

VM paging

./paging-linear-translate.py -v

Page Table

[0]	0x8000000c
[1]	0x00000000
[2]	.. 0
[3]	0x800006

VA trace

VA 0x00003229 (decimal: 12841) → PA or invalid address

VPN and offset

$$a\text{size} = 16KB$$

$$p\text{size} = 4KB$$

$$14 \text{ bits} \cdot VA \rightarrow 12 \text{ bits} \begin{matrix} \text{offset} \\ \downarrow \end{matrix} + 2 \text{ bits} \begin{matrix} \text{VPN} \end{matrix}$$

0x3229 → 0b11001000101001
↓
1, VPN

$\Rightarrow 3 \rightarrow 6$ PFN (from
page table)

$0x6000$ OR $0x0229$ (offset) $\Rightarrow 0x6229$ valid

VA $0x1369$

VPN = b01 = ① $\Rightarrow 0x0$ invalid

VA $0x1e80$

VPN = b10 = ② $\Rightarrow 0x0$ invalid \times

VA $0x2556$

VPN = b10 = ③ $\Rightarrow 0x0$ invalid

VA $0x3a1e$

VPN = b11 = ④ $\Rightarrow 0x6000$ valid

$$0x6000 \text{ OR } 0x1e = 0x6a1e \checkmark$$

① $\alpha_{size} \uparrow$ page-table size \uparrow since
page size is same

$$\alpha_{size} = 1m$$

[1012]	0x8001d1ab
[1013]	0x8007df94
[1014]	0x800052d0
[1015]	0x00000000
[1016]	0x00000000
[1017]	0x00000000
[1018]	0x00000000
[1019]	0x8002e9c9
[1020]	0x00000000
[1021]	0x00000000
[1022]	0x00000000
[1023]	0x00000000

$$\alpha_{size} = 2m$$

[2042]	0x00000000
[2043]	0x00000000
[2044]	0x00000000
[2045]	0x00000000
[2046]	0x8000eedd
[2047]	0x00000000

$$\alpha_{size} = 4m$$

[4091]	0x800160f8
[4092]	0x80015abc
[4093]	0x8001483a
[4094]	0x00000000
[4095]	0x8002e298

Page size increase \uparrow , page table size \downarrow

$P = 1K$

[1020]	0x00000000
[1021]	0x00000000
[1022]	0x00000000
[1023]	0x00000000

$R = 2K$

[507]	0x00000000
[508]	0x8001a7f2
[509]	0x8001c337
[510]	0x00000000
[511]	0x00000000

$P = 4K$

[250]	0x00000000
[251]	0x8001efec
[252]	0x8001cd5b
[253]	0x800125d2
[254]	0x80019c37
[255]	0x8001fb27

Using big pages we don't use

① general because

① Need more time to load
from disk \rightarrow memory

② Takes more space in
memory, leading to more
quickly memory fill up
potentially leading to quicker
eviction of pages.

$$\textcircled{1} \quad \text{a size} = 16\text{K} = 2^4 \times 2^{10} = 2^{14}$$

✓

$$\text{p size} = 1\text{K}$$

$$14 \text{ bits} \Rightarrow \frac{\text{a size}}{\text{p size}} = 16 = 2^4$$

↑ Pages

$$\begin{array}{c} 4 \text{ bits} + 10 \text{ bits} \\ \text{VPN} \qquad \text{offset} \end{array}$$

2^{4+8}

$$\text{VA } 0x3986 \Rightarrow 0b\underbrace{110}_{\downarrow}0110000110$$

(page table)

$$\text{VPN} = 14 \Rightarrow 0x00$$

invalid

$$\text{VA } 0x2bc6 \Rightarrow 0b\underbrace{1010111}_{\downarrow}000110$$

(page table)

$$\text{VPN} = 2+8 = 10 \Rightarrow 0x1300$$

valid

$$\text{Offset} = 0x3c6$$

$$\text{PA} = \text{PFN} \times \text{Page size} + \text{Offset}$$

$$= 0x4fec6$$

$$\text{VA } 0x1e37 \Rightarrow 0b\underbrace{0111}_{\downarrow}000110111$$

(page table)

$$\text{VPN} = 1+2+4 = 7 \Rightarrow 0x00$$

invalid X

VA $0x671 \Rightarrow$ 0b000100110001

\downarrow
 $VFN = 1 \Rightarrow 0x00$
invalid

-

VA $0x1bc9 \Rightarrow$ 0b0110111001001

\downarrow

$VFN = 2+4=6 \Rightarrow 0x00$
invalid X

With $u=50$

VA = $0x3385 \Rightarrow$ 0b100110000101

\downarrow
 $NPR = 4+8=12$

0xf
valid

offset = $0x385$

$$\begin{aligned}
 PA &= \text{psize} \times \text{PFN} + \text{offset} \\
 &= 0x4 \times 0xf + 0x385 \\
 &= 0x3f85
 \end{aligned}$$

$$\begin{aligned}
 VA &= 0x231d \Rightarrow 0b\underline{100}\underline{100}\underline{0}\underline{1}\underline{1}\underline{0}\underline{1} \\
 &\quad \downarrow \\
 &\quad \text{VPN} = 8 \Rightarrow 0x0 \\
 &\quad \text{invalid}
 \end{aligned}$$

$$\begin{aligned}
 VA &= 0xe6 \Rightarrow 0b\underline{0}\underline{0}\underline{0}\underline{0}\underline{1}\underline{1}\underline{0}\underline{0}\underline{1}\underline{1}\underline{0} \\
 &\quad \text{VPN} = 0 \Rightarrow 0x18
 \end{aligned}$$

$$\text{Offset} = 0xe6$$

$$\begin{aligned}
 PA &= \text{psize} \times \text{PFN} + \text{offset} \\
 &= \underbrace{\text{PFN} \ll 10}_{\substack{\text{just index} \\ \leftarrow}} + \text{offset} \\
 &= \underbrace{\text{PFN} \ll 10}_{\substack{\downarrow \\ \text{base addr}}} + \text{offset} \\
 &= 0x60e6
 \end{aligned}$$

left size by number
 of offset bits to
 multiply

VA $0x2e0f \Rightarrow 0b101100000111$

$$VPN = 1 + 2 + 8 = 11$$



$0x00$

invalid

VA $0x1986 \Rightarrow 0b100100000110$

$$VPN = 2 + 4 = 6$$

offset = $0x186$

↓
 $0x186$

$$\begin{aligned} PA &= PPN \ll 10 + \text{offset} \\ &= 0x7586 \end{aligned}$$

```
Page Table (from entry 0 down to the max size)
[ 0] 0x80000018
[ 1] 0x80000008
[ 2] 0x8000000c
[ 3] 0x80000009
[ 4] 0x80000012
[ 5] 0x80000010
[ 6] 0x8000001f
[ 7] 0x8000001c
[ 8] 0x80000017
[ 9] 0x80000015
[ 10] 0x80000003
[ 11] 0x80000013
[ 12] 0x8000001e
[ 13] 0x8000001b
[ 14] 0x80000019
[ 15] 0x80000000
```

Virtual Address Trace

VA 0x00002e0f (decimal:	11791)	-->	00004e0f (decimal	19983)	[VPN 11]
VA 0x00001986 (decimal:	6534)	-->	00007d86 (decimal	32134)	[VPN 6]
VA 0x000034ca (decimal:	13514)	-->	00006cca (decimal	27850)	[VPN 13]
VA 0x00002ac3 (decimal:	10947)	-->	00000ec3 (decimal	3779)	[VPN 10]
VA 0x00000012 (decimal:	18)	-->	00006012 (decimal	24594)	[VPN 0]

```

Page Table (from entry 0 down to the max size)
[ 0] 0x80000018
[ 1] 0x00000000
[ 2] 0x00000000
[ 3] 0x00000000
[ 4] 0x00000000
[ 5] 0x80000009
[ 6] 0x00000000
[ 7] 0x00000000
[ 8] 0x80000010
[ 9] 0x00000000
[10] 0x80000013
[11] 0x00000000
[12] 0x8000001f
[13] 0x8000001c
[14] 0x00000000
[15] 0x00000000

Virtual Address Trace
VA 0x00003986 (decimal: 14726) --> Invalid (VPN 14 not valid)
VA 0x0002bc6 (decimal: 11206) --> 00004fc6 (decimal 20422) [VPN 10]
VA 0x0001e37 (decimal: 7735) --> Invalid (VPN 7 not valid)
VA 0x0000671 (decimal: 1649) --> Invalid (VPN 1 not valid)
VA 0x0001bc9 (decimal: 7113) --> Invalid (VPN 6 not valid)

```

$w = 25$

```

Page Table (from entry 0 down to the max size)
[ 0] 0x00000000
[ 1] 0x00000000
[ 2] 0x00000000
[ 3] 0x00000000
[ 4] 0x00000000
[ 5] 0x00000000
[ 6] 0x00000000
[ 7] 0x00000000
[ 8] 0x00000000
[ 9] 0x00000000
[10] 0x00000000
[11] 0x00000000
[12] 0x00000000
[13] 0x00000000
[14] 0x00000000
[15] 0x00000000

Virtual Address Trace
VA 0x00003a39 (decimal: 14905) --> Invalid (VPN 14 not valid)
VA 0x0003ee5 (decimal: 16101) --> Invalid (VPN 15 not valid)
VA 0x000033da (decimal: 13274) --> Invalid (VPN 12 not valid)
VA 0x000039bd (decimal: 14781) --> Invalid (VPN 14 not valid)
VA 0x000013d9 (decimal: 5081) --> Invalid (VPN 4 not valid)

```

$w = 0$

```

Page Table (from entry 0 down to the max size)
[ 0] 0x80000018
[ 1] 0x80000008
[ 2] 0x8000000c
[ 3] 0x80000009
[ 4] 0x80000012
[ 5] 0x80000010
[ 6] 0x8000001f
[ 7] 0x8000001c
[ 8] 0x80000017
[ 9] 0x80000015
[10] 0x80000003
[11] 0x80000013
[12] 0x8000001e
[13] 0x8000001b
[14] 0x80000019
[15] 0x80000000

Virtual Address Trace
VA 0x00002e0f (decimal: 11791) --> 00004e0f (decimal 19983) [VPN 11]
VA 0x00001986 (decimal: 6534) --> 00007d86 (decimal 32134) [VPN 6]
VA 0x000034ca (decimal: 13514) --> 00006cca (decimal 27850) [VPN 13]
VA 0x00002ac3 (decimal: 10947) --> 00000ec3 (decimal 3779) [VPN 10]
VA 0x00000012 (decimal: 18) --> 00006012 (decimal 24594) [VPN 0]

```

$w = 100$

With increase of allocated space used,

seg violation reduce.

③ -P 8 -a 32 -p 1024

$$\text{psize} = 8 \quad \text{physical memory} = 1024$$

$$\text{asize} = 32 = 2^5$$

VA → 5 bits

$$\frac{\text{asize}}{\text{psize}} = \frac{32}{8} = 4 = 2^2$$

↓
pages

2 bits + 3 bits
VPN offset

-P 8k -a 32k -p 1m

$$\text{psize} = 8k, \text{asize} = 32k = 2^5 \times 2^{10}$$

physical memory
= 1m

2 bits + 13 bits

VPN offset

-P1m - a 256m - p 52m

$$\frac{256}{1} = 2^8 = 8 \text{ bits}$$

$$256m = 2^8 \times 2^{10} \times 2^{10}$$

8bits + 20bits
VPN offset

The most unrealistic seems to be the last one with page size = 1mb,
mostly smaller page size are more used and standard. 4kb is that value.

Similarly page size = 8B is very small leading to more pages needed to fetch even little info.

PTE \Rightarrow Page table entry that tracks the page, itself is 4-8B in size. Memory wasted per page:

with page size that is good that same PTE size can track the page more efficiently memory usage wise.

- ④ - $u \Rightarrow$ used \Rightarrow percent of virtual address space that is used basically how many virtual addresses have valid physical memory mapping

$u = 75\%$. I was expecting 25%. VPN to be invalid but none were according to the simulator.

- Then realised that it is possible that within VPNs the unused percent across is 25% on aggregate, leading to pages overall being valid.
- Also looked into the code it uses random generate along with "used" param to mark page as used or unused overall.

Hence with smaller page size = 512 I got whole invalid pages

```
./paging-linear-translate.py -P 512 -a 16k -p 32k -v -u 75
```

[15]	0x80000000
[16]	0x8000002a
[17]	0x00000000
[18]	0x00000000
[19]	0x00000000
[20]	0x8000000f
[21]	0x80000005
[22]	0x8000002d
[23]	0x80000034
[24]	0x80000026
[25]	0x80000024
[26]	0x8000000c
[27]	0x00000000

Similarly with slightly lower u = 73
I got couple of pages

```
./paging-linear-translate.py -P 1k -a 16k -p 32k -v -u 73
```

```
[ 6] 0x8000001f  
[ 7] 0x8000001c  
[ 8] 0x80000017  
[ 9] 0x80000015  
[10] 0x80000003  
[11] 0x80000013  
[12] 0x8000001e  
[13] 0x8000001b  
[14] 0x00000000  
[15] 0x80000011
```

Error: physical memory size must be GREATER than address space size (for this simulation)

Error: must use smaller sizes (less than 1 GB) for this simulation.