

# Week 2 Lab – Arrays & Complexity Intuition

FM121: Programming & Data Structures  
Spring Semester 2026

## Objective

To understand arrays and searching techniques, and to analyze their time complexity.

## Concepts Covered

- One-dimensional arrays
- Linear and binary search
- Time complexity basics

## Key Notes

- An array is a linear data structure that stores elements of the same data type.
- Array elements are stored in contiguous memory locations.
- Arrays are 0-indexed, meaning the first element is accessed using index 0.
- The array name represents the base address of the first element.
- Accessing an array element using its index takes constant time, i.e.,  $O(1)$ .
- Linear search checks elements sequentially and has time complexity  $O(n)$ .
- Binary search works only on sorted arrays and has time complexity  $O(\log n)$ .
- Finding minimum, maximum, or peak elements requires careful comparison of neighboring values.
- Understanding memory layout helps in deriving address calculation formulas for array elements.

# Problem 1: Linear Search for Positive Integer Values

## Problem Statement

Write a program to implement the Linear Search algorithm to search for a given positive integer in an unsorted list of positive integers.

**Logic:** The program should scan the array sequentially and report whether the element is found. If found, display the index position of the element; otherwise, display an appropriate message indicating that the element is not present.

## Objectives

- To understand the working of the Linear Search algorithm
- To analyse sequential searching in an unsorted array
- To practice array traversal and analyze the number of comparisons in best and worst case

## Input Specifications

- An integer  $n$  representing the number of elements ( $n > 0$ )
- An array of  $n$  positive integers
- A positive integer key to be searched

## Constraints

- All array elements must be positive integers
- $1 \leq n \leq 1000$

## Algorithm (Brief)

1. Read the value of  $n$
2. Read  $n$  positive integers into an array
3. Read the search key
4. Compare the key with each element sequentially
5. If a match is found, display the index and terminate
6. If the loop ends without a match, display *Element not found*

## Sample Test Cases

### Test Case 1

- Input:  $n = 5$ , Array = 12 45 7 23 9, Key = 23
- Output: Element found at index 3

### Test Case 2

- Input:  $n = 6$ , Array = 10 20 30 40 50 60, Key = 25
- Output: Element not found

### Test Case 3

- Input:  $n = 1$ , Array = 15, Key = 15
- Output: Element found at index 0

## Problem 2: Find Minimum and Maximum Elements in a Positive Integer Array

### Problem Statement

Write a program to find the minimum and maximum elements present in a given array of integers. The program should scan the array elements and determine the smallest and largest values without modifying the original array.

### Objectives

- To understand array traversal techniques
- To identify minimum and maximum values in a dataset
- To practice conditional comparison and iteration
- To analyze the efficiency of single-pass array processing

### Input Specifications

- An integer  $n$  representing the number of elements in the array ( $n > 0$ )
- An array of  $n$  integers

### Output Specifications

- Display the minimum element in the array
- Display the maximum element in the array

## Constraint

- All array elements must be integers
- $1 \leq n \leq 1000$

## Algorithm (Single Pass)

1. Read the value of  $n$
2. Read  $n$  integers into an array
3. Initialize:
  - $\text{min} = \text{array}[0]$
  - $\text{max} = \text{array}[0]$
4. Traverse the array from index 1 to  $n - 1$ 
  - If  $\text{array}[i] < \text{min}$ , update min
  - If  $\text{array}[i] > \text{max}$ , update max
5. After traversal, display the minimum and maximum values

## Sample Input

$n = 5$

Array = [2, 45, 7, 23, 9]

## Sample Output

Minimum element = 2   Maximum element = 45

## Problem 3: Binary Search for Sorted Positive Integer Values

### Problem Statement

Write a program to implement the Binary Search algorithm to search for a given positive integer in a sorted array of positive integers.

**Logic:** The program should repeatedly divide the search interval in half until the element is found or the search interval becomes empty.

### Objectives

- To understand divide-and-conquer searching techniques
- To implement Binary Search on sorted data
- To analyze the efficiency of Binary Search compared to Linear Search

## Input Specifications

- An integer  $n$  representing the number of elements ( $n > 0$ )
- A sorted array of  $n$  positive integers (ascending order)
- A positive integer key to be searched

## Output Specifications

- If the element is found, display the index position
- If the element is not found, display "Element not found"

## Constraint

- The array must be sorted in ascending order
- All elements must be positive integers
- $1 \leq n \leq 1000$

## Algorithm (Brief)

1. Read the value of  $n$
2. Read  $n$  sorted positive integers into an array
3. Read the search key
4. Set  $low = 0$ ,  $high = n - 1$
5. Repeat until  $low \leq high$ 
  - Compute  $mid = (low + high) / 2$
  - If  $array[mid] == key$ , display index and terminate
  - If  $key < array[mid]$ , set  $high = mid - 1$
  - Else set  $low = mid + 1$
6. If the element is not found, display "Element not found"

## Sample Test Cases

### Test Case 1

- Input:  $n = 7$ , Array = [ 5, 10, 15, 20, 25, 30, 35], Key = 20
- Output: Element found at index 3

### Test Case 2

- Input:  $n = 5$ , Array = [2, 4, 6, 8, 10], Key = 7

- Output: Element not found

### Test Case 3

- Input:  $n = 1$ , Array = 100, Key = 100
- Output: Element found at index 0

## Problem 4: Find Peak Element in an Integer Array

### Problem Statement

Write a program to find a peak element in a given 0-indexed integer array. A peak element is defined as an element that is strictly greater than its immediate neighbors. The program should return the index of the peak element.

### Objectives

- To understand the concept of peak elements in arrays
- To apply search techniques for identifying local maxima
- To analyze time complexity improvements over brute-force methods as well as using binary search.

### Input Specifications

- An integer  $n$  representing the number of elements in the array ( $n \geq 1$ ).
- A distinct positive integer array `nums` which is first sorted in ascending order and then in descending order.
- **Example:**

10	20	30	40	50	35	15
----	----	----	----	----	----	----

- The peak element is 50.

### Output Specifications

- An integer representing the index of a peak element

### Constraint

- $1 \leq n \leq 10^5$
- $-10^9 \leq \text{nums}[i] \leq 10^9$
- The array is **0-indexed**.

## Algorithm (Binary Search Based – Recommended)

1. Initialize  $low = 0$  and  $high = n - 1$ .
2. While  $low < high$ :
  - Compute  $mid = \frac{low+high}{2}$ .
  - If  $nums[mid] < nums[mid + 1]$ , then a peak lies on the right side.
    - Set  $low = mid + 1$ .
  - Else, a peak lies on the left side or at  $mid$ .
    - Set  $high = mid$ .
3. When  $low == high$ , return  $low$  as the peak index.

## Alternative Algorithm (Linear Scan – Basic Approach)

1. Traverse the array from index 0 to  $n - 1$ .
2. For each element, check:
  - It is greater than its left neighbor (if it exists).
  - It is greater than its right neighbor (if it exists).
3. Return the index of the first element satisfying the peak condition.

## Sample Test Cases

### Test Case 1

- Input:  $n = 4$ , Array =  $nums = [10, 20, 30, 5]$
- Output: 2 (index of element 30)
- Explanation: Element 30 at index 2 is greater than both neighbours, 20 and 10.

### Test Case 2

- Input:  $n = 6$ , Array =  $[15, 25, 41, 63, 5, 3]$
- Output: 3
- Explanation: Element 63 (index 3) is greater than both neighbours, 41 and 5.

### Test Case 3

- Input:  $n = 1$ , Array =  $[10]$
- Output: 0
- Explanation: A single element is always considered a peak.

## Reference

LeetCode 162: Find Peak Element