TUTORIAL-4

1)
$$T(n) = 3T(n/2) + n^2$$

 $a = 3, b = 2$
 $n\log b^a = n\log 2^3$
 $n^2 > n\log 2^3$
 $n = 0$

2)
$$T(n) = 4T(\frac{\eta}{2}) + n^{2}$$

 $a = 4, b = 2$
 $n^{\log_{b}q} = n^{\log_{2}4} = n^{2}$
 $n^{2} = n^{2}$
 $one{a} = n^{2}$

3)
$$T(n) = T(n/2) + 2^n$$

$$a = 1, b = 2$$

$$n \log_b a = n \log_2 1 = 1$$

$$1 < 2^n$$

$$n = 0 (2^n)$$

- 4) $T(n) = 2^n \tau(n/2) + n^2$ Marter th. not applicable as a is func of n.
- 5) T(n) = 16T(n/4) + n a = 16, b = 4, f(n) = n $n \log_b a = n^2$ $n^2 > n$ $o \theta(n^2)$
- 6) $T(n) = 2T(n/2) + n\log n$ $a = 2, b = 2, f(n) = n\log n$ $n\log a = n\log 2^2 = n$ f(n) > n $o = T(n) = 0 (n\log n)$
 - 7) $T(n) = 2T(n/2) + n/\log n$ a = 2, b = 2 $n \log a = n$ n > f(n)i. T(n) = O(n)
- 8) $T(n) = 2T(\gamma_4) + n^{0.51}$ $a = 2, b = 4, f(n) = n^{0.51}$ $n^{\log_b a} = n^{\log_4 2} = n^{0.5}$ $n^{0.51} > n^{0.5}$ $T(n) = O(n^{0.51})$

10)
$$T(n) = 16T(n) + n!$$

 $a = 16, 6 = 4, f(n) = n!$
 $n \log_b a = n^2$
 $n! > n^2$
 $T(n) = O(n!)$

11)
$$T(n) = 4T(\frac{n}{2}) + \log n$$

 $a = 4, b = 2$
 $n \log_b a = n^2$
 $n^2 > f(n)$
 $\therefore T(n) = O(n^2)$

13)
$$T(n) = 3T(n/2) + n$$

$$a = 3, b = 2$$

$$n \log_b a = n \log_2 3 = n^{1.58}$$

$$n^{1.58} > f(n)$$

$$\therefore T(n) = O(n^{\log_2 3})$$

14)
$$T(n) = 3T(n)_3) + \sqrt{n}$$
 $a = 3, b = 3$
 $n \log_b a = n$
 $n > \sqrt{n}$
 $f = T(n) = O(n)$

15)
$$T(n) = 4T(n/2) + cn$$

$$a = 4, b = 2$$

$$n^{\log_b a} = n^2$$

$$n^2 > cn$$

$$\therefore T(n) = \Theta(n^2)$$

16)
$$T(n) = 3T(n/4) + n\log n$$

 $a = 3, b = 4$
 $n\log_b a = n^{0.79}$
 $n^{0.79} < n\log n$
 $n < T(n) = \Theta(n\log n)$

17)
$$T(n) = 3T(n/3) + n/2$$
 $n \log 6^{\alpha} = n$
 $n > n/2$

... $T(n) = O(n^{\frac{3}{2}} \log n)$

... $O(n) = O(n/2)$

18)
$$T(n) = 6T(n)_3) + n^2 \log n$$

$$a = 6, b = 3$$

$$n^{\log 6} = n^{\log 3} 6 = n^{1.63}$$

$$n^{1.63} < n^2 \log n$$

$$n^{1.63} < n^2 \log n$$

$$n^{1.63} < n^2 \log n$$

19)
$$T(n) = 4T(n/2) + n/\log n$$

 $a = 4, b = 2$
 $n\log 6 = n^2$
 $n^{2} > n/\log n$
 $o = 7(n) = O(n^2)$

20)
$$T(n) = 64T(78) - n^2\log n$$

Master's not applicable as $f(n)$ is not increasing func

21)
$$T(n) = T(n/3) + n^2$$

$$n^{\log_b a} = n^{1.7}$$

$$n^{1.7} < n^2$$

$$n^{1.7} < n^2$$

$$n^{1.7} < n^2$$

22)
$$T(n) = T(^{n}/_{2}) + n(2-\cos n)$$

Marter's theorem un't applicable since regularity condition is isolated in case 3.