

UID: 230CS10087

Experiment - 4.

Name: Vanshit Kumar

We define $f(x, y)$ as

number of different corresponding bits in the binary representation of x and y . For example, $f(2, 7) = 2$, since the binary representation of 2 and 7 are 010 and 111, respectively. The first and third bit differ, so $f(2, 7) = 2$. You are given an array of N positive integers, A_1, A_2, \dots, A_N . Find sum of $f(A_i, A_j)$ for all pairs (i, j) such that $1 \leq i, j \leq N$. Return the answer modulo $10^9 + 7$.

Constraints

$$2 \leq N \leq 10^5$$

$$1 \leq A[i] \leq 2^{31} - 1$$

Approach \rightarrow

- ① We will create a frequency array of counting ^{number} for each position in binary representation that how many ~~bits~~ are ~~set~~ having the bit set at that position.
- ② We will count the sum of total such pairs ~~at~~ for bit position i ,

$$sm = \sum_{i=0}^{i=31} pos[i] \times [pos[i] + N]$$

- ③ finally, since i, j and j, i are two different pairs, we will double the answer

$$sm = sm \times 2$$

- ④ It returns the final answer.

Code →

```
#include <bits/stdc++.h>
const int MOD = 1000000007;
```

```
int main() {
    int n;
    cin >> n;
```

```
    vector<int> a(n);
    for (int i = 0; i < n; i++)
        cin >> a[i];
```

```
    int freq[31];
```

```
    for (int i = 0; i < n; i++) {
```

```
        for (int j = 0; j < 31; j++) {
```

```
            if (a[i] & (1 << j))
```

```
                freq[j] += 1;
```

```
        }
```

```
    }
```

```
    int ans = 0;
```

```
    for (int i = 0; i < 31; i++) {
```

```
        int p = freq[i] * (n - freq[i]);
```

```
        ans = (ans + p) % MOD;
```

```
    }
```

```
    ans = (ans * 2) % MOD;
```

```
    cout << ans << endl;
```

```
    return 0;
```

```
}
```

Test case : $n = 3$ $a = [3, 1, 5]$

$ans = 8$

high

while (low ≤ high)

0 1 0
0 0 1
1 0 1

1 x 2

1 x 2 x 1 (≤ 2)

1 2 3 4 5