

I have used MNIST dataset from kaggle in csv format.

```
import pandas as pd
import numpy as np
import math
df = pd.read_csv('/content/drive/MyDrive/mnist_train.csv')
```

```
print(df)
```

Using first column of dataset as label.

```
label = df.iloc[:,0]
label = pd.DataFrame(label)
# label = label.drop(0).reset_index(drop=True)
print(label)
```

I have padded the image with 0 from all direction.

This function will create 1d array to 2d array and also apply padding at the boundary of each image

```
def padding(arr):
    n = int(len(arr)**0.5)
    arr = arr.reshape(n,n)
    arr1 = [[0 for i in range(n+1)] for j in range(n+1)]
    for i in range(n):
        for j in range(n):
            arr1[i][j]=arr[i][j]
    return arr1
```

Code for making differential filter

```
x_diff = [[1,0,-1],[1,0,-1],[1,0,-1]]
y_diff = [[1,1,1],[0,0,0],[-1,-1,-1]]
```

Making Gaussian filter and random sigma and size of kernel so that hypertuning can be easy.

Code for making Gaussian filter

```
def gaussian_filter(sigma,n):
    d = 2*(np.pi)*(sigma**2)
    arr = np.zeros((n,n))
    for i in range(n):
        for j in range(n):
            x = n//2-i
            y = n//2-j
            arr[i][j] = (np.exp(-((x**2+y**2)/(2*sigma**2))))/d
    return arr
```

Code for multiply two differential and gaussian filter

```
def multiply(arr1,arr2):
```

```

arr = [[0 for i in range(len(arr1))] for j in range(len(arr1[0]))]
for i in range(len(arr1)):
    for j in range(len(arr1[0])):
        arr[i][j] = arr1[i][j]*arr2[i][j]
return arr

```

Taking the cell size of 4*4 and block size of 2*2 and computing the gradient magnitude and direction and making an array of pairs to store both values simultaneously.

Calculating Gradient magnitude and tan theta and storing these values into arr of pairs

```

def gradient(arr,f1,f2):
    arr1 = [[[0,0] for i in range(len(arr)-1)] for j in
range(len(arr[0])-1)]
    for i in range(1,len(arr)-1):
        for j in range(1,len(arr[0])-1):
            a = 0
            b = 0
            for k in range(i-1,i+2):
                for l in range(j-1,j+2):
                    a+= (arr[k][l]*f1[abs(i-1-k)][abs(j-1-l)])
                    b+= (arr[k][l]*f2[abs(i-1-k)][abs(j-1-l)])
            c = (a**2+b**2)**0.5
            d = math.atan2(b,a)
            d = math.degrees(d)
            arr1[i][j][0] = c
            arr1[i][j][1] = d
    return arr1

```

*# Calculating histogram for n*n square and storing them in array*

```

def histogram(arr):
    n = len(arr)
    m = len(arr[0])
    arr1 = np.zeros((n//4, m//4, 9))
    for i in range(0,n,4):
        for j in range(0,m,4):
            for k in range(i,i+4):
                for l in range(j,j+4):
                    a = arr[i][j][0]
                    b = arr[i][j][1]
                    c = abs((b//45)+1)*45-a
                    if b > 0:
                        # print(b)
                        ind = int(4+b//45)
                        if b == 180:
                            arr1[i//4][j//4][ind]+= a
                        else:
                            arr1[i//4][j//4][ind]+= (c/45)*a
                            arr1[i//4][j//4][ind+1]+= (45-c/45)*a
                    else:

```

```

                                ind = int(4-b//45)
                                if b==180:
                                    arr1[i//4][j//4][ind]+= (c/45)*a
                                else:
                                    arr1[i//4][j//4][ind]+= (c/45)*a
                                    arr1[i//4][j//4][ind-1]+= (45-c/45)*a

    return arr1

```

Here I will perform normalization of the array and taking e =1 to avoid division by zero that will lead to 36*36 features of image as I used 9 bins

Now We will perform normalization of the array

```

def normalization(arr):
    n,m = len(arr),len(arr[0])
    arr1 = np.zeros((n-1,m-1,36))
    r = [0,0,1,1]
    c = [0,1,0,1]
    for i in range(n-1):
        for j in range(m-1):
            arr2 = []
            norm = 1
            for k in range(4):
                ind1 = i+r[k]
                ind2 = j+c[k]
                for val in arr[ind1][ind2]:
                    arr2.append(val)
                    norm+=val**2
            norm = norm**0.5
            for k in range(36):
                arr1[i][j][k]=arr2[i]/norm

    return arr1

```

Code for making final feature vector

```

def make_vector(arr):
    arr1 = []
    for i in range(len(arr)):
        for j in range(len(arr[0])):
            for k in range(36):
                arr1.append(arr[i][j][k])
    return arr1

```

Getting Our training dataset

```

train = df.drop(df.columns[0],axis=1)
print(train.head())
print(train.values.shape)

```

Combining all these functions generating dataset which will contain features

```

data = [[]]
# Gaussian filter

```

```

gf = gaussian_filter(1,3)
xf = multiply(gf,x_diff)
yf = multiply(gf,y_diff)

new_data = train.values
for row in range(train.values.shape[0]):
    temp = padding(new_data[row])
    temp = gradient(temp,xf,yf)
    temp = histogram(temp)
    temp = normalization(temp)
    temp = make_vector(temp)
    data.append(temp)

feature_data = pd.DataFrame(data)

feature_data = feature_data.drop(0).reset_index(drop=True)


test = pd.read_csv('/content/drive/MyDrive/mnist_test.csv')

test_label = test.iloc[:,0]
test = test.drop(test.columns[0],axis=1)

new_data = test.values
test_data = [[]]
for row in range(test.values.shape[0]):
    temp = padding(new_data[row])
    temp = gradient(temp,xf,yf)
    temp = histogram(temp)
    temp = normalization(temp)
    temp = make_vector(temp)
    test_data.append(temp)

test_data = pd.DataFrame(test_data)

test_data = test_data.drop(0).reset_index(drop=True)

# Using Random forest classifier for classification problem of dataset
and predicting the values and checking the accuracy

import pandas as pd
from sklearn.ensemble import RandomForestClassifier # Import Random
Forest
from sklearn.metrics import accuracy_score
from sklearn.preprocessing import StandardScaler

scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(feature_data)
X_test_scaled = scaler.transform(test_data)

```

```
rf_classifier = RandomForestClassifier(n_estimators=100,
random_state=42) # You can tune n_estimators, etc.
rf_classifier.fit(X_train_scaled, label) # Fit the model on the
training data
```

```
y_pred = rf_classifier.predict(X_test_scaled)
```

```
accuracy = accuracy_score(test_label, y_pred)
```

```
print(f'Accuracy: {accuracy * 100:.2f}%')
```

I initially used a Random Forest Classifier for classification, which gave an accuracy of 46.39%. However, after optimizing my code with the assistance of ChatGPT and switching to a Neural Network for classification, my accuracy significantly improved to 98.41%. Although I learned a lot from the code, I unfortunately didn't have enough time to implement it from scratch, as the earlier code consumed a considerable amount of time. Below is the code that I used for the same:

```
import numpy as np
import tensorflow as tf
import cv2
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.preprocessing import StandardScaler
from sklearn.metrics import classification_report, confusion_matrix

def gaussian_filter(sigma, n):
    d = 2 * np.pi * (sigma ** 2)
    arr = np.zeros((n, n))
    center = n // 2
    for i in range(n):
        for j in range(n):
            x = i - center
            y = j - center
            arr[i, j] = np.exp(-(x ** 2 + y ** 2) / (2 * sigma ** 2))
    / d
    return arr

def multiply(arr1, arr2):
    return arr1 * arr2
```

```

def gradient(arr, f1, f2):
    arr = np.float32(arr)
    grad_x = cv2.filter2D(arr, -1, f1)
    grad_y = cv2.filter2D(arr, -1, f2)
    gradient_magnitude = np.sqrt(grad_x ** 2 + grad_y ** 2)
    gradient_angle = np.arctan2(grad_y, grad_x) * (180 / np.pi)
    return np.stack((gradient_magnitude, gradient_angle), axis=-1)

def histogram(arr, cell_size=4, bins=9):
    n, m, _ = arr.shape
    hist = np.zeros((n // cell_size, m // cell_size, bins))
    bin_edges = np.linspace(-180, 180, bins + 1)

    for i in range(0, n, cell_size):
        for j in range(0, m, cell_size):
            block = arr[i:i + cell_size, j:j + cell_size, 1]
            magnitude = arr[i:i + cell_size, j:j + cell_size, 0]
            block_angles = block.flatten()
            block_magnitudes = magnitude.flatten()
            indices = np.digitize(block_angles, bin_edges) - 1
            indices = np.clip(indices, 0, bins - 1)
            for idx, mag in zip(indices, block_magnitudes):
                hist[i // cell_size, j // cell_size, idx] += mag
    return hist

def normalization(hist, block_size=(2, 2), bins=9):
    n, m, _ = hist.shape
    norm_hist = np.zeros_like(hist)

    # Iterating over the image using block_size
    for i in range(0, n - block_size[0] + 1):
        for j in range(0, m - block_size[1] + 1):
            block = hist[i:i + block_size[0], j:j + block_size[1], :]
            block_flattened = block.flatten()
            norm = np.linalg.norm(block_flattened) # Compute the L2
norm of the block
            if norm > 0:
                norm_hist[i:i + block_size[0], j:j + block_size[1], :]
= block / norm
    return norm_hist

def make_vector(arr):
    return arr.flatten()

def extract_hog_features(image, sigma=1, n=3, cell_size=4,
block_size=(2, 2), bins=9):
    gf = gaussian_filter(sigma, n)
    sobel_x = np.array([[ -1, 0, 1], [ -2, 0, 2], [ -1, 0, 1]])
    sobel_y = np.array([[ 1, 2, 1], [ 0, 0, 0], [ -1, -2, -1]])
    if len(image.shape) == 3:

```

```

        image = cv2.cvtColor(image, cv2.COLOR_BGR2GRAY)
        grad = gradient(image, sobel_x, sobel_y)
        hist = histogram(grad, cell_size, bins)
        norm_hist = normalization(hist, block_size, bins)
        feature_vector = make_vector(norm_hist)
        return feature_vector

def train_and_evaluate(train_data, test_data, label_col=0,
test_size=0.2, epochs=10, batch_size=32):
    X_train =
train_data.drop(columns=[train_data.columns[label_col]]).values
    y_train = train_data.iloc[:, label_col].values
    X_test =
test_data.drop(columns=[test_data.columns[label_col]]).values
    y_test = test_data.iloc[:, label_col].values

    X_train_images = X_train.reshape(-1, 28, 28)
    X_test_images = X_test.reshape(-1, 28, 28)

    hog_features_train = [extract_hog_features(image) for image in
X_train_images]
    hog_features_test = [extract_hog_features(image) for image in
X_test_images]

    X_train_hog = np.array(hog_features_train)
    X_test_hog = np.array(hog_features_test)

    scaler = StandardScaler()
    X_train_hog = scaler.fit_transform(X_train_hog)
    X_test_hog = scaler.transform(X_test_hog)

    model = tf.keras.Sequential([
tf.keras.layers.InputLayer(input_shape=(X_train_hog.shape[1],)),
        tf.keras.layers.Dense(256, activation='relu'),
        tf.keras.layers.Dropout(0.5),
        tf.keras.layers.Dense(128, activation='relu'),
        tf.keras.layers.Dropout(0.5),
        tf.keras.layers.Dense(10, activation='softmax')
    ])

    model.compile(optimizer='adam',
        loss='sparse_categorical_crossentropy',
        metrics=['accuracy'])

    history = model.fit(X_train_hog, y_train, epochs=epochs,
batch_size=batch_size, validation_data=(X_test_hog, y_test))

    test_loss, test_accuracy = model.evaluate(X_test_hog, y_test)

```

```
print(f"Test Accuracy: {test_accuracy * 100:.2f}%")
```

```
train_data = pd.read_csv('/content/drive/MyDrive/mnist_train.csv')  
test_data = pd.read_csv('/content/drive/MyDrive/mnist_test.csv')
```

```
train_and_evaluate(train_data, test_data)
```