

## RULES FOR PROPAGATION OF UNCERTAINTY

These are approximate rules that simplify the computation and slightly exaggerate the uncertainty at each step.

### 1. Addition and Subtraction:

e.g.

$$(4.35 \pm 0.02) \text{ Hz} + (2.12 \pm 0.01) \text{ Hz} \\ = (6.47 \pm 0.03) \text{ Hz}$$

RULE: Add absolute uncertainties

### 2. Multiplication and Division:

e.g.

$$(44.01 \pm 0.05) \text{ m} / (2.1 \pm 0.05) \text{ s} \\ = (44.01 \text{ m} \pm 0.11\%) / (2.1 \text{ s} \pm 2.4\%)$$

This was derived by taking the  $\pm$  value and dividing it by the given value and then multiplying by 100 to get a percentage.

For the above:

$$0.05/44.01 = 0.11\% \text{ and } 0.05/2.1 = 2.4\%$$

After this is done, the two *percent* uncertainties are added:

$$0.11 + 2.4 = 2.5$$

e.g.

$$(44.01 \pm 0.05) \text{ m} / (2.1 \pm 0.05) \text{ s} \\ = 21. \text{ m/s} \pm 2.5\%$$

To finish the problem, the *percent* uncertainty must be converted back into the absolute uncertainty:

$$(21)(2.5\%) = 0.525 \text{ but to one significant digit: } \pm 0.5$$

Therefore:

$$\text{e.g. } (44.01 \pm 0.05) \text{ m} / (2.1 \pm 0.05) \text{ s} \\ = 21. \text{ m/s} \pm 0.5$$

### 3. Multiplying or Dividing by a pure number (with no uncertainty):

e.g.

$$(12.3 \pm 0.1) \text{ m} (3.00) \\ = 36.9 \text{ m} \pm 0.3$$

RULE: Multiply or divide the absolute uncertainty by the pure number

### 4. Taking the square root:

$$\text{e.g. } \sqrt{25 \pm 5\%} = 5 \pm 2.5\%$$

RULE: divide the percent uncertainty by 2