

## Data Structure

(1)

- Data structure is a way of organizing all data items and relationship to each other.

Data  $\Rightarrow$  Anything to give information is called data.

Ex  $\Rightarrow$  Student Name, Student Roll no.

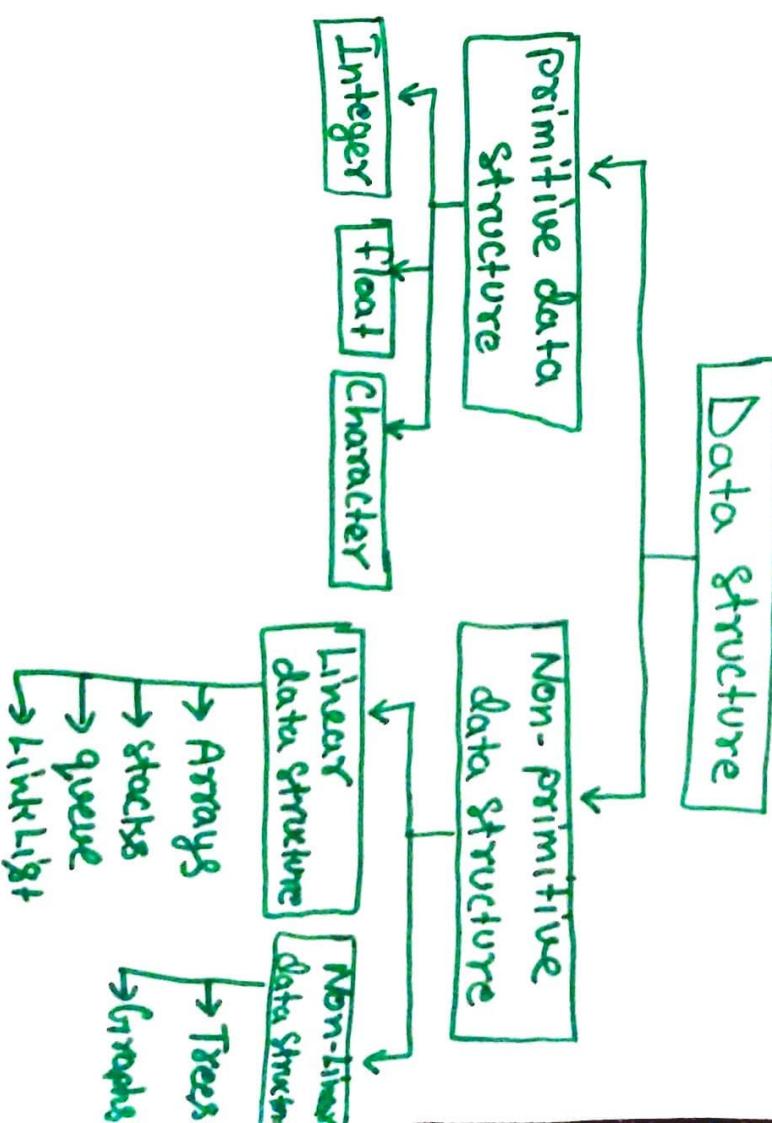
Structure  $\Rightarrow$  Representation of data is

Called structure.

Ex  $\Rightarrow$  graph, Arrays, List.

Data structure  $\Rightarrow$

- Data structure = Data + structure
- Data structure is a way to store and organize data so that it can be used efficiently (better way)



Primitive data structure ⇒ These are basic structure and

are directly operated by machine instruction.

Ex ⇒ integer, float, character.

Non- Primitive data structure ⇒ These are

derived from the primitive data structure. It's a collection of same type or different type primitive data structure.

Ex ⇒ Arrays, Stack, trees.

(3)

### Data Structure Operation ⇒

The data which is stored in our data structure are processed by some set of operations.

- v) Insertion ⇒ Add a new data in the data structure.
- vi) Deleting ⇒ Remove a data from the data structure.
- vii) Sorting ⇒ Arrange data in increasing or decreasing order.

viii) Searching ⇒ find the location of data in data structure.

v) Merging ⇒ Combining the data of two different sorted files into a single sorted file.

vii) Traversing ⇒ Accessing each data

Exactly one in the data structure so that each data item is traversed or visited.

(4)

## Arrays

(5)

- An Array can be defined as an infinite Collection of homogeneous (similar type) elements.

- Array are always stored in consecutive (specific) memory location.
- Array can be store multiple values which can be referenced by a single name.

### Types of Arrays



- ↳ Single Dimensional Arrays ➔ It's also known as One Dimensional (1D) Array.
- It's use only one subscript to define the elements of Arrays.

[row]      [col]

Declaration  $\Rightarrow$

Data-type var-name [expression],  
size

Ex: int num[10];

char c[5];

Initialization one-dimensional Array  $\Rightarrow$

Data-type var-name [expression] = {values};

Ex: int num[10] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};

char a[5] = {'A', 'B', 'C', 'D', 'E'};

2)

Multi-dimensional Arrays  $\Rightarrow$  multidimensional

Arrays use more

then one Subscript to describe the

Arrays Elements.  $\{ \} \{ \} \{ \}$  ---

Two dimensional Arrays  $\Rightarrow$   $I+j$  use two

Subscript, one subscript

+ to represent row value and second

Subscript + to represent column value.

$I+j$  mainly use for matrix representation.

(6)

Declaration two-dimensional Arrays  $\Rightarrow$

Data-type var-name [rows] [columns],

Ex: int num[3][2];

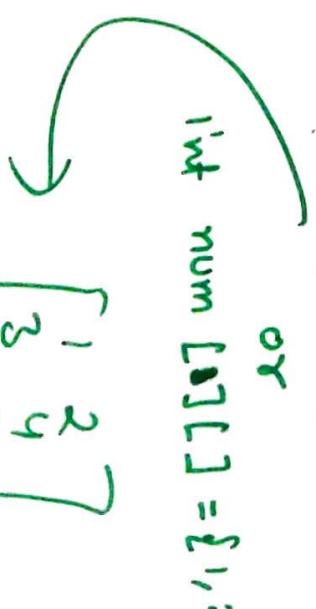
Initialization 2-D Arrays  $\Rightarrow$

Data-type var-name [rows][columns] = {values};

Ex: int num[3][2] = {1, 2, 3, 4, 5, 6};

Or

int num[1][5] = {1, 2, 3, 4, 5, 6};



$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \end{bmatrix}$$

num[0][0] = 1

num[0][1] = 2

num[1][0] = 3

num[1][1] = 4

num[2][0] = 5

num[2][1] = 6

(7)

## Stacks (Data Structure) 9

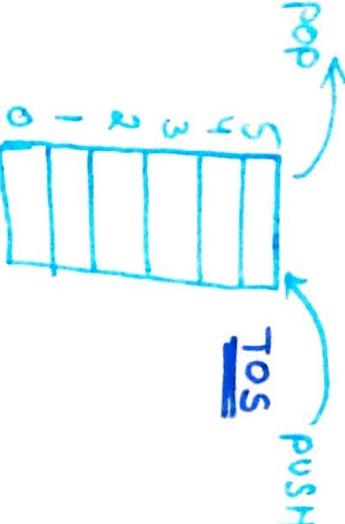
# write a program to read & write one dimensional Array.

# include < stdio.h> Standard input and output  
# include < conio.h> → Console input and output

```

void main()
{
    int a[10], i;
    clrscr();
    printf (" Enter the Array Elements ");
    for (i=0; i<=9; i++)
    {
        scanf ("%d", &a[i]);
    }
    printf (" the Entered Array is ");
    for (i=0; i<=9; i++)
    {
        printf ("%d\n", a[i]);
    }
    getch();
}

```

- Stack is a Non-primitive Linear data structure.
  - It is an ordered list in which addition of new data item and deletion of already existing data item is done from only one end known as Top of stack (Tos)
- 
- The last added element will be the first to be removed from the stack.  
This is the reason stack is called Last-in-first out (LIFO) type of list.

## Operations on stack.

There are two operation of stack.

(10)

- 1) PUSH operation  $\Rightarrow$  The process of adding a new element to the top of stack is called PUSH operation.

- Every new element is adding to stack top is incremented by one.

- In case the array is full and no new element can be added it is called stack full or Stack overflow Condition

- 2) POP operation  $\Rightarrow$  The process of

deleting an element from the

top of stack is called POP operation,

- After every POP operation the stack is decremented by one.

- If there is no element on the stack and

the POP is performed then this will result into Stack Underflow Condition.

## Stack Operation & Algorithm

(11)

- Stack has two operation.

- 1) PUSH operation  $\Rightarrow$

- 2) POP operation  $\Rightarrow$  The process of adding a new element of the top of stack is called PUSH operation  $\Rightarrow$  The process of

- Every PUSH operation TOP is incremented by one.

$$\boxed{\text{TOP} = \text{TOP} + 1}$$

- In case the Array is full no new Element is added. this condition is called Stack full or Stack overflow Condition.

Condition.

# Algorithm for inserting an item into (12)

the stack (push operation).

PUSH (stack [maxsize], item)

Step 1: initialise

Set top = -1

Step 2: Repeat steps 3 to 5 until Top < maxsize - 1

Step 3: Read Item

Step 4: Set top = top + 1

Step 5: Set stack [top] = item

Step 6: Print "Stack overflow"

- If there is no element on the

stack and the pop operation is performed then this will

result into STACK UNDERFLOW

Condition.

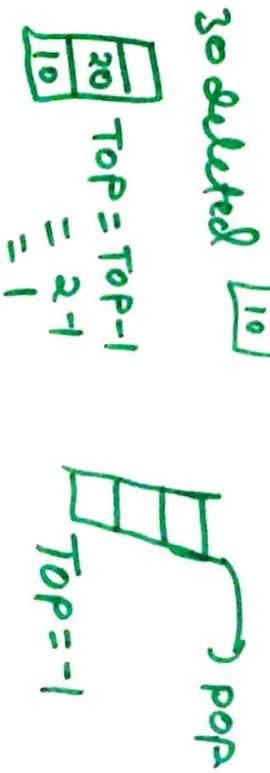


$$\text{Top} = \text{Top} - 1$$

- After every pop operation the stack top is decremented by one.

2 → POP operation ⇒

The process of deleting an element from the top of stack is called POP operation.



(13)

## \* Algorithm for deleting an item from the Stack (pop)

pop (Stack [maxSize], item)

Step1: Repeat steps 2 + 04 until  $TOP \geq 0$

Step2: Set item = Stack [TOP]

Step3: Set  $TOP = TOP - 1$

Step4: print, No. deleted is, item

Step5: Print stack under flows.

## Stacks (prefix & postfix)

Stack Notation  $\Rightarrow$  There are three stack

Notation.

1) Infix Notation  $\Rightarrow$  where the operator is written in-between the operands.

Ex  $\Rightarrow$  A + B + operator  
A, B operands

2) Prefix Notation  $\Rightarrow$  In this operator is written before the operands.

It is also known as Polish Notation.

Ex  $\Rightarrow$  + A B

3) Postfix Notation  $\Rightarrow$  In this operator is written after the operands.

It is also known as Suffix Notation.

Ex  $\Rightarrow$  A B +

Q  $\Rightarrow$  Convert the following Infix to prefix and postfix for  $(A+B)*C/D+E^F/G$

prefix  $\Rightarrow$   $(A+B)*C/D+E^F/G$   
 $+ A B * C / D + E ^ F / G$

Let  $+ A B = R_1$

$$R_1 * C/\Delta + \varepsilon^A F/G$$

$$R_1 * C/\Delta + \varepsilon^A F/G$$

$$\text{Let } \Rightarrow \underline{\wedge EF} = R_2$$

$$R_1 * C/\Delta + R_2/G$$

$$R_1 * C/\Delta + R_2/G$$

$$\text{Let } \Rightarrow \underline{| CD} = R_3$$

$$R_1 * R_3 + R_2/G$$

$$R_1 * R_3 + R_2/G$$

$$\text{Let } \Rightarrow \underline{| R_2G} = R_4$$

$$R_1 * R_3 + R_4$$

$$* R_1 R_3 + R_4$$

$$\text{Let } * \underline{R_1 R_3} = R_5$$

$$R_5 + R_4$$

$$+ R_5 R_4$$

Now enter the value of  $R_5, R_4, R_3, R_2, R_1$

$$+ * R_1 R_3 / R_2 G$$

$$+ * + AB / CD / \wedge EF G$$

(16)

postfix  $\Rightarrow$

$$(A+B) * C/\Delta + \varepsilon^A F/G$$

$$(\widehat{AB}) * C/\Delta + \varepsilon^A F/G$$

$$\text{Let } AB+ = R_1$$

$$R_1 * C/\Delta + \varepsilon^A F/G$$

$$R_1 * C/\Delta + (\varepsilon^A F)/G$$

$$\text{Let } \varepsilon F \wedge = R_2$$

$$R_1 * C/\Delta + R_2/G$$

$$R_1 * (C\Delta) + R_2/G$$

$$\text{Let } C\Delta/ = R_3$$

$$R_1 * R_3 + R_2/G$$

$$R_1 * R_3 + \underline{R_2G/}$$

$$\text{Let } R_2G/ = R_4$$

$$R_1 * R_3 + R_4$$

$$(\underline{R_1 R_3} *) + R_4$$

$$\text{Let } \underline{R_1 R_3 *} = R_5$$

$$\underline{R_5 + R_4} +$$

$$R_5 R_4 +$$

(17)

Now enter the value of  $R_5, R_4, R_3, R_2, R_1$

$R_5 R_4 +$

$R_1 R_3 * R_4 +$

$A B + C D / * R_2 G_1 +$

$A B + C D / * (E F) G_1 / +$

postfix expression

(18)

prefix and postfix using tabular form

(19)

$\Rightarrow$  convert  $(A + B * C)$  into prefix and postfix

using tabular form

# to convert in prefix following operation

perform

1) reverse the input string

2) perform tabular method and find postfix expression.

3) reverse this postfix expression string to find the prefix.

$\Rightarrow A + B * C$

fixes + to add brackets

$(A + B * C)$

Reverse string

$(C * B + A)$

Tabular form:

Symbol Scanned      stack      postfix expression

Priority	
$\wedge$ > implicit	
$* / \rightarrow 2$ highest	
$+ - \rightarrow$ lowest	
precedence	

Symbol Scanned	stack	postfix expression
(	(	-
C	C	
*	C	
(*	C	
(*	CB	
(*	CB	
(+	CB*	
(+	CB*A	
)	CB*A	A
		B
		C
		*
		+

So the postfix expression  $CB*A+$ . Now reverse this expression to get the prefix

So prefix is

$+ A * B C$  prefix

# to convert postfix  $\Rightarrow$  direct + perform tabular form

$(A + B * C)$

Symbol Scanned      stack

postfix expression

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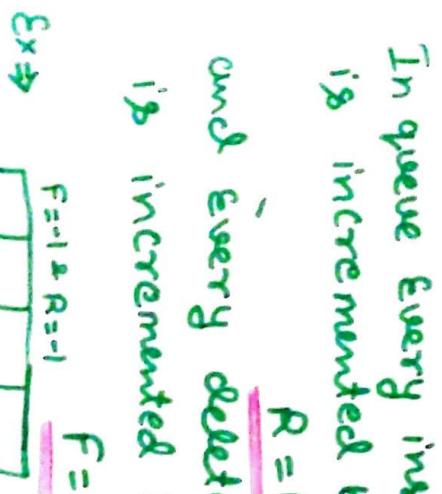
+

+

# Queues

(21)

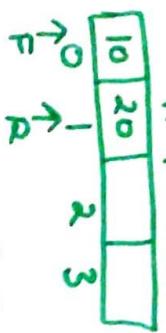
- Queue is a Non-primitive Linear data structure.
- It is an homogeneous Collection of elements in which new Elements are added at one end called the Rear End, and the existing Element are deleted from other end called the front End.
- The first added Element will be the first to be remove from the queue. that is the reason queue is called (FIFO) first-in first-out type List.
- In queue Every insert operation Rear is incremented by one  
$$R = R + 1$$
 and every deleted operation front is incremented by one

Ex  $\Rightarrow$    
 $F = F + 1$   
 $R = R + 1$   
Empty queue

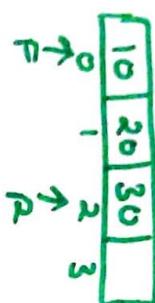
insert 10 R=0 F=0



insert 20 R=1 F=0

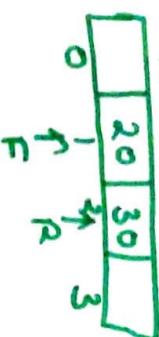


insert 30 R=2 F=0



# deleted element. first delete 10

R=2 F=1



Deleted second element.

R=2 F=2



(22)

## Operations on Queue

(23)

↳ To insert an element in a Queue ↳

Algo ↳

QINSERT [QUEUE[maxSize], ITEM]

Step 1: Initialization

Set front = -1

Set Rear = -1

Step 2: Repeat steps 3 + 5 until

Rear < maxSize - 1

Step 3: Read item

Step 4: If front == -1 then

front = 0

Rear = 0

else

Rear = Rear + 1

Step 5: Set QUEUE[Rear] = item

Step 6: Print, Queue is overflow

## 2) To Delete an Element from the Queue

DELETE(Queue[maxsize], item)

(24)

Step 1: Repeat step 2 to 4 until front >= 0

Step 2: Set item = Queue[front]

Step 3: If front == Rear

Set front = -1

Set Rear = -1

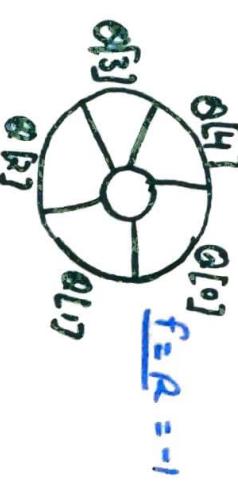
Else

front = front + 1

Step 4: Print, No. Deleted is, item

Steps: Print "Queue is Empty or underflow".

\* A circular queue overcome the problem of unutilized space in linear queues implemented as arrays.



## CIRCULAR QUEUE

(25)

A circular queue is one in which the insertion of a new element is done at the very first location of the queue if the last location of queue is full.

- 4) Each time an element is deleted from the queue the value of front is incremented by one.  
front = front + 1

Insert an element in Circular Queue  $\Rightarrow$  26

Algo  $\Rightarrow$  QINSERT (QUEUE[SIZE], item)

Step 1  $\Rightarrow$  if (front == (Rear+1)/ maxsize)

write queue is overflow & Exit.

else: take the value

if (front == -1)

set front = 0

Rear = 0

else

Rear = ((Rear+1)%, maxsize)

[Assign value] Queue[Rear] = Value.

[End : F]

Step 2  $\Rightarrow$  Exit

Queue (Data Structure) 27

Operation on Queue

10, 20, 30, 40



front = -1  $\checkmark$  empty queue  
Rear = -1

2) 3 to 5 step Repeat

R < maxsize - 1

-1 < 3 - 1

-1 < 2 + true

3  $\xrightarrow{K_1}$  4  $\xleftarrow{K_2}$

3) Read item  
Read 10

4) f = -1

-1 == -1 + true

f = 0

R = 0

5) set q[0] = item  
q[0] = 10



queue

10		
9,10	9,11	9,12

$$f=0 \quad R=0$$

Rear < maxsize - 1

$$0 < 3 - 1$$

$$0 < 2 \text{ true}$$

Read 20

if  $f == -1$

$$0 == -1 \text{ false}$$

else

$$R = R + 1$$

$$R = 0 + 1$$

$$R = 1$$

4)  $q[1] = 20$

10	20	
9,10	9,11	9,12

$$f=0 \quad R=1$$

Rear < maxsize - 1

$$1 < 3 - 1$$

$$1 < 2 \text{ true}$$

Read 30

$$\begin{aligned} \text{if } f &= -1 \\ 0 &= -1 \text{ false} \end{aligned}$$

Else

$$\begin{aligned} R &= R + 1 \\ R &= 1 + 1 = 2 \end{aligned} \quad (28)$$

(5) set  $q[2] = 30$

else

Algo  $\rightarrow$  Q DELETE(queue[maxsize], I+em)

DELETE an Element in Circular Queue

(29)

1) if (front == -1)

    write queue underflow and exit.

else: item = Queue[front]

    if (front == Rear)

        Set front = -1

        Set Rear = -1

    else: front = ((front + 1) % maxsize)

        [ End if Statement ]

    → item deleted.

2. exit.

# QUEUE (Data structure)

(30)

Delete

operation on queue

$\Rightarrow$

10	20	30
q[0]	q[1]	q[2]

maxsize = 3

f=0 R=2

Case 1

$f >= 0$

$0 >= 0$

+ne

2) set item = q[0]

item = 10

3) f == R

0 == 2 false

else

f = f + 1

f = 0 + 1 = 1

4) item is deleted  
10 is deleted

20	30
q[0]	q[1]

f=1 R=2

20	30
----	----

4) item is deleted

--	--

(31)

Case 2.1)  
 $f \geq 0$   
 $l \geq 0 + \text{tree}$

2)  $\text{item} = q[1]$  Case 4.

$\text{item} = 20$

$f \geq 0$   
 $-l \geq 0 \text{ false}$

Step 5: queue is empty

else  
 $f = f + 1$   
 $f = 1 + 1 = 2$

4) item is deleted  
 20 is deleted

queue is underflow.

	30
--	----

$f = 2$   $R = 2$

Case 3)  
 $f \geq 0$   
 $2 \geq 0 + \text{tree}$

2)  $\text{item} = q[2]$   
 $\text{item} = 30$

3)  $\text{if } f == R$   
 $2 == 2 + \text{true}$

set  $f = -1$   
 $R = -1$

## Linked Lists

(32)

- A Linked List is a Linear data structure, in which the elements are not stored at contiguous memory location.

- A Linked List is a dynamic data structure. The No. of nodes in a List is not fixed and can grow and shrink on demand.

- Each element is called a node, which has two parts.

info part which stores the information and pointer which point to the next element.

Element:



Node



## Advantages of Linked Lists

(33)

- 1) **Linked Lists are dynamic data structure:** That is, they can grow and shrink during the execution of a program.
- 2) **Efficient memory utilization:** Here, memory is not pre-allocated. Memory is allocated whenever it's required. And it's deallocated (Removed) when it's no longer needed.
- 3) **Insertion and deletions are easier and efficient:** It provide flexibility in inserting a data item at a specified position and deletion of a data item from the given position.
- 4) **Many complex Applications can be easily carried out with linked lists.**

## Operations ON Linked List:

(34)

The Basic operation to be performed on the linked lists are:-

- 1) **Creation :-** This operation are used to create a linked list. In this node is created and linked to the another node.
- 2) **Insertion :-** This operation is used to insert a new node in the linked list. A new node may be inserted
  - ⇒ At the beginning of a linked list.
  - ⇒ At the end of a linked list.
  - ⇒ At the specified position in a linked list.
- 3) **Deletion :-** This operation is used to delete an item (a node) from the linked list. A node may be deleted from
  - ⇒ Beginning of a linked list
  - ⇒ End of a linked list
  - ⇒ Specified position in the list.

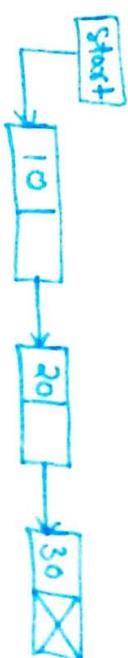
4) Traversing: It's a process of going through all the nodes of a linked list from one end to the other end.

5) Concatenation: It's the process of joining the second list to the end of the first list.

6) Display: This operation is used to print each and every node's information.

• Basically, there are four types of linked list.

1) Singly-linked list  $\Rightarrow$  It's one in which all nodes are linked together in some sequential manner. It's also called linear linked list.



2) Doubly-linked list  $\Rightarrow$  It's one in which all nodes are linked together by multiple links which help in accessing both the successor node (Next node) and predecessor node (Previous node) within the list. This helps to traverse the list in the forward direction and backward direction.

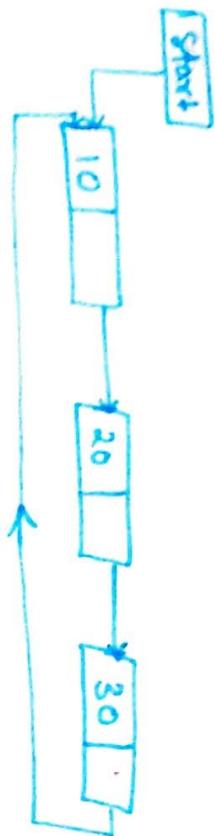


## Types of Linked List

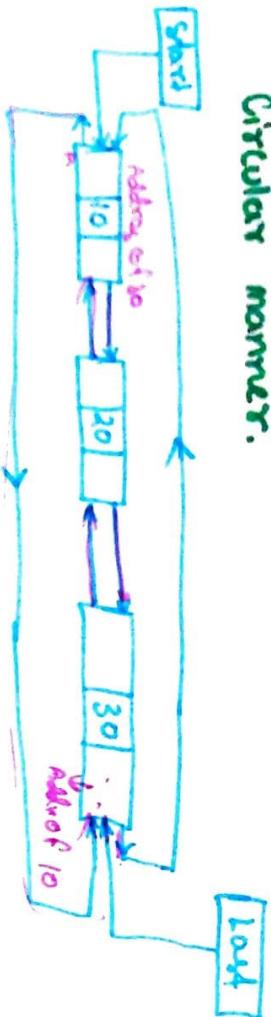
3 Circular Linked List  $\Rightarrow$  It's one which has no beginning and no end.

A singly linked list can be made a Circular linked list by simply sorting the address of the very first node in the link field of the last node.

(37)



4 Circular doubly linked List  $\Rightarrow$  It's one which has both the successor pointer and predecessor pointer in a circular manner.



# Inserting Nodes in Linked List

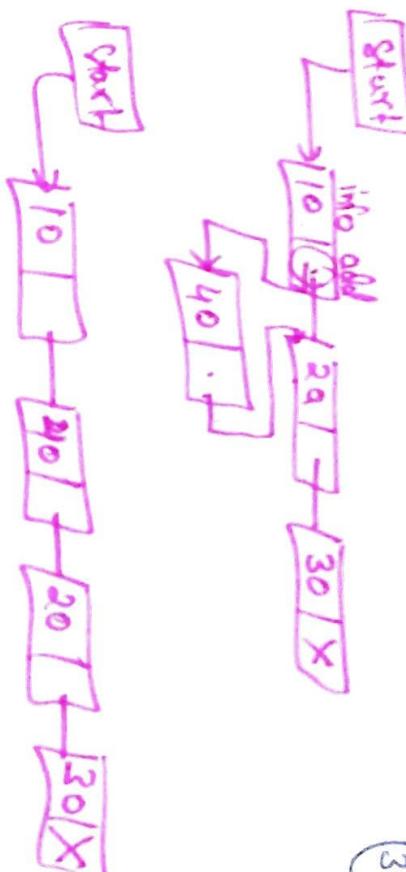
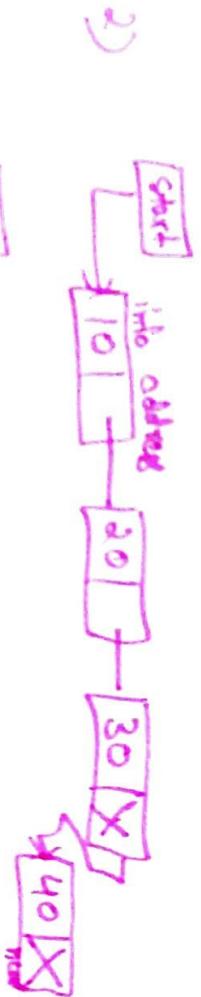
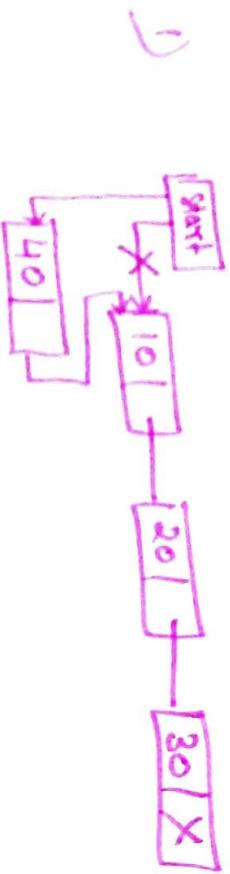
(38)

(39)

- 1) Inserting at the beginning of the list.

- 2) Inserting at the end of the list

- 3) Inserting at the specified position within the list.



3

## LINKED LIST

Inserting A Node AT the Beginning in Linked List

(40)

Algorithm  $\Rightarrow$   
**INSERT-FIRST(START, ITEM)**

**INSET-FIRST(START, ITEM)**

Step1: [Check for overflow]

IF PTR = NULL then

Print overflow

Exit

Else  
PTR = (Node\*) malloc(sizeof(Node))

//Create new node from memory and  
assign its address to PTR.

Step2: set PTR  $\rightarrow$  INFO = Item

Step3: set PTR  $\rightarrow$  Next = START

Step4: Set START = PTR



ptr  
newnode

After insertion



## LINKED LIST

Insert A Node AT THE End in singly Linked List

(41)

Algorithm  $\Rightarrow$   
**Insert-Last(START, ITEM)**

**INSET-LAST(START, ITEM)**

Step1: Check for overflow

IF PTR = NULL then

Print overflow

Exit

Else  
PTR = (Node\*) malloc(sizeof(Node))

//Create new node from memory and  
assign its address to PTR.

Step2: Set PTR  $\rightarrow$  INFO = Item

Step3: set PTR  $\rightarrow$  Next = NULL;

Step4: IF start = NULL and then

Set START = PTR;

Else,

Set LOC = start;

Step5: Set LOC  $\rightarrow$  Next = PTR;

Step6: Repeat Step 7 until LOC  $\rightarrow$  Next != NULL;

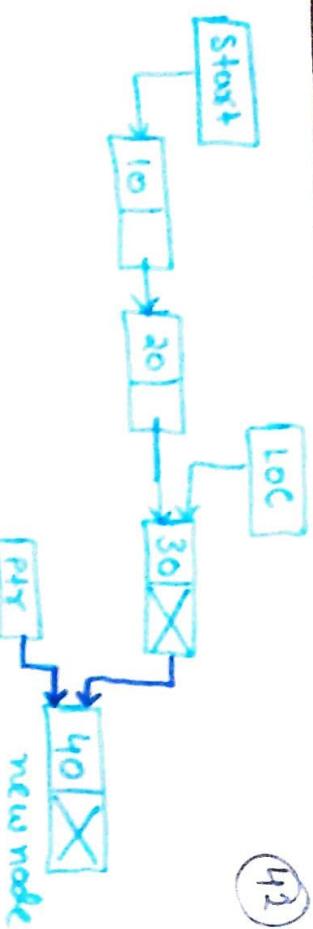
Step7: Set LOC  $\rightarrow$  Next  $\rightarrow$  Next = PTR;

Step8: Set LOC  $\rightarrow$  Next = PTR;

## LINKED LIST

(42)

Inserting a Node at the Specified Position in  
Singly Linked List.



Algorithm  $\Rightarrow$

Insert-Location (START, ITEM, LOC)

Step1: Check for overflow

If  $ptr == NULL$  then  
Print overflow  
Exit

Else

$ptr = (\text{Node}*) \text{malloc}(\text{size of Node})$

Step2: set  $ptr \rightarrow \text{Info} = \text{item}$

Step3: IF  $\text{start} = \text{NULL}$  then

    set  $\text{start} = ptr$   
    set  $ptr \rightarrow \text{Next} = \text{NULL}$

Step4: Initialize the Counter I and pointers

Set  $I = 0$

Set  $\text{temp} = \text{start}$

(43)

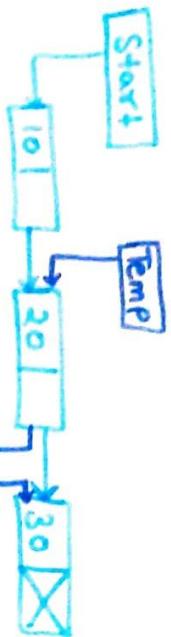
Step5: Repeat Steps 6 and 7 until  $I < loc$

Step6: set  $temp = temp \rightarrow Next$

Step7: set  $I = I + 1$

Step8: set  $ptr \rightarrow Next = temp \rightarrow Next$

Step9: set  $temp \rightarrow Next = ptr$ .



After Insertion



(44)

## Deleting Node in Linked List



(45)

• Deleting a node from the linked list has three instances.

1 ➔ Deleting the first node of the linked list.

2 ➔ Deleting the last node of the linked list.

3 ➔ Deleting the node from Specified position of the linked list.



## LINKED LIST

## DELETING NODES

(46)

Deleting the first Node in singly linked List

Algorithms

Deleted & first (START)

Deleted & first (START)

Step 1: Check for under flow

Step 1: Check for under flow

If start = NULL, then

If start = NULL, then

Print linked list empty

Print linked list empty

Exit

Exit

Step 2: Set PTR = START

Step 2: Set PTR = START

Step 3: Set START = START  $\rightarrow$  Next

Step 3: Set START = START  $\rightarrow$  Next

Step 4: Print element deleted is PTR  $\rightarrow$  info

Step 4: Print element deleted is PTR  $\rightarrow$  info

Step 5: free(PTR).

Step 5: free(PTR).

End if

End if

Step 6: Set PTR = START

Step 6: Set PTR = START

Step 7: Repeat Step 5 and 6 until PTR  $\rightarrow$  Next != NULL

Step 7: Repeat Step 5 and 6 until PTR  $\rightarrow$  Next != NULL

After Selection

After Selection



Algorithm  $\Rightarrow$

Deleting (START)

Step 1: Check for underflow

Step 1: Check for underflow

If start = NULL then

If start = NULL then

Print linked list is empty

Exit

Step 2: If start  $\rightarrow$  Next = NULL then

Step 2: If start  $\rightarrow$  Next = NULL then

Set PTR = start

Set PTR = start

Set start = NULL

Set start = NULL

Print element deleted is = PTR  $\rightarrow$  Info

free (PTR)

free (PTR)

End if

End if

Step 3: Set PTR = START

Step 3: Set PTR = START

Step 4: Repeat Step 5 and 6 until PTR  $\rightarrow$  Next != NULL

Step 4: Repeat Step 5 and 6 until PTR  $\rightarrow$  Next != NULL

Step 5: Set LOC = PTR

Step 5: Set LOC = PTR

Step 6: Set PTR = PTR  $\rightarrow$  Next

Step 6: Set PTR = PTR  $\rightarrow$  Next

(47)

Deleting the last node in singly linked List

Algorithms

Deleted & first (START)

Deleted & first (START)

Step 1: Check for under flow

Step 1: Check for under flow

If start = NULL then

If start = NULL then

Print linked list is empty

Print linked list is empty

Exit

Exit

Step 2: Set PTR = START

Step 2: Set PTR = START

Step 3: Set START = PTR  $\rightarrow$  Next

Step 3: Set START = PTR  $\rightarrow$  Next

Step 4: Print element deleted is = PTR  $\rightarrow$  info

Step 4: Print element deleted is = PTR  $\rightarrow$  info

Step 5: free(PTR)

Step 5: free(PTR)

End if

End if

Step 6: Set PTR = START

Step 6: Set PTR = START

Step 7: Repeat Step 5 and 6 until PTR  $\rightarrow$  Next != NULL

Step 7: Repeat Step 5 and 6 until PTR  $\rightarrow$  Next != NULL

Step 8: Set LOC = PTR

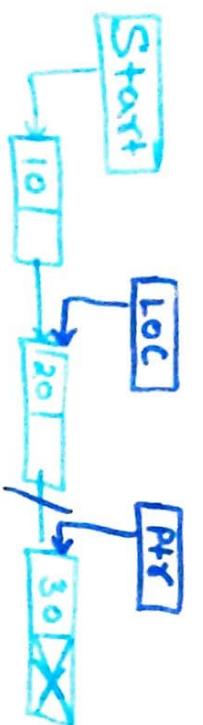
Step 8: Set LOC = PTR

Step 9: Set PTR = PTR  $\rightarrow$  Next

Step 9: Set PTR = PTR  $\rightarrow$  Next

Step 7: set LOC → Next = NULL

Step 8: free (PTR)



After deletion



(48)

## LINKED LIST

## DELETING NODES

Deleting the Node from Specified position

In singly linked list

Algorithm →

Delete - Location (START, LOC)

Step 1 : Check for underflow

If PTR = NULL then  
print underflow

Exit

Step 2 : Initialize the Counter I and pointers

Set I = 0;  
Set PTR = Start;

Step 3 : Repeat step 4 to 6 until I < LOC

Step 4 : Set temp = PTR

Step 5 : Set PTR = PTR → Next

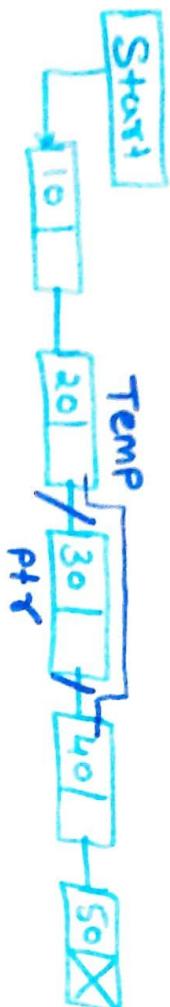
Step 6 : Set I = I + 1

(49)

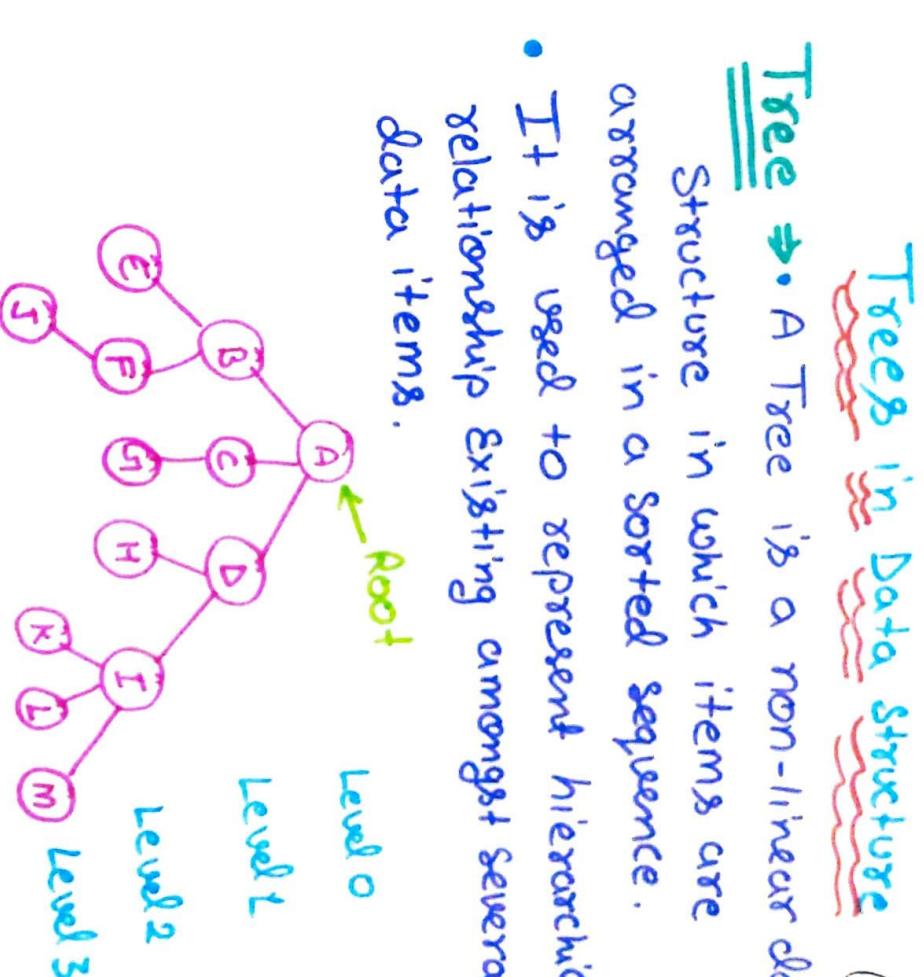
Step 7: print element deleted  $\&= \text{ptr} \rightarrow \text{info}$

Step 8: set  $\text{Temp} \rightarrow \text{Next} = \text{ptr} \rightarrow \text{Next}$  (50)

Step 9: free( $\text{ptr}$ )



After deletion



Tree Terminology  $\Rightarrow$  Tree has different terminology such as:

1  $\Rightarrow$  Root  $\Rightarrow$  It is specially designed data item in a tree. It is the first in the hierarchical arrangement of data item.

In the above tree, A is root item.

2  $\Rightarrow$  Node  $\Rightarrow$  Each data item in a tree is called a node. In the given

Tree in Data Structure (51)

Tree  $\Rightarrow$  A Tree is a non-linear data structure in which items are arranged in a sorted sequence.

• It is used to represent hierarchical relationship existing amongst several data items.

Tree there are 13 Node such as -

A, B, C, D, E, F, G, H, I, J, K, L, M

3. Degree of a node  $\Rightarrow$  It is the no. of

Subtrees of a node in a given tree:

The degree of A = 3

The degree of C = 1

The degree of L = 0

4. Degree of a tree  $\Rightarrow$  It is the maximum degree

of nodes in a given tree. In the given tree the node A and node I has maximum degree(3). so the degree of tree is 3.

5. Terminal node  $\Rightarrow$  A node with degree

zero is called terminal node. In given tree, E, J, G, H, K, L and M are terminal node.

6. Non-terminal Node  $\Rightarrow$  Any node whose

degree is not zero is called non-terminal node. In given tree - A, B, C, D, E, F, I are Non-terminal node.

(52)

7. Siblings  $\Rightarrow$  The child nodes of a given parent node are called Siblings. They are also called brothers.

In the given table.

- B, C, D are Siblings of parent node A.
- H & I are Siblings of parent node D.

8. Level  $\Rightarrow$  The entire tree structure is

Levelled in such a way that the root node is always at level 0.

9. Edge  $\Rightarrow$  It is a connecting line of two nodes. That is, the line drawn from one node to another node is called an Edge.

10. Path  $\Rightarrow$  It is a sequence of

Consecutive edges from the source node to the destination node. In the given tree the path between

A and J is as.  
(A, B) (B, F) and (F, J)  
A  $\rightarrow$  B  $\rightarrow$  F  $\rightarrow$  J

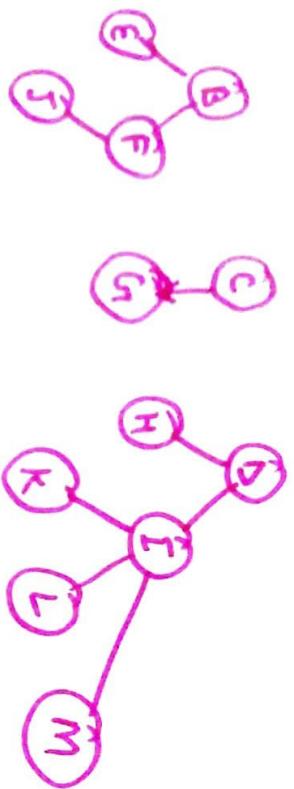
(33)

11) Depth  $\Rightarrow$  It is the maximum level of any node in a given tree. In the given tree, the root node A has the maximum level.

(54)

12) forest  $\Rightarrow$  It is a set of disjoint trees. In a given tree if you remove its root node then it becomes a forest. In the given tree, there is a forest with three tree such as.

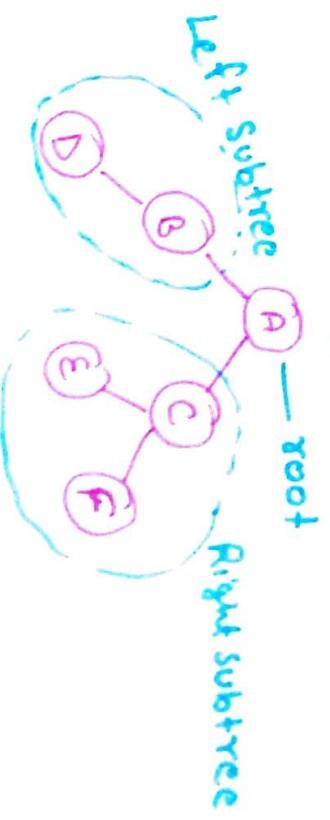
After removing root A, forest is.



right subtree

In Binary tree, every node can have

maximum of 2 children which are known as left child and right child.



(55)

BINARY TREES

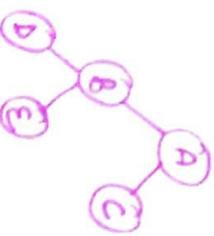
Binary tree is a finite set of data item which is either empty

or consists of a single item called root and two disjoint binary tree called the Left subtree and

## Types of Binary trees $\Rightarrow$

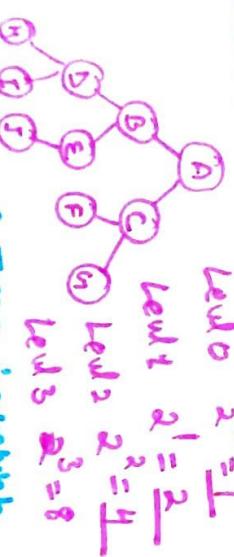
(56)

- full Binary tree  $\Rightarrow$  A binary tree is full if every node has 0 or 2 child.



- Complete binary tree  $\Rightarrow$  A binary tree is completely filled except possibly the last level and the last level has all keys as left or possible.

$$\begin{array}{l} \text{Level 0 } 2^0 = 1 \\ \text{Level 1 } 2^1 = 2 \\ \text{Level 2 } 2^2 = 4 \\ \text{Level 3 } 2^3 = 8 \end{array}$$



- Perfect binary tree  $\Rightarrow$  A tree in which all internal nodes have two children and all leaves are at the same level.

in which all level has  $2^n$  child

$$\begin{array}{l} \text{Level 0 } 2^0 = 1 \\ \text{Level 1 } 2^1 = 2 \\ \text{Level 2 } 2^2 = 4 \\ \text{Level 3 } 2^3 = 8 \end{array}$$



## Traversal of a Binary Tree $\Rightarrow$

(57)

It is a way in which each node in the tree is visited exactly once in a systematic manner.

There are three ways which we use to traverse a tree - Node Left, Right + to + traverse a tree - NLR (LN R)

- Pre Order traversal (NLR) (LN R)
- In Order traversal (LNR) (LN R)
- Post Order traversal (LRN) (LNR)

- $\Rightarrow$  Pre Order Traversal  $\Rightarrow$  In this

Traversal method, the root node is visited first, then the left subtree and finally the right subtree.

Algorithm  $\Rightarrow$

Until all nodes are traversed -

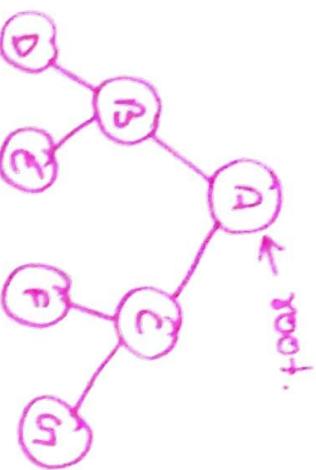
Step 1: Visit root node.

Step 2: Recursively traverse left subtree.

Step 3: Recursively traverse right subtree.

Ex ⇒

(58)



Pre-order traversal  
A, B, D, E, C, F, G.

↳

2 ⇒ Inorder Traversal ⇒ In this traversal method, the left subtree is visited first, then the root and later the right subtree.

Algorithm ⇒

Algorithm ⇒

Until all nodes are traversed -

Step1: Recursively traverse left subtree.

Step2: Visit root node.

Step3: Recursively traverse Right Subtree.

## Binary Search tree(BST)

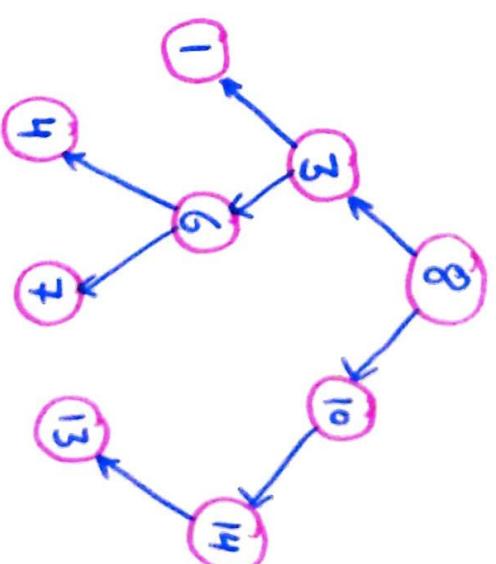
(59)

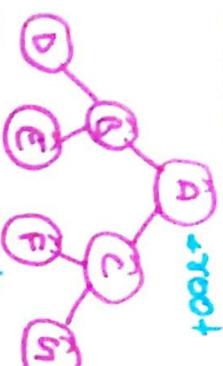
Binary search tree is a node-based binary tree data structure which has the following Rules:

1 ⇒ The value of the key in the left child or left subtree is less than the value of root.

2 ⇒ The value of the key in the right child or right subtree is more than or equal to the root.

3 ⇒ The right and left subtree each must also be a binary search tree (BST).





Inorder Traversal is -  
D, B, E, A, F, C, G.

3) Post-order Traversal  $\Rightarrow$  In this method the root node is visited last, hence the name first we traverse Left subtree, then the right subtree and finally the root node.

Algorithm =

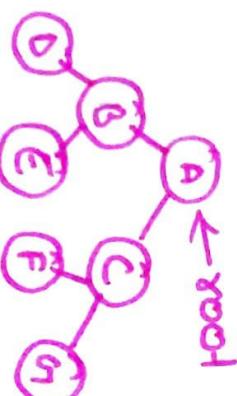
until all nodes are traversed -

Step 1: Recursively traverse Left subtree.

Step 2: Recursively traverse right subtree.

Step 3: Visit root node.

Ex-2



Post-order Traversal is -

D, E, B, F G, C, A

# Difference between Stack and Queue

(61)

## Stack

- 1 → It represents the collection of elements in Last In First Out (LIFO) order. Elements in Last in first out (LIFO) order.
- 2 → Objects are inserted and removed at the same end called Top of Stack (TOS).
- 3 → Insert operation is called push operation.

## Queue

- 1 → It represents the collection of elements in First In First Out (FIFO) order. Elements in First In First Out (FIFO) order.
- 2 → Objects are inserted and removed from different ends called front and rear ends.
- 3 → Insert operation is called Enqueue operation.
- 4 → Delete operation is called Dequeue operation.
- 5 → In Queue there is a wastage of memory space.

- 6 → In Stack There is no wastage of memory space.
- 7 → Stack Counter at marriage Reception is an example of stack.
- 8 → Delete operation is called pop operation.
- 9 → In Stack There is no wastage of memory space.
- 10 → Students Standing in a line at fees counter is an example of queue.

# Difference between Singly and Doubly Linked List

62

## Singly Linked List

- 1 → Singly Linked List has nodes with data field and next link field (forward link).

Ex:-

Data	next
------	------

## Doubly Linked List

- 1 → Doubly Linked List has nodes with data field and two pointer field.(backward and forward link).

Ex:-

Previous	Data	Next
----------	------	------

- 2 → It allows traversal only in one way.
- 3 → It requires one List pointer variable (start)
- 4 → It occupies less memory
- 5 → Complexity of Insertion and Deletion at known position is  $O(n)$ .

$O(1)$

## (6.3) Difference between Linear and Non-Linear data Structure

Linear Data Structure	Non-Linear data structure
<p>1 ➔ In this data structure The elements are organized in a sequence such as :-</p> <p>2 ➔ Array, stack, queue etc.</p> <p>3 ➔ In linear data structure Single Level is involved.</p> <p>4 ➔ Data Elements can be traversed in a single run only.</p> <p>5 ➔ Memory is not utilized in a efficient way.</p> <p>6 ➔ Applications of linear D.S are mainly in Application software development.</p>	<p>1 ➔ In this data structure data is organized without any sequence.</p> <p>2 ➔ In non-Linear D.S multiple Levels are involved.</p> <p>3 ➔ It is difficult to implement.</p> <p>4 ➔ Data Elements can't be traversed in a single run only.</p> <p>5 ➔ memory utilization in an efficient way.</p> <p>6 ➔ Applications of non-Linear D.S are in Artificial Intelligence and image processing.</p>

# Difference between Array and Linked List

(63)

Array	Linked-List
<ul style="list-style-type: none"> <li>1 → Size of an Array is fixed.</li> <li>2 → Array is a collection of Homogeneous (Similar) data type.</li> <li>3 → Memory is allocated from Stack.</li> <li>4 → Array work with Static data Structure.</li> <li>5 → Elements are stored in contiguous memory locations.</li> <li>6 → Array elements are independent to each other.</li> <li>7 → Array take more time. (<i>Insertion &amp; Deletion</i>)</li> </ul>	<ul style="list-style-type: none"> <li>1 → Size of a List is not fixed.</li> <li>2 → Linked-List is a collection of node (data &amp; address).</li> <li>3 → Memory is allocated from heap.</li> <li>4 → Linked-List work with Dynamic data structure.</li> <li>5 → Elements can be stored anywhere in the memory.</li> <li>6 → Linked List elements are depend to each other.</li> <li>7 → Linked-List take less time. (<i>Insertion &amp; Deletion</i>)</li> </ul>

# Difference between Tree and Graph

64

## Tree

- 1 → Tree is a collection of nodes and edges.
- Ex →  $T = \{ \text{node, edges} \}$
- Ex →  $G_1 = \{ V, E \}$
- 2 → There is a unique node called root in tree.
- 3 → There will not be any cycle/loops.
- 4 → Represents data in the form of a tree structure in a hierarchical manner.
- 5 → In tree only one path between two nodes.
- 6 → In this Preorder, Inorder and Postorder Traversal.



## Graph

- 1 → Graph is a collection of vertices/nodes and edges.
- 2 → There is no unique node.
- 3 → There can be loops/cycle.
- 4 → Represents data similar to a network.
- 5 → In graph one or more than one path between two nodes.
- 6 → In this BFS and DFS traversal.



## (DS) Data Structure Most important question for Exam.

- Q 1  $\Rightarrow$  What do you mean by data structure? Explain different types of Data structure in detail.
- Q 2  $\Rightarrow$  What do you mean by Space Complexity and time Complexity of an algorithm? Write an algorithm / pseudo code for Binary Search and mention the best case and worst case time Complexity of Binary search.
- Q 3  $\Rightarrow$  How array is implemented in memory and how the address of an element can be calculated in one and two dimensional array.
- Q 4  $\Rightarrow$  What do you mean by Stack? Write an algorithm for stack push and pop operation.
- Q 5  $\Rightarrow$  Write the Prefix and Postfix form of each of the following infix notation:-
- a)  $A - B + (M \$ N) * (O + P) - Q / R ^ S * T + Z$
  - b)  $K + L - M * N + (O ^ P) * W / U / V * T + Q$
- Q 6  $\Rightarrow$  What is meant by Circular queue and priority queue. Write a function to insert and delete an element from a Circular queue.
- Q 7  $\Rightarrow$  Define recursive function. What are the essential conditions to be satisfied by a recursive function.

Q 8  $\Rightarrow$  What do you mean by Linked List?

Explain different types of Linked List.

Describe the functional code for inserting and deleting a desired node in singly linked list.

Q 9  $\Rightarrow$  What is B-tree. Generate a B-tree of order 5 with the alphabets arrive in the sequence as:

a, g, b, k, d, h, m, j, e, s, i, r, x, c, l, n, t, u, p

Q 10  $\Rightarrow$  Describe Sorting and types. Write an algorithm for insertion sort and quick sort.

Q 11  $\Rightarrow$  The inorder and preorder traversal of a tree are given below:

Inorder: DBMINEAFCLGJK

Preorder: ABDEIMNCFGJK

- Construct the corresponding Binary tree.
- Determine the postorder traversal of the tree.

Q 12  $\Rightarrow$  Write Kruskal's and Prim's algorithm and explain with Example.

Q 13  $\Rightarrow$  Explain the following.

- BFS and DFS
- AVL tree
- hash function
- BST