# Interpretation of salamboR models

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## **About this presentation**

A number of things happened since February 2014:

- · Updated the code in salamboR.
- · Re-computed the models for 2 studies (on-going publications).
- Initiated the data repositories on github.com/ugcd/

In this presentation we would like to share with you:

- · the achieved results
- · our rules on computing' and interpreting'em all
- · focus on details when interpreting the models

### **Work 1: Platelets traits**

TRAIT1	TRAIT 2	RHOG	RHOG.SE	RHOG.P	RHOE	RHOE.SE	RHOE.P
BA	VT	-0.104	0.158	0.511	0.367	0.238	0.169
EO	VT	-0.237	0.151	0.133	-0.436	0.225	0.045
LE	VT	0.030	0.194	0.876	0.225	0.268	0.361
LI	VT	0.117	0.160	0.472	0.073	0.277	0.786
MOt	VT	0.178	0.185	0.365	0.236	0.209	0.285
NE	VT						

#### Comments

- $\cdot$  None of the genetic correlations are significant.
- $\cdot$  Correlation between  $\ensuremath{\text{NT}}$  and  $\ensuremath{\text{VT}}$  is not computable.

### **Work 2: TEG traits**

TRAIT1	TRAIT 2	RHOG	RHOG.SE	RHOG.P	RHOE	RHOE.SE	RHOE.P
VT	TGTlagtime	0.125	0.140	3.784e-01	0.186	0.235	4.515e-01
VT	TGTPeak	0.356	0.136	1.079e-02	0.257	0.234	2.907e-01
VT	TGTETP	0.314	0.121	2.079e-02	0.323	0.211	1.406e-01

#### Comments

· Two genetic correlations with TGTPeak and TGTETP, which of them does make more sense?

### **Work 2: TEG traits**

TRAIT1	TRAIT2	RHOG	RHOG.SE	RHOG.P
VT	TGTETP	-0.25	0.32	
VT	TGTPeak	0.42	0.044	
TGTPeak	TGTETP	0.729	0.062	

#### Idea

• The genes affecting all traits VT, TGTPeak and TGTETP are considered simultaneously.

# **Decision making**

## Questions we had at the beginning

- What is **N** of the GAIT2 study?
- · What disease to model in correlation with a trait: VT, AT or Throm?
- How to use covariates like antiAgreg?
- · If  $\rho_p$  is not significant, should I panic?
- · If  $\rho_g$  is estimated as  $0.9\pm0.001$  with p-value  $1.2\times10^{-8}$ , should I make the boss happy by reporting this?

# **Modeling background**

# **Model and its parameters**

Think of a statistical model in terms of its parameters.

#### Univariate Model:

FIXED EFFECTS PARAMETERS	RANDOM EFFECTS PARAMETERS
$\mu, \beta_{AGE}, \beta_{SEX}$	$\sigma_{\rm g}^2,\sigma_{\rm e}^2$

# A fixed effect controlling the mean of height









# A random effect controlling the variance of height









**Tests of model parameters** 

FIXED EFFECTS PARAMETERS	RANDOM EFFECTS PARAMETERS	
$\mu, \beta_{AGE}, \beta_{SEX}$	$\sigma_{\rm g}^2,\sigma_{\rm e}^2$	
Heritability: $h^2 = \frac{\sigma_g^2}{\sigma_g^2 + \sigma_e^2}$ .		

Is the heritability significant? Likelihood Ratio Test (LRT):

HYPOTHESIS	FREE PARAMETERS	RESTRICTED PARAMETERS
No polygenic effect	$\mu, \beta_{AGE}, \beta_{SEX}, \sigma_e^2$	$\sigma_g^2 = 0$

Is **AGE** covariate significant? Likelihood Ratio Test (LRT):

$$\mu, \beta_{SEX}, \sigma_g^2, \sigma_e^2$$

$$\beta_{AGE} = 0$$

### **Bivariate Model for correlations**

Univariate Model

FIXED EFFECTS PARAMETERS	RANDOM EFFECTS PARAMETERS
$\mu, \beta_{AGE}, \beta_{SEX}$	$\sigma_{\rm g}^2, \sigma_{\rm e}^2$

#### **Bivariate Model**

FIXED EFFECTS PARAMETERS	RANDOM EFFECTS PARAMETERS
$\mu_1, \mu_2, (\beta_1, \beta_2)_{AGE}, (\beta_2)_{SEX}$	$(\sigma_1^2, \sigma_2^2, \rho)_g, (\sigma_1^2, \sigma_2^2, \rho)_e$

Is the genetic correlation significant? Likelihood Ratio Test (LRT):

HYPOTHESIS	FREE PARAMETERS	RESTRICTED PARAMETERS

No genetic correlation	, $(\sigma_1^2, \sigma_2^2)_g$ , $(\sigma_1^2, \sigma_2^2, \rho)_e$	$\rho_{\rm g} = 0$
No pleiotropy	, $(\sigma_1^2, \sigma_2^2)_g$ , $(\sigma_1^2, \sigma_2^2, \rho)_e$	$\rho_{\rm g}=1$

# **Changes in code**

# **Changes in code**

Fixes

1) Trait-specific covariates in bivariate models

Example: bivariate model of VT and TGTETP

· Independent univariate models

TRAIT	COVARIATES
VT	AGE
TGTETP	AGE, AGE2, contraception, sedentaryD

· A bivariate model before February 2014

TRAIT	COVARIATES
VT	AGE, AGE2, contraception, sedentaryD

# **Changes in code**

Fixes

2) P-values of all test covariates vs. final covariates (in reports)

Example: univariate model of VT.

· Testing model with 6 covariates

AGE	AGE.P	SEX.P	CONTRA.P	AINES.P	ANTIAGREG.P	SMOKE.P
-0.02	5.15e-10	1.36e-01	1.68e-01	7.85e-01	9.26e-01	8.92e-01

• Final model with 1 covariates

AGE	AGE.P
-0.02	6.2843e-12

# **Changes in code**

#### New options

- 1. Compute hard options (see solarPolyg function).
- 2. Computing the phenotypic correlation can be skipped.
- 3. Trivariate models are available.



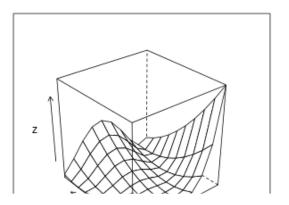
# Rule: think twice when adding a covariate

Example: antiAgreg covariate in a model for AT

## **Rule: Filter out suspicious results**

#### Problem:

- · If the optimization algorithm does not converge, then the returned model is not OK.
- $\cdot\;$  Consequently, SOLAR warnings and extreme estimations like  $\rho_g=1.$
- · See optim R function and an example with Rosenbrock Banana function.
  - z = f(x, y) has the global minimum at (1, 1) point, where the function is equal to 0.



# Rule: Filter out suspicious results

Example: bivariate correlation **NE** and **VT** (not OK)

TRAIT1	TRAIT 2	RHOG	RHOG.SE	RHOG.P	RHOE	RHOE.SE	RHOE.P
NE	VT	0.6748	NA	7.9140e-04	1.0000e+00	0.8246	NA

#### What is wrong?

- · Estimation of standard errors are NA.
- Estimation of  $\rho_e$  is 1.

## Rule: Filter out suspicious results

Example: bivariate correlation E0 and VT executed with compute hard options (not OK)

TRAIT1	TRAIT 2	RHOG	RHOG.SE	RHOG.P	RHOE	RHOE.SE	RHOE.P
EO	VT	-0.7623	0.0977	1.3693e-11	-0.9000	0.0723	7.6188e-18

#### What is wrong?

- Estimation of  $\rho_e$  is -0.9 (it is on the boundary).
  - Estimations of standard errors are suspiciously small.
  - P-values are suspiciously small.

## Rule: Throm is preferred to VT

#### Problem

· Small  $N \rightarrow$  instability, low statistical power

#### Solution

- Try correlation with VT
- · Change the order of traits to test the consistence of the results
- Confirm results by comparing with correlation with Throm

## Rule: Throm is preferred to VT

Example: trivariate correlation VT, TGTPeak and TGTETP

· Order VT, TGTlagtime, TGTETP

Not computable.

· Order VT, TGTPeak, TGTETP (not OK)

TRAIT1	TRAIT2	RHOG	RHOG.SE
VT	TGTETP	0.008	0.005
VT	TGTPeak	0.506	0.004
TGTPeak	TGTETP	0.796	NA

# Rule: Throm is preferred to VT

Example: trivariate correlation VT, TGTPeak and TGTETP

· Order VT, TGTETP, TGTPeak (OK)

TRAIT1	TRAIT2	RHOG	RHOG.SE
VT	TGTETP	-0.25	0.32
VT	TGTPeak	0.42	0.044
TGTPeak	TGTETP	0.729	0.062

Model with Throm, order Throm, TGTPeak, TGTETP (OK?)

TRAIT1	TRAIT2	RHOG	RHOG.SE
Throm	TGTETP	-0.117	0.007
Throm	TGTPeak	0.438	0.006

**TGTPeak** TGTETP 0.755 0.007

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# Rule: only $\rho_g$ matters

#### Explanation:

- · The genetic correlation  $\rho_g$  has a co-variance matrix **structured** (kinship), while the residual environmental  $\rho_e$  has the identity matrix (i.i.d.)
- · Indeed, the environmental correlation  $\rho_e$  is a part of not explained residual (error).
- Phenotipic correlation  $\rho_p$ 
  - is not a model parameter
  - it has a large error
  - it computationally complicated to test (remember its formula)

# Rule: only $\rho_g$ matters

Why  $\rho_e$  and  $\rho_p$  are out?

· Have you ever tried to response to such a Reviewer's comment of a submitted manuscript?

Page 9, lines 36-38. It is stated that there is no environmental correlation between BMI and thrombosis risk. This is in contrary to conventional perception about these two phenotypes. For example, diet is a risk factor for both obesity and thrombosis, especially arterial thrombosis. Other risk factors, such as physical inactivity, could also influence both phenotypes.

# Rule: only $\rho_g$ matters

Example: bivariate correlation between **E0** and **VT** 

TRAIT1	TRAIT 2	RHOG	RHOG.SE	RHOG.P	RHOE	RHOE.SE	RHOE.P
EO	VT	-0.237	0.151	0.133	-0.436	0.225	0.045

#### Comments:

- · The environmental correlation  $\rho_e$  is significant, but the genetic correlation  $\rho_g$  is not.
  - That means the model must be recomputed with restriction  $\rho_g$  = 0 , that will give the correct estimation of  $\rho_e$  .

# Alessandra's Rule: p-value 1e-22

Example: bivariate correlation between **E0** and **VT** 

· The current results

TRAIT1	TRAIT 2	RHOG	RHOG.P	RHOE	RHOE.P
ЕО	VT	-0.237	0.133	-0.436	0.045

· Computed before Feb 2014

TRAIT1	TRAIT 2	RHOG	RHOG.P	RHOE	RHOE.P
EO	VT	-0.81	6.2e-12	-0.9	3.6e-22

What was wrong?

- · All the issues commented above
  - bmi as covariate

- covariates not trait-specific
- Bad luck Lack of our rules for interpretation the results



# Our experience (our feeling)

All models are wrong, but some are useful.

Most of correlations are insignificant, but some are ... incomputable.

# **Our proposal**

Work hard / Keep learning / Share all at <a href="https://github.com/ugcd/">https://github.com/ugcd/</a>

## **Credits**

- <u>slidify</u>, <u>io2012</u>
- knitr
- knitcitations

# Thank you