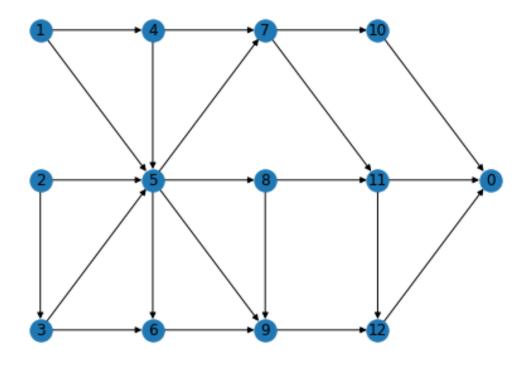
Graph

March 25, 2023

```
[1]: import networkx as nx
import matplotlib.pyplot as plt

[2]: # Define a graph
G_plot = nx.DiGraph()
```

```
G_plot.add_edges_from([(1, 4), (1, 5), (2, 3), (2, 5), (3, 5), (3, 6), (4, 5), [
 \rightarrow (4, 7), (5, 6), (5, 7),
                   (5, 8), (5, 9), (6, 9), (7, 10), (7, 11), (8, 9), (8, 11), 
 \hookrightarrow (9, 12), (10, 0), (11, 12), (11, 0),
                   (12, 0)])
pos = \{0: (4, 1), 1: (0, 2), 2: (0, 1), 3: (0, 0), 4: (1, 2), 5: (1, 1), 6: (1, 1)\}
 \Rightarrow 0), 7: (2, 2), 8: (2, 1), 9: (2, 0),
       10: (3, 2), 11: (3, 1), 12: (3, 0)}
n=12
# Draw the graph
nx.draw(G plot, pos=pos, with labels=True) # Draw nodes and edges
plt.show() # Display the graph
G = nx.DiGraph()
G.add_edges_from([(1, 4), (1, 5), (2, 3), (2, 5), (3, 5), (3, 6), (4, 5), (4, _{\sqcup}
 (5, 6), (5, 7),
                    (5, 8), (5, 9), (6, 9), (7, 10), (7, 11), (8, 9), (8, 11), 
 \rightarrow (9, 12), (11, 12)])
```



```
[3]: # Calculate the adjacency matrix A
A = nx.adjacency_matrix(G, range(1, n+1)).todense()
print("Adjacency matrix A:\n", A)

idx = 1
currA = A
delta = 0
while (currA.sum() != 0):
   idx += 1
   delta += currA
   currA = currA @ A
   print(f"\nAdjacency matrix A_{idx}:\n", currA)
print("\nDelta:\n", delta)
```

Adjacency matrix A:

```
[[0 0 0 1 1 0 0 0 0 0 0 0 0]
[0 0 1 0 1 0 1 0 0 0 0 0 0 0]
[0 0 0 0 1 1 0 0 0 0 0 0 0]
[0 0 0 0 1 1 0 1 0 0 0 0 0]
[0 0 0 0 0 1 1 1 1 0 0 0 0]
[0 0 0 0 0 0 0 1 1 1 1 0 0 0]
[0 0 0 0 0 0 0 0 0 1 1 0 0]
[0 0 0 0 0 0 0 0 0 1 1 0]
```

```
[0 0 0 0 0 0 0 0 0 0 0 1]
[0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 1]
[0 0 0 0 0 0 0 0 0 0 0 0]]
```

Adjacency matrix A_3:

Adjacency matrix A_4:

Adjacency matrix A_5:

```
[[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 4]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 4]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0 0]
```

Adjacency matrix A_6:

```
[[0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
[0 0 0 0 0 0 0 0 0 0 0 0 0]
```

Delta:

```
0 0]]
                    3
                              3 5 11]
              2
                 3
                     2
                        2
                           7
                              2
                                 4 11]
                 2
                     1
                                    61
           0
              1
                        1
                              1
[ 0
        0
           0
              1
                 1
                     2
                        1
                           3
                              2
                                    6]
[ 0
    0
        0
           0
              0
                 1
                     1
                        1
                           3
                              1
                                 2
                                    5]
ΓΟ
    0
        0
           0
              0
                 0
                    0
                        0
                          1
                              0
                                 0
                                    1]
[ 0
        0
           0
              0
                 0
                    0
                        0
                           0
                              1
                                    1]
ΓΟ
    0
        0
           0
              0
                 0
                     0
                        0
                           1
                              0
                                    2]
[ 0
                                    1]
              0
                           0
                              0
        0
           0
              0
                 0
                           0
                              0
                                    07
              0
                 0
                     0
                        0
                           0
                              0
                                 0
                                    1]
[ 0
   0
        0
           0
[ 0 0 0 0 ]
              0
                 0 0
                       0
                          0 0 0 0]]
```

/var/folders/2k/n9362ktx4hzctxmb23t1jv8m0000gn/T/ipykernel_7174/2466777551.py:2: FutureWarning: adjacency_matrix will return a scipy.sparse array instead of a matrix in Networkx 3.0.

A = nx.adjacency_matrix(G, range(1, n+1)).todense()

```
[6]: # get the nodes with in and out arrows intermediate_nodes = []
```

```
for node in G.nodes:
        in_degree = G.in_degree(node)
        out_degree = G.out_degree(node)
        if in_degree > 0 and out_degree > 0:
            intermediate_nodes.append(node)
    print("Intermediate nodes:", intermediate_nodes)
    print("\nCoefficient of intermediate elements:", len(intermediate_nodes)/len(G))
    Intermediate nodes: [4, 5, 3, 6, 7, 8, 9, 11]
    [7]: num_internal_connections = 0
    for node in G.nodes():
        neighbors = set(G.neighbors(node))
        for neighbor in neighbors:
            if node < neighbor and neighbor in neighbors:</pre>
               num_internal_connections += 1
    print("Number of internal connections: ", num_internal_connections)
```

Number of internal connections: 19

[]: