## Churn Decision tree, Pruning tree. & Kernel Classifications

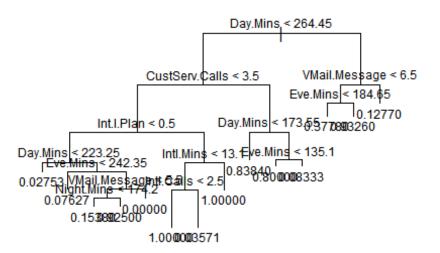
### S. Varatharajan

Tue Oct 16 15:24:51 2018

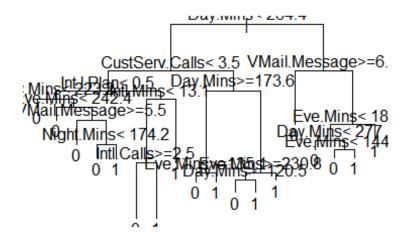
```
setwd("C:/Users/tsraj/Desktop/Acadgild project")
library(readr)
Churn <- read.csv("C:/Users/tsraj/Desktop/Acadgild project/Churn.csv")</pre>
View(Churn)
# enable multi-core processing
library(doParallel)
## Loading required package: foreach
## Loading required package: iterators
## Loading required package: parallel
registerDoParallel()
set.seed(12345)
churnTrain<-Churn[1:2500,]</pre>
churnTest<-Churn[2501:3033,]</pre>
library(C50)
head(churnTrain)
     Account.Length VMail.Message Day.Mins Eve.Mins Night.Mins Intl.Mins
##
## 1
                 128
                                 25
                                       265.1
                                                 197.4
                                                             244.7
                                                                         10.0
## 2
                 107
                                 26
                                       161.6
                                                 195.5
                                                             254.4
                                                                         13.7
## 3
                 137
                                  0
                                       243.4
                                                 121.2
                                                             162.6
                                                                         12.2
                                  0
## 4
                  84
                                       299.4
                                                 61.9
                                                             196.9
                                                                          6.6
## 5
                  75
                                  0
                                       166.7
                                                 148.3
                                                             186.9
                                                                         10.1
## 6
                 118
                                  0
                                       223.4
                                                 220.6
                                                             203.9
                                                                          6.3
     CustServ.Calls Churn Int.l.Plan VMail.Plan Day.Calls Day.Charge
##
## 1
                         0
                   1
                                                 1
                                                          110
                                                                   45.07
## 2
                   1
                         0
                                     0
                                                 1
                                                          123
                                                                   27.47
                   0
                         0
                                     0
                                                 0
## 3
                                                          114
                                                                   41.38
                   2
                         0
                                     1
                                                 0
                                                          71
## 4
                                                                   50.90
## 5
                   3
                         0
                                     1
                                                 0
                                                          113
                                                                   28.34
                                                 0
## 6
                   0
                         0
                                     1
                                                           98
                                                                   37.98
     Eve.Calls Eve.Charge Night.Calls Night.Charge Intl.Calls Intl.Charge
## 1
            99
                     16.78
                                     91
                                                11.01
                                                                3
                                                                          2.70
## 2
           103
                                    103
                                                11.45
                                                                3
                                                                          3.70
                     16.62
                                                                5
## 3
           110
                     10.30
                                    104
                                                 7.32
                                                                          3.29
                                                                7
## 4
            88
                      5.26
                                     89
                                                 8.86
                                                                          1.78
                                                                3
## 5
           122
                     12.61
                                    121
                                                 8.41
                                                                          2.73
## 6
           101
                     18.75
                                    118
                                                 9.18
                                                                6
                                                                          1.70
     State Area.Code
                         Phone
                  415 382-4657
## 1
     KS
```

```
## 2
        ОН
                  415 371-7191
## 3
        NJ
                  415 358-1921
        ОН
## 4
                  408 375-9999
## 5
        OK
                  415 330-6626
## 6
        ΑL
                  510 391-8027
head(churnTest)
        Account.Length VMail.Message Day.Mins Eve.Mins Night.Mins Intl.Mins
##
## 2501
                                    41
                                           215.5
                                                    241.8
                    121
                                                                147.0
                                                                             9.6
## 2502
                    101
                                     0
                                           124.8
                                                    257.2
                                                                193.2
                                                                            13.4
## 2503
                    115
                                     0
                                           178.7
                                                    271.0
                                                                245.9
                                                                            16.4
## 2504
                    168
                                     0
                                           183.2
                                                    179.2
                                                                292.8
                                                                             9.9
## 2505
                     90
                                     0
                                           167.5
                                                    139.1
                                                                138.4
                                                                            13.0
                     70
## 2506
                                     0
                                           147.1
                                                    200.0
                                                                234.9
                                                                            12.5
        CustServ.Calls Churn Int.1.Plan VMail.Plan Day.Calls Day.Charge
##
## 2501
                      1
                             0
                                        0
                                                    1
                                                              95
                                                                       36.64
## 2502
                      0
                             0
                                        0
                                                    0
                                                              66
                                                                       21.22
## 2503
                      2
                             0
                                        0
                                                    0
                                                             114
                                                                       30.38
                      2
                             0
                                        0
                                                    0
                                                             131
## 2504
                                                                       31.14
## 2505
                      1
                             0
                                        0
                                                    0
                                                              96
                                                                       28.48
## 2506
                      3
                             0
                                         0
                                                    0
                                                             105
                                                                       25.01
        Eve.Calls Eve.Charge Night.Calls Night.Charge Intl.Calls Intl.Charge
                92
                        20.55
                                                    6.61
## 2501
                                        108
                                                                    3
                                                                             2.59
## 2502
                85
                        21.86
                                        115
                                                    8.69
                                                                   4
                                                                             3.62
                96
## 2503
                        23.04
                                         94
                                                   11.07
                                                                    5
                                                                             4.43
                                                                    5
## 2504
                73
                                        100
                        15.23
                                                   13.18
                                                                             2.67
                                                                   1
## 2505
               104
                        11.82
                                         87
                                                    6.23
                                                                             3.51
## 2506
               135
                        17.00
                                         65
                                                   10.57
                                                                    9
                                                                             3.38
##
        State Area.Code
                             Phone
                     415 337-2348
## 2501
           UT
## 2502
           ΙL
                     415 342-8702
           DC
## 2503
                     408 393-5802
## 2504
           ΙN
                     415 384-2219
## 2505
           NM
                     415 347-6164
## 2506
           MS
                     510 376-9940
library(tree)
data<-Churn
View(data)
names(data)
##
    [1] "Account.Length" "VMail.Message"
                                             "Day.Mins"
                                                               "Eve.Mins"
  [5] "Night.Mins"
                           "Intl.Mins"
                                             "CustServ.Calls"
                                                               "Churn"
##
  [9] "Int.l.Plan"
                           "VMail.Plan"
                                             "Day.Calls"
                                                               "Day.Charge"
                                             "Night.Calls"
                                                               "Night.Charge"
## [13] "Eve.Calls"
                           "Eve.Charge"
        "Intl.Calls"
                                                               "Area.Code"
## [17]
                           "Intl.Charge"
                                             "State"
## [21] "Phone"
nrow(data)
```

```
## [1] 3333
ncol(data)
## [1] 21
str(data)
## 'data.frame':
                   3333 obs. of 21 variables:
## $ Account.Length: int 128 107 137 84 75 118 121 147 117 141 ...
## $ VMail.Message : int 25 26 0 0 0 0 24 0 0 37 ...
## $ Day.Mins
                    : num 265 162 243 299 167 ...
## $ Eve.Mins
                    : num 197.4 195.5 121.2 61.9 148.3 ...
## $ Night.Mins
                    : num 245 254 163 197 187 ...
## $ Intl.Mins
                    : num 10 13.7 12.2 6.6 10.1 6.3 7.5 7.1 8.7 11.2 ...
## $ CustServ.Calls: int 1 1 0 2 3 0 3 0 1 0 ...
## $ Churn
                   : int 0000000000...
## $ Int.l.Plan
                   : int 0001110101...
## $ VMail.Plan
                   : int 1100001001...
## $ Day.Calls
                    : int 110 123 114 71 113 98 88 79 97 84 ...
## $ Day.Charge
                   : num 45.1 27.5 41.4 50.9 28.3 ...
## $ Eve.Calls
                   : int 99 103 110 88 122 101 108 94 80 111 ...
## $ Eve.Charge
                   : num 16.78 16.62 10.3 5.26 12.61 ...
## $ Night.Calls
                   : int 91 103 104 89 121 118 118 96 90 97 ...
## $ Night.Charge : num 11.01 11.45 7.32 8.86 8.41 ...
## $ Intl.Calls
                    : int 3 3 5 7 3 6 7 6 4 5 ...
## $ Intl.Charge
                   : num 2.7 3.7 3.29 1.78 2.73 1.7 2.03 1.92 2.35 3.02 ...
## $ State
                    : Factor w/ 51 levels "AK", "AL", "AR", ...: 17 36 32 36 37 2
20 25 19 50 ...
## $ Area.Code
                    : int 415 415 415 408 415 510 510 415 408 415 ...
                    : Factor w/ 3333 levels "327-1058", "327-1319",...: 1927 15
## $ Phone
76 1118 1708 111 2254 1048 81 292 118 ...
select_rows<-sample(1:nrow(data), round(0.2*nrow(data)))</pre>
datatest<-data[select rows,]
datatrain<-data[-select_rows,]</pre>
#modelRegtree<-tree(Mark~Motivation+Gender+Age, data=stutrain)</pre>
modelRegtree<-tree(Churn~Account.Length+ VMail.Message+Day.Mins+Eve.Mins+Nigh
t.Mins+Intl.Mins+CustServ.Calls+Int.l.Plan+VMail.Plan+Day.Calls+Day.Charge+Ev
e.Calls+Eve.Charge+Night.Calls+Night.Charge+Intl.Calls+Intl.Charge,data =data
train)
plot(modelRegtree)
text(modelRegtree, pretty = 0, cex=0.75)
```



```
library(rpart)
churn_data<-as.data.frame(data)
tree<-rpart(Churn~Account.Length+ VMail.Message+Day.Mins+Eve.Mins+Night.Mins+
Intl.Mins+CustServ.Calls+Int.l.Plan+VMail.Plan+Day.Calls+Day.Charge+Eve.Calls
+Eve.Charge+Night.Calls+Night.Charge+Intl.Calls+Intl.Charge,data =datatrain,m
ethod="class")
plot(tree)
text(tree, pretty=0)</pre>
```



```
library(rattle)

## Rattle: A free graphical interface for data science with R.

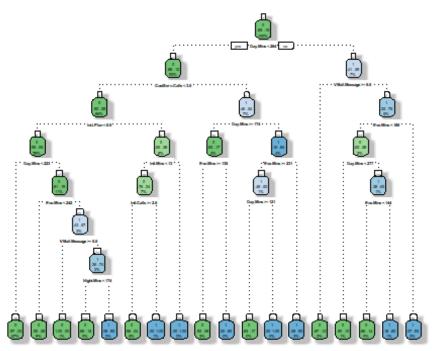
## Version 5.2.0 Copyright (c) 2006-2018 Togaware Pty Ltd.

## Type 'rattle()' to shake, rattle, and roll your data.

rattle()

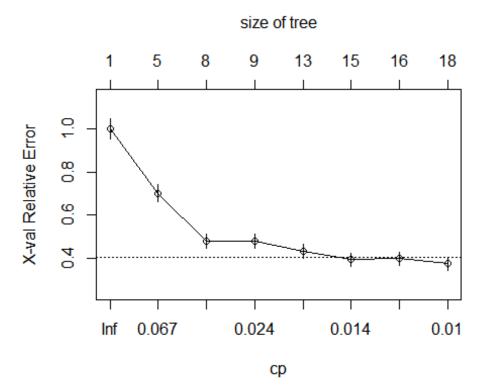
## Loading required package: RGtk2

library(rpart.plot)
library(RColorBrewer)
fancyRpartPlot(tree)
```



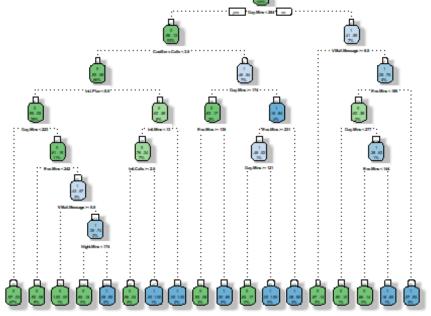
Rattle 2018-Oct-16 15:25:00 tsraj

```
printcp(tree)
##
## Classification tree:
## rpart(formula = Churn ~ Account.Length + VMail.Message + Day.Mins +
       Eve.Mins + Night.Mins + Intl.Mins + CustServ.Calls + Int.l.Plan +
##
       VMail.Plan + Day.Calls + Day.Charge + Eve.Calls + Eve.Charge +
##
       Night.Calls + Night.Charge + Intl.Calls + Intl.Charge, data = datatrai
##
n,
##
       method = "class")
## Variables actually used in tree construction:
## [1] CustServ.Calls Day.Mins
                                      Eve.Mins
                                                     Int.l.Plan
  [5] Intl.Calls
                      Intl.Mins
                                      Night.Mins
                                                     VMail.Message
##
## Root node error: 393/2666 = 0.14741
##
## n= 2666
##
##
           CP nsplit rel error
                                xerror
## 1 0.084606
                       1.00000 1.00000 0.046577
## 2 0.053435
                   4
                       0.66158 0.70229 0.040025
                   7
                       0.46056 0.48092 0.033719
## 3 0.027990
## 4 0.021204
                   8
                       0.43257 0.48092 0.033719
## 5 0.015267
                  12
                       0.34606 0.43511 0.032189
## 6 0.012723
                  14
                       0.31552 0.39440 0.030744
```



```
ptree<- prune(tree, cp= tree$cptable[which.min(tree$cptable[,"xerror"]),"CP"]
)
fancyRpartPlot(ptree, uniform=TRUE, main="Pruned Classification Tree")</pre>
```

# Pruned Classification Tree



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```
pred<-predict(modelRegtree, newdata = datatest)</pre>
head(pred, nrow = 5)
##
         2403
                     2919
                                 2535
                                             2951
                                                                     554
                                                        1520
## 0.83838384 0.08333333 0.02752809 0.02752809 0.02752809 0.03571429
head(pred, n = 5)
##
                     2919
                                 2535
                                             2951
                                                        1520
## 0.83838384 0.08333333 0.02752809 0.02752809 0.02752809
ME<-sum(datatest$Mark-pred)/nrow(datatest)</pre>
ME
## [1] 0
RSS<-sum(datatest$Mark-pred)^2
RSS
## [1] 0
RMSE<-sqrt(RSS/nrow(datatest))</pre>
RMSE
## [1] 0
MAPE<-sum(abs(datatest$Mark-pred)/datatest$Mark)*100
MAPE
```

```
## [1] 0
names(churnTrain)
    [1] "Account.Length"
                         "VMail.Message"
                                           "Day.Mins"
                                                            "Eve.Mins"
                                           "CustServ.Calls"
                                                            "Churn"
##
    [5]
       "Night.Mins"
                         "Intl.Mins"
  [9] "Int.l.Plan"
                         "VMail.Plan"
                                                            "Day.Charge"
                                           "Day.Calls"
## [13] "Eve.Calls"
                                           "Night.Calls"
                         "Eve.Charge"
                                                            "Night.Charge"
                                                            "Area.Code"
## [17] "Intl.Calls"
                         "Intl.Charge"
                                           "State"
## [21] "Phone"
library(rpart)
fit1 <- rpart(Churn~.,data=churnTrain[,-1])</pre>
fit1
## n= 2500
##
## node), split, n, deviance, yval
##
         * denotes terminal node
##
## 1) root 2500 298.8364 0.1388
     2) Phone=327-1319,327-3053,327-3850,327-3954,327-4795,327-5525,327-5817,
327-6179, 327-6194, 327-6764, 327-8732, 327-9289, 327-9341, 328-1206, 328-1222, 328-1
373,328-1522,328-1768,328-2110,328-2236,328-2478,328-2647,328-2982,328-3266,3
28-3402,328-4231,328-5050,328-6289,328-6770,328-7209,328-8147,328-9006,328-93
15,328-9869,329-1955,329-2045,329-2204,329-2388,329-2789,329-2918,329-3222,32
9-3458,329-4391,329-5114,329-5377,329-6144,329-6191,329-6192,329-6562,329-710
2,329-8056,329-8115,329-9001,329-9046,329-9364,329-9847,330-1175,330-1835,330
-2693,330-2849,330-2881,330-3008,330-3429,330-3589,330-4419,330-4914,330-5168
,330-5255,330-5462,330-6165,330-6208,330-6436,330-6626,330-6630,330-7483,330-
7486,330-8142,330-8173,330-8351,330-9833,331-2144,331-3174,331-3202,331-3698,
331-3842,331-4807,331-4902,331-5138,331-5919,331-5962,331-5999,331-6229,331-6
270,331-6629,331-7342,331-7425,331-8462,331-8484,331-8909,331-9149,331-9293,3
31-9861,332-1060,332-1109,332-1494,332-1502,332-2126,332-2137,332-2258,332-24
62,332-2965,332-3381,332-3544,332-3642,332-4289,332-4291,332-5582,332-5596,33
2-5964,332-6633,332-6934,332-6958,332-7607,332-8103,332-8160,332-8764,332-911
8,332-9446,332-9460,332-9525,332-9891,333-1967,333-2337,333-2611,333-2906,333
-3221,333-3421,333-3447,333-3460,333-3531,333-3595,333-3704,333-4154,333-5295
,333-5430,333-5551,333-5609,333-7449,333-7460,333-7637,333-7749,333-7961,333-
8180,333-8822,333-8954,333-9133,333-9253,333-9266,333-9511,333-9728,333-9826,
334-1311,334-1337,334-1508,334-1872,334-2577,334-2729,334-2730,334-3142,334-3
289,334-4354,334-4438,334-4506,334-4678,334-5223,334-5263,334-5337,334-5634,3
34-5844,334-6142,334-6605,334-7443,334-7618,334-7685,334-8817,334-8967,334-91
82,334-9806,335-1838,335-2261,335-2274,335-2331,335-3110,335-3133,335-3320,33
5-3681,335-3880,335-3913,335-4414,335-4584,335-4719,335-5591,335-5806,335-588
2,335-7257,335-8146,335-8427,335-8836,335-9066,335-9501,335-9726,335-9786,336
-1043,336-1090,336-1462,336-1574,336-1749,336-2090,336-2829,336-3488,336-3738
,336-4281,336-4656,336-5406,336-5616,336-5661,336-5702,336-5900,336-5920,336-
6085,336-6128,336-6533,336-6907,336-6997,336-7143,336-7155,336-7357,336-7600,
336-8010, 336-9390, 336-9901, 337-1151, 337-1225, 337-1506, 337-2442, 337-3740, 337-3
769,337-4101,337-4339,337-4697,337-4749,337-6851,337-6898,337-7163,337-7377,3
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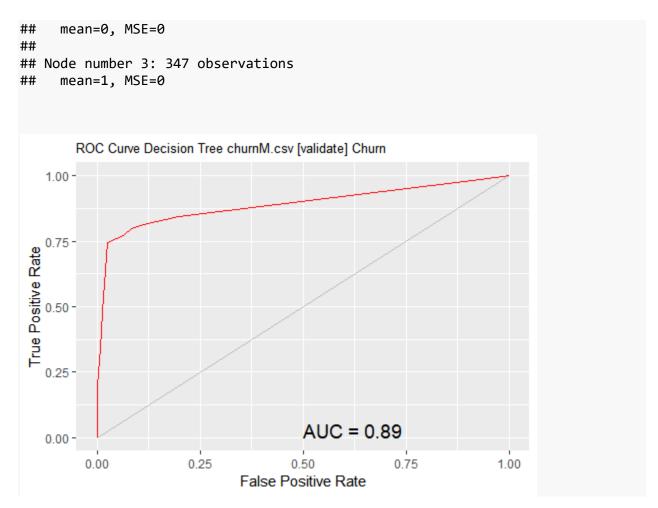
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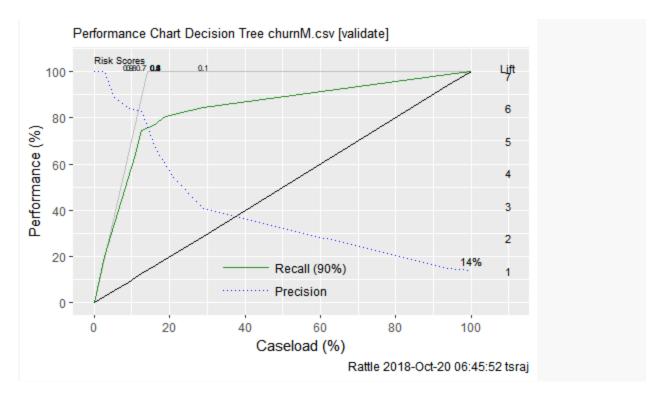
3) Phone=327-3587,327-8495,328-6011,328-7833,328-8980,329-2786,329-6603, 329-7347, 329-9067, 329-9667, 330-4978, 330-7754, 330-9354, 331-1391, 332-2889, 332-5 084,332-5521,332-5949,332-6139,332-6181,333-4594,333-5101,333-7631,334-1275,3 34-5029,334-6519,334-8694,334-9505,335-1697,335-1874,335-2019,335-2967,335-48 58,335-4888,335-6508,336-3819,336-8343,337-7167,337-8618,338-1027,338-6018,33 8-6962,339-1330,339-3049,339-6477,339-6637,339-7541,340-1876,340-4972,340-690 8,340-8323,341-1191,341-4463,341-7686,341-8719,342-4122,342-8167,343-1965,343 -2592,343-5219,343-5709,343-6940,343-7019,344-1136,344-3160,344-3466,344-7197 ,345-1524,345-9140,346-1629,346-2020,346-5068,346-7656,347-3406,348-4316,348-5725,348-6720,348-6853,348-7193,348-8015,349-3112,350-7114,350-7306,351-4025, 351-7005, 351-7269, 351-7309, 352-4418, 352-5118, 352-5466, 352-6068, 352-6976, 352-7 752,352-8327,353-3759,353-6007,353-7292,353-8363,353-9998,354-5689,355-2464,3 55-2634,355-3801,355-6291,355-6837,356-5475,356-8449,357-1909,357-5696,357-60 39,357-9136,358-2490,358-4576,358-9095,359-4336,359-5731,360-1171,360-1596,36 0-3324,361-2349,361-6563,362-5111,362-9748,363-1069,364-3286,364-5510,364-764 4,364-7719,364-9040,364-9904,365-2008,365-5979,365-7774,366-1613,366-2273,366 -3358, 366-5829, 366-6345, 366-7247, 366-7912, 367-1681, 367-3220, 367-8168, 367-8692 ,368-1288,368-5437,368-7555,368-7706,369-5449,369-7017,369-8024,370-2688,370-5527,370-7574,370-9116,370-9755,371-1727,371-2500,371-6284,371-9457,372-3750, 372-6497,372-7990,373-1448,373-2053,373-4264,373-8483,373-8908,374-1981,374-5 353, 374-7787, 374-8042, 374-8329, 374-9107, 374-9203, 374-9576, 375-1476, 375-2184, 3 75-2975,375-3826,375-4107,376-8573,376-9607,377-1273,377-1293,377-4169,377-50 43,378-3508,378-3625,378-6276,379-1720,379-2503,379-6970,379-7215,379-8681,37 9-9524,380-2558,380-3437,380-4080,380-7742,380-7816,380-8727,381-4029,382-493 2,382-5401,383-1657,383-4061,383-6029,383-6095,384-2372,384-3299,384-5004,384 -5632,384-8723,385-7148,385-8184,385-8997,386-2810,386-4170,387-1535,387-2604 ,387-5453,387-5533,387-5860,387-7371,387-9137,388-2240,388-6026,388-9285,390-

```
2390,390-5055,390-7930,390-9627,390-9811,391-1737,392-2555,393-4823,393-6840,
393-7826,393-7984,394-4520,394-7447,394-8402,395-3026,395-6195,395-7923,395-9
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7,405-3916,405-4109,405-4920,405-5305,405-5403,405-6189,405-7676,406-2242,406
-3069,406-9926,407-2259,407-7258,408-4529,408-4836,408-6326,409-4447,409-4734
,409-7523,409-9911,410-6791,410-7611,411-2958,411-4714,411-5958,411-7778,412-
1991,412-2520,413-2194,413-2241,413-4040,413-5190,413-7468,413-7743,413-9269,
414-1496,414-7090,414-8718,415-4564,415-8448,416-1676,416-2778,416-5660,416-6
886,416-8701,417-3999,417-4810,417-4826,418-5300,418-6455,418-6651,418-6737,4
18-7055,418-9036,419-1674,419-1714,419-1863,419-5171,419-8987,420-6465,420-78
23,420-8435,420-8897,420-9838,420-9971,421-8537,422-5350 347 0.0000 1.0000
summary(fit1)
## Call:
## rpart(formula = Churn ~ ., data = churnTrain[, -1])
   n= 2500
##
    CP nsplit rel error
                  xerror
         0
## 1 1.00
               1 1.000371 0.04180395
## 2 0.01
         1
               0 1.187941 0.05840154
##
## Variable importance
##
       Phone
             Day.Charge
                        Day.Mins CustServ.Calls
##
         84
                             6
##
## Node number 1: 2500 observations,
                         complexity param=1
##
   mean=0.1388, MSE=0.1195346
   left son=2 (2153 obs) right son=3 (347 obs)
##
##
   Primary splits:
     Phone
               splits as
                      -LLRLLLL-LLL-RLLL-LLLLLLLLLLLL-RLL-RL-
##
--LLLLLLL-RRLLLL----LLRLL-LLLL--LLRLL-LLLLL--LLLLLRLLLLRLLLLL-LRLLLLRLL-LR
L-RL-LLL---RRLLLRLLLLLLR-LLLLL-LLLR-LLLLL-LRL-L-RL-L-LLRLLL-LLRL-LLRL-LL
```

```
---LLRLRL-LL-LLL-LL-LLL-LLLLLLLL-LLLLLL-LLLLRLL-R-R--LLRR--LLRLLLR-RL
, (0 missing)
##
  Day.Mins
      < 264.55 to the left,
            improve=0.09769634, (0 missing
)
##
  Day.Charge
      < 44.975 to the left,
            improve=0.09769634, (0 missing
)
##
  CustServ.Calls < 3.5
        to the left,
            improve=0.09755406, (0 missing
)
##
  Int.1.Plan
      < 0.5
        to the left,
            improve=0.06796193, (0 missing
)
##
 Surrogate splits:
##
  Day.Mins
      < 284.15 to the left,
            agree=0.870, adj=0.066, (0 spl
it)
            agree=0.870, adj=0.066, (0 spl
      < 48.305 to the left,
##
  Day.Charge
it)
  CustServ.Calls < 4.5
            agree=0.869, adj=0.058, (0 spl
##
        to the left,
it)
  Eve.Mins
            agree=0.862, adj=0.003, (0 spl
##
      < 335.85 to the left,
it)
##
  Eve.Charge
      < 28.545 to the left,
            agree=0.862, adj=0.003, (0 spl
it)
##
## Node number 2: 2153 observations
```



The area under the Risk and Recall curves for Decision Tree model Area under the Recall (green) curve: 90% (0.898)



Error matrix for the Decision Tree model on churnM.csv [validate] (counts):

#### Predicted

Actual 0 1 Error

0 418 11 2.6

1 18 52 25.7

Error matrix for the Decision Tree model on churnM.csv [validate] (proportions):

#### Predicted

Actual 0 1 Error

 $0\ 83.8\ 2.2\ 2.6$ 

1 3.6 10.4 25.7

Overall error: 5.8%, Averaged class error: 14.15%

```
#Kernlab Classification
require(kernlab)
## Loading required package: kernlab
installed.packages("kernlab")
##
        Package LibPath Version Priority Depends Imports LinkingTo Suggests
##
        Enhances License License is FOSS License restricts use OS type Archs
        MD5sum NeedsCompilation Built
##
library(kernlab)
churn classifier<-ksvm(Churn ~., data =datatrain , kernel='vanilladot')</pre>
   Setting default kernel parameters
churn classifier
## Support Vector Machine object of class "ksvm"
##
## SV type: eps-svr (regression)
## parameter : epsilon = 0.1 cost C = 1
##
## Linear (vanilla) kernel function.
## Number of Support Vectors : 2203
##
## Objective Function Value : -718.7691
## Training error : 0.221987
churn_predictions<-predict(churn_classifier,datatest)</pre>
head(churn predictions)
##
               [,1]
## 2403 0.17884755
## 2919 0.22759370
## 2535 0.08201885
## 2951 -0.01274966
## 1520 0.14549398
## 554 0.21449679
table(churn_predictions, datatest$Churn)
##
## churn_predictions
                           0 1
     -0.246864954149444
                           1 0
```

```
##
     -0.199376134699389
                             1 0
##
                             1 0
     -0.169327799847542
##
     -0.167466134077193
                             1 0
##
     -0.153902400184883
                             1 0
##
     -0.129407777518702
                             1 0
##
     -0.119184901940138
                             1 0
##
     -0.108528032074328
                             1 0
##
     -0.0986546483714096
                             1 0
##
     -0.0978416954500534
                             1 0
##
     -0.0959979081211554
                             1 0
##
     -0.0953575595732112
                             1 0
##
     -0.092792110536179
                             1 0
##
     -0.0885310736611716
                             1 0
##
     -0.0846768157831452
                             1 0
##
     -0.0815618723621662
                             1 0
##
     -0.0809232395464094
                             1 0
##
     -0.0807271032893598
                             1 0
##
     -0.0801305846795515
                             1 0
##
     -0.0793766990903454
                             1 0
##
     -0.0766755154776203
                             1 0
##
     -0.0747586808437682
                             1 0
##
     -0.0727274215576317
                             0 1
##
     -0.0709561111655188
                             1 0
##
     -0.0703283845416149
                             1 0
##
     -0.0695000702156509
                             1 0
##
     -0.0656235089571222
                             1 0
     -0.0642209534347146
##
                             1 0
##
     -0.06097837436165
                             1 0
##
     -0.0607365290186764
                             1 0
##
     -0.0590208815558827
                             1 0
##
     -0.0585917262607419
                             1 0
##
     -0.0580494290470151
                             1 0
##
     -0.0542350152938703
                             1 0
##
     -0.0538633654592075
                             1 0
##
     -0.0513850499725406
                             1 0
##
     -0.0506137046752094
                             1 0
##
     -0.0502048065785007
                             1 0
##
     -0.0488587771900107
                             1 0
##
     -0.0487443993104588
                             1 0
##
     -0.0486287061741893
                             1 0
##
     -0.0478585795397038
                             1 0
##
     -0.0475623528782321
                             1 0
##
     -0.0468148450816511
                             1 0
##
     -0.0450317294011737
                             1 0
##
     -0.043477897838293
                             1 0
                             1 0
##
     -0.0417286152768088
##
     -0.0417022546337522
                             1 0
##
     -0.0414912835944619
                             1 0
##
     -0.0401541332083682
                             1 0
##
     -0.0399947126230921
                             0 1
```

```
##
     -0.0391761700860333
                             1 0
##
                             1 0
     -0.0382630098379608
##
     -0.037425799161757
                             1 0
##
     -0.0369095021803348
                             1 0
##
     -0.0366210845211981
                             1 0
##
     -0.0364036684152444
                             1 0
##
     -0.0358084767302908
                             1 0
##
     -0.0355072900549292
                             1 0
##
     -0.034722971492802
                             1 0
##
     -0.0342046721611682
                             1 0
##
     -0.0339384069847862
                             1 0
##
     -0.033684548870159
                             1 0
##
     -0.0335615474565367
                             1 0
##
     -0.0290539244068106
                             1 0
##
     -0.028780832993049
                             1 0
##
     -0.0279722306987139
                             1 0
##
     -0.0278959475993048
                             1 0
##
     -0.0274254719251915
                             1 0
##
     -0.0261689884540718
                             1 0
     -0.02507972450408
##
                             1 0
##
     -0.0245117028132695
                             1 0
##
     -0.0243769918466528
                             1 0
##
     -0.0230370319290666
                             1 0
##
     -0.022676255297833
                             1 0
##
     -0.0223047333150429
                             1 0
##
     -0.0218405712205973
                             1 0
##
     -0.0212428633206152
                             1 0
     -0.0205227224256447
##
                             1 0
##
     -0.0203253100228142
                             1 0
##
     -0.019600045375044
                             1 0
##
     -0.0187688064650692
                             0 1
##
     -0.0180621928981769
                             1 0
##
     -0.018056520002233
                             1 0
##
     -0.0174541147741836
                             1 0
##
     -0.0160931550477125
                             1 0
##
     -0.0156098517474016
                             1 0
##
     -0.0153673880536793
                             1 0
##
     -0.015365473100468
                             1 0
     -0.0152504594841301
##
                             1 0
##
     -0.0127496557004724
                             0 1
##
     -0.0111055098235918
                             1 0
##
     -0.0106615318484521
                             1 0
##
     -0.0106166521040775
                             1 0
##
     -0.0100556685335028
                             1 0
##
     -0.00993408683304367
                             1 0
     -0.00882737026536493
##
                             1 0
##
     -0.00791777370717872
                             1 0
##
     -0.00753439242064932
                             1 0
##
     -0.00708538792277791
                             1 0
##
     -0.00682479685585138
                             1 0
```

```
##
     -0.00646976309265887
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##
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##
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##
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     0.280814644540291
```

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     0.303726176120791
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     0.313943628502287
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##
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##
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##
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     0.323863056355359
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##
     0.327548818864728
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##
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##
##
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##
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##
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##
                             1 0
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     0.350598220470265
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##
     0.354153666135993
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##
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##
     0.361322074553591
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##
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##
     0.380736162398554
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##
     0.383994601945891
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##
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     0.389367764556234
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     0.389797556787527
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##
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##
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##
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##
     0.402839508549078
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##
     0.40310270880616
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```

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##
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     0.414658347176808
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##
                            0 1
     0.416040655732383
##
     0.416467014263133
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##
     0.423725866093656
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##
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##
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##
     0.44743234282441
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##
     0.464671775752811
                            0 1
##
     0.468488043807066
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##
     0.476221336505797
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##
     0.488694695208939
                           1 0
##
     0.57464617741042
                            0 1
##
     0.585560042556624
                            0 1
agreement<-churn_predictions == datatest$Churn</pre>
table(agreement)
## agreement
## FALSE
##
     667
prop.table(table(agreement))
## agreement
## FALSE
##
       1
agreement
         [,1]
## 2403 FALSE
## 2919 FALSE
## 2535 FALSE
## 2951 FALSE
## 1520 FALSE
## 554 FALSE
## 1082 FALSE
## 1694 FALSE
## 2420 FALSE
## 3290 FALSE
## 115 FALSE
## 507 FALSE
## 2444 FALSE
## 4
        FALSE
## 1299 FALSE
## 1535 FALSE
## 1288 FALSE
## 1335 FALSE
```

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## 594 FALSE
## 3154 FALSE
## 1504 FALSE
## 1083 FALSE
## 3197 FALSE
## 2342 FALSE
## 2133 FALSE
## 1290 FALSE
## 2311 FALSE
## 1799 FALSE
## 749 FALSE
## 1601 FALSE
## 2620 FALSE
## 20
        FALSE
## 620 FALSE
## 2251 FALSE
## 1221 FALSE
## 1193 FALSE
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## 2981 FALSE
## 2035 FALSE
## 442 FALSE
## 2576 FALSE
## 1413 FALSE
## 3052 FALSE
## 2544 FALSE
## 855 FALSE
## 1057 FALSE
## 198 FALSE
## 143 FALSE
## 181 FALSE
## 2055 FALSE
## 3167 FALSE
## 2716 FALSE
## 1034 FALSE
## 699 FALSE
## 2402 FALSE
## 1637 FALSE
## 2392 FALSE
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## 1427 FALSE
## 775 FALSE
## 2591 FALSE
## 847 FALSE
## 3226 FALSE
## 2475 FALSE
## 3203 FALSE
## 716 FALSE
## 3100 FALSE
## 489 FALSE
```

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## 2247 FALSE
## 1650 FALSE
## 1217 FALSE
## 1095 FALSE
## 158 FALSE
## 2017 FALSE
## 3132 FALSE
## 3309 FALSE
## 1662 FALSE
## 3266 FALSE
## 2832 FALSE
## 1673 FALSE
## 29
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        FALSE
## 470 FALSE
## 991 FALSE
## 2681 FALSE
## 1631 FALSE
## 2608 FALSE
## 197 FALSE
## 3010 FALSE
## 2621 FALSE
## 256 FALSE
## 1948 FALSE
## 2316 FALSE
## 1664 FALSE
## 2332 FALSE
## 2427 FALSE
## 310 FALSE
## 1287 FALSE
## 953 FALSE
## 1995 FALSE
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## 1997 FALSE
## 1684 FALSE
## 2914 FALSE
## 2058 FALSE
## 2789 FALSE
## 810 FALSE
## 694 FALSE
## 1965 FALSE
## 1236 FALSE
## 2433 FALSE
## 1223 FALSE
## 2560 FALSE
## 2915 FALSE
## 3166 FALSE
## 1891 FALSE
```

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## 31 FALSE
## 1032 FALSE
## 1798 FALSE
## 1654 FALSE
## 289 FALSE
## 2194 FALSE
## 2279 FALSE
## 2568 FALSE
## 3028 FALSE
## 599 FALSE
## 894 FALSE
## 2481 FALSE
## 108 FALSE
## 2152 FALSE
## 2602 FALSE
## 2123 FALSE
## 3022 FALSE
## 2798 FALSE
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## 592 FALSE
## 312 FALSE
## 2580 FALSE
## 1667 FALSE
## 2214 FALSE
## 691 FALSE
## 2010 FALSE
## 469 FALSE
## 3058 FALSE
## 3156 FALSE
## 1582 FALSE
## 2930 FALSE
## 1185 FALSE
## 2633 FALSE
## 1779 FALSE
## 2532 FALSE
## 1120 FALSE
## 663 FALSE
## 2495 FALSE
## 2171 FALSE
## 1373 FALSE
## 2688 FALSE
## 1911 FALSE
## 2351 FALSE
## 1888 FALSE
## 2701 FALSE
## 2581 FALSE
## 1206 FALSE
## 1560 FALSE
## 3147 FALSE
## 552 FALSE
```

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## 2641 FALSE
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## 3066 FALSE
## 596 FALSE
## 2369 FALSE
## 975 FALSE
## 1198 FALSE
## 2371 FALSE
## 2224 FALSE
## 2906 FALSE
## 2510 FALSE
## 2615 FALSE
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## 1094 FALSE
## 2953 FALSE
## 514 FALSE
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## 3158 FALSE
## 2784 FALSE
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## 3091 FALSE
## 22
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## 764 FALSE
## 1437 FALSE
## 1845 FALSE
## 2796 FALSE
## 388 FALSE
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## 1738 FALSE
## 3295 FALSE
## 925 FALSE
## 2172 FALSE
## 1179 FALSE
## 815 FALSE
## 2933 FALSE
## 1344 FALSE
## 1020 FALSE
## 3193 FALSE
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## 1950 FALSE
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## 3211 FALSE
## 1663 FALSE
## 2787 FALSE
## 2207 FALSE
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## 1857 FALSE
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## 2603 FALSE
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## 2434 FALSE
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## 2289 FALSE
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## 1686 FALSE
## 90
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## 1028 FALSE
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## 842 FALSE
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## 1024 FALSE
## 3084 FALSE
## 862 FALSE
## 3270 FALSE
## 653 FALSE
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## 1980 FALSE
## 1749 FALSE
## 2054 FALSE
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## 718 FALSE
## 1382 FALSE
## 1029 FALSE
## 1213 FALSE
## 1305 FALSE
## 2887 FALSE
## 672 FALSE
## 1103 FALSE
## 2664 FALSE
## 1591 FALSE
## 1767 FALSE
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## 1215 FALSE
## 3261 FALSE
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## 948 FALSE
## 3034 FALSE
## 483 FALSE
## 689 FALSE
## 1170 FALSE
## 2549 FALSE
## 2211 FALSE
## 2025 FALSE
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## 2881 FALSE
## 2187 FALSE
## 1470 FALSE
## 2638 FALSE
## 1734 FALSE
## 2078 FALSE
## 2725 FALSE
## 2506 FALSE
## 1538 FALSE
## 1873 FALSE
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## 2819 FALSE
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## 2249 FALSE
## 2043 FALSE
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## 1895 FALSE
## 1954 FALSE
## 2167 FALSE
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## 1713 FALSE
## 104 FALSE
## 2341 FALSE
## 538 FALSE
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## 1428 FALSE
## 721 FALSE
## 1018 FALSE
## 2129 FALSE
## 2584 FALSE
## 754 FALSE
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## 3173 FALSE
## 3326 FALSE
## 1572 FALSE
## 2324 FALSE
## 2745 FALSE
## 1841 FALSE
## 1912 FALSE
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## 2883 FALSE
## 910 FALSE
## 1351 FALSE
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## 3128 FALSE
## 906 FALSE
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## 2313 FALSE
## 2536 FALSE
## 1823 FALSE
## 556 FALSE
## 2666 FALSE
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## 1484 FALSE
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## 222 FALSE
## 1391 FALSE
## 776 FALSE
## 677 FALSE
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## 695 FALSE
## 3237 FALSE
## 230 FALSE
## 1584 FALSE
## 2095 FALSE
## 120 FALSE
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## 2162 FALSE
## 2248 FALSE
## 2963 FALSE
## 1132 FALSE
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## 732 FALSE
## 2916 FALSE
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## 2851 FALSE
## 891 FALSE
## 786 FALSE
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## 1976 FALSE
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## 1138 FALSE
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## 3271 FALSE
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## 3188 FALSE
## 2370 FALSE
## 1454 FALSE
## 2004 FALSE
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## 1527 FALSE
## 265 FALSE
## 2875 FALSE
## 2655 FALSE
## 626 FALSE
## 2472 FALSE
## 1625 FALSE
## 1140 FALSE
## 2993 FALSE
## 1079 FALSE
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## 2331 FALSE
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## 916 FALSE
## 1194 FALSE
## 2220 FALSE
## 1832 FALSE
## 745 FALSE
## 3205 FALSE
## 2100 FALSE
## 2216 FALSE
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## 3191 FALSE
## 2966 FALSE
## 814 FALSE
## 1522 FALSE
## 1131 FALSE
## 1835 FALSE
## 410 FALSE
## 2466 FALSE
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## 2559 FALSE
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## 2833 FALSE
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## 1325 FALSE
## 940 FALSE
## 2005 FALSE
## 2148 FALSE
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## 2383 FALSE
## 2644 FALSE
## 2959 FALSE
## 2430 FALSE
## 215 FALSE
## 1796 FALSE
## 1117 FALSE
## 2112 FALSE
## 2088 FALSE
## 1049 FALSE
## 957 FALSE
## 1898 FALSE
## 911 FALSE
## 1928 FALSE
## 603 FALSE
## 2926 FALSE
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## 2523 FALSE
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## 1245 FALSE
## 840 FALSE
## 852 FALSE
## 1610 FALSE
## 2612 FALSE
## 2270 FALSE
## 3299 FALSE
## 998 FALSE
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## 1827 FALSE
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## 1135 FALSE
## 735 FALSE
## 2858 FALSE
## 674 FALSE
## 1500 FALSE
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## 2790 FALSE
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## 2128 FALSE
## 3163 FALSE
## 1234 FALSE
## 1407 FALSE
## 2477 FALSE
## 1050 FALSE
## 717 FALSE
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## 1893 FALSE
## 996 FALSE
## 3285 FALSE
## 189 FALSE
## 1567 FALSE
## 1890 FALSE
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## 736 FALSE
## 2614 FALSE
## 1438 FALSE
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## 1730 FALSE
## 1494 FALSE
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## 690 FALSE
## 1291 FALSE
## 2301 FALSE
## 645 FALSE
## 2136 FALSE
## 3134 FALSE
## 921 FALSE
## 2143 FALSE
## 654 FALSE
## 927 FALSE
## 1167 FALSE
## 2799 FALSE
## 1801 FALSE
## 1983 FALSE
## 451 FALSE
## 139
       FALSE
## 2917 FALSE
## 314 FALSE
## 44
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## 2130 FALSE
## 731 FALSE
## 1863 FALSE
## 608 FALSE
## 2945 FALSE
## 3104 FALSE
## 2137 FALSE
## 2829 FALSE
## 3251 FALSE
## 1377 FALSE
## 1996 FALSE
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## 2413 FALSE
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## 3222 FALSE
## 1282 FALSE
## 1403 FALSE
## 446 FALSE
## 2406 FALSE
## 546 FALSE
## 1726 FALSE
## 121 FALSE
## 1009 FALSE
## 1641 FALSE
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## 2457 FALSE
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## 2594 FALSE
## 1483 FALSE
## 3018 FALSE
## 3013 FALSE
## 1017 FALSE
## 1136 FALSE
## 3135 FALSE
## 180 FALSE
## 216 FALSE
## 1168 FALSE
## 2736 FALSE
## 305 FALSE
## 2841 FALSE
## 2695 FALSE
## 1746 FALSE
## 1371 FALSE
## 1958 FALSE
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## 2276 FALSE
## 1361 FALSE
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## 2896 FALSE
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## 1399 FALSE
## 2213 FALSE
## 880 FALSE
## 1831 FALSE
## 1656 FALSE
## 2929 FALSE
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## 883 FALSE
## 2242 FALSE
## 3131 FALSE
## 2467 FALSE
## 233 FALSE
## 1833 FALSE
## 2967 FALSE
## 1699 FALSE
## 1122 FALSE
## 2836 FALSE
```

#### **KSVM Classification**

```
set.seed(12345)
churn_classifier_rbf<-ksvm(Churn ~., data = datatrain, kernel='rbfdot')
churn_predictions_rbf<-predict(churn_classifier_rbf,datatest)
agreement_rbf<-churn_predictions_rbf == datatest$Churn
table(agreement_rbf)

## agreement_rbf
## FALSE
## 667
prop.table(table(agreement_rbf))

## agreement_rbf
## FALSE
## 1</pre>
```

