

1) Grammar to CNF

$$G = S \rightarrow bA | aB$$

$$A \rightarrow bAA | aS | a$$

$$B \rightarrow aBB | bS | b$$

After removing RHS with terminal and more than two non terminals.

$$S_0 \rightarrow S$$

$$P \rightarrow a \quad Q \rightarrow b$$

$$S \rightarrow QA | PB$$

$$A \rightarrow QAA | PS | a$$

$$B \rightarrow PBB | OS | b$$

$$S_0 \rightarrow S$$

$$P \rightarrow a \quad Q \rightarrow b$$

$$T \rightarrow AA$$

$$U \rightarrow BB$$

$$A \rightarrow QT | PS | a$$

$$B \rightarrow PU | OS | b$$

2)  $S \rightarrow aAbB \quad A \rightarrow aA | a \quad B \rightarrow bB | b$ 

Convert to CNF

$$\text{let } P \rightarrow a, \quad Q \rightarrow b$$

$$S \rightarrow PAQB \quad A \rightarrow PA | a \quad B \rightarrow QB | b$$

$$\text{let } R \rightarrow PA \quad T \rightarrow QB$$

$$S \rightarrow RT$$

$$A \rightarrow R | a$$

$$B \rightarrow T | b$$

$$R \rightarrow PA$$

$$T \rightarrow QB$$

4)  $S \rightarrow ASB | \epsilon$ 

$$B \rightarrow SbS | A | bb$$

$$A \rightarrow AS | a$$

Eliminating  $\epsilon$  production,

$$S \rightarrow ASB | AB$$

$$B \rightarrow Shs | Abb | Sb | bS | b$$

$$A \rightarrow aAS | a | aA$$

Eliminating

$$S \rightarrow ASB | AB \quad A \rightarrow aAS | a | aA$$

$$B \rightarrow Shs | bb | Sb | bS | b | aAS | a | aA$$

Simplifying,

$$S_0 \rightarrow S \quad S \rightarrow ASB | AB \quad A \rightarrow aAS | a | aA$$

$$B \rightarrow Shs | bb | Sb | bS | b | aAS | a | aA$$

Removing unit productions:

$$S_0 \rightarrow ASB | AB \quad S \rightarrow ASB | AB \quad A \rightarrow aAS | a | aA$$

$$B \rightarrow Shs | bb | Sb | bS | b | aAS | a | aA$$

$$\text{Let } P \rightarrow a \quad Q \rightarrow b \quad R \rightarrow aA \quad T \rightarrow bS \quad U \rightarrow SB$$

$$S_0 \rightarrow AU | AB \quad S \rightarrow AU | AB \quad A \rightarrow RS | a | PA$$

$$B \rightarrow ST | QQ | SQ | QS | RS | b | a | AA$$