENT OF COMPUTER SCIENCE AND ENGINEERING**
**MID SEMESTER EXAMINATION-II**

Course Title with code	Data Mining, 18CS54	Maximum Marks	30 Marks
Date and Time	30/12/2021, 9.30am to 10.30am		
Course Instructor(s)	Dr. Vijaya Shetty S, Dr. Sujata Joshi, Dr. Vani V		
SCHEME AND SOLUTION			

Q. No	Question	MA X MA RKS
1. a	<p><b>Solution</b></p> <ul style="list-style-type: none"> <li>We can solve a classification problem by asking a series of carefully crafted questions about the attributes of the test record.</li> <li>Each time we receive an answer? a follow-up question is asked until we reach a conclusion about the class label of the record.</li> <li>The series of questions and their possible answers can be organized in the form of a decision tree, which is a hierarchical structure consisting of nodes and directed edges.</li> <li>The tree has three types of nodes:             <ul style="list-style-type: none"> <li>A root node that has no incoming edges and zero or more outgoing edges.</li> <li>Internal nodes, each of which has exactly one incoming edge and two or more outgoing edges.</li> <li>Leaf or terminal nodes, each of which has exactly one incoming edge and no outgoing edges.</li> </ul> </li> <li>In a decision tree, each leaf node is assigned a class label. The non-terminal nodes, which include the root and other internal nodes, contain attribute test conditions to separate records that have different characteristics.</li> </ul> <div style="text-align: center;"> <pre> graph TD     Root([Body Temperature]) -- Warm --&gt; IB([Gives Birth])     Root -- Cold --&gt; NM1[Non-mammals]     IB -- Yes --&gt; M[Mammals]     IB -- No --&gt; NM2[Non-mammals]     style Root stroke-dasharray: 5 5     style IB stroke-dasharray: 5 5     style M stroke-dasharray: 5 5     style NM2 stroke-dasharray: 5 5             </pre> <p>A decision tree for the mammal classification problem.</p> </div> <ul style="list-style-type: none"> <li><b>Classifying a test record</b> is straightforward once a decision tree has been constructed. Starting from the root node, we apply the test condition to the record and follow the appropriate branch based on the outcome of the test.</li> </ul>	4M



Classifying an unlabeled vertebrate. The dashed lines represent the outcomes of applying various attribute test conditions on the unlabeled vertebrate. The vertebrate is eventually assigned to the Non-mammal class.

2M

1. b

**Scheme:**

Coverage:2m

Accuracy:2m

**Solution:**rule: (Give Birth = yes)  $\wedge$  (Blood Type = warm)  $\rightarrow$  Mammals

2M

$$\text{Coverage}(r) = \frac{|A|}{|D|}$$

$$= 6 \cdot 100 / 20 = 30\%$$

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$$\text{Accuracy}(r) = \frac{|A \cap y|}{|A|},$$

$$= 6 \cdot 100 / 6 = 100\%$$

2M

1. c

**Normalization: 2m****Euclidian distance:2m****Prediction with result:1m****Solution :**

After standardizing the input attributes Height and weight between 0 and 1 range using min-max normalization.

$$v'_i = \frac{v_i - \min_A}{\max_A - \min_A} (\text{new\_max}_A - \text{new\_min}_A) + \text{new\_min}_A.$$

Query Eample: Height=0.2 weight=0.3			k=3		
Height	Weight	Euclidian distance from query example $d(p, q) = \sqrt{\sum_i (p_i - q_i)^2}$	Rank min distance	Distance included	Class
0	0	0.36	4	no	
1	0.6	0.85	7	no	
0.6	1	0.81	6	no	
0.4	0.7	0.45	5	no	
0.3	0.2	0.14	2	no	Normal
0.5	0.3	0.3	3	yes	Underweight
0.1	0.4	0.14	1	yes	Normal

- Use simple majority of the category of nearest neighbors as the prediction value of the query instance

5

- We have 2 Normal and 1 Underweight, since  $2 > 1$ , we conclude that the person in the query example with height = 170cm and weight=57kg is included in Normal category

2. a Consider the following 5 transactions and 6 items. Shown in Table 2.1 With the help of **Apriori algorithm** find the association rules with **50% support** and **75% confidence**

8

Table 2.a Dataset

TID	Items Bought
1	A,B,C,D
2	A,B,D
3	A,E,F
4	A,D,E
5	B,D,E

**Solution**

First find  $L_1$ . 50% support requires that each frequent item appear in at least three transactions. Therefore,  $L_1$  is given by:

A	4
B	3
D	4
E	3

The candidate 2-itemsets or  $C_2$  therefore has six pairs. These pairs and their frequencies are:

A,B	2
A,D	3
A,E	2
B,D	3
B,E	1
D,E	2

$L_2$  has only two frequent item pairs {A, D} and {B, D}. After these two frequent pairs, there are no candidate 3-itemsets (since we do not have two 2-itemsets that have the same first item).

The two frequent pairs lead to the following possible rules:

**A  $\rightarrow$  D**

**D  $\rightarrow$  A**

**B  $\rightarrow$  D**

**D  $\rightarrow$  B**

The confidence of these rules is obtained by dividing the support for both items in the rule by the support of the item on the left-hand side of the rule.

The confidence of the four rules therefore are

$$3/4 = 75\% (A \rightarrow D)$$

$$3/4 = 75\% (D \rightarrow A)$$

$$3/3 = 100\% (B \rightarrow D)$$

$$3/4 = 75\% (D \rightarrow B)$$

Since all of them have a minimum 75% confidence, they all qualify as association rules.

	<p><b>Marking Scheme:</b> L1 : 2 Marks, frequency and support calculation C2 : 1 Mark, L2 : 2 Marks, frequency and support calculation Confidence calculation: 2 Marks Conclusion: 1 Mark</p>																							
2. b	<p>Write the pseudocode for the frequent itemset generation part of the Apriori algorithm.</p> <p><b>Solution:</b></p> <hr/> <p><b>Algorithm 6.1</b> Frequent itemset generation of the <i>Apriori</i> algorithm.</p> <hr/> <pre>1: <math>k = 1</math>. 2: <math>F_k = \{ i \mid i \in I \wedge \sigma(\{i\}) \geq N \times \text{minsup} \}</math>.    {Find all frequent 1-itemsets} 3: <b>repeat</b> 4:   <math>k = k + 1</math>. 5:   <math>C_k = \text{apriori-gen}(F_{k-1})</math>.    {Generate candidate itemsets} 6:   <b>for each</b> transaction <math>t \in T</math> <b>do</b> 7:     <math>C_t = \text{subset}(C_k, t)</math>.    {Identify all candidates that belong to <math>t</math>} 8:     <b>for each</b> candidate itemset <math>c \in C_t</math> <b>do</b> 9:       <math>\sigma(c) = \sigma(c) + 1</math>.    {Increment support count} 10:    <b>end for</b> 11:  <b>end for</b> 12:  <math>F_k = \{ c \mid c \in C_k \wedge \sigma(c) \geq N \times \text{minsup} \}</math>.    {Extract the frequent <math>k</math>-itemsets} 13: <b>until</b> <math>F_k = \emptyset</math> 14: <b>Result</b> = <math>\bigcup F_k</math>.</pre> <hr/> <p><b>Marking Scheme:</b> 4 marks for writing down all the steps and partial marks can be given based on the writeup.</p>	4																						
2. c	<table><tr><th>Transaction ID</th><th>Items Bought</th></tr><tr><td>1</td><td>{Milk, Beer, Diapers}</td></tr><tr><td>2</td><td>{Bread, Butter, Milk}</td></tr><tr><td>3</td><td>{Milk, Diapers, Cookies}</td></tr><tr><td>4</td><td>{Bread, Butter, Cookies}</td></tr><tr><td>5</td><td>{Beer, Cookies, Diapers}</td></tr><tr><td>6</td><td>{Milk, Diapers, Bread, Butter}</td></tr><tr><td>7</td><td>{Bread, Butter, Diapers}</td></tr><tr><td>8</td><td>{Beer, Diapers}</td></tr><tr><td>9</td><td>{Milk, Diapers, Bread, Butter}</td></tr><tr><td>10</td><td>{Beer, Cookies}</td></tr></table> <p>Consider the market basket transactions shown in Table 2.c to answer (a) and (b)</p> <p>(a) What is the maximum number of association rules that can be extracted from this data (including rules that have zero support)?</p> <p>(b) What is the maximum size of frequent itemsets that can be extracted (assuming minsup &gt; 0)?</p> <p><b>Solution:</b></p> <p>(a) Milk, Beer, Diaper, Butter, Cookies, Bread =&gt; 6 items d = 6, <math>3^d - 2^{d+1} + 1 = 602</math> <b>rules</b></p> <p>(b) Maximum size frequent itemset extracted from the given with minsup&gt;0: 4 {Milk, Diapers, Bread , Butter}.</p> <p><b>Marking Scheme</b></p> <p>(a) 2 Marks (b) 1 Mark</p>	Transaction ID	Items Bought	1	{Milk, Beer, Diapers}	2	{Bread, Butter, Milk}	3	{Milk, Diapers, Cookies}	4	{Bread, Butter, Cookies}	5	{Beer, Cookies, Diapers}	6	{Milk, Diapers, Bread, Butter}	7	{Bread, Butter, Diapers}	8	{Beer, Diapers}	9	{Milk, Diapers, Bread, Butter}	10	{Beer, Cookies}	3
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3. a	<p><b>Scheme</b></p> <p>i. Overall Entropy : 1 mark Info Gain(Temperature)=2 marks Info Gain(Wind)=2 marks</p>	6																						

- ii. Best attribute - 0.5 mark  
 iii. Attribute used as the first split – 0.5 mark

**Solution**

- i. Entropy at a given node t:

$$Entropy(t) = -\sum_j p(j|t) \log p(j|t)$$

Where  $p(j|t)$  is the relative frequency of class j at node

- Overall Entropy Entropy(Temperature)

No. of positive examples = 9, No. of negative examples = 5

Overall Entropy =  $-9/14 \log 9/14 - 5/14 \log 5/14 = 0.940$

- Entropy(Temperature)

The counts for this attribute are:

	Hot	Mild	Cool
No	2	2	1
Yes	2	4	3

Entropy(Temperature=Hot) =  $-2/4 \log 2/4 - 2/4 \log 2/4 = 1.00$

Entropy(Temperature=Mild) =  $-2/6 \log 2/6 - 4/6 \log 4/6 = 0.918$

Entropy(Temperature=Cool) =  $-1/4 \log 1/4 - 3/4 \log 3/4 = 0.811$

Entropy(Temperature) =  $4/14 * 1.00 + 6/14 * 0.918 + 4/14 * 0.811 = 0.911$

Info gain(Temperature) = Overall Entropy - Entropy(Temperature) =  $0.940 - 0.911 = 0.029$

- Entropy(Wind)

The counts for this attribute are:

	Weak	Strong
No	2	3
Yes	6	3

Entropy(Wind=Weak) =  $-2/8 \log 2/8 - 6/8 \log 6/8 = 0.811$

Entropy(Wind=Strong) =  $-3/6 \log 3/6 - 3/6 \log 3/6 = 1.00$

Entropy(Wind) =  $8/14 * 0.811 + 6/14 * 1.00 = 0.892$

Info gain(Wind) = Overall Entropy - Entropy(Wind) =  $0.940 - 0.892 = 0.048$

- ii. According to the information gain measure, the best split among temperature and wind is Wind as the info gain of Wind is 0.048 which is greater than that of the temperature which is 0.029
- iii. The decision tree algorithm uses the attribute “Wind” as the first split

3. b) a)

$$\text{FOIL's information gain} = p_1 \times \left( \log_2 \frac{p_1}{p_1 + n_1} - \log_2 \frac{p_0}{p_0 + n_0} \right)$$

Assume the initial rule is  $\emptyset \rightarrow +$ . This rule covers  $p_0 = 100$  positive examples and  $n_0 = 400$  negative examples.

The rule  $R_1$  covers  $p_1 = 4$  positive examples and  $n_1 = 1$  negative example. Therefore, the FOIL's information gain for this rule is

$P_0=100, n_0=400$   
 $P_1=4, n_1=1$

$$4 \times \left( \log_2 \frac{4}{5} - \log_2 \frac{100}{500} \right) = 8.$$

2.5m

The rule  $R_2$  covers  $p_1 = 30$  positive examples and  $n_1 = 10$  negative example. Therefore, the FOIL's information gain for this rule is

$$30 \times \left( \log_2 \frac{30}{40} - \log_2 \frac{100}{500} \right) = 57.2.$$

According to Foil's information gain,  $R_2$  is the best rule and  $R_1$  is the worst rule.

b)

The Laplace measure.

$$\text{Laplace} = \frac{f_+ + 1}{n + k}$$

**Answer:**

The Laplace measure of the rules are 71.43% (for  $R_1$ ) and 73.81% (for  $R_2$ )

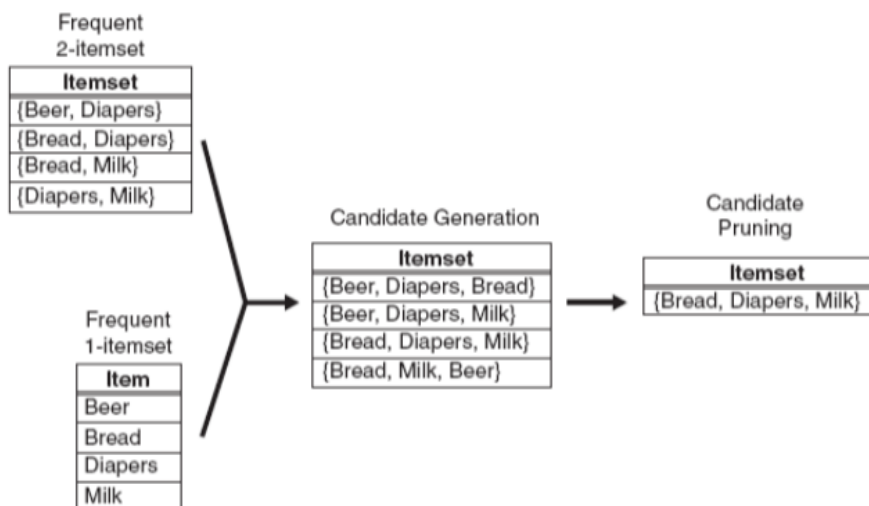
Therefore  $R_2$  is the best candidate and  $R_1$  is the worst candidate according to the Laplace measure.

2.5m

3. c  $F_{k-1} \times F_1$  Method of candidate generation and pruning.

This is a method for candidate generation. The idea here is to extend each frequent  $(k - 1)$ -itemset with other frequent items. As shown in the figure, we can see that a frequent 2-itemset such as {Beer, Diapers} can be augmented with a frequent item such as Bread to produce a candidate 3-itemset {Beer, Diapers, Bread}. This method will produce  $O(|F_{k-1}| \times |F_1|)$  candidate  $k$ -itemsets, where  $|F_j|$  is the number of frequent  $j$ -itemsets.

2m



Generating and pruning candidate  $k$ -itemsets by merging a frequent  $(k - 1)$ -itemset with a frequent item. Note that some of the candidates are unnecessary because their subsets are infrequent.

2m

- The procedure is complete because every frequent  $k$ -itemset is composed of a frequent  $(k - 1)$ -itemset and a frequent 1-itemset.
- Avoid generating duplicate candidates by ensuring that the items in each frequent itemset are kept sorted in their lexicographic order. Each frequent  $(k-1)$ -itemset  $X$  is then extended with frequent items that are lexicographically larger than the items in  $X$ .
- For example, the itemset {Bread, Diapers} can be augmented with {Milk} since Milk is lexicographically larger than Bread and Diapers. However, we should not augment {Diapers, Milk} with {Bread} nor {Bread, Milk} with {Diapers} because they violate the

lexicographic ordering condition.

- For every candidate  $k$ -itemset that survives the pruning step, every item in the candidate must be contained in at least  $k - 1$  of the frequent  $(k - 1)$ -itemsets. Otherwise, the candidate is guaranteed to be infrequent.