NBA Rookies

```
Dataset CSV file: nba_logreg.csv
```

Group No.: 18

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Import libraries

```
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt
import numpy as np
```

Reading Dataset

```
NBA_dataset = pd.read_csv("nba_logreg.csv")
```

NBA_dataset.shape

(1340, 21)

NBA_dataset.info()

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1340 entries, 0 to 1339
Data columns (total 21 columns):
 # Column
                          Non-Null Count Dtype
0 Name 1340 non-null object
1 GP 1331 non-null float64
2 MIN 1336 non-null float64
         PTS
                               1340 non-null float64
                             1340 non-null float64
1340 non-null float64
1340 non-null float64
         FGM
 5
         FGA
         FG%
 6
 7
         3P Made 1340 non-null float64

        3P Made
        1340 non-null
        float64

        3PA
        1340 non-null
        float64

        3P%
        1329 non-null
        float64

        FTM
        1340 non-null
        float64

        FTA
        1340 non-null
        float64

        FT%
        1328 non-null
        float64

        OREB
        1336 non-null
        float64

        DREB
        1340 non-null
        float64

        DFP
        1360 non-null
        float64

 8
 9
 10 FTM
 11 FTA
 12 FT%
 13 OREB
 14 DREB
 15 REB
                               1340 non-null float64
                                  1337 non-null float64
1337 non-null float64
 16 AST
 17 STL
                                1340 non-null float64
 19 TOV 1340 non-null float64
20 TARGET_5Yrs 1340 non-null int64
dtypes: float64(19), int64(1), object(1)
```

```
memory usage: 220.0+ KB
```

Data Visualization and Exploration

Handling Duplicates

```
NBA_dataset = NBA_dataset.drop_duplicates(subset='Name', keep='last')
NBA_dataset.reset_index(inplace = True, drop = True)

NBA_dataset.shape

(1294, 21)

print("Number of Duplicates after processing the dataset: ",NBA_dataset.duplicated().sum())

Number of Duplicates after processing the dataset: 0
```

Printing 2 rows for sanity check

0 Brandon Ingram NaN 27.4 7.4

1 Andrew Harrison 35.0 26.9 7.2

NBA_dataset.head(2) Name GP MIN PTS FGM FGA FG% 3P Made 3PA 3P% ... FTA FT% OREB DREB REB AST STL BLK TOV TARGET_5Yrs

2.3

3.4

69.9 0.7

76.5 0.5

4.1

2.0 2.4

1.9 0.4

3.7 1.1

2.1 25.0 ...

2.8 23.5 ...

1.3

0.4

0.5 1.6 0

34.7 0.5

29.6 0.7

2.6 7.6

2.0 6.7

2 rows × 21 columns

```
#Removing Name column
NBA_dataset = NBA_dataset.loc[ :, NBA_dataset.columns != 'Name' ]
```

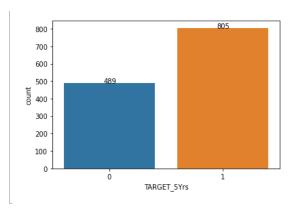
Visualization on Class imbalance

Minority class(0) is ~37%, so the class imbalance is mild. This slight imbalance is often not a concern, and the problem can often be treated like a normal classification predictive modeling problem. Therefore, we will not take any action.

```
NBA_dataset.shape
(1294, 20)
```

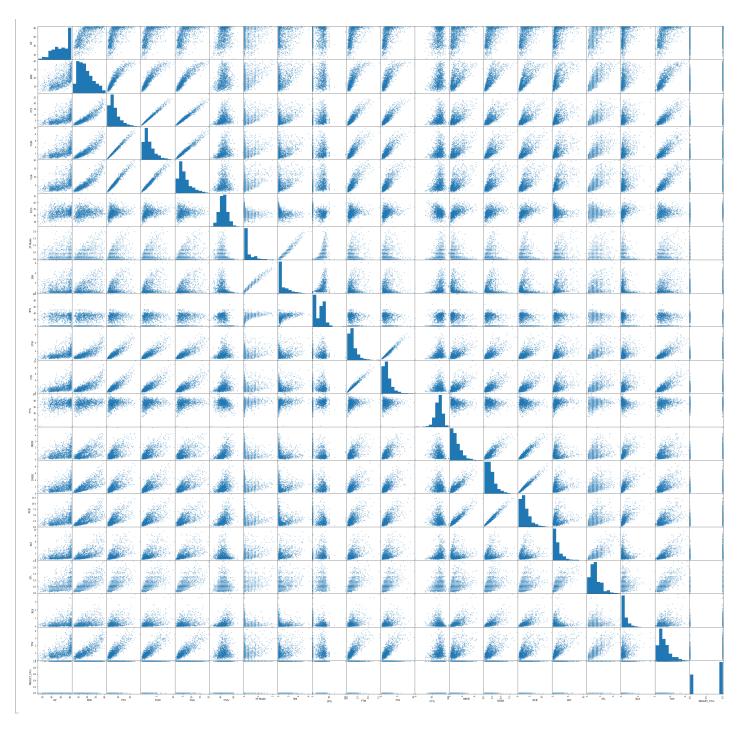
```
plt.figure(figsize=(6, 4))
ax = sns.countplot( x="TARGET_5Yrs", data=NBA_dataset )

for p in ax.patches:
    ax.annotate('{:}'.format(p.get_height()), (p.get_x()+0.35, p.get_height()+0.05))
```



Scatter Matrix

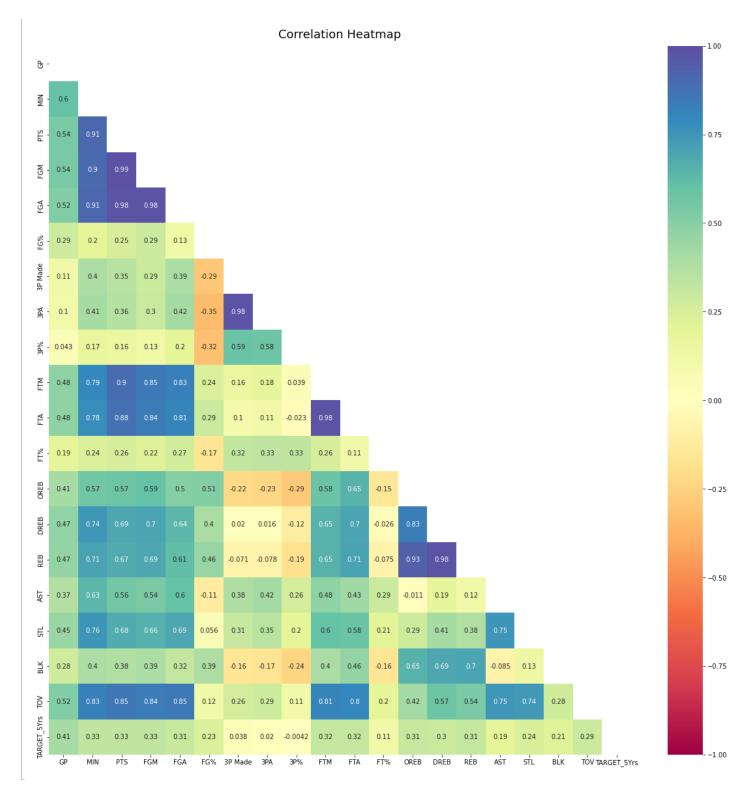
```
from pandas.plotting import scatter_matrix
scatter_matrix(NBA_dataset, figsize=(50, 50))
plt.show()
```



Correlational Analysis

```
corr = NBA_dataset.corr()

plt.figure(figsize=(20, 20))
mask = np.triu( np.ones_like(corr) )
hm = sns.heatmap( corr, mask=mask, vmin=-1, vmax=1, annot=True, cmap='Spectral' )
hm.set_title('Correlation Heatmap', fontdict={'fontsize':18}, pad=12)
Text(0.5, 1.0, 'Correlation Heatmap')
```



Following are the pairs having correlation more than 0.9(>0.9)

- 1. PTS-MIN
- 2. FGM-MIN
- 3. FGA-MIN
- 4. FGM-PTS
- 5. FGA-PTS
- 6. FGA-FGM 7. FTM-PTS
- 8. 3PA-3P Made
- 9. FTA-FTM
- 10. REB-OREB

11. REB-DREB

Features with high correlation are more linearly dependent and hence have almost the same effect on the dependent variable. So, when two features have high correlation, we can drop one of the two features. Hence, on analysis, we will be removing the following columns:

- 1. MIN
- 2. PTS
- 3. REB
- 4. 3P Made
- 5. FGM
- 6. FTM

NBA_dataset = NBA_dataset.drop(['MIN','PTS','REB','3P Made','FGM','FTM'], axis = 1)

NBA_dataset

	GP	FGA	FG%	3PA	3P%	FTA	FT%	OREB	DREB	AST	STL	BLK	TOV	TARGET_5Yrs
0	NaN	7.6	34.7	2.1	25.0	2.3	69.9	0.7	3.4	1.9	0.4	0.4	1.3	0
1	35.0	6.7	29.6	2.8	23.5	3.4	76.5	0.5	2.0	3.7	1.1	0.5	1.6	0
2	74.0	4.7	42.2	1.7	24.4	1.3	67.0	0.5	1.7	1.0	0.5	0.3	1.0	0
3	58.0	5.5	42.6	0.5	22.6	1.3	68.9	1.0	0.9	8.0	0.6	0.1	1.0	1
4	48.0	3.0	52.4	0.1	0.0	1.9	67.4	1.0	1.5	0.3	0.3	0.4	0.8	1
1289	80.0	3.6	43.3	0.2	14.3	1.5	79.2	0.4	0.8	2.5	0.6	0.2	8.0	0
1290	68.0	4.1	35.8	0.7	16.7	1.0	79.4	0.4	1.1	2.3	8.0	0.0	1.3	1
1291	43.0	3.9	55.0	0.0	0.0	1.6	64.3	1.5	2.3	0.3	0.3	0.4	0.9	0
1292	52.0	3.8	43.9	0.2	10.0	1.8	62.5	0.2	0.4	2.2	0.4	0.1	0.8	1
1293	47.0	4.4	36.9	1.3	33.3	1.0	67.3	0.2	0.7	1.4	0.7	0.1	0.9	1

1294 rows × 14 columns

Data Pre-processing and cleaning

#Dataset Information before Data pre-processing
NBA_dataset.info()

<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1294 entries, 0 to 1293
Data columns (total 14 columns):

Data	columns	(total 14	columns):	
#	Column	Non-I	Null Count	Dtype
0	GP	1286	non-null	float64
1	FGA	1294	non-null	float64
2	FG%	1294	non-null	float64
3	3PA	1294	non-null	float64
4	3P%	1284	non-null	float64
5	FTA	1294	non-null	float64
6	FT%	1284	non-null	float64
7	OREB	1290	non-null	float64
8	DREB	1294	non-null	float64
9	AST	1291	non-null	float64
10	STL	1292	non-null	float64
11	BLK	1294	non-null	float64
12	TOV	1294	non-null	float64
13	TARGET_5	Yrs 1294	non-null	int64

dtypes: float64(13), int64(1)

memory usage: 141.7 KB

Replacing the NULL values present in columns of NBA_dataset with mean(average) value of their respective columns. Columns which are having NULL values are as follows:

```
2. 3P%
3. FT%
4. OREB
5. AST
6. STL
```

1. GP

```
# NaN values being replaced by the mean value of the column

NBA_dataset['GP'] = NBA_dataset['GP'].fillna(NBA_dataset['GP'].mean())

NBA_dataset['3P%'] = NBA_dataset['3P%'].fillna(NBA_dataset['3P%'].mean())

NBA_dataset['FT%'] = NBA_dataset['FT%'].fillna(NBA_dataset['FT%'].mean())

NBA_dataset['OREB'] = NBA_dataset['OREB'].fillna(NBA_dataset['OREB'].mean())

NBA_dataset['AST'] = NBA_dataset['AST'].fillna(NBA_dataset['AST'].mean())

NBA_dataset['STL'] = NBA_dataset['STL'].fillna(NBA_dataset['STL'].mean())
```

```
#Dataset Information after Data pre-processing
NBA dataset.info()
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 1294 entries, 0 to 1293
Data columns (total 14 columns):
# Column Non-Null Count Dtype
                    ___________
              1294 non-null float64
1294 non-null float64
0 GP
1 FGA
                 1294 non-null float64
1294 non-null float64
     FG%
 2
 3
     3PA
                  1294 non-null float64
   3P%
            1294 non-null float64
1294 non-null float64
1294 non-null float64
1294 non-null float64
5 FTA
 6
    FT%
7 OREB
 8 DREB
                 1294 non-null float64
1294 non-null float64
1294 non-null float64
9 AST
10 STL
11 BLK
12 TOV 1294 non-null float64
13 TARGET_5Yrs 1294 non-null int64
dtypes: float64(13), int64(1)
memory usage: 141.7 KB
```

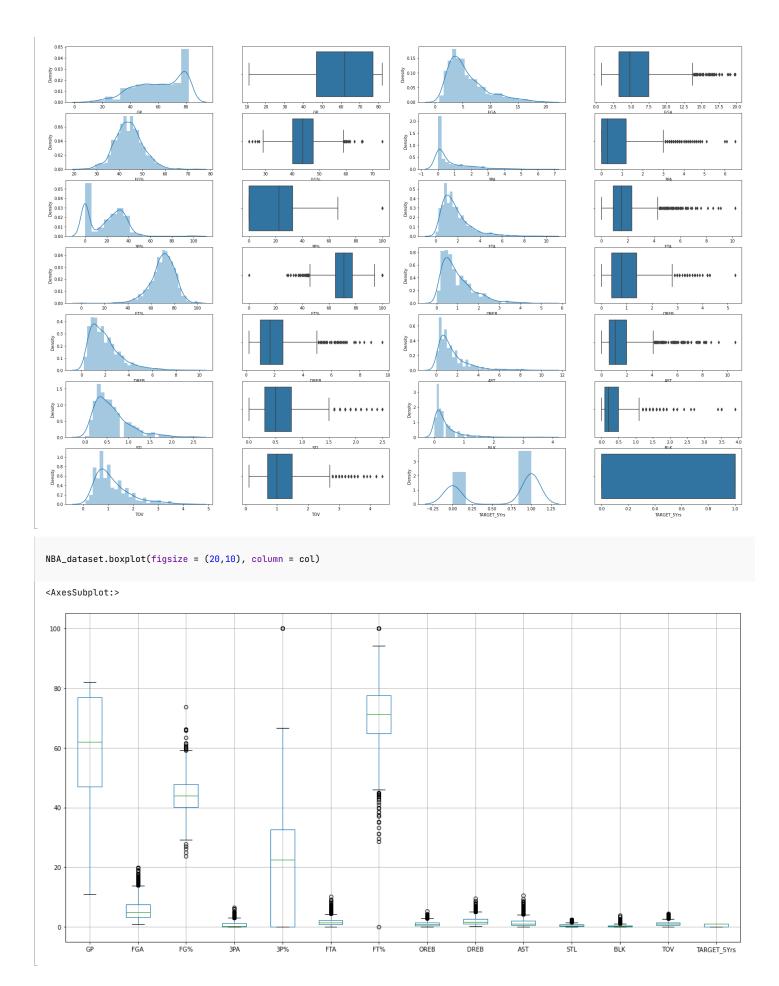
```
# Columns of dataset

col = ['GP','FGA','FG%','3PA','3P%','FTA','FT%','OREB','DREB','AST','STL','BLK','TOV','TARGET_5Yrs']
```

Checking Data Distribution and Outlier Analysis on dataset

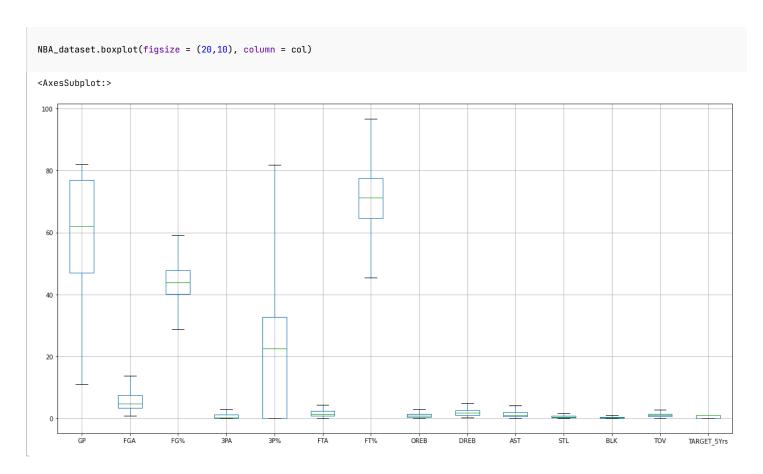
```
import warnings
warnings.filterwarnings('ignore')

plt.figure(figsize=(30,30))
num = 1
for i in col:
    plt.subplot(10,4,num)
    sns.distplot(NBA_dataset[str(i)])
    num = num + 1
    plt.subplot(10,4,num)
    sns.boxplot(NBA_dataset[str(i)])
    num = num + 1
```



Winsorization of Outliers is the process of replacing the extreme values of statistical data in order to limit the effect of the outliers on the calculations or the results obtained by using that data.

After the processing the data, no outlier is present in dataset.



Standardising the dataset

Standard Scaler helps to get standardized distribution, with a zero mean and standard deviation of one (unit variance). It standardizes features by subtracting the mean value from the feature and then dividing the result by feature standard deviation.

MinMaxScaler scales all the data features in the range [0, 1] or else in the range [-1, 1] if there are negative values in the dataset.

```
#Standardising the data
from sklearn.preprocessing import StandardScaler
sc = StandardScaler()

NBA_dataset_standardised = sc.fit_transform(NBA_dataset.iloc[: ,:-1])
NBA_dataset_standardised
```

```
#Resetting the index
NBA_dataset_standardised = NBA_dataset_standardised.reset_index(drop = True)
NBA_dataset['TARGET_5Yrs'] = NBA_dataset['TARGET_5Yrs'].reset_index(drop = True)
```

```
#Adding target column to standardised dataset

NBA_dataset_standardised['TARGET_5Yrs'] = NBA_dataset['TARGET_5Yrs']

NBA_dataset_standardised
```

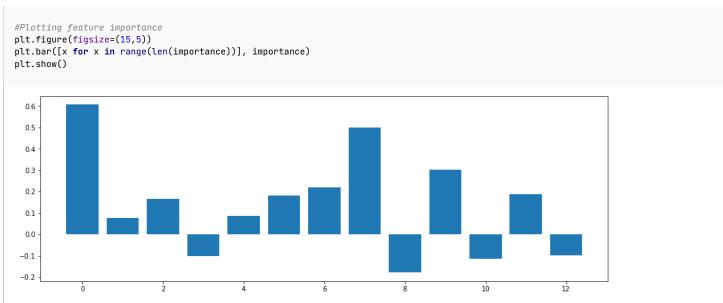
	GP	FGA	FG%	3PA	3P%	FTA	FT%	OREB	DREB	AST	STL	BLK	TOV	TARGET_5Yrs
0	0.000000	0.549947	-1.576571	1.477965	0.351494	0.508073	-0.054831	-0.405009	1.179961	0.405359	-0.548760	0.203532	0.213049	0.0
1	-1.464623	0.277674	-2.430302	2.237706	0.256372	1.511948	0.606984	-0.686301	0.020544	1.989360	1.323896	0.520845	0.677164	0.0
2	0.785682	-0.327378	-0.321084	1.043827	0.313445	-0.404540	-0.345628	-0.686301	-0.227903	-0.386641	-0.281238	-0.113782	-0.251067	0.0
3	-0.137520	-0.085357	-0.254125	-0.258587	0.199299	-0.404540	-0.155106	0.016929	-0.890427	-0.562641	-0.013716	-0.748408	-0.251067	1.0
4	-0.714521	-0.841672	1.386379	-0.692725	-1.233873	0.143028	-0.305518	0.016929	-0.393534	-1.002642	-0.816283	0.203532	-0.560478	1.0
1289	1.131882	-0.660157	-0.136946	-0.584191	-0.327043	-0.222018	0.877726	-0.826947	-0.973243	0.933360	-0.013716	-0.431095	-0.560478	0.0
1290	0.439481	-0.508894	-1.392433	-0.041518	-0.174848	-0.678324	0.897781	-0.826947	-0.724796	0.757360	0.521329	-1.065721	0.213049	1.0
1291	-1.003022	-0.569399	1.821614	-0.801260	-1.233873	-0.130756	-0.616371	0.720160	0.268991	-1.002642	-0.816283	0.203532	-0.405773	0.0
1292	-0.483721	-0.599651	-0.036507	-0.584191	-0.599726	0.051766	-0.796866	-1.108239	-1.304505	0.669359	-0.548760	-0.748408	-0.560478	1.0
1293	-0.772221	-0.418136	-1.208295	0.609689	0.877836	-0.678324	-0.315546	-1.108239	-1.056058	-0.034641	0.253807	-0.748408	-0.405773	1.0

1294 rows × 14 columns

Feature Importance

```
X = NBA_dataset_standardised.iloc[:, :-1].values
Y = NBA_dataset_standardised.iloc[:, -1].values
```

```
# logistic regression for feature importance
from sklearn.linear_model import LogisticRegression
# define the model
model = LogisticRegression()
# fit the model
model.fit(X, Y)
# get importance
importance = model.coef_[0]
df = pd.DataFrame()
df["Column"] = NBA_dataset_standardised.columns[:-1]
df["Coeff. Value"] = importance
print(df)
           Coeff. Value
   Column
0
               0.606579
               0.077200
1
      FGA
2
      FG%
               0.166894
              -0.099992
3
      3PA
4
      3P%
              0.086335
5
      FTA
               0.182809
6
      FT%
               0.220859
7
     OREB
              0.498275
8
     DREB
              -0.178822
9
      AST
              0.304009
10
      STL
              -0.112890
              0.186723
11
      BLK
              -0.098818
12
      TOV
```



The coefficients can provide the basis for a crude feature importance score. This assumes that the input variables have the same scale or have been scaled prior to fitting a model. Recall that this is a classification problem with classes 0 and 1. Coefficients are both positive and negative. The positive scores indicate a feature that predicts class 1, whereas the negative scores indicate a feature that predicts class 0.

Model Building

Splitting the dataset into training and test sets as per below conditions:

```
Case 1 : Train = 80 % Test = 20% [ x_{train1,y_{train1}} = 80\% ; [ x_{test1,y_{test1}} = 20\% Case 2 : Train = 10 % Test = 90% [ x_{train2,y_{train2}} = 10\% ; [ x_{test2,y_{test2}} = 90\%
```

```
from sklearn.model_selection import train_test_split

#Case 1 with test size 20%

X_train_r_case1, X_test_r_case1, Y_train_r_case1, Y_test_r_case1 = train_test_split(X, Y, test_size = 0.2, random_state = 0)

X_train_case1 = np.c_[np.ones((X_train_r_case1.shape[0], 1)), X_train_r_case1]

X_test_case1 = np.c_[np.ones((X_test_r_case1.shape[0], 1)), X_test_r_case1]

Y_train_case1 = Y_train_r_case1[:, np.newaxis]

#Case 2 with test size 90%

X_train_r_case2, X_test_r_case2, Y_train_r_case2, Y_test_r_case2 = train_test_split(X, Y, test_size = 0.9, random_state = 0)

X_train_case2 = np.c_[np.ones((X_train_r_case2.shape[0], 1)), X_train_r_case2]

X_test_case2 = np.c_[np.ones((X_test_r_case2.shape[0], 1)), X_test_r_case2]

Y_train_case2 = Y_train_r_case2[:, np.newaxis]

Y_test_case2 = Y_test_r_case2[:, np.newaxis]
```

k-fold cross validation

```
from sklearn.model_selection import cross_val_score
from sklearn.linear_model import LogisticRegression
k_fold_score = cross_val_score(LogisticRegression(), X, Y, cv=5)
print("K-Fold Cross Validation score with k = 5: \n\
print("Individual Accuracies: \n", [i for i in k_fold_score] ,"\n")
print("Accuracies: {:.2f}% \n".format(k_fold_score.mean()*100))
print("Standard Deviation: {:.2f} \n".format(k_fold_score.std()*100))
k_fold_score = cross_val_score(LogisticRegression(), X, Y, cv=10)
print("K-Fold Cross Validation score with k = 10: \n\
print("Individual Accuracies: \n", [i for i in k_fold_score] ,"\n")
print("Accuracies: {:.2f}% \n".format(k_fold_score.mean()*100))
print("Standard Deviation: {:.2f} \n".format(k_fold_score.std()*100))
K-Fold Cross Validation score with k = 5:
Individual Accuracies:
  [0.6872586872586872,\ 0.7297297297297297,\ 0.694980694980695,\ 0.6988416988416989,\ 0.7054263565891473] 
Accuracies: 70.32%
Standard Deviation: 1.45
K-Fold Cross Validation score with k = 10:
Individual Accuracies:
Accuracies: 71.02%
Standard Deviation: 2.80
```

```
#Initialising Theta
Theta_train_case1 = np.zeros((X_train_case1.shape[1], 1))
Theta_test_case1 = np.zeros((X_test_case1.shape[1], 1))
Theta_train_case2 = np.zeros((X_train_case2.shape[1], 1))
Theta_test_case2 = np.zeros((X_test_case2.shape[1], 1))
def sigmoid(a):
    return 1.0 / (1 + np.exp(-a))
def cost(x, y, theta):
   m = x.shape[0]
    h = sigmoid(np.matmul(x, theta))
    cost = (np.matmul(-y.T, np.log(h)) - np.matmul((1 - y.T), np.log(1 - h)))/m
def gradient_descent(theta, learning_rate, x , y):
    m = x.shape[0]
    h = sigmoid(np.matmul(x, theta))
    grad = np.matmul(x.T, (h - y)) / m
    J = cost(x, y, theta)
   theta = theta - learning_rate * grad * J
    return theta
def training_model_LR_GD(Theta, X_train, Y_train):
    n_{iterations} = 10000
    learning_rate = 0.05 # hyperparameter - fixed by trail and error methods
    # to store the cost values
    cost_history = []
    l1_loss_history = []
    l2_loss_history = []
    #Theta values
    Theta = np.zeros((X_train_case1.shape[1], 1))
    for i in range( n_iterations+1 ):
        Theta1 = gradient_descent(Theta, learning_rate, X_train, Y_train)
        J_new = cost(X_train, Y_train, Theta1)
        cost_history.append(J_new.flatten())
       Theta = Theta1
       # if i % 100 == 0:
             print('epoch = {}, cost = {}' .format(i, J_new))
    print('Training completed')
    return cost_history, Theta1
```

Training & Prediction

```
cost_history_train_case1, Theta_train_case1 = training_model_LR_GD(Theta_train_case1, X_train_case1, Y_train_case1)
cost_history_test_case1, Theta_test_case1 = training_model_LR_GD(Theta_test_case1, X_test_case1, Y_test_case1)
cost_history_train_case2, Theta_train_case2 = training_model_LR_GD(Theta_train_case2, X_train_case2, Y_train_case2)
cost_history_test_case2, Theta_test_case2 = training_model_LR_GD(Theta_test_case2, X_test_case2, Y_test_case2)

Training completed
Training completed
Training completed
Training completed
Training completed
```

```
# Case-1 train prediction data
h = sigmoid(np.matmul( X_train_case1, Theta_train_case1 ))
Y_pred_train_case1 = (h > .5).astype(int)

# Case-1 test prediction data
h = sigmoid(np.matmul( X_test_case1, Theta_test_case1 ))
Y_pred_test_case1 = (h > .5).astype(int)

# Case-2 train prediction data
h = sigmoid(np.matmul( X_train_case2, Theta_train_case2 ))
Y_pred_train_case2 = (h > .5).astype(int)

# Case-2 test prediction data
h = sigmoid(np.matmul( X_test_case2, Theta_test_case2 ))
Y_pred_test_case2 = (h > .5).astype(int)
```

Loss Function for Logistics Regression

L1 Loss function is used to minimize the error which is the sum of the all the absolute differences between the true value and the predicted value.

L2 Loss Function L2 Loss Function is used to minimize the error which is the sum of the all the squared differences between the true value and the predicted value.

The cost function of L1 and L2 can't be used in Logistic Regression because it is a non-convex function of weights. Optimizing algorithms like i.e gradient descent only converge convex function into a global minimum.

Cost Function would be:

```
J = -y\log(h(x)) - (1 - y)\log(1 - h(x))
here, y is the real target value
and, h(x) is sigmoid(wx + b)
```

Plotting Losses for both test and train data

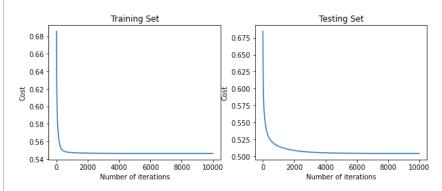
```
plt.figure(figsize=(10,8))
plt.suptitle('CASE 1 - Cost/Loss Function of Logistic Regression using Gradient Descent', fontsize=16)

plt.subplot(2,2,1)
plt.plot(cost_history_train_case1)
plt.title("Training Set")
plt.xlabel("Number of iterations")
plt.ylabel("Cost")

plt.subplot(2,2,2)
plt.plot(cost_history_test_case1)
plt.title("Testing Set")
plt.xlabel("Number of iterations")
plt.ylabel("Cost")

plt.ylabel("Cost")
```

CASE 1 - Cost/Loss Function of Logistic Regression using Gradient Descent



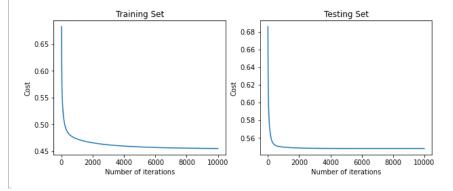
```
plt.figure(figsize=(10,8))
plt.suptitle('CASE 2 - Cost/Loss Function of Logistic Regression using Gradient Descent', fontsize=16)

plt.subplot(2,2,1)
plt.plot(cost_history_train_case2)
plt.title("Training Set")
plt.xlabel("Number of iterations")
plt.ylabel("Cost")

plt.subplot(2,2,2)
plt.plot(cost_history_test_case2)
plt.title("Testing Set")
plt.xlabel("Number of iterations")
plt.ylabel("Cost")

plt.ylabel("Cost")
```

CASE 2 - Cost/Loss Function of Logistic Regression using Gradient Descent



Comparing Accuracy of Train data with Test data

Types of Gradient Descent

There are three types of gradient descent learning algorithms: batch gradient descent, stochastic gradient descent and mini-batch gradient descent.

1. Batch gradient descent

Batch gradient descent sums the error for each point in a training set, updating the model only after all training examples have been evaluated. This process referred to as a training epoch.

While this batching provides computation efficiency, it can still have a long processing time for large training datasets as it still needs to store all of the data into memory. Batch gradient descent also usually produces a stable error gradient and convergence, but sometimes that convergence point isn't the most ideal, finding the local minimum versus the global one.

2. Stochastic gradient descent

Stochastic gradient descent (SGD) runs a training epoch for each example within the dataset and it updates each training example's parameters one at a time. Since you only need to hold one training example, they are easier to store in memory. While these frequent updates can offer more detail and speed, it can result in losses in computational efficiency when compared to batch gradient descent. Its frequent updates can result in noisy gradients, but this can also be helpful in escaping the local minimum and finding the global one.

3. Mini-batch gradient descent

Mini-batch gradient descent combines concepts from both batch gradient descent and stochastic gradient descent. It splits the training dataset into small batch sizes and performs updates on each of those batches. This approach strikes a balance between the computational efficiency of batch gradient descent and the speed of stochastic gradient descent.

Logistic Regression using MLE

Logistic regression is a model for binary classification predictive modeling. The parameters of a logistic regression model can be estimated by the probabilistic framework called maximum likelihood estimation. Under this framework, a probability distribution for the target variable (class label) must be assumed and then a likelihood function defined that calculates the probability of observing the outcome given the input data and the model. This function can then be optimized to find the set of parameters that results in the largest sum likelihood over the training dataset.

The maximum likelihood approach to fitting a logistic regression model both aids in better understanding the form of the logistic regression model and provides a template that can be used for fitting classification models more generally. This is particularly true as the negative of the log-likelihood function used in the procedure can be shown to be equivalent to cross-entropy loss function.

Maximum Likelihood Estimation is a frequentist probabilistic framework that seeks a set of parameters for the model that maximizes a likelihood function. n Maximum Likelihood Estimation, we wish to maximize the conditional probability of observing the data (X) given a specific probability distribution and its parameters (theta), stated formally as:

```
P(X; theta)
```

Where X is, in fact, the joint probability distribution of all observations from the problem domain from 1 to n.

This resulting conditional probability is referred to as the likelihood of observing the data given the model parameters and written using the notation L() to denote the likelihood function. For example:

L(X; theta)

The joint probability distribution can be restated as the multiplication of the conditional probability for observing each example given the distribution parameters. Multiplying many small probabilities together can be unstable; as such, it is common to restate this problem as the sum of the log conditional probability.

```
sum i to n log(P(xi ; theta))
```

Given the frequent use of log in the likelihood function, it is referred to as a log-likelihood function. It is common in optimization problems to prefer to minimize the cost function rather than to maximize it. Therefore, the negative of the log-likelihood function is used, referred to generally as a Negative Log-Likelihood (NLL) function.

```
minimize -sum i to n log(P(xi ; theta))
```

The Maximum Likelihood Estimation framework can be used as a basis for estimating the parameters of many different machine learning models for regression and classification predictive modeling. This includes the logistic regression model.

Regularization

Regularization is a technique used to reduce the errors by fitting the function appropriately on the given training set and avoid overfitting. Sometimes the machine learning model performs well with the training data but does not perform well with the test data. It means the model is not able to predict the output when deals with unseen data by introducing noise in the output, and hence the model is called overfitted. This problem can be deal with the help of a regularization technique.

There are mainly two types of regularization techniques, which are given below:

1. Ridge Regression

Ridge regression is a regularization technique, which is used to reduce the complexity of the model. It is also called as L2 regularization. In this technique, the cost function is altered by adding the penalty term to it. The amount of bias added to the model is called Ridge Regression penalty. It is also called as L2 regularization.

2. Lasso Regression

It is similar to the Ridge Regression except that the penalty term contains only the absolute weights instead of a square of weights. Since it takes absolute values, hence, it can shrink the slope to 0, whereas Ridge Regression can only shrink it near to 0. It is also called as L1 regularization.

```
from sklearn.model_selection import cross_val_score

#defining a generic Function to give ROC_AUC Scores in table format for better readability

def crossvalscore(model, X, y):
    scores = cross_val_score(model, X, y, cv=5, scoring='roc_auc', n_jobs=-1)
    acc = cross_val_score(model, X, y, cv=5, scoring='accuracy', n_jobs=-1)
    rand_scores = pd.DataFrame({
    'cv':range(1,6),
    'roc_auc score':scores,
    'accuracy score':acc
    })

AUC = rand_scores['roc_auc score'].mean()
    ACC = rand_scores['accuracy score'].mean()
    print('AUC : ', AUC)
    print('AuC : ', AUC)
    return AUC, ACC
```

L1 and L2 Regularisation

```
from sklearn.linear_model import LogisticRegression
print("+++++++++++++++++++++++\n
                                L1 Regularisation\n++++++++++++++++\n")
#Case 1
print("--- CASE 1 ---")
log_clf = LogisticRegression(C = 0.1, class_weight= 'balanced', penalty= 'l1', solver= 'liblinear', random_state=42)
L1_reg_auc_case1, L1_reg_acc_case1 = crossvalscore(log_clf, X_train_r_case1, Y_train_r_case1)
print("\n--- CASE 2 ---")
log_clf = LogisticRegression(C = 0.1, class_weight= 'balanced', penalty= 'l1', solver= 'liblinear', random_state=42)
L1_reg_auc_case2, L1_reg_acc_case2 = crossvalscore(log_clf, X_train_r_case2, Y_train_r_case2)
#Case 1
print("--- CASE 1 ---")
log_clf = LogisticRegression(C = 0.1, class_weight= 'balanced', penalty= 'l2', solver= 'liblinear', random_state=42)
L2_reg_auc_case1, L2_reg_acc_case1 = crossvalscore(log_clf, X_train_r_case1, Y_train_r_case1)
#Case 2
print("\n--- CASE 2 ---")
log_clf = LogisticRegression(C = 0.1, class_weight= 'balanced', penalty= 'l2', solver= 'liblinear', random_state=42)
L2_reg_auc_case2, L2_reg_acc_case2 = crossvalscore(log_clf, X_train_r_case2, Y_train_r_case2)
+++++++++++++++++++++
   L1 Regularisation
--- CASE 1 ---
AUC: 0.7595961210344496
Accuracy Score: 0.6859903381642511
--- CASE 2 ---
AUC : 0.8009803921568628
Accuracy Score: 0.6975384615384617
L2 Regularisation
--- CASE 1 ---
AUC : 0.763460609298295
Accuracy Score: 0.6995169082125604
--- CASE 2 ---
AUC : 0.7866013071895424
Accuracy Score: 0.728923076923077
```

Compare models with and without regularization in a tabular format

```
#Getting Scores of Accuracy and AUC for WITHOUT Regularisation

WO_Reg_acc_case1 = accuracy_score(Y_train_case1, Y_pred_train_case1)
WO_Reg_acc_case2 = accuracy_score(Y_train_case2, Y_pred_train_case2)
WO_Reg_auc_case1 = roc_auc_score(Y_train_case1, Y_pred_train_case1)
WO_Reg_auc_case2 = roc_auc_score(Y_train_case2, Y_pred_train_case2)

warnings.filterwarnings('ignore')
!pip install tabulate
```

Requirement already satisfied: tabulate in /opt/python/envs/default/lib/python3.8/site-packages (0.8.10)

You should consider upgrading via the '/opt/python/envs/default/bin/python -m pip install --upgrade pip' command.

WARNING: You are using pip version 21.3.1; however, version 22.1.2 is available.

```
from tabulate import tabulate
data1 = [
  ["Without Regularization", WO_Reg_acc_case1*100, WO_Reg_acc_case2*100],
  ["L1 Regularization", L1_reg_acc_case1*100, L1_reg_acc_case2*100],
  ["L2 Regularization", L2_reg_acc_case1*100, L2_reg_acc_case2*100]
1
data2 = [
  ["Without Regularization", WO_Reg_auc_case1*100, WO_Reg_auc_case2*100],
  ["L1 Regularization", L1_reg_auc_case1*100, L1_reg_auc_case2*100],
  ["L2 Regularization", L2_reg_auc_case1*100, L2_reg_auc_case2*100]
]
print(tabulate(data1 , headers=["", "Case 1", "Case 2"]))
print(tabulate(data2 , headers=["", "Case 1", "Case 2"]))
```

Accuracy Score									
	Case 1	Case 2							
Without Regularization L1 Regularization L2 Regularization	71.7874 68.599 69.9517	79.0698 69.7538 72.8923							
++++++++++++++++++++++++++++++++++++++									
	Case 1	Case 2							
Without Regularization L1 Regularization L2 Regularization	67.8046 75.9596 76.3461	75 80.098 78.6601							

Regularization did not improve the Accuracy Score as the accuracy score for without regularisation is more than the accuracy score for L1 or L2 regularisation. And, AUC is more in L1/L2 regularisation than without regularisation.

Higher the AUC, the better the model is at predicting 0 classes as 0 and 1 classes as 1. We could see that AUC for Case-2 is more than Case-1; therefore, we could say that Case-2 model is more apt than Case-1 model for prediction.

Performance Evaluation

Prediction Performance

```
from sklearn.metrics import confusion_matrix, accuracy_score, precision_score, recall_score, f1_score

def accuracy(y_pred, y_test):
    cm = confusion_matrix(y_test, y_pred)
    print("Confusion Matrix : \n", cm, '\n')
    print("Accuracy Score : {0:.2f}%".format(accuracy_score(y_test, y_pred)*100))
    print("Precision : {0:.2f}".format(precision_score(y_test, y_pred)))
    print("Recall : {0:.2f}".format(recall_score(y_test, y_pred)))
    print("F1 Score : {0:.2f}".format(f1_score(y_test, y_pred)))
```

```
print("======\n \
   CASE - 1 | Prediction Evaluation metrics\n\
----\n")
accuracy(Y_pred_test_case1, Y_test_case1)
accuracy(Y_pred_train_case1, Y_train_case1)
CASE - 1 | Prediction Evaluation metrics
_____
++++++++++++++++
Test Set Accuracy:
++++++++++++++++
Confusion Matrix :
[[ 74 32]
[ 31 122]]
Accuracy Score: 75.68%
Precision: 0.79
Recall: 0.80
F1 Score: 0.79
+++++++++++++++++
Train Set Accuracy:
++++++++++++++++
Confusion Matrix :
[[201 182]
[110 542]]
Accuracy Score : 71.79%
Precision: 0.75
Recall: 0.83
F1 Score : 0.79
```

Prediction Performance Analysis with Case-2 Test data

```
print("\n ======\n \
  CASE - 2 | Prediction Evaluation metrics \n \
======\n")
accuracy(Y_pred_test_case2, Y_test_case2)
accuracy(Y_pred_train_case2, Y_train_case2)
______
   CASE - 2 | Prediction Evaluation metrics
______
+++++++++++++++
Test Set Accuracy:
+++++++++++++++
Confusion Matrix :
[[251 195]
[123 596]]
Accuracy Score : 72.70%
Precision: 0.75
Recall: 0.83
F1 Score : 0.79
++++++++++++++++
Train Set Accuracy:
+++++++++++++++
Confusion Matrix :
[[27 16]
[11 75]]
```

Accuracy Score : 79.07%

Precision: 0.82 Recall: 0.87 F1 Score: 0.85

1. Case 1 (Train = 80 % Test = 20%)

Accuracy of Training set is 71.79% and Accuracy for Test set is 75.68%. We could say that the case-1 model is **underfit**.

2. Case 2 (Train = 10 % Test = 90%)

Accuracy of Training set is 79.07% and Accuracy for Test set is 72.70%. We could say that the case-2 model is overfit.