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TUTORIAL-

- Ans-1 Asymptotic Notation: Are the mathematical notations used to describe the running time of an algorithm when the input tends towards a particular value or a limiting value.
 - 1) Big-O notation It describes the worst case complexity of an algorithm. It gives the upper bound of a program/algo. eg. O(log n) describes the Big O of binary search algo.
 - 2) Big-O notation → It specifies both upper and lower bounds for a function and provides the average time complexity of an algo.
 - 3) Big-12 notation It specifies the lower bound for a function i-e it describes the best case running time of a program. eg. bubble Sort Big-12 complexity is 12 (N) when the away is sorted.

- 4) Small-0 notation → It is used to describe an upper bound that cannot be tight i.e it provides loose upper bound of f(n).
- 5) Small omega notation -> It denotes the lower bound (that is not asymptotically tight) on the growth rate of runtime of an algo:

Ans-2

for (i=1 to N)
$$\{i=i*2; \}$$
 $i=1,2,4- i=2^{\circ},2^{\circ},2^{\circ},--n$

This is a GP

 $a=1,r=2/1=2$
 $t_{k}=ar^{k-1}$
 $an=a^{k}$
 $log_{2}2+log_{2}n=klog_{2}2$
 $k=1+lg_{2}n$
 $k \propto log_{2}n \Rightarrow O(log_{2}n)$ hy

 $\sum_{i=1}^{N} (1+1+...log_{2}n) = O(log_{2}n)$

$$T(n) = 3(3T(n-2))$$

$$T(n) = 9 T(n-2)$$

$$T(n) = 27 T(n-3)$$

$$T(n) = 3^k T(n-k)$$

assume n-k=0 => n=k

$$T(n) = 3^n \cdot T(0)$$

Ans-4

$$T(n) = 2T(n-1) - 1 - 0$$

$$T(n-1) = 2T(n-2) - 1$$

$$T(n) = 4T(n-2)-2-1-2$$
put $n=n-2$ in (1)
$$T(n-2) = 2T(n-3)-1$$
Substitute in (2)
$$T(n) = 4\left[2T(n-3)-1\right]-2-1$$

$$T(n) = 8T(n-3)-4-2-1$$

$$T(n) = 2^{k}T(n-k)-\left(2^{k}+2^{k}+2^{k}-2^{k}-1\right)$$

$$= 2^{k}T(0)-1\cdot\left(2^{k}-1\right)$$

$$= 2^{k}T(0)-1\cdot\left(2^{k}-1\right)$$

$$= 2^{k}-2^{k}+1$$

$$T(n) = 2^{k}-2^{k}+1$$

$$T(n) = 1$$

int
$$i=1, s=1;$$

while $(s < = n)$ {

 $i++;$ $\rightarrow O(i)$
 $s+=i;$ $\rightarrow O(i)$

print $("#");$ $\rightarrow O(i)$

}

difference in AP

$$T_n = AK^2 + BK + C$$

putting K=1

putting K= 2

putting K=3

solving (1), (2) 2(3)

$$T(n) = \frac{k^2}{2} + \frac{k}{2} = \frac{k(k+1)}{2}$$
, $n < \frac{k(k+1)}{2}$

Time Complexity = O(Vn) Any

$$n = Ak^2 + Bk + C$$

$$N = K^2$$

Ans-7 i j k

$$1/2$$
 log n log n x log n

 $1/2+1$ log n log n x log n

i log n log n x log n

$$\Rightarrow O(n \times (\log_2 n)^2)$$
 Any

Ans-8

$$(n-3)$$
, $(n-6)$, $(n-9)$, $-- (1)$ $\rightarrow k$ terms $a = n-3$, $d = n-6-n+3 = -3$

$$1 = (n-3) + (k-1)(-3)$$

$$1 = (n-3) - 3k + 3$$

$$1 = n-3/3 + 3$$

$$3k = n-1$$

$$k = \frac{n-1}{3}$$

$$\Rightarrow$$
 $O(n^3)$ Ay

 $O(n \times n^2)$

for
$$i=1$$
, $j=n$ times $i=2$, $j=n/2$ times $i=3$, $j=n/3$ times $i=k$, $j=n/k$ times $i=k$, $j=n/k$ times $i=n$, $j=n/n$ times

Total time complexety=
$$n + \frac{n}{2} + \frac{n}{3} + \dots + \frac{n}{n}$$

 $n * (1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n})$
 $\log n$

$$1 + \frac{1}{2} + \frac{1}{3} + \dots + \frac{1}{n} = \frac{2}{K_{-1}} \frac{1}{K}$$

$$= \log n + O(1)$$

$$O(\log n \times n) \Rightarrow O(n \log n) \text{ Arg}$$

Ans-10

$$f(n) = n^{k}$$
, $g(n) = c^{n}$
where $K > = 1$ $f(n) = 1$
Let $f(n) = 1$ $f(n) = 1$
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Satisfies O notation

$$f(n) \leq c \cdot g(n)$$

$$n_{o}^{1} = c_{o} \cdot 2^{n_{o}}$$

$$\left(\frac{n_o}{C_o}\right)^1 = \left(2\right)^{n_o}$$

Comparing, no=1

$$\frac{n_o}{C_o} = 2$$

$$\frac{1}{2} = c_0$$

$$f(n) \leq 0.5g(n)$$

$$f(n) = 0 g(n)$$