# Toward a Genome Scale Dynamic Model of Cell-Free Protein Synthesis in *Escherichia coli*

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### **Abstract**

Cell-free protein expression systems have become widely used in systems and synthetic biology. In this study, we developed an ensemble of dynamic *E. coli* cell-free protein synthesis (CFPS) models. Model parameters were estimated from measurements of glucose, organic acids, energy species, amino acids, and the protein product, chloramphenicol acetyltransferase (CAT). The ensemble described all of the training data, especially the central carbon metabolism. The model predicted a carbon yield for CAT production that was equal to 23% of the maximum theoretical yield, calculated using sequence-specific flux balance analysis. This suggests that CAT production could be further optimized. The dynamic modeling approach predicted that substrate consumption of glucose and pyruvate and oxidative phosphorylation were most important to both CAT production and the system as a whole, while CAT production alone depended heavily on the CAT synthesis reaction. Conversely, CAT production was robust to allosteric control, as was most of the network, with the exception of the organic acids in central carbon metabolism. This study is the first to model dynamic protein production in *E. coli*, and should provide a foundation for genome-scale, dynamic modeling of cell-free *E. coli* protein synthesis.

Keywords: Biochemical engineering, systems biology, cell-free protein synthesis

## Introduction

Cell-free systems offer many advantages for the study, manipulation and modeling of metabolism compared to *in vivo* processes. Central amongst these, is direct access to metabolites and the biosynthetic machinery without the interference of a cell wall, or complications associated with cell growth. This allows us to interrogate the chemical environment while the biosynthetic machinery is operating, potentially at a fine time resolution. Cell-free protein synthesis (CFPS) systems are arguably the most prominent examples of cell-free systems used today [1]. However, CFPS is not new; CFPS in crude *E. coli* extracts has been used since the 1960s to explore fundamentally important biological mechanisms [2, 3]. Today, cell-free systems are used in a variety of applications ranging from therapeutic protein production [4] to synthetic biology [5, 6]. However, if CFPS is to become a mainstream technology for applications such as point of care manufacturing, we must first understand the performance limits of these systems. One tool to address this question is mathematical modeling.

Mathematical modeling has long contributed to our understanding of metabolism. Dec-15 ades before the genomics revolution, mechanistically structured metabolic models arose 16 from the desire to predict microbial phenotypes resulting from changes in intracellular 17 or extracellular states [7]. The single cell E. coli models of Shuler and coworkers pio-18 neered the construction of large-scale, dynamic metabolic models that incorporated multi-19 ple, regulated catabolic and anabolic pathways constrained by experimentally determined 20 kinetic parameters [8]. Shuler and coworkers generated many single cell kinetic mod-21 els, including single cell models of eukaryotes [9, 10], minimal cell architectures [11], as 22 well as DNA sequence based whole-cell models of E. coli [12]. In the post genomics 23 world, large-scale stoichiometric reconstructions of microbial metabolism popularized by techniques such as flux balance analysis (FBA) have become a standard approach [13]. Since the first genome-scale stoichiometric model of E. coli, developed by Edwards and

Palsson [14], well over 100 organisms, including industrially important prokaryotes are now available [15-17]. Stoichiometric models rely on a pseudo-steady-state assumption to reduce unidentifiable genome-scale kinetic models to an underdetermined linear algebraic system, which can be solved efficiently even for large systems. Traditionally, 30 stoichiometric models have also neglected explicit descriptions of metabolic regulation 31 and control mechanisms, instead opting to describe the choice of pathways by prescribing an objective function on metabolism. Interestingly, similar to early cybernetic mod-33 els, the most common metabolic objective function has been the optimization of biomass 34 formation [18], although other metabolic objectives have also been estimated [19]. Re-35 cent advances in constraint-based modeling have overcome the early shortcomings of the platform, including capturing metabolic regulation and control [20]. Thus, modern 37 constraint-based approaches have proven extremely useful in the discovery of metabolic 38 engineering strategies and represent the state of the art in metabolic modeling [21, 22]. However, genome-scale kinetic models of industrial important organisms such as *E. coli* have yet to be constructed. 41

In this study, we developed an ensemble of kinetic cell-free protein synthesis (CFPS)
models using dynamic metabolite measurements in an *E. coli* cell free extract. Model parameters were estimated from measurements of glucose, organic acids, energy species,
amino acids, and the protein product, chloramphenicol acetyltransferase (CAT). Characteristic values for model parameters and initial conditions, estimated from literature, were
used to constrain the parameter estimation problem. The ensemble of parameter sets
described the training data with a median cost that was greater than two orders of magnitude smaller than random sets constructed using the literature parameter constraints. We
then used the ensemble of kinetic models to analyze the CFPS reaction. First, sensitivity
analysis of the dynamic model suggested that CAT production was most sensitive to CAT
synthesis parameters, as well as reactions in oxidative phosphorylation and pyruvate con-

sumption. Sensitivity analysis also showed that the system as a whole was most sensitive to these same parts of the network and glucose consumption. CAT production and other 54 metabolites, specifically organic acid intermediates such as pyruvate, were sensitive to the presence of allosteric control mechanisms. Next, to gauge the performance of the 56 cell-free reaction, we compared the observed CAT carbon yield with the maximum the-57 oretical CAT carbon yield calculated using sequence-specific flux balance analysis. The 58 CAT yield estimated from the kinetic model was 23% of the maximum theoretical yield, but 59 36% of the theoretical yield when physiologically realistic constraints were used. Taken 60 together, we have integrated traditional kinetics with a logical rule-based description of 61 allosteric control to simulate a comprehensive CFPS dataset. This study provides a foun-62 dation for genome-scale, dynamic modeling of cell-free *E. coli* protein synthesis.

### 84 Results

The ensemble of kinetic CFPS models captured the time evolution of CAT biosynthesis (Fig. 1 - 3). The cell-free E. coli metabolic network was constructed by removing growth 66 associated reactions from the MG1655 reconstruction [16], and by adding reactions de-67 scribing chloramphenicol acetyltransferase (CAT) biosynthesis, a model protein for which there exists a comprehensive training dataset [23]. The CFPS model equations were formulated using the hybrid cell-free modeling framework of Wayman et al. [24]. An ensemble of model parameters (N > 10,000) was estimated from measurements of glucose, CAT, organic acids (pyruvate, lactate, acetate, succinate, malate), energy species (A(x)P, G(x)P, C(x)P, U(x)P), and 18 of the 20 proteinogenic amino acids using a constrained Markov Chain Monte Carlo (MCMC) approach. The MCMC algorithm minimized the error between the training data and model simulations starting from an initial parameter set assembled from literature and inspection. Parameter sets were selected for the ensemble based upon their error, and the Pearson correlation coefficient between the candidate and 77 existing sets in the ensemble. The parameter set with the lowest error value was defined 78 as the best-fit set. Central carbon metabolism (Fig. 1, top), energy species (Fig. 2), and amino acids (Fig. 3) were captured by the ensemble and the best-fit set. The constrained 80 MCMC approach estimated parameter sets with a median error greater than two-order 81 of magnitude less than random parameter sets generated within the same parameter 82 bounds (Fig. 4); thus, we have confidence in the predictive capability of the estimated pa-83 rameters. The model captured the biphasic CAT production: during the first hour glucose 84 powers production, and CAT is produced at ~10  $\mu$ M/h; subsequently, pyruvate and lactate 85 reserves are consumed to power metabolism, and CAT is produced less efficiently at ~5  $\mu$ M/h. Allosteric control was important to biphasic CAT production; without control, the CAT production rate increased and then ceased after 1.5 hr (Fig. 1, bottom). In addition, acetate no longer accumulated after 1.5 hours, in the absence of allosteric control. Inter-

estingly, the simulated malate abundance tracked the experimental measurements during the glucose consumption phase, but increased sharply during the pyruvate consumption phase, without allosteric control. Taken together, we produced an ensemble of kinetic models that was consistent with time series measurements of the production of a model protein. However, while the ensemble described the experimental data, it was unclear 94 which kinetic parameters most influenced CAT production, and whether the performance 95 of the CFPS reaction was optimal. 96

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To better understand which parameters and parameter combinations influenced the performance of the kinetic model, we performed sensitivity analysis (Fig. 5). We per-98 turbed each  $V^{max}$  parameter, either individually or in pairwise combinations and measured the change in either CAT production or the overall system state. CAT production was most sensitive to the CAT synthesis reaction, oxidative phosphorylation, and the pyruvate-consuming alanine synthesis reaction (Fig. 5, top, section A). We saw a common theme of the most important reactions producing or consuming the cofactors ATP, NADH, NADPH, and coenzyme A, as well as the metabolites pyruvate and glutamate. Of the 25 reactions to which CAT production was most sensitive, 9 produced or consumed ATP, making it the most represented in these top reactions (with the exception of hydrogen and phosphate ion). The next most represented were pyruvate, glutamate, and ADP with 7 reactions each, followed by coenzyme A,  $\alpha$ -ketoglutarate, NAD/NADH, and NADP/NADPH, with 6 reactions each. This makes sense, as glutamate was an important precursor for the synthesis of other amino acids required by CAT production. Meanwhile, the cofactors provided energy to power CAT synthesis, while pyruvate was important for energy generation following glucose depletion. In addition, pyruvate was required for the synthesis of several amino acids. The pairwise sensitivities (off-diagonal elements) were different from the corresponding first-order sensitivities (diagonal elements), and led to interesting outcomes. The combination of certain reactions had a much greater or lesser effect on CAT production than that of the individual reactions by themselves. For example, glutamine synthesis and arginine degradation were both among the most important reactions to CAT production (they ranked 5th and 10th, respectively). This was likely because they both affected the sensitive glutamine-glutamate balance; glutamine synthesis consumes glutamate, while arginine degradation produces it. However, when both were perturbed, their combined effect on the model was low, as the respective contributions to consumption and production of glutamate cancelled. An example of positive synergy can be seen in cometabolite interconversion. Pyridine nucleotide transhydrogenase catalyzes two reactions: one converts NAD and NADPH into NADH and NADP, while the other does the reverse and also generates a proton gradient. Increasing one or the other has little effect on the model, as the reaction is hampered by the loss of reactants. Increasing both, however, allows all cometabolites to be conserved and the reactions to continue unhindered. Thus, the pairwise sensitivity is much higher than the sum of the first-order sensitivities.

The overall system state was also sensitive to cofactors and substrates; however, instead of pyruvate and glutamate, the substrates driving metabolism were pyruvate and G3P. The system was most sensitive to an oxidative phosphorylation reaction (cytochrome oxidase), which converted ubiquinol to ubiquinone while generating a proton gradient. The next 4 most important reactions were all consumers of pyruvate: lactate dehydrogenase, pyruvate formate lyase, alanine synthesis, and PEP synthase. Of the 25 reactions to which the system was most sensitive, 7 produced or consumed pyruvate and 7 participated in NAD/NADH exchange. With the exception of hydrogen, these were the most represented species in the top 25 reactions. Also important were coenzyme A (5 reactions) and acetyl coenzyme A (4 reactions), as well as ubiquinone/ubiquinol, NADP/NADPH, G3P, and ATP (4 reactions each). The system state also had pairwise sensitivities that differed from the corresponding first-order sensitivities and stood out as significant. For

example, alanine degradation was among the most important reactions, as it produced pyruvate; GMP synthesis was also moderately important, as it produced glutamate. However, when both reactions were increased, the combined effect on the model was almost zero. This can be understood by considering the reactions that involve both pyruvate and glutamate: they all either produced both of these substrates or consumed both. When alanine degradation was increased, the excess pyruvate stimulated these reactions to consume both pyruvate and glutamate; the amounts of both of these substrates could not be conserved. But when GMP synthesis was perturbed as well, the glutamate deficiency was corrected, cancelling much of the effect on the system. One of the pyruvate- and glutamate-consuming reactions was alanine synthesis; in this case, the levels of pyruvate, glutamate, and alanine were all virtually unchanged. An example of positive synergy can be seen in histidine synthesis, one of the least influential reactions that consumes three units of ATP. When perturbed in combination with the reverse reaction of succinyl coenzyme A synthetase, another reaction with little overall effect on the model, the combined effect on the system is much greater. This may be because the reverse reaction of succinyl coenzyme A synthetase produced ATP, which further stimulated histidine synthesis. Taken together, sensitivity analysis identified blocks of parameters that either individually, or in combination influenced model performance.

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Gene knockouts in the electron transport chain significantly reduced the performance of the CFPS reaction (Fig. 6). A key finding of both the CAT and overall system state sensitivity analysis was the importance of oxidative phosphorylation. To investigate this further, we knocked out key oxidative phosphorylation reactions in the ensemble of kinetic models to examine the effect on glucose uptake and CAT production. A single *cyd* knockout reduced the CAT carbon yield from 8.6% to 2.8%. In addition, the glucose uptake rate was reduced compared to that of the control (no knockouts). On the other hand, a *nuo* knockout showed a less dramatic decrease in yield, reducing the CAT carbon yield to

6.8%; however, the glucose uptake rate remained similar to that of the control. Knocking out app increased CAT yield to 8.8%, but this increase was not statistically significantly 169 different from that of the control. Lastly, knocking out all three reactions reduced the CAT yield to 2.7%, but this was not statistically significantly different from the cyd knockout 171 alone. Thus, the model suggested the key step in oxidative phosphorylation was cat-172 alyzed by the gene product of cyd. However, while disruption of cyd significantly reduced 173 the CAT carbon yield, it did not eliminate the ability of CFPS reaction to produce CAT. 174 This suggested there was a mixture of energy sources supporting CAT production, with 175 the most significant being oxidative phosphorylation. 176

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Sequence-specific flux balance analysis (ssFBA) predicted optimal CAT yields with no adjustable parameters (Fig. 7). Before exploring CFPS optimality, we first validated the ssFBA approach by comparing simulated and measured concentrations of CAT for the first hour of glucose consumption. We chose this time window (during the first phase of CAT production) because it was approximately linear in both glucose consumption and by-/production formation. The ssFBA calculation had no adjustable parameters; bounds on transcription and translation rates, and biochemical fluxes were either estimated from data, or from mechanistic models parameterized from literature. Uncertainty in experimental factors such as RNA polymerase, ribosome concentrations, elongation rates, or the upper bounds for oxygen and glucose consumption rates was addressed by sampling plausible ranges for these parameters. The ensemble of ssFBA simulations predicted CAT formation as a function of time during the first hour of production when constrained by the experimental metabolite data (Fig. 7A). Thus, the molecular description of transcription and translation were consistent with experimental measurements. Next, to gauge the performance of the CFPS reaction, we next calculated the CAT carbon yield for three classes of constraints: (i) theoretical maximum glucose, amino acid and oxygen upper bounds, and no transcriptional/translational constraints; (ii) theoretical maximum

glucose, amino acid and oxygen upper bounds, and realistic transcriptional/translational constraints; and (iii) metabolite fluxes constrained by the CAT data, and realistic transcrip-195 tional/translational constraints (Fig. 7B). The unconstrained theoretical maximum CAT 196 carbon yield (case i) was  $36.3\% \pm 2.0\%$  (Fig. 7B, left); this represents optimal network 197 performance if glucose, oxygen and amino acids were produced or consumed at their 198 upper bounds, and transcription and translation were unbounded. On the other hand, for 199 realistic transcription and translation constraints (case ii), the optimal CAT carbon yield 200 decreased to 22.6%  $\pm$  3.0% (Fig. 7B, middle). Lastly, when both realistic metabolite and 201 transcription/translation constraints were applied (case iii), the predicted carbon yield was 202  $6.2\% \pm 2.0\%$  By comparison, the best-fit parameter set for the kinetic model predicted a 203 CAT carbon yield of 8.6%  $\pm$  0.4%, equivalent to 23% of the theoretical maximum (i) and 204 36% of the physiological case (ii). The experimental dataset had a CAT carbon yield of 205 8.2%, similar to both the kinetic model and the experimentally constrained ssFBA calcu-206 lation (case iii). Thus, while the CFPS reaction was not optimal, the ssFBA calculations 207 suggested that an approximately three-fold increase in carbon yield was theoretically pos-208 sible. 209

To investigate the differences in carbon yields, we compared the flux distributions predicted by ssFBA simulations for the different constraint cases (Fig. 8). The constrained cases (ii & iii) heavily utilized the first step in the pentose phosphate pathway to generate NADPH; the carbon flux then continued through the Entner–Doudoroff pathway toward pyruvate. For case ii, the majority of the flux proceeded toward acetate accumulation, whereas in case iii, the flux accumulated as pyruvate, lactate, and acetate with some flux through the TCA cycle. In comparison, the unconstrained case (i) showed the majority of flux traveling through glycolysis towards pyruvate, leading to accumulation of lactate, acetate and malate. In all cases, the energy source was primarily oxidative phosphorylation, and to a lesser extent the TCA cycle. However, the accumulation of acetate and lactate

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signifies that the system is not operating at its highest efficiency. The system produced NADH through lactate dehydrogenase as well as through pyridine nucleotide transhydro-221 genase (pntAB) to power oxidative phosphorylation. Oxidative phosphorylation lead to 222 a high redox ratio contributing to the accumulation of acetate overflow and diverting flux 223 away from the TCA cycle. This suggested CAT production could be increased by reducing 224 the accumulation of acetate and lactate. To investigate this further, we simulated potential 225 knockouts with constrained transcription/translation rates (Fig. 9). Knocking out the gnd 226 reaction, the first step in Entner-Doudoroff pathway, decreased acetate flux by about half. 227 In addition, less uptake of amino acids were required which increased the carbon yield 228 of CAT by 2.7% (up to approximately 25.3%  $\pm$  3.6%) compared to the control (no knock-229 outs). The simulation showed an increase in oxidative phosphorylation flux and the flux 230 splitting between glycolysis and pentose phosphate pathway. A second simulation with 231 both gnd and phosphate acetyltransferase knocked out, showed less carbon was needed 232 to meet the translation bound, which increased the carbon yield by 4% compared to the 233 control (up to approximately 26.7%  $\pm$  3.4%). In the dual knockout, flux towards acetate 234 was almost negligible with some coming from amino acid degradation. Sixty-one percent 235 of the carbon flux traveled through glycolysis, while the remaining traveled through pentose phosphate pathway. This was similar to the flux distribution of the unconstrained 237 case (case i). Taken together, the dual knockout decreased acetate production and required less amino acid consumption, thus it is a promising strategy to increase the CAT 239 carbon yield.

### Discussion

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In this study we present an ensemble of E. coli cell-free protein synthesis (CFPS) mod-242 els that accurately predict a comprehensive CFPS dataset of glucose, CAT, central carbon 243 metabolites, energy species, and amino acid measurements. We used the hybrid cell-free 244 modeling approach of Wayman and coworkers, which integrates traditional kinetic mod-245 eling with a logic-based description of allosteric regulation. CFPS is seen to be biphasic 246 relying on glucose during the first hour and pyruvate and lactate afterward. Allosteric con-247 trol was essential to the maintenance of the network and production of CAT, as without it, 248 central carbon metabolism is exhuasted within 1.5 hours leading to low CAT production. Having captured the experimental data, we investigated if CAT yield and CFPS performance could be further improved. We showed that the model produces CAT at 23% of the 251 theoretical maximum in terms of carbon yield, and at 36% of a physiological case in which transcription and translation are constrained. The accumulation of waste byproducts, es-253 pecially acetate, is responsible for this sub-optimal yield. Sensitivity analysis showed that 254 certain substrates and energy species are instrumental to CAT production and overall 255 metabolism. The system heavily relied on oxidative phosphorylation for the system's en-256 ergetic needs as well as for CAT synthesis. A single knockout in oxidative phosphorylation 257 reduced the CAT carbon yield ~3-fold, as well as disrupting the system state showing its 258 crucial role in CFPS. In comparing flux distributions between low and high yield cases, 259 carbon flux could be potentially diverted toward CAT by reducing acetate overflow and 260 minimizing flux through the Entner-Doudoroff pathway. Taken together, these findings 261 represent the first dynamic model of E. coli cell-free protein synthesis, and an important 262 step toward a functional genome scale description. 263

We present an ensemble of models that quantitatively describes the system behavior of cell-free metabolism and production of CAT. Experimental observations of the metabolites and cometabolites validate the structure of the model and the estimation of kinetic

parameters. This is important in applying metabolic engineering principles to rationally design cell-free production processes and predict the redirection of carbon fluxes to prod-268 uct forming pathways. In analyzing the model parameters' effect on CAT production, CAT 269 synthesis is the most important, followed by oxidative phosphorylation and the glutamate 270 and pyruvate consuming reactions, as well as cofactor reactions which are necessary 271 to drive CAT synthesis. For example, the conversion of ATP to GTP shows significance 272 since it is necessary for CAT synthesis. While Jewett and coworkers have shown that 273 ATP may be at saturation in CFPS [1], GTP is also required for CAT synthesis and may 274 be a limiting reactant. Thus, supplementation with additional GTP may improve the ef-275 ficiency of CAT production. A similar theme is seen in the sensitivity of overall model 276 state, where the most important reactions are glucose and pyruvate consuming reactions 277 and cofactor reactions which are vital to drive CFPS. This can be seen in the biphasic 278 operation of CFPS, with the first phase operating on glucose and the second phase op-279 erating on pyruvate. During the first phase, there is an accumulation of byproducts from 280 central carbon with the majority of flux going toward acetate and some toward pyruvate, 281 lactate, and succinate; with the exception of acetate, these are all consumed in the sec-282 ond phase. This shows that CAT production can be sustained by pyruvate and glutamate 283 in the absence of glucose, which provides alternative strategies to optimize CFPS perfor-284 mance. This is in accordance with literature, which showed pyruvate provided a relatively slow but continuous supply of ATP [25]. Taken together, this shows CFPS can be de-286 signed towards a specified application either requiring a slow stable energy source or 287 faster production. This outstanding control on model performace was expected as these 288 metabolites are responsible for driving CFPS and represent the first step in the model 289 network. Nevertheless, there are further reactions with considerable impact on model 290 performance. In examining oxidative phosphorylation activity, knockouts in the electron 291 transport pathways disrupt metabolism across the network and show CAT carbon yield

dropping from 8.6% to 2.7%; Jewett and coworkers also saw a decrease in CAT yield, ranging from 1.5-fold to 4-fold, when knocking out oxidative phosphorylation reactions[1]. 294 Oxidative phosphorylation is vital, since it provides most of the energetic needs of CFPS. 295 However, it is unknown how active oxidative phosphorylation is compared to that of in vivo 296 systems, and both of our modeling approaches suggest its importance to CAT production 297 and CFPS. Thus, oxidative phosphorylation is a potential area for improvement for CFPS 298 performance and protein yield. Comparing the theoretical maximum carbon yield of CAT 299 from ssFBA predictions to those of the kinetic model and experimental measurements 300 suggests that there is potential for increasing CAT yield as well as CFPS performance. 301 The model and experimental yields were 36% of the theoretical maximum and 23% of 302 a physiologically constrained case. Knockouts of gnd and phosphate acetyltransferase 303 show that carbon can be diverted away from acetate and toward CAT or other proteins of 304 interest expressed in CFPS. Another limitation to be addressed in CFPS is the transcrip-305 tion and translation description, since protein production is ultimately bounded by these 306 kinetic rates. Li et al. have increased productivity of firefly lucifease by 5-fold in CFPS 307 systems by adding and adjusting factors that affect transcription and translation such as 308 elongation factors, ribosome recycling factor, release factors, chaperones, BSA, and tR-NAs [26]. Underwood and coworkers have also shown that an increase in ribosome levels does not significantly increase protein yields or rates; however, adding elongation factors increased yields by 23% at 30 minutes [27].

A logical next step for this work would be sequence-specific dynamic modeling, as the kinetic modeling approach in this study used a single reaction to approximate CAT synthesis. Including specific transcription and translation steps for CAT would allow more accurate modeling of the complexity and the resource cost of protein synthesis. In addition, sensitivity analysis could be performed on these new parameters to determine the robustness of CAT synthesis to the processes of transcription and translation. Another

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area for future work is to more thoroughly sample parameter space. Parameters were varied so as to best fit the dataset; however, the resulting ensemble may not represent every biological possibility. In a different region of parameter space, the system may behave differently but still fit the experimental data. This could include the flux distribution through the network, the variation of predictions across the ensemble, and the relative sensitivity values. Testing the model under a variety of conditions could strengthen or challenge the findings of this study. Further experimentation could also be used to gain a deeper understanding of model performance under a variety of conditions. Specifically, CAT production performed in the absence of amino acids could inform the system's ability to manufacture them, while experimentation in the absence of glucose or oxygen could shed light on how important they are to protein synthesis, and under which conditions. Finally, the approach should be extended to other protein products. CAT is only a test protein used for model identification; the modeling framework, and to some extent the parameter values, should be protein agnostic. An important extension of this study would be to apply its insights to other protein applications, where possible.

## Materials and Methods

Formulation and solution of the model equations. We used ordinary differential equations (ODEs) to model the time evolution of metabolite  $(x_i)$  and scaled enzyme abundance  $(\epsilon_i)$  in hypothetical cell-free metabolic networks:

$$\frac{dx_i}{dt} = \sum_{j=1}^{\mathcal{R}} \sigma_{ij} r_j(\mathbf{x}, \epsilon, \mathbf{k}) \qquad i = 1, 2, \dots, \mathcal{M}$$
 (1)

$$\frac{d\epsilon_i}{dt} = -\lambda_i \epsilon_i \qquad i = 1, 2, \dots, \mathcal{E}$$
 (2)

where  $\mathcal{R}$  denotes the number of reactions,  $\mathcal{M}$  denotes the number of metabolites and 338  $\mathcal{E}$  denotes the number of enzymes in the model. The quantity  $r_i(\mathbf{x}, \epsilon, \mathbf{k})$  denotes the 339 rate of reaction j. Typically, reaction j is a non-linear function of metabolite and enzyme 340 abundance, as well as unknown kinetic parameters  $\mathbf{k}$  ( $\mathcal{K} \times 1$ ). The quantity  $\sigma_{ij}$  denotes 341 the stoichiometric coefficient for species i in reaction j. If  $\sigma_{ij} > 0$ , metabolite i is produced 342 by reaction j. Conversely, if  $\sigma_{ij} < 0$ , metabolite i is consumed by reaction j, while  $\sigma_{ij} = 0$ 343 indicates metabolite i is not connected with reaction j. Lastly,  $\lambda_i$  denotes the scaled 344 enzyme activity decay constant. The system material balances were subject to the initial 345 conditions  $\mathbf{x}(t_o) = \mathbf{x}_o$  and  $\epsilon(t_o) = 1$  (initially we have 100% cell-free enzyme abundance). 346 The reaction rate was written as the product of a kinetic term  $(\bar{r}_j)$  and a control term 347  $(v_i)$ ,  $r_i(\mathbf{x}, \mathbf{k}) = \bar{r}_i v_i$ . We used multiple saturation kinetics to model the reaction term  $\bar{r}_i$ :

$$\bar{r}_j = V_j^{max} \epsilon_i \prod_{s \in m_j^-} \frac{x_s}{K_{js} + x_s} \tag{3}$$

where  $V_j^{max}$  denotes the maximum rate for reaction j,  $\epsilon_i$  denotes the scaled enzyme activity which catalyzes reaction j,  $K_{js}$  denotes the saturation constant for species s in reaction j and  $m_j^-$  denotes the set of *reactants* for reaction j. On the other hand, the control term  $0 \le v_j \le 1$  depended upon the combination of factors which influenced

rate process j. For each rate, we used a rule-based approach to select from competing control factors. If rate j was influenced by  $1,\ldots,m$  factors, we modeled this relationship as  $v_j = \mathcal{I}_j\left(f_{1j}\left(\cdot\right),\ldots,f_{mj}\left(\cdot\right)\right)$  where  $0 \leq f_{ij}\left(\cdot\right) \leq 1$  denotes a transfer function quantifying the influence of factor i on rate j. The function  $\mathcal{I}_j\left(\cdot\right)$  is an integration rule which maps the output of regulatory transfer functions into a control variable. We used hill-like transfer functions and  $\mathcal{I}_j \in \{min, max\}$  in this study [24].

We included 17 allosteric regulation terms, taken from literature, in the CFPS model. PEP was modeled as an inhibitor for phosphofructokinase [28, 29], PEP carboxykinase [28], PEP synthetase [28, 30], isocitrate dehydrogenase [28, 31], and isocitrate lyase/malate synthase [28, 31, 32], and as an activator for fructose-biphosphatase [28, 33–35]. AKG was modeled as an inhibitor for citrate synthase [28, 36, 37] and isocitrate lyase/malate synthase [28, 32]. 3PG was modeled as an inhibitor for isocitrate lyase/malate synthase [28, 32]. FDP was modeled as an activator for pyruvate kinase [28, 38] and PEP carboxylase [28, 39]. Pyruvate was modeled as an inhibitor for pyruvate dehydrogenase [28, 40, 41] and as an activator for lactate dehydrogenase [42]. Acetyl CoA was modeled as an inhibitor for malate dehydrogenase [28].

Estimation of kinetic model parameters. We estimated an ensemble of diverse parameter sets using a constrained Markov Chain Monte Carlo (MCMC) random walk strategy. Starting from a single best fit parameter set estimated by inspection and literature, we calculated the cost function, equal to the sum-squared-error between experimental data and model predictions:

$$cost = \sum_{i=1}^{\mathcal{D}} \left[ \frac{w_i}{\mathcal{Y}_i^2} \sum_{j=1}^{\mathcal{T}_i} \left( y_{ij} - x_i|_{t(j)} \right)^2 \right] \tag{4}$$

where  $\mathcal{D}$  denotes the number of datasets ( $\mathcal{D}=37$ ),  $w_i$  denotes the weight of the  $i^{th}$  dataset,  $\mathcal{T}_i$  denotes the number of timepoints in the  $i^{th}$  dataset, t(j) denotes the  $j^{th}$  time-

point,  $y_{ij}$  denotes the measurement value of the  $i^{th}$  dataset at the  $j^{th}$  timepoint, and  $x_i|_{t(j)}$  denotes the simulated value of the metabolite corresponding to the  $i^{th}$  dataset, interpolated to the  $j^{th}$  timepoint. Lastly, the cost calculation was scaled by the maximum experimental value in the  $i^{th}$  dataset,  $\mathcal{Y}_i = \max_j{(y_{ij})}$ . We then perturbed each model parameter between an upper and lower bound that varied by parameter type:

$$k_i^{new} = \min\left(\max\left(k_i \cdot \exp(a \cdot r_i), l_i\right), u_i\right) \qquad i = 1, 2, \dots, \mathcal{P}$$
(5)

where  $\mathcal{P}$  denotes the number of parameters ( $\mathcal{P} = 815$ ), which includes 163 maximum re-381 action rates  $(V^{max})$ , 163 enzyme activity decay constants, 455 saturation constants  $(K_{is})$ , 382 and 34 control parameters,  $k_i^{new}$  denotes the new value of the  $i^{th}$  parameter,  $k_i$  denotes 383 the current value of the  $i^{th}$  parameter, a denotes a distribution variance,  $r_i$  denotes a ran-384 dom sample from the normal distribution,  $l_i$  denotes the lower bound for that parameter 385 type, and  $u_i$  denotes the upper bound for that parameter type. Maximum reaction rates 386 were bounded between 0 and 500,000 mM/h [43]. Assuming a total enzyme concen-387 tration of 5.0  $\mu$ M, this corresponds to catalytic rate bounds of 0 and 27,780 s<sup>-1</sup>. These 388 bounds resulted in a median catalytic rate of 0.16 s<sup>-1</sup> across the ensemble. Enzyme 389 activity decay constants were bounded between 0 and 1 h<sup>-1</sup>, corresponding to half lives 390 of 42 minutes and infinity; median = 25 h. Saturation constants were bounded between 391 0.001 and 10 mM; median = 0.16 mM. Control parameters (gains and orders) were left unbounded; gain median = 0.076, order median = 0.69. For each newly generated pa-393 rameter set, we re-solved the balance equations and calculated the cost function. All sets 394 with a lower cost (and some with higher cost) were accepted into the ensemble. After 395 generating greater that 10,000 sets, we selected N = 100 sets with minimal set to set 396 correlation to avoid over-sampling any region of parameter space. 397

Sensitivity analysis of the kinetic CFPS model. We determined the reactions most important to protein production by computing the local sensitivity of CAT concentration (denoted as CAT) to each individual maximum reaction rate, and each pair of maximum reaction rates in the network. The sensitivity index was formulated as:

$$S_{ij}^{\text{CAT}} = \|\text{CAT}(p_i, p_j, t) - \text{CAT}(\alpha \cdot p_i, \alpha \cdot p_j, t)\|_2 \qquad i, j = 1, 2, \dots \mathcal{P}$$
(6)

where  $S_{ij}^{\mathtt{CAT}}$  denotes the sensitivity of CAT production to the  $i^{th}$  and  $j^{th}$  parameters,  $\mathtt{CAT}(p_i, p_j, t)$ 402 denotes CAT concentration as a function of time and the  $i^{th}$  and  $j^{th}$  parameters,  $\alpha$  denotes 403 the perturbation factor, and  $\mathcal{P}$  denotes the number of maximum reaction rates ( $\mathcal{P} = 163$ ). 404 In calculating the pairwise sensitivities, each parameter was perturbed by 1%; first-order 405 sensitivities (i = j) were subject to two 1% perturbations. Parameters and parameter 406 combinations were stratified into five degrees of importance, from least to most sensitive. 407 Likewise, we determined which reactions were most important to global system per-408 formance by computing the sensitivity of all species for which data exists (denoted as X) 409 to each maximum reaction rate in the network. In this case, each sensitivity index was 410 formulated as: 411

$$S_{ij}^{\mathbf{X}} = \left\| \mathbf{X}(p_i, p_j, t) - \mathbf{X}(\alpha \cdot p_i, \alpha \cdot p_j, t) \right\|_2 \qquad i, j = 1, 2, \dots \mathcal{P}$$
(7)

where  $S_{ij}^{\mathbf{X}}$  denotes the sensitivity of the system state to the  $i^{th}$  and  $j^{th}$  parameters, and  $\mathbf{X}(p_i,p_j,t)$  denotes the system state, an array consisting of the concentration of every species for which data exists as a function of time and the  $i^{th}$  and  $j^{th}$  parameters. The parameter sensitivities were stratified into five degrees of importance, from least to most sensitive, as above.

Sequence specific calculation of carbon yield. We estimated the theoretical maximum CAT carbon yield using sequence-specific flux balance analysis (ssFBA) [44]. The sequence specific flux balance analysis problem was formulated as a linear program:

$$\max_{\boldsymbol{w}} (w_{TL} = \boldsymbol{\theta}^T \boldsymbol{w})$$
Subject to:  $\mathbf{S} \mathbf{w} = \mathbf{0}$  (8)
$$\alpha_i < w_i < \beta_i \qquad i = 1, 2, \dots, \mathcal{R}$$

where S denotes the stoichiometric matrix,  $\mathbf{w}$  denotes the unknown flux vector,  $\boldsymbol{\theta}$  denotes the objective selection vector and  $\alpha_i$  and  $\beta_i$  denote the lower and upper bounds on flux  $w_i$ , respectively. The stoichiometry of the kinetic model was used for the ssFBA calculations, with the execpetion of the transcription and translation rates. The transcription (TX) and translation (TL) stoichiometry was modeled using the template reactions taken from Allen and Palsson [44]:

where  $G_{\mathcal{P}}$  denotes the gene encoding protein product  $\mathcal{P}$ ,  $R_1$  denotes the concentration of RNA polymerase,  $G_{\mathcal{P}}^*$  denotes the gene bounded by the RNA polymerase,  $\eta_i$  and  $\alpha_j$  denote the stoichiometric coefficients for nucleotide and amino acid, respectively,  $P_i$  denotes inorganic phosphate,  $R_2$  denotes the ribosome concentration,  $R_2^*$  denotes bounded ribosome, and  $AA_j$  denotes  $j^{th}$  amino acid.

The transcription rate  $(w_{TX})$  was fixed in the ssFBA calculation at:

431

$$w_{TX} = V_{TX}^{max} \left( \frac{G}{K_{TX} + G} \right) \tag{9}$$

where G denotes the gene concentration, and  $K_{TX}$  denotes a transcription saturation coefficient. The maximum rate of transcription  $V_{TX}^{max}$  was formulated as:

$$V_{TX}^{max} \equiv \left[ R_1 \left( \frac{v_{TX}}{l_G} \right) \left( \frac{K_{T7}}{1 + K_{T7}} \right) \right] \tag{10}$$

The term  $R_1$  denotes the RNA polymerase abundance,  $v_{TX}$  denotes the RNA polymerase elongation rate (nt/hr),  $l_G$  denotes the gene length in nucleotides, and the last term describes T7 promoter activity, where  $K_{T7}$  denotes a T7 RNA polymerase binding constant [45]. On the other hand, the translation rate ( $w_{TL}$ ) was bounded by:

$$0 \le w_{TL} \le V_{TL}^{max} \left( \frac{\text{mRNA}_{SS}}{K_{TL} + \text{mRNA}_{SS}} \right)$$
 (11)

where  ${
m mRNA_{SS}}$  denotes the steady state mRNA abundance, and  $K_{TL}$  denotes the translation saturation constant. The maximum translation rate  $V_{TL}^{max}$  was formulated as:

$$V_{TL}^{max} \equiv \left[ K_P R_2 \left( \frac{v_{TL}}{l_P} \right) \right] \tag{12}$$

The term  $K_P$  denotes the polysome amplification constant,  $v_{TL}$  denotes the ribosome

elongation rate (amino acids per hour),  $l_P$  denotes the number of amino acids in the protein of interest, and  ${
m mRNA_{SS}}$  denotes the steady-state mRNA concentration:

$$mRNA_{SS} \simeq \frac{w_{TX}}{\lambda}$$
 (13)

where  $\lambda$  denotes the rate constant controlling the mRNA degradation rate.

The objective of the sequence specific flux balance calculation was to maximize the rate of CAT translation,  $w_{TL}$ . The total glucose uptake rate was bounded by [0,40 mM/h] according to experimental data; while the amino acid uptake rates were bounded by [0,30 mM/h], but did not reach the maximum flux. The CAT gene and protein sequences were taken from literature. The sequence specific flux balance linear program was solved using the GNU Linear Programming Kit (GLPK) v4.52 [46].

Calculation of the carbon yield. The CAT carbon yield  $(Y_C^{CAT})$  was calculated as the ratio of carbon produced as CAT dived by the carbon consumed as reactants (glucose and amino acids):

$$Y_C^{CAT} = \frac{\Delta \text{CAT} \cdot C_{CAT}}{\sum_{i=1}^{\mathcal{R}} \max(\Delta m_i, 0) \cdot C_{m_i}}$$
(14)

where  $\Delta$ CAT denotes the abundance of CAT produced,  $C_{CAT}$  denotes carbon number of 453 CAT,  ${\cal R}$  denotes the number of reactants,  $\Delta m_i$  denotes the amount of the  $i^{th}$  reactant 454 consumed (never allowed to be negative), and  $C_{m_i}$  denotes the carbon number of the 455 ith reactant. Arginine or glutamate were not considered in the yield calculations, as no 456 experimental measurements were available for these amino acids. Yield of the best-fit 457 parameter set and the experimental data were calculated by setting  $\Delta$ CAT equal to the 458 final minus the initial CAT concentration, and setting  $\Delta m_i$  equal to the initial minus the 459 final reactant concentration. 460

Quantification of uncertainty. An ensemble of 100 sets of flux distributions was calculated for three different cases: unconstrained, constrained by transcription/translation 462 rates, and constrained by transcription/translation rates and experimental measurements. 463 For the unconstrained case, all rates were left unbounded, except the specific glucose 464 uptake rate. An ensemble of flux distributions was then calculated by randomly sampling 465 the maximum specific glucose uptake rate from within a range of 30 to 40 mM/h, de-466 termined from experimental data. For the case constrained by transcription/translation 467 rates, an ensemble was generated by randomly sampling RNAP polymerase levels, ri-468 bosome levels, and elongation rates in a physiological range determined from literature. 469 RNA polymerase levels were sampled between 60 and 80 nM, ribosome levels between 470 7 and 16 µM, the RNA polymerase elongation rate between 20 and 30 nt/sec, and the 471 ribosome elongation rate between 1.5 and 3 aa/sec [27, 47]. For the case constrained 472 by transcription/translation rates and experimental measurements, the lower and upper 473 bounds on the fluxes for the data-informed metabolites were sampled within the range 474 given by the experimental noise. This included the data for glucose, organic acids, en-475 ergy species, and amino acids; CAT was not constrained by experimental data, but by the transcription/translation rates as stated above.

# 478 Competing interests

The authors declare that they have no competing interests.

## **480 Author's contributions**

J.V directed the modeling study. K.C and J.S conducted the cell free protein synthesis experiments. J.V, J.W, and N.H developed the cell free protein synthesis mathematical model, and parameter ensemble. J.V and M.V performed the sequence specific flux balance analysis calculations. The manuscript was prepared and edited for publication by J.S, N.H, M.V, J.W and J.V.

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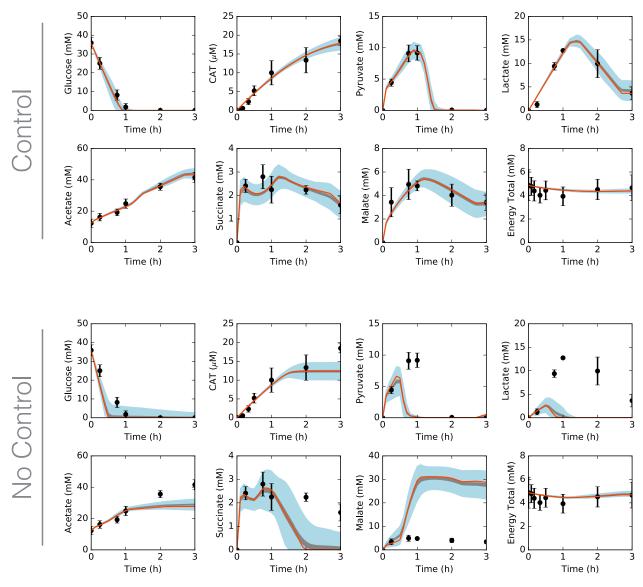
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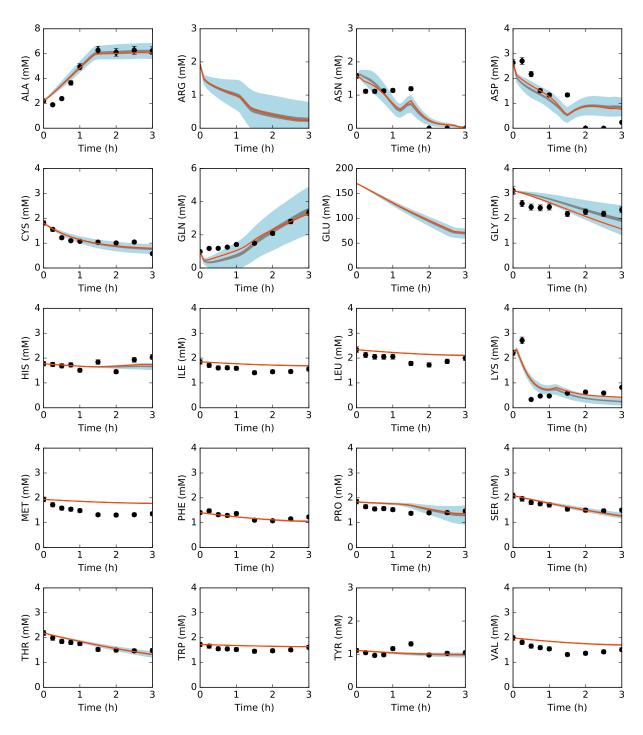
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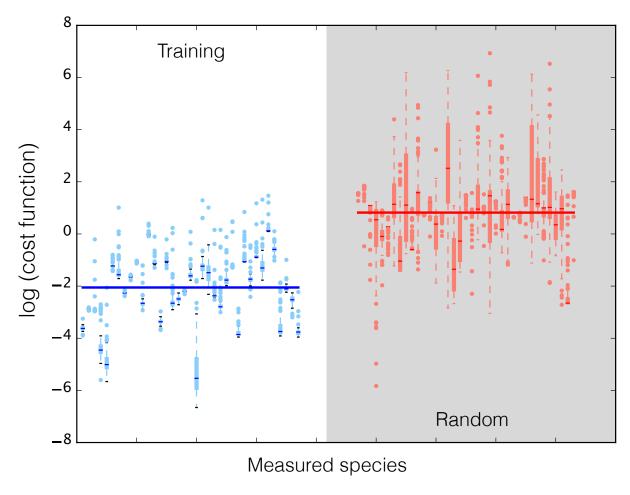
**Fig. 1:** Central carbon metabolism in the presence (top) and absence (bottom) of allosteric control, including glucose (substrate), CAT (product), and intermediates, as well as total concentration of energy species. Best-fit parameter set (orange line) versus experimental data (points). 95% confidence interval (blue shaded region) and 95% confidence interval of the mean (gray shaded region) over the ensemble of 100 sets.



**Fig. 2:** Energy species and energy totals by base in the presence of allosteric control. Best-fit parameter set (orange line) versus experimental data (points). 95% confidence interval (blue shaded region) and 95% confidence interval of the mean (gray shaded region) over the ensemble of 100 sets.

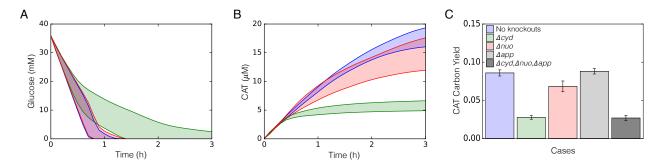


**Fig. 3:** Amino acids in the presence of allosteric control. Best-fit parameter set (orange line) versus experimental data (points). 95% confidence interval (blue shaded region) and 95% confidence interval of the mean (gray shaded region) over the ensemble of 100 sets.

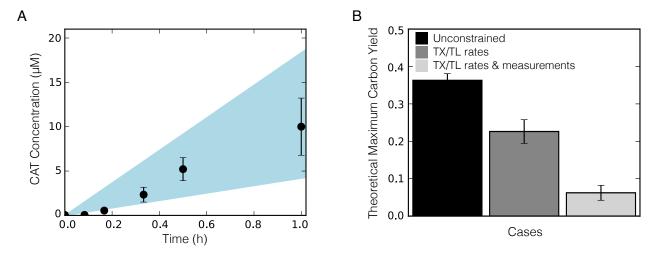


**Fig. 4:** Log of cost function across 37 datasets for data-trained ensemble (blue) and randomly generated ensemble (red, gray background). Median (bars), interquartile range (boxes), range excluding outliers (dashed lines), and outliers (circles) for each dataset. Median across all datasets (large bar overlaid).

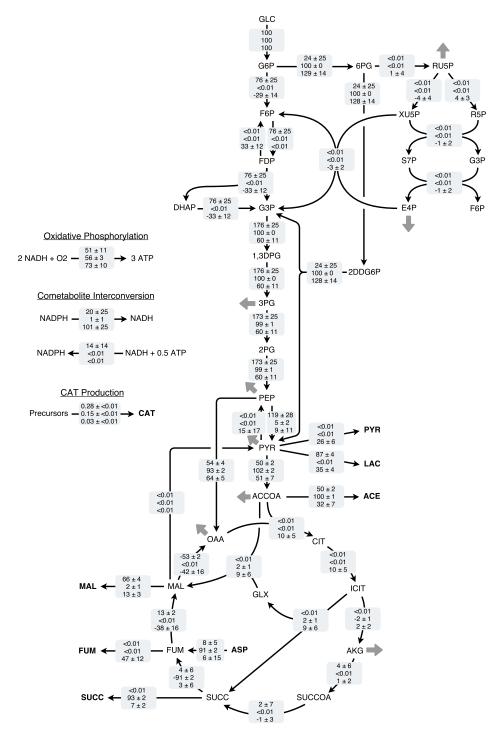
**Fig. 5:** Normalized first-order and pairwise sensitivities of CAT production (top) and system state (bottom) to maximum reaction rates.



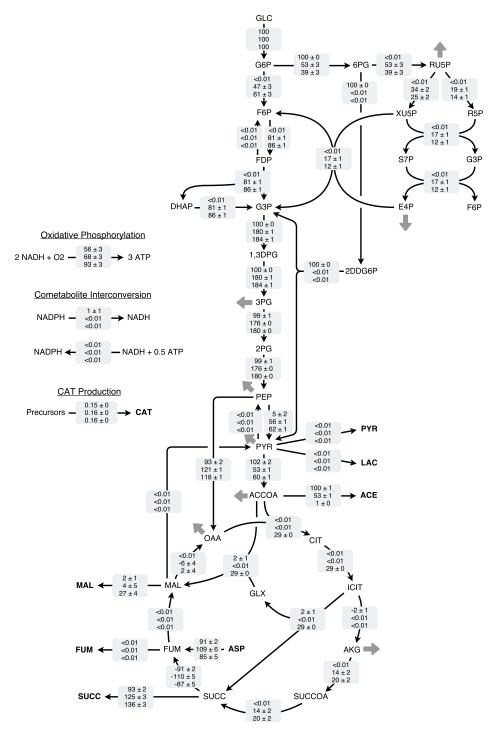
**Fig. 6:** The effect of oxidative phosphorylation on glucose uptake, CAT production and CAT carbon yield. A. 95% confidence interval of an ensemble for glucose concentration versus time for no knockouts (blue shaded region), *cyd* knockout (green shaded region), and *nuo* knockout (red shaded region). B. 95% confidence interval of an ensemble for CAT concentration versus time for no knockouts (blue shaded region), *cyd* knockout (green shaded region), and *nuo* knockout (red shaded region). C. CAT carbon yield for 5 different cases of oxidative phosphorylation: no knockouts (blue), *cyd* knockout (green), *nuo* knockout (red), *app* knockout (light grey), and a combination of *cyd*, *nuo*, *app* knockouts (dark grey).



**Fig. 7:** Sequence-specific flux balance analysis of CAT production and yield. A. 95% confidence interval of the ensemble (light blue region) for CAT concentration versus time. B. Theoretical maximum carbon yield of CAT calcualted by ssFBA for three different cases: unconstrained except for glucose uptake (black), constrained by transcription/translation (TX/TL) rates (grey), and constrained by transcription/translation (TX/TL) rates and experimental measurements where available (light grey). Error bars represent standard deviation of the ensemble.



**Fig. 8:** Flux profile for glycolysis, pentose phosphate pathway, Entner-Doudoroff pathway, TCA cycle, NADPH/NADH transfer, and oxidative phosphorylation. Sequence-specific FBA flux value (mean ± standard deviation) across ensemble for 1 hr, normalized to glucose uptake flux. Flux distribution for three different cases: unconstrained except for glucose uptake (top row), constrained by transcription and translation rates (second row), and constrained by transcription, translation rates and experimental measurements where available (bottom row).



**Fig. 9:** Flux profile with knockouts for glycolysis, pentose phosphate pathway, Entner-Doudoroff pathway, TCA cycle, NADPH/NADH transfer, and oxidative phosphorylation. Sequence-specific FBA flux value (mean ± standard deviation) across ensemble for 1 hr, normalized to glucose uptake flux. Flux distribution for three different cases: constrained by transcription and translation rates (top row), constrained by transcription and translation rates with *gnd* knocked out (second row), and constrained by transcription and translation rates with *gnd* and phosphate acetyltransferase knocked out.