

**MCA/D06**  
**Discrete Mathematical Structures**  
**MCA -103**

**Time : 3 Hours**

**MM:50**

**Note:- Attempt Five questions by selecting One Question from each unit.**

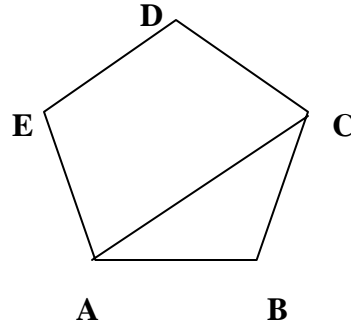
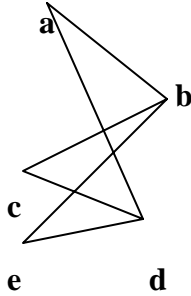
**UNIT-I**

- 1(a) Consider the group  $Z$  of integers under addition. Let  $H$  be the subset of  $Z$  consisting of all multiples of 6. Show that  $H$  is a normal subgroup of  $Z$ . Find the quotient group  $Z/H$ .**
- (b) Let  $S_3$  be a symmetric group over  $(1,2,3)$ . Write elements and the multiplication table for  $S_3$ .**
- 2(a) Determine all values of  $x$  from the given field, which satisfy the given equation.**
- (i)  $x+1 = -1$  over  $Z_2, Z_3$  and  $Z_5$
- (ii)  $2x+1 = 2$  over  $Z_3$  and  $Z_5$
- 3(a) Give an example of a finite integral domain and prove that it is field.**
- (b) Let  $M$  be the set of non-singular  $2 \times 2$  matrices over the set of real numbers. Prove that  $M$  under multiplication is a non-abelian group.**
- 4(a) Determine the type of the grammar  $G$  which consists of the productions, and the language defined by  $G$  respectively.**
- (i)  $S \rightarrow asb, S \rightarrow AB, A \rightarrow a, B \rightarrow b$
- (ii)  $S \rightarrow aB, B \rightarrow AB, aA \rightarrow b, A \rightarrow b, B \rightarrow Aa$
- (b) Define finite state machine and construct a finite state machine which will accept the language  $L = \{a^m b^n : m \text{ and } n \text{ are positive integers}\}$  over  $A = \{a+b\}$**

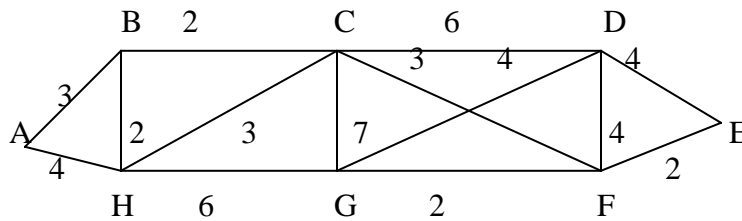
**UNIT-II**

- 5(a) Define Eulerian graph and Hamiltonian graph. Draw a graph with six vertices which is Eulerian but not Hamiltonian.**

(b) Define isomorphism of graphs. Verify whether the following graphs are isomorphic or not.



6(a) Describe two methods for finding minimal spanning tree from the following graph.



(b) Enumerate the nodes of the arithmetic tree for the expression  $(x+y)^2 - 3x(x+y) + 6x^2y$  in preorder and postorder respectively

7(a) consider the digraph  $G = \{V, E\}$ ,  $V = \{a, b, c, d\}$ ,  $E = \{(a, b), (a, d), (b, c), (b, d), (c, a), (d, c)\}$ . Using a suitable method determine how many paths of length 3 exist in  $G$  and which vertices are connected by a path of length three.

(b) Define acyclic digraph and prove that acyclic digraph has at least one source and one sink.

### UNIT-III

8(a) Let  $N$  be set of natural numbers and less than or equal to be a relation  $R$  on  $N$ . Prove that  $R$  is a partial order and draw the Hasse diagram for  $R$ .

(b) Define bounded lattice. Give an example each for bounded lattice and unbounded lattice.

- 9(a) Consider the Boolean expression on  
 $(B_2 = \{0,1\}, -, +, \cdot)$   
 $Y = A \cdot b \cdot C + A \cdot B \cdot C + A \cdot B$
- Draw the circuit (gate) diagram for Y.
  - Draw the switching (on-off) circuit for Y
  - Simplify Y algebraically if possible.
- (b) State the principle of duality for Boolean Algebras and state the dual of
- $a \vee [(b \vee a) \wedge b] = 1$ ,
  - $(a \wedge b) \wedge b = a \vee b$ .
- 10(a) Define Boolean Algebra and atoms of Boolean Algebra. Give an example to show that atoms of Boolean Algebra B generate the Non-zero element of B.
- (b) Consider the Boolean expression  
 $(x_3 \wedge x_2) \vee (x_2 \wedge x_3) \vee (x_2 \wedge x_3)$  on  $[B, \vee, \wedge]$ ,  $B = \{0,1\}$ .  
 Find min term normal form of f.