# MCA/D11

4518

### **Discrete Mathematical Structures**

Paper: MCA-103

Time: Three Hours [Maximum Marks: 80

Note: - Attempt FIVE questions. Question No.1 is compulsory and attempt ONE question from each Unit.

- (a) Prove that a subgroup of an abelian group is a normal subgroup.
  - (b) Find order of each element of permutation group P, over {1, 2, 3}.
  - (c) State necessary and sufficient condition for a graph to represent as an Euler circuit.
  - (d) Differentiate between reachability matrix and adjacency matrix of a digraph.
  - (e) What is splitting field?
  - Find complement of each element of the lattice  $L = \{1, 2, 3, 5, 10, 30\}$ under the relation divides.
  - (g) Write join and meet operation table for the lattice  $L = \{1, 2, 3, 6, 10, 30\}.$ 
    - (h) Prove that the polynomial  $x^2 + x + 1$  is reducible over  $z_3$ .

## UNIT-I

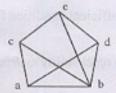
- (a) Let G be a finite group under the operation multiplication and (H, \*) be a subgroup of (G, \*). Prove that the set of left cosets of H in G partitions the set G.
  - (b) Write generating set for each element of (z6, t6). Describe whether (z<sub>6</sub>, t<sub>6</sub>) is a cyclic group or not.



- (a) Find the regular expression that defines the language consisting of all words in which the pattern abb appears. Draw finite state machine for the language.
  - (b) Characterize the language defined by the regular expression (b)\* + [(b\*) (a) (b)\* (a) (b)\*]\*.
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## UNIT-II

- (a) Write algorithm for breadth first-search tree and breadth first spanning tree.
  - (b) Define Planar graph, and state and prove Euler's formula for this graph.
- Write Warshall's algorithm to find reachability matrix and find the reachability matrix for the following digraph:



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### UNIT-III

- (a) Let L = {1, 2, 3, 4, 5, 6, 7, 8} and R be a relation ≤ on L. Verify whether L is a lattice.
  - (b) Define complement lattice and distributive lattice. Prove that if a lattice is complement and distributive then complement of each element is unique.
- Define Boolean algebra. Verify the set D<sub>105</sub> of positive divisors of 105 under the relation divides is a Boolean algebra or not.

#### UNIT-IV

- 8. Find splitting for the polynomial  $f = x^2 + 1$  over z<sub>2</sub>.
- (a) Write an example of an integral domain that is not a field.
  - (b) Write an example of a field. 7