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Section: KRG-10

Name: Vanshit Kumar

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Q Given three integers  $n$ ,  $a$  and  $b$  return  $n^{\text{th}}$  magical no.  
Since the answer may be very large return  $10^9 + 7$  %.

A positive integer is magical if the number is divisible by either  $a$  or  $b$ .

$$n = 1, b = 3, a = 2 \\ \text{ans} = 2$$

$$n = 4, a = 2, b = 3 \\ \text{ans} = 6$$

Ans Given  $n, a, b$ .

Constraints  $\rightarrow n \rightarrow 1$  to  $10^9$   
 $a, b \rightarrow 1$  to  $10^4$

Algorithm:

1. Calculate lcm of  $a, b$ .  
set  $l = \text{lcm}(a, b)$

2. We can binary search on the answer  
in the range,  $[\min(a, b), \min(a, b) \times n]$ .  
set  $\text{low} = \min(a, b)$   
 $\text{high} = n \times \min(a, b)$

3. Binary Search:

$$\text{set } \text{mid} = (a + b) / 2$$

count no. of ~~same~~ magical no.  $< \text{mid}$ .

$$\text{set } \text{count} = \text{mid}/a + \text{mid}/b + \text{mid}/\text{lcm}(a, b)$$

if  $\text{count} < n$ :

$$\text{Set } \text{low} = \text{mid} + 1$$

else:

$$\text{set } \text{high} = \text{mid} - 1$$

$$4. \text{Ans} = \text{low} \% 10^9 + 7$$



Time Complexity:  $O(\log(n \times \min(a, b)))$

Space Complexity:  $O(1)$

### Explanation:

- We use binary search on the range of the answer.
- We check for the smallest no. which has magical number count  $\geq n$ .
- For counting no. of magical numbers,  
$$\text{count} = \frac{x}{a} + \frac{x}{b} - \frac{x}{\text{lcm}(a, b)}$$

We decremented the nos. counted twice with the use of calculated LCM.

TC 1:

$$n=1, a=2, b=3$$

$$\text{magical no.s} = 2 \ 3 \ 4 \ 6$$

$$\text{Ans} = 2.$$

TC 2:

$$n=4, a=2, b=3$$

$$\text{magical no.s} = 2 \ 3 \ 4 \ 6 \ 8 \ 9$$

$$\text{Ans} = 6.$$