

# COMPUTER ORIENTED NUMERICAL METHODS

Time : Three Hours

Maximum Marks : 80

**Note :** Attempt *five* questions in all. Select *one* question from each section. Question No. 1 is compulsory. All questions carry equal marks.

## (COMPULSORY QUESTION)

### 1. Compulsory Questions.

- (a) If  $\mu_r$  is the moment of a variable about mean and  $\mu'_r$  is the moment about an arbitrary point, determine relationship between  $\mu_r$  and  $\mu'_r$ .
- (b) One bag contains 4 white and 2 black balls; and another contains 4 white and 5 black balls. If one

- ball is drawn from each bag, find the probability that both are white.
- Show that Co-efficient of correlation  $r(x, y)$  is independent of change of scale and shift of origin.
  - Determine Arithmetic mean and Standard deviation of Poisson distribution.
  - Define Regression co-efficient and Regression lines.
  - Explain the significance of Chi-square distribution with degree of freedom and confidence interval.
- (3×6=18)

### UNIT-I

2. A class interval of weight (in lbs unit) and frequencies are given below :

Class (Weight)	Frequencies (f)
118-126	3
127-135	5
136-144	9
145-153	12
154-162	5
163-171	5
172-180	2

Find Arithmetic mean, Mode and Median. 6,6,6

3. (a) A frequency distribution is given below :

x :	61	64	67	70	73
f :	5	18	42	27	8

Find first four moments about Arithmetic mean.

- (b) Write an algorithm to determine Arithmetic mean of a distribution. 9,9

### UNIT-II

4. The heights of father (X) and son (Y) are given below :

X :	65	63	67	64	68	62	70	66	68	67	69	71
Y :	68	66	68	65	69	66	68	65	71	67	68	70

- (a) Find Co-relation coefficient.

- (b) Find Regression coefficient ( $b_{yx}$ ) of Y on X. 6,9

5. (a) Find 3% of the electric bulbs manufactured by a company.

- (i) 0  
 (ii) 1  
 (iii) 2  
 (iv) 4 bulbs are defective.
- (b) Write an algorithm to find variance of a frequency distribution  $x_i$  and  $f_i$  for  $i = 1, 2, \dots, n$ . 9,9

### UNIT-III

6. (a) A sample of 10 measurements of diameter of a sphere given as mean  $(\bar{X}) = 438$  cm and standard deviation  $(y) = 0.06$ . Find (a) 95% and (b) 99% confidence limits for the actual diameter.
- (b) The distribution of digits 0, 1, 2, 3, ....., 9 in a random sample of 250 digits are as follows :

Digits :	0	1	2	3	4	5	6	7	8	9
Observed frequencies :	17	31	29	18	14	20	35	30	20	36
Expected frequencies :	25	25	25	25	25	25	25	25	25	25

Does the observed distribution differ significantly from the expected distribution ? 9,9

7. (a) Fit a Least square curve  $y = a + bx + cx^2$  for the following distribution :

x :	0	1	2	3	4	5	6
y :	2.4	2.1	3.2	5.6	9.3	14.6	21.9

- (b) Write an algorithm to fit the curve  $y = a + bx + cx^2$ ? 9,9

### UNIT-IV

8. (a) Explain the terms :
- Random experiment
  - Conditional experiment
  - Mutually exclusive events.
- (b) The contents of two bags of same appearance are as follows :
- |         |        |         |     |          |     |
|---------|--------|---------|-----|----------|-----|
| Bag 1 : | 4 red, | 3 black | and | 3 white  | and |
| Bag 2 : | 3 red, | 4 black | and | 4 white. |     |

One bag is chosen at random and two balls are drawn. They happen to be red and white. What is the probability that they come from Bag 2 ? 9,9

9. A company wishes to test four different types of tyres : A, B, C and D. The tyre's life-time, as determined from their threads, are given (in thousand miles) in table below, where each type has been tried on six similar automobiles assigned at random to the tyres. Using one-way classification, determine that there is a significant difference between the tyres at (a) 0.05 and (b) 0.01 levels.

A	33	38	36	40	31	35
B	32	40	42	38	30	34
C	31	37	35	33	34	30
D	29	34	32	30	33	31