

# ADDRESSING SURPRISAL DEFICIENCIES IN READING TIME MODELS

---

Marten van Schijndel   William Schuler

December 11, 2016

Department of Linguistics, The Ohio State University

- Surprisal is a way to estimate text complexity

- Surprisal is a way to estimate text complexity
- Experienced complexity is reflected in reading speed

- Surprisal is a way to estimate text complexity
- Experienced complexity is reflected in reading speed

Claim:

Current surprisal models inadequately estimate reading complexity

- Surprisal is a way to estimate text complexity
- Experienced complexity is reflected in reading speed

Claim:

Current surprisal models inadequately estimate reading complexity

Consequence:

Other reading time predictors may get too much credit

## READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING


<sup>1</sup>  
The red apple that the <sup>2</sup>  
girl ate ...

## READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING

The red apple that the girl ate ...  
 $w_1$   $w_2$   $w_3$   $w_4$   $w_5$   $w_6$

Reading model of 'girl':  
sentence position

## READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING

The red apple that the  ate ...  
 $w_6$

Reading model of 'girl':  
sentence position, word length



## READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING

The red apple that the girl ate ...

4 chars  
 $w_6$

Reading model of 'girl':  
sentence position, word length,  $P(\text{girl}|\text{the})$

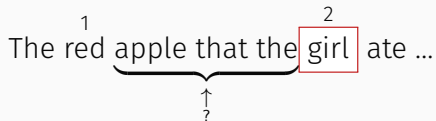
READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING

The red apple that the <sup>2</sup>girl<sup>1</sup> ate ...  
↑  
important

Reading model of 'girl':  
sentence position, word length,  $P(\text{girl}|\text{the})$

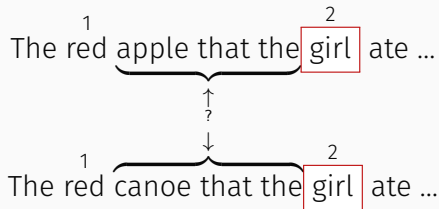
## READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING

The red <sup>1</sup>apple that the <sup>2</sup>girl ate ...



Reading model of 'girl':  
sentence position, word length,  $P(\text{girl}|\text{the})$

READING COMPLEXITY IS ESTIMATED BASED ON REGION ENDING



Reading model of 'girl':  
sentence position, word length,  $P(\text{girl}|\text{the})$

This study:  $n$ -gram and PCFG surprisal

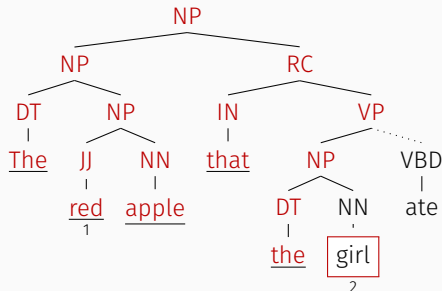
This study:  $n$ -gram and PCFG surprisal

The red apple that the girl ate ...

$$N\text{-gram-surp}(\text{girl}) = -\log P(\text{girl} \mid \text{the})$$

# SURPRISAL: PROBABILITY OF OBSERVATION GIVEN CONTEXT

This study:  $n$ -gram and PCFG surprisal



$$\text{PCFG-surp}(\text{girl}) = - \sum_{T \in \text{Trees}} \log P(T_6 = \text{girl} \mid T_1 \dots T_5 = \text{The} \dots \text{the})$$

## Cumulative $N$ -gram Surprisal

The red<sup>1</sup> apple that the girl<sup>2</sup> ate ...



## Cumulative $N$ -gram Surprisal

The <sup>1</sup>red apple that the <sup>2</sup>girl ate ...

$$\text{cumu-}n\text{-gram}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}+1}^{f_t} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

## Cumulative $N$ -gram Surprisal

The red<sup>1</sup> apple that the girl<sup>2</sup> ate ...

$$\text{cumu-}n\text{-gram}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}+1}^{f_t} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

## Cumulative $N$ -gram Surprisal

The red<sup>1</sup> apple that the girl<sup>2</sup> ate ...

$$\text{cumu-}n\text{-gram}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}+1}^{f_t} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

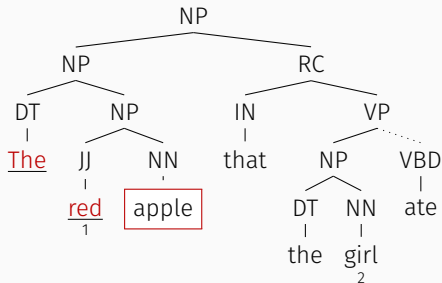
## Cumulative N-gram Surprisal

The red <sup>1</sup> apple that the <sup>2</sup> girl ate ...

$$\text{cumu-}n\text{-gram}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}+1}^{f_t} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

# ACCUMULATED SURPRISAL FIXES THE THEORETICAL PROBLEM

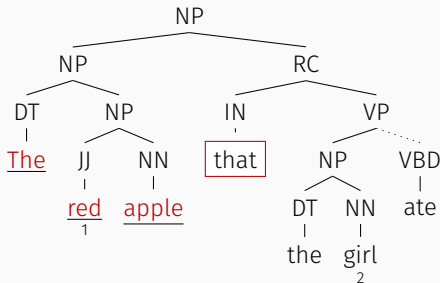
## Cumulative PCFG Surprisal



$$\text{Cumulative PCFG}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}}^{f_t} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$

# ACCUMULATED SURPRISAL FIXES THE THEORETICAL PROBLEM

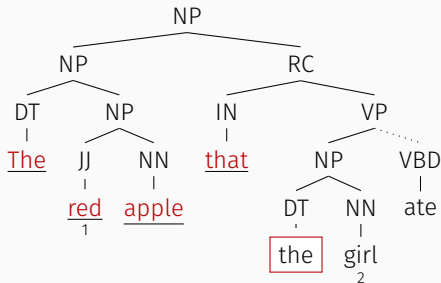
## Cumulative PCFG Surprisal



$$\text{Cumulative PCFG}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}}^{f_t} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$

# ACCUMULATED SURPRISAL FIXES THE THEORETICAL PROBLEM

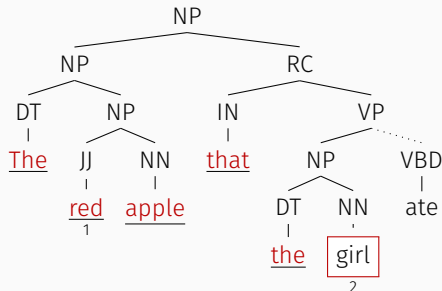
## Cumulative PCFG Surprisal



$$\text{Cumulative PCFG}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}}^{f_t} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$

# ACCUMULATED SURPRISAL FIXES THE THEORETICAL PROBLEM

## Cumulative PCFG Surprisal



$$\text{Cumu-PCFG}(w, f_{t-1}, f_t) = \sum_{i=f_{t-1}}^{f_t} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$



# HOW WELL DOES THIS FIX WORK?

## *N*-gram surprisal

- 5-grams
- Trained on Gigaword 3.0 (Graff and Cieri, 2003)
- Computed with KenLM (Heafield et al., 2013)

# HOW WELL DOES THIS FIX WORK?

## *N*-gram surprisal

- 5-grams
- Trained on Gigaword 3.0 (Graff and Cieri, 2003)
- Computed with KenLM (Heafield et al., 2013)

## PCFG surprisal

- Trained on WSJ 02-21 (Marcus et al., 1993)
- Computed with van Schijndel et al., (2013) parser

# HOW WELL DOES THIS FIX WORK?

University College London (UCL) Corpus (Frank et al., 2013)

- 43 subjects
- reading online novels
- frequent comprehension questions

# HOW WELL DOES THIS FIX WORK?

Baseline mixed effects model

Fixed Factors

- sentence position
- word length
- region length
- whether the previous word was fixated

# HOW WELL DOES THIS FIX WORK?

Baseline mixed effects model

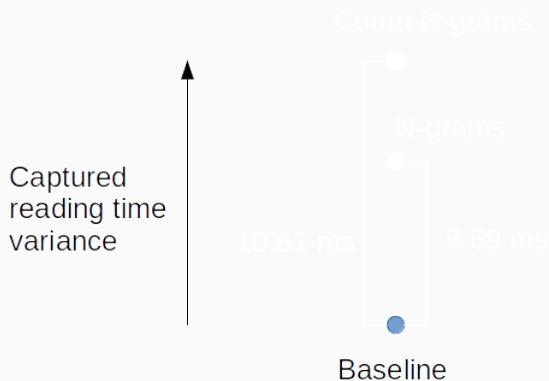
Fixed Factors

- sentence position
- word length
- region length
- whether the previous word was fixated

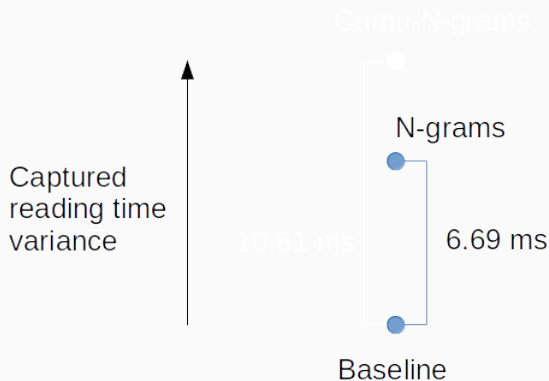
Random Factors

- All fixed factors as by-subject random slopes
- Item, subject and subject $\times$ sentence intercepts

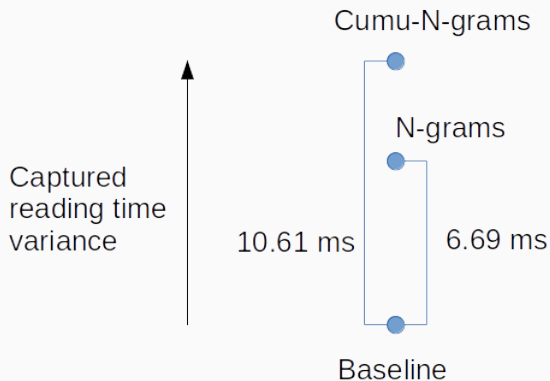
# ACCUMULATION IMPROVES $N$ -GRAM SURPRISAL



# ACCUMULATION IMPROVES $N$ -GRAM SURPRISAL



# ACCUMULATION IMPROVES $N$ -GRAM SURPRISAL





# ACCUMULATION DOES NOT HELP PCFG SURPRISAL

After adding cumulative  $n$ -gram surprisal to model:

# ACCUMULATION DOES NOT HELP PCFG SURPRISAL

After adding cumulative  $n$ -gram surprisal to model:

- PCFG surprisal is not useful ( $p > 0.05$ )

# ACCUMULATION DOES NOT HELP PCFG SURPRISAL

After adding cumulative  $n$ -gram surprisal to model:

- PCFG surprisal is not useful ( $p > 0.05$ )
- Cumulative PCFG surprisal is not useful ( $p > 0.05$ )

Parafoveal processing

<sup>1</sup>  
The red apple that the girl ate ...

Parafoveal processing

Th(e<sup>1</sup> red apple that t)he girl ate ...

Parafoveal processing

Th(e<sup>1</sup> red apple that t)he<sup>2</sup> girl ate ...

Prediction

<sup>1</sup>  
The red apple that the girl ate ...

Prediction

The red<sup>1</sup> (apple that the girl) ate ...



Prediction

The red <sup>1</sup>(apple that the <sup>2</sup>girl) ate ...

Subsequent regression

<sup>1</sup>  
The red apple that the girl ate ...

Subsequent regression

The red <sup>1</sup>apple that the <sup>2</sup>girl ate ...

Subsequent regression

<sup>1</sup>   <sup>3</sup>   <sup>2</sup>  
The red apple that the girl ate ...

Subsequent regression

<sup>1</sup>   <sup>3</sup>   <sup>4</sup>   <sup>2</sup>  
The red apple that the girl ate ...

Subsequent regression

<sup>1</sup>   <sup>3</sup>   <sup>4</sup>   <sup>2</sup>   <sup>5</sup>  
The red apple that the girl ate ...

Cumulative PCFG surprisal only handles subsequent regression

## ACCUMULATION ALTERNATIVE: SUCCESSOR SURPRISAL

Cumulative PCFG surprisal only handles subsequent regression

Parafoveal: Th(e <sup>1</sup>red apple that t)he <sup>2</sup>girl ate ...

Prediction: The red <sup>1</sup>(apple that the <sup>2</sup>girl) ate ...  
  └──────────┘  
  accumulated



## Cumulative PCFG surprisal only handles subsequent regression

Parafoveal: Th(e<sup>1</sup> red apple that t)he<sup>2</sup> girl ate ...

Prediction: The red <sup>1</sup>(apple that the <sup>2</sup>girl) ate ...  
└──────────┘  
accumulated

Other accumulation mechanisms presuppose earlier accumulation

Upcoming material influences reading times

Upcoming material influences reading times

- Orthographic effects  
(Pynte, Kennedy, & Ducrot, 2004; Angele, Tran, & Rayner, 2013)

Upcoming material influences reading times

- Orthographic effects  
(Pynte, Kennedy, & Ducrot, 2004; Angele, Tran, & Rayner, 2013)
- Lexical effects  
(Kliegl et al., 2006; Li et al., 2014; Angele et al., 2015)

The <sup>1</sup>red apple that the <sup>2</sup>girl ate ...

$$\text{future-}n\text{-gram}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

The <sup>1</sup>red apple that the <sup>2</sup>girl ate ...

$$\text{future-}n\text{-gram}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

The red <sup>1</sup> apple that the <sup>2</sup> girl ate ...

$$\text{future-}n\text{-gram}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

The red <sup>1</sup> apple that the <sup>2</sup> girl ate ...

$$\text{future-}n\text{-gram}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

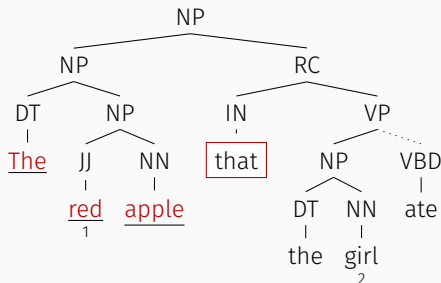


The red <sup>1</sup> apple that the <sup>2</sup> girl ate ...

$$\text{future-}n\text{-gram}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} -\log P(w_i \mid w_{i-n} \dots w_{i-1})$$

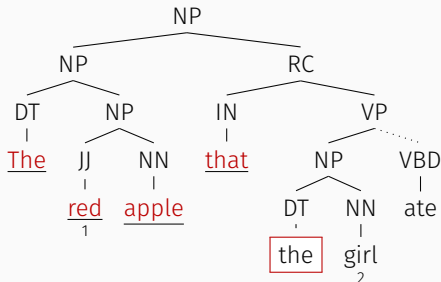


# SUCCESSOR PCFG SURPRISAL



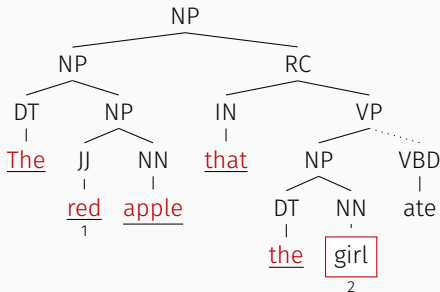
$$\text{Future-PCFG}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$

# SUCCESSOR PCFG SURPRISAL

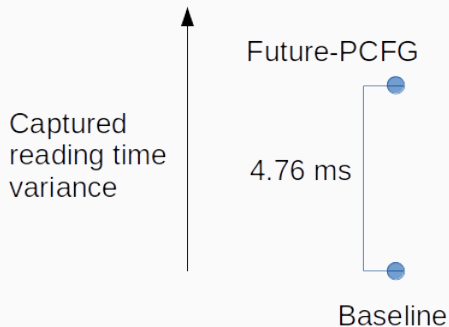


$$\text{Future-PCFG}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$

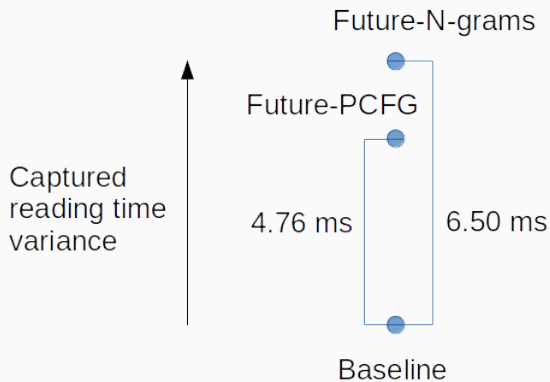
# SUCCESSOR PCFG SURPRISAL



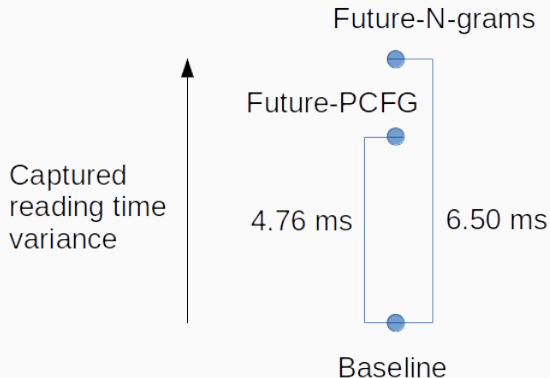
$$\text{Future-PCFG}(w, f_t, f_{t+1}) = \sum_{i=f_t}^{f_{t+1}} \sum_{T \in \text{Trees}} -\log P(T_i = w_i \mid T_1 \dots T_{i-1} = w_1 \dots w_{i-1})$$



# SUCCESSOR N-GRAMS WORK BETTER



# SUCCESSOR N-GRAMS WORK BETTER



PCFG surprisal may require a richer grammar



# SUCCESSOR *N*-GRAMS HAVE LIMITED INFLUENCE

Successor *n*-grams are most predictive for 2 future words ( $p < 0.001$ )

Successor *n*-grams are most predictive for 2 future words ( $p < 0.001$ )

6% of UCL saccades ( $n=3500$ )  $>2$  words

- $N$ -gram surprisal should be accumulated to predict reading times

- $N$ -gram surprisal should be accumulated to predict reading times
- $N$ -gram surprisal accumulates pre- and post-saccade

- $N$ -gram surprisal should be accumulated to predict reading times
- $N$ -gram surprisal accumulates pre- and post-saccade
  - Pre-saccade  $n$ -grams are limited

- $N$ -gram surprisal should be accumulated to predict reading times
- $N$ -gram surprisal accumulates pre- and post-saccade
  - Pre-saccade  $n$ -grams are limited
- PCFG surprisal does not accumulate

- $N$ -gram surprisal should be accumulated to predict reading times
- $N$ -gram surprisal accumulates pre- and post-saccade
  - Pre-saccade  $n$ -grams are limited
- PCFG surprisal does not accumulate
  - PCFG surprisal still predictive on Dundee



- $N$ -gram surprisal should be accumulated to predict reading times
- $N$ -gram surprisal accumulates pre- and post-saccade
  - Pre-saccade  $n$ -grams are limited
- PCFG surprisal does not accumulate
  - PCFG surprisal still predictive on Dundee
  - UCL corpus may not be syntactically complex enough

- $N$ -gram surprisal should be accumulated to predict reading times
- $N$ -gram surprisal accumulates pre- and post-saccade
  - Pre-saccade  $n$ -grams are limited
- PCFG surprisal does not accumulate
  - PCFG surprisal still predictive on Dundee
  - UCL corpus may not be syntactically complex enough
  - PCFG surprisal may need a richer grammar

# THANKS! QUESTIONS?

Thanks to:

- Stefan Frank
- National Science Foundation (DGE-1343012)

## CUMU-*N*-GRAM RESULTS

Model	N-gram vs Cumu- <i>N</i> -gram		
	$\beta$	Log-Likelihood	AIC
Baseline		-12702	25476
Base+Basic	0.035	-12689*	25451
Base+Cumulative	0.055	-12683*	25440
Base+Both		-12683*	25442

Base random: sentpos, wlen, rlen, prefix, 5-gram, cumu-5-gram

Base fixed: sentpos, wlen, rlen, prefix

Significance for the Base+Both model applies to improvement over the Base+Basic model.

## FUTURE SURPRISAL RESULTS

Model	Future- $N$ -grams vs Future-PCFG		
	$\beta$	Log-Likelihood	AIC
Baseline		-12276	24642
Base+Future- $N$ -grams	0.034	-12259*	24610
Base+Future-PCFG	0.025	-12266*	24624
Base+Both		-12259*	24612

Base random: sentpos, wlen, rlen, prefix, cumu-5-gram,  
future-5-grams, future-PCFG

Base fixed: sentpos, wlen, rlen, prefix, cumu-5-gram

Significance for the Base+Both model applies to improvement over the Base+Future-PCFG model.