Reduced order modeling and analysis of the human complement system

Adithya Sagar, Wei Dai#, Mason Minot#, and Jeffrey D. Varner*

School of Chemical and Biomolecular Engineering Cornell University, Ithaca NY 14853

Running Title: A reduced order model of complement

To be submitted: Scientific Reports

Denotes equal contribution

*Corresponding author:

Jeffrey D. Varner,

Professor, School of Chemical and Biomolecular Engineering,

244 Olin Hall, Cornell University, Ithaca NY, 14853

Email: jdv27@cornell.edu

Phone: (607) 255 - 4258

Fax: (607) 255 - 9166

Abstract

Complement is an important pathway in innate immunity, inflammation, and many disease processes. However, despite its importance, there have been few validated mathematical models of complement activation. In this study, we developed an ensemble of experimentally validated reduced order complement models. We combined ordinary differential equations with logical rules to produce a compact yet predictive complement model. The model, which described the lectin and alternative pathways, was an order of magnitude smaller than comparable models in the literature. We estimated an ensemble of model parameters from *in vitro* dynamic measurements of the C3a and C5a complement proteins. Subsequently, we validated the model on unseen C3a and C5a measurements not used for model training. Despite its small size, the model was surprisingly predictive. Global sensitivity and robustness analysis suggested complement was robust to any single therapeutic intervention. Only dual dual-knockdown of both C3 and C5 consistently reduced C5a formation when all pathways were activated. Taken together, we developed a reduced order complement model that was computationally inexpensive, and could easily be incorporated into pre-existing or new pharmacokinetic models of immune system function. The model described experimental data, and predicted the need for multiple points of therapeutic intervention to disrupt complement activation.

Keywords: Complement system, systems biology, reduced order models, biochemical engineering

Introduction

Complement is an important pathway in innate immunity. It plays a significant role in inflammation, host defense as well as many disease processes. Complement was discovered in the late 1880s where it was found to 'complement' the bactericidal activity of natural antibodies (1). However, research over the past decade has shown that the importance of complement extends well beyond innate immunity. For example, complement contributes to tissue homeostasis by inducing tissue repair (2). Complement has also been linked with several diseases including Alzheimers, Parkinson's disease, multiple sclerosis, schizophrenia, rheumatoid arthritis and sepsis (3, 4). Complement plays both positive and negative roles in cancer; attacking tumor cells with altered surface proteins in some cases, while potentially contributing to tumor growth in others (5, 6). Lastly, several other important biochemical subsystems are integrated with complement including the coagulation cascade, the autonomous nervous system and inflammation (6). Thus, complement is important in a variety of beneficial and potentially harmful functions in the body.

The complement cascade involves over 30 soluble and cell surface proteins, receptors 16 and regulators. The molecular connectivity of complement involves both fluid phase and 17 cell surface events, see the review of Walport (7, 8). The central outputs of complement 18 are the Membrane Attack Complex (MAC), and the inflammatory mediator proteins C3a 19 and C5a. The membrane attack complex, generated during the terminal phase of the re-20 sponse, forms transmembrane channels which disrupt the membrane integrity of targeted 21 cells, leading to cell lysis and death. On the other hand, the C3a and C5a proteins act as a bridge between innate and adaptive immunity, and play an important role in regulating 23 inflammation (5). Complement activation takes places through three pathways: the classical, the lectin binding and the alternate pathways. The classical pathway is triggered by antibody recognition of foreign antigens or other pathogens. A multimeric protein com-

plex C1 binds to antibody-antigen complexes and undergoes a conformational change, leading to an activated form with proteolytic activity. This activated complex then cleaves soluble complement proteins C4 and C2 into C4a, C4b, C2a and C2b, respectively. The C4a and C2b fragments bind to form the C4bC2a protease, also known as the classical 30 C3 convertase. The lectin pathway is initiated through the binding of L-ficolin or Mannose 31 Binding Lectin (MBL) to carbohydrates on the surfaces of bacterial pathogens. These 32 complexes, in combination with the associated mannose-associated serine proteases 1 33 and 2 (MASP-1/2), also cleave C4 and C2, leading to additional classical C3 conver-34 tase. Thus, the classical and lectin pathways, initiated by the recognition of different cues 35 on foreign surfaces, converge at the classical C3 convertase. However, the alternate pathway works differently. It is activated by a 'tickover' mechanism in which complement 37 protein C3 is spontaneously hydrolyzed to form an activated intermediate C3w; C3w re-38 cruits factor B and factor D, leading to the formation of C3wBb. C3wBb cleaves C3 into C3a and C3b, where the C3b fragment further recruits additional factor B and factor D to form C3bBbC3b, the alternate C3 convertase (9). The role of classical and alternate 41 C3 convertases is varied. First, C3 convertases mediate signal amplification. C3 convertases cleave C3 into C3a and C3b; the C3b fragment is then free to form additional alternate C3 convertases, thereby forming a positive feedback loop. Next, C3 convertases link complement initiation with the terminal phase of the cascade through the formation of C5 convertases. Both classical and alternate C3 convertases can recruit C3b subunits to form the classical C5 convertase (C4bC2aC3b), and the alternate C5 convertase 47 (C3bBbC3b), respectively. C5 convertases cleave C5 into the C5a and C5b fragments. The C5b fragment, along with the C6, C7, C8 and multiple C9 complement proteins, form the membrane attack complex. On the other hand, both C3a and C5a are important in-50 flammatory signals involved in several responses (7, 8). Thus, the complement cascade 51 directly attacks the invading pathogen, and signals for help from the immune system.

The complement cascade is regulated by plasma and host cell proteins which bal-53 ance host cell safety with effectiveness. The initiation of the classical pathway via complement protein C1 is controlled by the C1 Inhibitor (C1-Inh). C1-Inh irreversibly binds 55 to and deactivates the active subunits of C1, preventing chronic complement activation (10). Regulation of upstream processes in the lectin and alternate pathways also oc-57 curs through the interaction of the C4 binding protein (C4BP) with C4b, and factor H with 58 C3b (11). Interestingly, both factor H and C4BP are capable of binding their respective 59 targets while in convertase complexes as well. At the host cell surface, membrane co-60 factor protein (MCP or CD46) can interact with C4b and C3b, which protects the host 61 cell from complement self-activation (12). Delay accelerating factor (DAF or CD55) also 62 recognizes and dissociates both C3 and C5 convertases on host cell surfaces (13). More 63 generally, Carboxypeptidase-N, a well known inflammation regulator, has broad activity 64 against the complement proteins C3a, C4a, and C5a, rendering them inactive by cleavage of carboxyl-terminal arginine and lysine residues (14). Although Carboxypeptidase-N does not directly influence complement activation, it silences the important inflammatory 67 signals produced by complement. Lastly, the assembly of the MAC complex itself can be inhibited by vitronectin and clusterin in the plasma, and CD59 at the host surface (15, 16). Thus, there are many points of control which influence complement across the three activation pathways.

Developing quantitative mathematical models of complement will be crucial to fully understanding its role in the body. Traditionally, complement models have been formulated as systems of linear or non-linear ordinary differential equations (ODEs). For example, Hirayama et al. modeled the classical complement pathway as a system of linear ODEs (17), while Korotaevskiy and co-workers modeled the classical, lectin and alternate pathways (up to C3a) as a system of non-linear ODEs (18). More recently, large mechanistic models of sections of complement have also been proposed. For example, Liu et al. an-

72

73

75

76

alyzed the formation of the classical and lectin C3 convertases, and the regulatory role of C4BP using a system of 45 non-linear ODEs with 85 parameters (19). Zewde and co-workers constructed a detailed mechanistic model of the alternative pathway which 81 consisted of 107 ODEs and 74 kinetic parameters and delineated between the host cell 82 and pathogen (16). However, these previous modeling studies involved little experimen-83 tal validation. Thus, while these models are undoubtably important theoretical tools, it 84 is unclear if they can describe or quantitatively predict complement measurements. The 85 central challenge of complement model identification is the estimation of model parame-86 ters from experimental measurements. Unlike other important cascades, such as coaqu-87 lation where there are well developed experimental tools and publicly available data sets, 88 the data for complement is relatively sparse. Missing or incomplete data sets, and limited 89 quantitative data make the identification of large mechanistic complement models difficult. 90 Thus, reduced order modeling approaches, which describe the key biology with a limited 91 number of parameters, will be important for developing validated models of complement, and to fully understandings its role in the body.

Results

117

In this study, we developed an ensemble of experimentally validated reduced order complement models. The modeling approach combined ordinary differential equations with 96 logical rules to produce a complement model with a limited number of equations and pa-97 rameters. The reduced order model, which described the lectin and alternative pathways, consisted of 18 differential equations with 28 parameters. Thus, the model was an order of 99 magnitude smaller and included more pathways than comparable models in the literature. 100 We estimated an ensemble of model parameters from in vitro time series measurements 101 of the C3a and C5a complement proteins. Subsequently, we validated the model on unseen C3a and C5a measurements that were not used for model training. Despite its 103 small size, the model was surprisingly predictive. After validation, we performed global 104 sensitivity and robustness analysis to estimate which parameters and species controlled 105 model performance. These analyses suggested complement was robust to any single 106 therapeutic intervention; only the knockdown of both C3 and C5 consistently reduced 107 C3a and C5a formation for all cases. Taken together, we developed a reduced order com-108 plement model that was computationally inexpensive, and could easily be incorporated 109 into pre-existing or new pharmacokinetic models of immune system function. The model 110 described experimental data, and predicted the need for multiple points of intervention to 111 disrupt complement activation. 112

Reduced order complement network. The complement model described the alternate 113 and lectin pathways (Fig. 1). A trigger event initiated the lectin pathway, which activated the cleavage of C2 and C4 into C2a, C2b, C4a and C4b respectively. Classical Pathway 115 (CP) C3 convertase (C4aC2b) then catalyzed the cleavage of C3 into C3a and C3b. The alternate pathway was initiated through the spontaneous hydrolysis of C3 into C3a and C3b (not C3w). The C3b fragment generated by hydrolysis (or by CP C3 convertase) 118 could then form the alternate pathway (AP) C3 convertase (C3bBb). We did not consider 119

C3w, nor the formation of the initial alternate C3 convertase (C3wBb). Rather, we assumed C3w was equivalent to C3b and only modeled the formation of the main AP C3 121 convertase. Both the CP and AP C3 convertases catalyzed the cleavage of C3 into C3a 122 and C3b. A second C3b fragment could then bind with either the CP or AP C3 convertase 123 to form the CP or AP C5 convertase (C4bC2aC3b or C3bBbC3b). Both C5 convertases 124 catalyzed the cleavage of C5 into the C5a and C5b fragments. In this initial study, we 125 simplified the model by assuming both Factor B and Factor D were in excess. However, 126 we did explicitly account for two control proteins, Factor H and C4BP. Lastly, we did not 127 consider MAC formation, instead we stopped at C5a and C5b. Lectin pathway activation, 128 and C3/C5 convertase activity was modeled using a combination of saturation kinetics 129 and non-linear transfer functions, which facilitated a significant reduction in the size of the 130 model while maintaining performance. Binding interactions were modeled using mass-131 action kinetics, where we assumed all binding was irreversible. Thus, while the reduced 132 order complement model encoded significant biology, it was highly compact consisting of 133 only 18 differential equations and 28 model parameters. Next, we estimated an ensemble 134 of model parameters from time series measurements of the C3a and C5a complement 135 proteins.

for the development of any dynamic model is the estimation of model parameters. We estimated an ensemble of complement model parameters in a hierarchical fashion using *in vitro* time-series data sets generated with and without zymosan, a lectin pathway activator (20). The residual between model simulations and experimental measurements was minimized using the dynamic optimization with particle swarms (DOPS) routine, starting from an initial random parameter guess. Unless otherwise specified, all initial conditions were assumed to be their mean physiological values. A hierarchical approach was taken in which the alternate pathway parameters were estimated first and then fixed during the

137

138

139

140

141

142

estimation of the lectin pathway parameters. While we had significant training data, the parameter estimation problem was underdetermined (we were not able to uniquely deter-147 mine model parameters). Thus, instead of using a best-fit yet uncertain parameter set, we 148 estimated an ensemble of probable parameter sets (N = 50, see materials and methods). 149 The reduced order complement model ensemble captured the behavior of both the alter-150 native and lectin pathways (Fig. 2). For the alternative pathway, we used C3a and C5a 151 measurements in the absence of zymosan, and only allowed the alternative parameters 152 to vary (Fig. 2A and B). On the other hand, lectin pathway parameters were estimated 153 from C3a and C5a measurements in the presence of 1g zymosan with alternate pathway 154 parameters fixed (Fig. 2C and D). The reduced order model reproduced a panel of alter-155 nate and lectin pathway data sets in the neighborhood of physiological factor and inhibitor 156 concentrations. However, it was unclear whether the reduced order model could predict 157 new data, without updating the model parameters. To address this question, we fixed the 158 model parameters and simulated data sets not used for model training. 159

We tested the predictive power of the reduced order complement model with data not used during model training (Fig. 3). Six validation cases were considered, three for C3a and C5a, respectively. All model parameters and initial conditions were fixed for the validation simulations (with the exception of zymosan, and other experimentally mandated changes). The ensemble of reduced order models predicted the qualitative dynamics of C3a formation (Fig. 3, top), and C5a formation (Fig. 3, bottom) at three inducer concentrations. The rate of C3a formation and C3a peak time were directly proportional to initiator dose. Similarly, the C5a plateau and rate of formation were also directly proportional to initiator dose, with the lag time being indirectly proportional to initiator exposure. However, there were shortcomings with model performance. First, while the overall C3a trend was captured (within the 99% confidence interval), the C3a dynamics were too fast with the exception of the low dose case. We believe the C3a timescale was related to

160

161

165

166

167

168

169

our choice of training data, how we modeled the tickover mechanism, and factor B and D limitation. We trained the model using either no or 1 mg/ml zymosan, but predicted cases 173 in a different initiator range; comparing the training to prediction, the model performance e.g., the shape of the C3a trajectory was biased towards either high or very low initiator 175 doses. Next, tickover was modeled as a first-order generation processes where C3wBb 176 formation and activity was lumped into the AP C3 convertase. Thus, we skipped an im-177 portant step which could strongly influence AP C3 convertase formation by slowing down 178 the rate C3 cleavage into C3a and C3b. We also assumed both factor B and factor D were 179 not limiting, thereby artificially accelerating the rate of AP C3 convertase formation. The 180 C5a predictions followed a similar trend as C3a; we captured the long-time C5a behavior 181 but over predicted the time scale of C5 cleavage. However, because the C5a time scale 182 depends strongly upon C3 convertase formation, we can likely correct the C5 issues by 183 fixing the rate of C3 cleavage. Despite these shortcomings, we qualitatively predicted un-184 seen experimental measurements within the 99% confidence of the ensemble, for three 185 inducer levels. Next, we used global sensitivity and robustness analysis to determine 186 which parameters and species controlled the performance of the complement model. 187

Global analysis of the reduced order complement model. We conducted sensitivity analysis to estimate which parameters controlled the performance of the reduced order complement model. We calculated the total sensitivity of the C3a and C5a residual to changes in model parameters with and without zymosan (Fig. 4). In the absence of zymosan (where only the alternative pathway is active), the most sensitive parameter was the rate constant governing the assembly of the AP C3 convertase, as well as the rate constant controlling basal C3b formation. The C5a trajectory was sensitive to the AP C5 convertase kinetic parameters (Fig. 4A). Interestingly, neither the rate nor the saturation constants governing AP C3-convertase activity were sensitive in the absence of zymosan. Thus, C3a formation in the alternative pathway was more heavily influenced by

188

189

190

191

192

193

194

195

the spontaneous hydrolysis of C3, rather than AP C3-convertase activity, in the absence of zymosan. In the presence of zymosan, the C3a residual was controlled by the formation and activity of the CP C3 convertase, as well as tickover and degradation parameters. On the other hand, the C5a residual was controlled by the formation and activity of CP C5 convertase, and tickover C3b formation in the presence of zymosan (Fig. 4B). The lectin initiation parameters were sensitive, but to a lesser extent than CP convertase kinetic parameters and tickover C3b formation. Thus, sensitivity analysis suggested that CP C3/C5 convertase formation and activity dominated in the presence of zymosan, but tickover parameters and AP C5 convertase were more important without initiator. Next, we compared the sensitivity results to current therapeutic approaches; pathways involving sensitive parameters have been targeted for clinical intervention (Fig. 4C). In particular, the sensitivity analysis suggested AP/CP C5 convertase inhibitors, or interventions aimed at attenuating C3 or C5 would most strongly influence complement performance. Thus, there was at least a qualitative overlap between sensitivity and the potential of biochemical efficacy. However, sensitivity coefficients are only a local measure of how small changes in parameters affect model performance. To more closely simulate a clinical intervention e.g., administration of an anti-complement inhibitor, we performed robustness analysis.

199

200

201

202

203

204

205

206

207

208

209

210

211

212

213

215

217

218

219

220

221

222

Robustness coefficients quantify the response of a marker to a macroscopic structural or operational perturbation to a biochemical network. Here, we computed how the C3a and C5a trajectories responded to a decrease in the initial abundance of C3 and/or C5. Robustness analysis suggested there was no single intervention that inhibited complement activation in the presence of both initiation pathways (Fig. 5). We calculated robustness indices for C3a and C5a for the parameter ensemble (N = 50) with and without the lectin pathway initiator. We simulated the addition of different doses of anti-complement inhibitor cocktails by decreasing the initial concentration of C3 or C5 or the combination of C3 and C5 by 50% and 90%. This would be conceptually analogous to the administration

of a C3 inhibitor e.g., compstatin alone or combination with eculizumab (Fig. 4E). A log₁₀ transformed robustness index of zero indicated no effect due to the perturbation, whereas an index of less than zero indicated decreased C3a or C5a. The response of the comple-226 ment model to different knock-down magnitudes was non-linear; a 90% knock-down had 227 an order of magnitude more impact than a 50% knock-down. As expected, a C5 knock-228 down had no effect on C3a formation for either the alternate (Fig. 5A, lanes 1 or 3) or 229 lectin pathways (Fig. 5B, lanes 1 or 3). However, C3a abundance and to a lesser extent 230 C5a abundance decreased with decreasing C3 concentration in the alternate pathway 231 (Fig. 5A or B, lanes 1 or 2). This agreed with the sensitivity results; changes in AP C3-232 convertase formation affected the downstream dynamics of C5a formation. Thus, if we 233 only considered the alternate pathway, C3 alone could be a reasonable target, especially 234 given that C5a formation was surprisingly robust to C5 levels in the alternate pathway 235 (Fig. 5A or B, lane 2). Yet, when both pathways were activated, C5a levels were robust to 236 the initial C3 concentration (Fig. 5A or B, lane 4); C5a formation was catalyzed by CP C3 237 and C5 convertases. Thus, the only reliable intervention that consistently reduced both 238 C3a and C5a formation for all cases was a dual-knockdown of C3 and C5. For example, 239 a 90% decrease of both C3 and C5 reduced the formation of C5a by over an order of 240 magnitude (Fig. 5B, lane 4), while C3a was reduced to a lesser extent (Fig. 5B, lane 3).

Discussion

252

253

257

261

262

263

264

265

266

267

In this study, we developed an ensemble of experimentally validated reduced order com-243 plement models. The modeling approach combined ordinary differential equations with 244 logical rules to produce a complement model with a limited number of equations and pa-245 rameters. The reduced order model, which described the lectin and alternative pathways, 246 consisted of 18 differential equations with 28 parameters. Thus, the model was an order 247 of magnitude smaller and included more pathways than comparable mathematical mod-248 els in the literature. We estimated an ensemble of model parameters from in vitro time 249 series measurements of the C3a and C5a complement proteins. Subsequently, we validated the model on unseen C3a and C5a measurements that were not used for model training. Despite its small size, the model was surprisingly predictive. After validation, we performed global sensitivity and robustness analysis to estimate which parameters and species controlled model performance. These analyses suggested complement was ro-254 bust to any single therapeutic intervention. The only intervention that consistently reduced 255 C5a formation for all cases was a dual-knockdown of both C3 and C5. Taken together, 256 we developed a reduced order complement model that was computationally inexpensive, and could easily be incorporated into pre-existing or new pharmacokinetic models of im-258 mune system function. The model described experimental data, and predicted the need 259 for multiple points of intervention to disrupt complement activation. 260

Despite its importance, there has been a paucity of validated mathematical models of complement pathway activation. To our knowledge, this study is one of the first complement models that combined multiple initiation pathways with experimental validation of important complement products like C5a. However, there have been several theoretical models of components of the cascade in the literature. Liu and co-workers modeled the formation of C3a through the classical pathway using 45 non-linear ODEs (19). In contrast, in this study we modeled lectin mediated C3a formation using only five ODEs. Though we did not model all the initiation interactions in detail, especially the cross-talk between the lectin and classical pathways, we successfully captured C3a dynamics with respect to different concentrations of lectin initiators. The model also captured the dynamics of C3a and C5a formed from the alternate pathway using only seven ODEs. The reduced order model predictions of C5a were qualitatively similar to the theoretical complement model of Zewde et al which involved over 100 ODEs (16). However, we found that the quantity of C3a produced in the alternate pathway was nearly 1000 times the quantity of C5a produced. Though this was in agreement with the experimental data (20), it differed from the theoretical predictions made by Zewde et al. who showed C3a was 10^8 times the C5a concentration (16). In our model, the time profile of C5a generation from the lectin pathway changed with respect to the quantity of zymosan (the lectin pathway initiator). The lag phase for generation was inversely proportional to the initiator concentration. Korotaevskiy et al. showed a similar trend using a theoretical model of complement, albeit for much shorter time scales (18). Thus, the reduced order complement model performed similarly to existing large mechanistic models, despite being significantly smaller.

Global analysis of the complement model estimated potential important therapeutic targets. Complement malfunctions are implicated in a number of diseases, however the development of complement specific therapeutics has been challenging (3, 21). Previously, we have shown that mathematical modeling and sensitivity analysis can be useful tools to estimate therapeutically important mechanisms in biochemical networks (22–25). In this study, we analyzed a validated ensemble of reduced order complement models to estimate therapeutically important mechanisms. In presence of an initiator, C5a formation was primarily sensitive to the lectin initiation parameters, and parameters governing the conversion of C5 to C5a and C5b. This result agrees well with the current protease inhibitors targeting initiating complexes, including mannose-associated serine proteases 1 and 2 (MASP-1,2) (26). The most commonly used anti-complement drug eculizumab

(21), targets the C5 protein which is cleaved to form C5a. Our sensitivity analysis showed that kinetic parameters governing C5 conversion were sensitive in both lectin initiated and alternate pathways, thus agreeing with targeting C5 protein. The formation of basal C3b was also a sensitive parameter in the formation of C3a through the alternate pathway. Thus, this mechanism can act as a target for both C3a and C5a inhibitors. Lectin initiated C3a formation showed a number of sensitive parameters. This included the lectin initiation parameters that controlled C5a formation, C3 convertase inhibition by C4BP, and parameters governing C3 convertase activity. All these mechanisms are potential drug targets.

296

297

298

299

300

301

302

303

304

305

306

307

308

309

314

315

316

317

318

To further validate these results from sensitivity analysis about potential drug targets we did a robustness analysis. We knocked down C3 and C5 levels and studied their impact on the generation of C3a and C5a. The C3a and C5a levels in the lectin pathway were strongly influenced by initial levels of C3 and C5. Thus direct inhibition of C3 and C5, or targeting complexes (MASP complex, C3 and C5 convertases) that act on C3 and C5 have a direct impact on production of C3a and C5a. This is also in agreement with sensitivity analysis that C5 is a good drug target. A number of drugs targeting C5 are being developed. For example LFG316 by Novartis is being used to target C5 in cases of Age-Related Macular Degeneration (27), Mubodina is an antibody that targets C5 in the treatment of Atypical Hemolytic-Uremic Syndrome (aHUS) (28), Coversin is a small molecule targeting C5 (29), Zimura is an aptamer targeting C5 (30), small peptides and RNAi are also being used to inhibit C5 (31). Another important conclusion that can be drawn together from sensitivity and robustness analysis is that C3 and C5 convertases can be important therapeutic targets. Though knockdown of C3 and C5 affects C3a and C5a levels downstream, the abundance and turnover rate (32, 33) of these proteins make them difficult targets. Thus targeting C3 and C5 directly will require high dosage of drugs. It is also well known that eculizumab dosage needs to be adjusted while treating for Atypical Hemolytic-Uremic Syndrome (aHUS), a disease that is caused due to uncontrolled complement activation (34). The issue of high dosage can potentially be circumvented by targeting convertases or fragile mechanisms that involve C3, C5 or their activated components. Our analysis shows that formation and assembly of these convertases are sensitive mechanisms that strongly impact downstream proteins like C5a. Formation of convertases is inhibited by targeting upstream protease complexes like MASP-1,2 from lectin pathway (or C1r, C1s from classical pathway). For example, Omeros is a protease inhibitor that targets MASP-2 complex and thereby inhibits formation of downstream convertases (35). Lampalizumab (an immunoglobulin) and Bikaciomab (an antibody fragment) target Factor B and Factor D respectively. Factor B and Factor D are crucial to formation alternate pathway convertases (36, 37). Novelmed Therapeutics recently developed antibody, NM9401 against propedin, a small protein that stabilizes alternate C3 convertase (38). Cobra Venom Factor (CVF), an analogue of C3b has been used to bind to Factor B to regulate alternate convertases (39). Thus, analysis of the ensemble of complement models identified potentially important therapeutic targets that are consistent with therapeutic strategies that are under development.

321

322

323

324

325

326

327

328

329

330

331

332

333

334

335

336

337

339

340

341

342

343

344

The performance of the complement model was impressive given its limited size. However, there are several questions that should be explored further. A logical progression for this work would be to expand the network to include the classical pathway and the formation of the membrane attack complex (MAC). However, it is unclear whether the addition of the classical pathway will decrease the predictive quality of our existing model. Liu et al have shown cross-talk between the activation of the classical and lectin pathways that could influence model performance (19). One potential approach to address such difficulties would be to incorporate C reactive proteins (CRP) and L-ficolin (LF) into the model, both of which are involved with the initiation of classical and lectin pathways. Liu et al. showed that under inflammation conditions interactions between lectin and classical

pathways was mediated through CRP and LF (19). Thus incorporating these two proteins would help us in modeling cross talk. Time course measurements of MAC abundance (and MAC formation dynamics) are also scarce, making the inclusion of MAC challenging. Next, we should address the under-prediction of C3a. We believe the C3a underprediction can be attributed to how we modeled C4BP interactions. C4BP interactions were modeled as irreversible binding steps resulting in completely inactive complexes; however, the binding of C4BP with complement proteins is likely reversible and C4BPbound convertases may have residual activity. We also did not capture the maximum concentration of C3a at low initiator levels. One possible reasons for this could the C2-by pass pathway, which was not included in the model. This pathway further accelerates C3a production without the involvement of a C3 convertase. Currently the C3a in the model is generated only through the activity of a C3 convertase. Incorporating this additional step within the reduced order modeling framework would be a future direction that we need to consider. We should test alternative model structures which include reversible C4BP binding, and partially active convertases. Alternatively, we could also perform sensitivity analysis on the C3a prediction residual to determine which parameters controlled the C3a prediction.

347

349

350

351

352

353

354

355

356

357

358

359

360

361

Materials and Methods

Formulation and solution of the complement model equations. We used ordinary differential equations (ODEs) to model the time evolution of complement proteins (x_i) in the reduced order model:

$$\frac{1}{\tau_i} \frac{dx_i}{dt} = \sum_{i=1}^{\mathcal{R}} \sigma_{ij} r_j \left(\mathbf{x}, \epsilon, \mathbf{k} \right) \qquad i = 1, 2, \dots, \mathcal{M}$$
 (1)

where \mathcal{R} denotes the number of reactions and \mathcal{M} denotes the number of protein species 367 in the model. The quantity τ_i denotes a timescale parameter for species i which captures 368 unmodeled effects; by default τ_i = 1, for all species unless otherwise specified. The quan-369 tity $r_{j}\left(\mathbf{x},\epsilon,\mathbf{k}\right)$ denotes the rate of reaction j. Typically, reaction j is a non-linear function of biochemical and enzyme species abundance, as well as unknown model parameters k 37 $(\mathcal{K} \times 1)$. The quantity σ_{ij} denotes the stoichiometric coefficient for species i in reaction j. If $\sigma_{ij} > 0$, species i is produced by reaction j. Conversely, if $\sigma_{ij} < 0$, species i is consumed by reaction j, while $\sigma_{ij} = 0$ indicates species i is not connected with reaction j. Species balances were subject to the initial conditions $\mathbf{x}(t_o) = \mathbf{x}_o$. Rate processes were written as the product of a kinetic term (\bar{r}_i) and a control term 376 (v_i) in the complement model. The kinetic term for the formation of C4a, C4b, C2a and 377

$$\bar{r}_j = k_j^{max} \epsilon_i \left(\frac{x_s^{\eta}}{K_{js}^{\eta} + x_s^{\eta}} \right) \tag{2}$$

where k_j^{max} denotes the maximum rate for reaction j, ϵ_i denotes the abundance of the enzyme catalyzing reaction j, η denotes a cooperativity parameter, and K_{js} denotes the saturation constant for species s in reaction j. We used mass action kinetics to model

C2b, lectin pathway activation, and C3 and C5 convertase activity was given by:

protein-protein binding interactions within the network:

$$\bar{r}_j = k_j^{max} \prod_{s \in m_j^-} x_s^{-\sigma_{sj}} \tag{3}$$

where k_j^{max} denotes the maximum rate for reaction j, σ_{sj} denotes the stoichiometric coefficient for species s in reaction j, and $s \in m_j$ denotes the set of *reactants* for reaction j. We assumed all binding interactions were irreversible.

The control terms $0 \le v_j \le 1$ depended upon the combination of factors which influenced rate process j. For each rate, we used a rule-based approach to select from
competing control factors. If rate j was influenced by $1, \ldots, m$ factors, we modeled this relationship as $v_j = \mathcal{I}_j \left(f_{1j} \left(\cdot \right), \ldots, f_{mj} \left(\cdot \right) \right)$ where $0 \le f_{ij} \left(\cdot \right) \le 1$ denotes a regulatory transfer
function quantifying the influence of factor i on rate j. The function $\mathcal{I}_j \left(\cdot \right)$ is an integration
rule which maps the output of regulatory transfer functions into a control variable. Each
regulatory transfer function took the form:

$$f_{ij}\left(\mathcal{Z}_{i}, k_{ij}, \eta_{ij}\right) = k_{ij}^{\eta_{ij}} \mathcal{Z}_{i}^{\eta_{ij}} / \left(1 + k_{ij}^{\eta_{ij}} \mathcal{Z}_{i}^{\eta_{ij}}\right) \tag{4}$$

where \mathcal{Z}_i denotes the abundance of factor i, k_{ij} denotes a gain parameter, and η_{ij} denotes a cooperativity parameter. In this study, we used $\mathcal{I}_j \in \{min, max\}$ (40). If a process has no modifying factors, $v_j = 1$. The model equations were implemented in Julia and solved using the SUNDIALS routine [REFs]. The complement model code and parameter ensemble is freely available under an MIT software license and can be downloaded from http://www.varnerlab.org.

Estimation of an ensemble of complement model parameters. We estimated a single initial parameter set using the using Dynamic Optimization with Particle Swarms (DOPS) technique [REF]. DOPS minimized the squared residual between simulated and experimental C3a and C5a measurements with and without zymosan as a single objective formulation. This initial best fit set then served as the starting point for multiobjective ensemble generation using Pareto Optimal Ensemble Technique in the Julia programming language (JuPOETs) [REF]. JuPOETs is a multiobjective approach which integrates simulated annealing with Pareto optimality to estimate model ensembles on or near the optimal tradeoff surface between competing training objectives. JuPOETs minimized training objective functions of the form:

$$E_j(\mathbf{k}) = \sum_{i=1}^{\mathcal{T}_j} \left(\hat{\mathcal{M}}_{ij} - \hat{y}_{ij}(\mathbf{k}) \right)^2 + \left(\frac{\mathcal{M}'_{ij} - \max y_{ij}}{\mathcal{M}'_{ij}} \right)^2$$
 (5)

The symbol $\hat{\mathcal{M}}_{ij}$ denotes scaled experimental observations (from training set j) while the symbol \hat{y}_{ij} denotes the scaled simulation output (from training objective j). The quantity i denotes the sampled time-index and \mathcal{T}_j denotes the number of time points for experiment j.

Sensitivity and robustness analysis of complement model performance. 413 ducted global sensitivity and robustness analysis to estimate which parameters and species 414 controlled the performance of the reduced order model. We computed the total variance-415 based sensitivity index of each parameter relative to the training residual for the C3a/C5a 416 alternate and C3a/C5a lectin objectives using the Sobol method (41). The sampling 417 bounds for each parameter were established from the minimum and maximum value for 418 that parameter in the parameter ensemble. We used the sampling method of Saltelli et 419 al. to compute a family of N(2d+2) parameter sets which obeyed our parameter ranges, 420 where N was the number of trials per parameters, and d was the number of parameters 421 in the model (42). In our case, N = 400 and d = 28, so the total sensitivity indices were computed using 23,200 model evaluations. The variance-based sensitivity analysis was 423 conducted using the SALib module encoded in the Python programming language (43).

Robustness coefficients quantify the response of a marker to a structural or operational perturbation to the network architecture. Robustness coefficients were calculated as shown previously (44). Log-transformed robustness coefficients denoted by $\hat{\alpha}\left(i,j,t_{o},t_{f}\right)$ are defined as:

425

426

427

428

$$\hat{\alpha}(i, j, t_o, t_f) = \log_{10} \left[\left(\int_{t_o}^{t_f} x_i(t) dt \right)^{-1} \left(\int_{t_o}^{t_f} x_i^{(j)}(t) dt \right) \right]$$
 (6)

Here t_o and t_f denote the initial and final simulation time, while i and j denote the indices 429 for the marker and the perturbation, respectively. A value of $\hat{\alpha}\left(i,j,t_{o},t_{f}\right)>0$, indicates 430 increased marker abundance, while $\hat{\alpha}(i, j, t_o, t_f) < 0$ indicates decreased marker abun-431 dance following perturbation j. If $\hat{\alpha}\left(i,j,t_{o},t_{f}\right)\sim0$, perturbation j did not influence the 432 abundance of marker i. In this study, we perturbed the initial condition of C3 or C5 or 433 a combination of C3 and C5 by 50% or 90% and measured the area under the curve 434 (AUC) of C3a or C5a with and without lectin initiator. Log-transformed robustness coeffi-435 cients were calculated for every member of the ensemble, where the mean \pm 1×standard-436 deviation are reported. 437

438 Competing interests

The authors declare that they have no competing interests.

Author's contributions

J.V directed the study. A.S developed the reduced order complement model and the parameter ensemble. A.S, W.D and M.M analyzed the model ensemble, and generated figures for the manuscript. The manuscript was prepared and edited for publication by A.S, W.D, M.M and J.V.

445 Acknowledgements

We gratefully acknowledge the suggestions from the anonymous reviewers to improve this manuscript.

448 Funding

This study was supported by an award from the US Army and Systems Biology of Trauma
Induced Coagulopathy (W911NF-10-1-0376) to J.V. for the support of A.S.

References

- 1. Nuttall G (1888) Experimente über die bacterienfeindlichen Einflüsse des thierischen Körpers. Z Hyg Infektionskr 4: 353-394.
- 2. Ricklin D, Hajishengallis G, Yang K, Lambris JD (2010) Complement: a key system for immune surveillance and homeostasis. NAT IMMUNOL 11: 785–797.
- Ricklin D, Lambris JD (2007) Complement-targeted therapeutics. NAT BIOTECHNOL
 25: 1265-1275.
- 4. Rittirsch D, Flierl MA, Ward PA (2008) Harmful molecular mechanisms in sepsis. NAT REV IMMUNOL 8: 776–787.
- 5. Sarma JV, Ward PA (2011) The complement system. Cell Tissue Res 343: 227–235.
- 6. Ricklin D, Lambris JD (2013) Complement in immune and inflammatory disorders: pathophysiological mechanisms. J Immunol 190: 3831–3838.
- 7. Walport MJ (2001) Complement. first of two parts. N Engl J Med 344: 1058-66.
- 8. Walport MJ (2001) Complement. second of two parts. N Engl J Med 344: 1140-4.
- 9. Pangburn MK, Müller-Eberhard HJ (1984) The alternative pathway of complement.

 Semin Immunopathol .
- 10. Walker D, Yasuhara O, Patston P, McGeer E, McGeer P (1995) Complement c1 inhibitor is produced by brain tissue and is cleaved in alzheimer disease. Brain Res 675: 75–82.
- 11. Blom AM, Kask L, Dahlbäck B (2001) Structural requirements for the complement regulatory activities of c4bp. J Biol Chem 276: 27136–27144.
- 12. Riley-Vargas RC, Gill DB, Kemper C, Liszewski MK, Atkinson JP (2004) Cd46: expanding beyond complement regulation. Trends Immunol 25: 496–503.
- 13. Lukacik P, Roversi P, White J, Esser D, Smith G, et al. (2004) Complement regulation at the molecular level: the structure of decay-accelerating factor. Proc Natl Acad Sci USA 101: 1279–1284.

- 14. Liszewski MK, Farries TC, Lublin DM, Rooney IA, Atkinson JP (1995) Control of the complement system. Adv Immunol 61: 201–283.
- 15. Chauhan A, Moore T (2006) Presence of plasma complement regulatory proteins clusterin (apo j) and vitronectin (s40) on circulating immune complexes (cic). Clin Exp Immunol 145: 398–406.
- 16. Zewde N, Gorham Jr RD, Dorado A, Morikis D (2016) Quantitative modeling of the alternative pathway of the complement system. PloS one 11: e0152337.
- Hirayama H, Yoshii K, Ojima H, Kawai N, Gotoh S, et al. (1996) Linear systems analysis of activating processes of complement system as a defense mechanism. Biosystems 39: 173–185.
- 18. Korotaevskiy AA, Hanin LG, Khanin MA (2009) Non-linear dynamics of the complement system activation. Math Biosci 222: 127–143.
- 19. Liu B, Zhang J, Tan PY, Hsu D, Blom AM, et al. (2011) A computational and experimental study of the regulatory mechanisms of the complement system. PLoS Comput
 Biol 7: e1001059.
- 492 20. Morad HO, Belete SC, Read T, Shaw AM (2015) Time-course analysis of c3a and c5a quantifies the coupling between the upper and terminal complement pathways in vitro. J Immunol Methods 427: 13–18.
- ⁴⁹⁵ 21. Morgan BP, Harris CL (2015) Complement, a target for therapy in inflammatory and degenerative diseases. NAT REV DRUG DISCOV 14: 857-877.
- Luan D, Zai M, Varner JD (2007) Computationally derived points of fragility of a human
 cascade are consistent with current therapeutic strategies. PLoS Comput Biol 3:
 e142.
- 23. Nayak S, Salim S, Luan D, Zai M, Varner JD (2008) A test of highly optimized tolerance reveals fragile cell-cycle mechanisms are molecular targets in clinical cancer trials. PLoS One 3: e2016.

- Tasseff R, Nayak S, Salim S, Kaushik P, Rizvi N, et al. (2010) Analysis of the molecular
 networks in androgen dependent and independent prostate cancer revealed fragile
 and robust subsystems. PLoS One 5: e8864.
- 25. Rice NT, Szlam F, Varner JD, Bernstein PS, Szlam AD, et al. (2016) Differential contributions of intrinsic and extrinsic pathways to thrombin generation in adult, maternal
 and cord plasma samples. PLoS One 11: e0154127.
- 26. Héja D, Harmat V, Fodor K, Wilmanns M, Dobó J, et al. (2012) Monospecific inhibitors
 show that both mannan-binding lectin-associated serine protease-1 (masp-1) and-2
 are essential for lectin pathway activation and reveal structural plasticity of masp-2. J
 Biol Chem: 20290–20300.
- 27. Roguska M, Splawski I, Diefenbach-Streiber B, Dolan E, Etemad-Gilbertson B, et al. (2014) Generation and characterization of lfg316, a fully-human anti-c5 antibody for the treatment of age-related macular degeneration. Investigative Ophthalmology & Visual Science: 3433–3433.
- ⁵¹⁷ 28. Melis JP, Strumane K, Ruuls SR, Beurskens FJ, Schuurman J, et al. (2015) Complement in therapy and disease: Regulating the complement system with antibodybased therapeutics. Molecular immunology: 117–130.
- 29. Weston-Davies WH, Nunn MA, Pinto FO, Mackie IJ, Richards SJ, et al. (2014) Clinical and immunological characterisation of coversin, a novel small protein inhibitor of complement c5 with potential as a therapeutic agent in pnh and other complement mediated disorders. Blood: 4280–4280.
- 30. Epstein D, Kurz JC (2007). Complement binding aptamers and anti-c5 agents useful in the treatment of ocular disorders. US Patent App. 12/224,708.
- 31. Borodovsky A, Yucius K, Sprague A, Banda NK, Holers VM, et al. (2014) Aln-cc5, an investigational rnai therapeutic targeting c5 for complement inhibition. Complement 20: 40.

- 32. Sissons J, Liebowitch J, Amos N, Peters D (1977) Metabolism of the fifth component of complement, and its relation to metabolism of the third component, in patients with complement activation. J Clin Invest 59: 704.
- 33. Swaak A, Hannema A, Vogelaar C, Boom F, van Es L, et al. (1982) Determination of
 the half-life of c3 in patients and its relation to the presence of c3-breakdown products
 and/or circulating immune complexes. Rheumatol Int: 161–166.
- 34. Noris M, Galbusera M, Gastoldi S, Macor P, Banterla F, et al. (2014) Dynamics of complement activation in ahus and how to monitor eculizumab therapy. Blood: 1715–1726.
- 35. Schwaeble HW, Stover CM, Tedford CE, Parent JB, Fujita T (2011). Methods for
 treating conditions associated with masp-2 dependent complement activation. US
 Patent 7,919,094.
- 36. Katschke KJ, Wu P, Ganesan R, Kelley RF, Mathieu MA, et al. (2012) Inhibiting alternative pathway complement activation by targeting the factor d exosite. Journal of Biological Chemistry: 12886–12892.
- 37. Hu X, Holers VM, Thurman JM, Schoeb TR, Ramos TN, et al. (2013) Therapeutic inhibition of the alternative complement pathway attenuates chronic eae. Mol Immunol : 302–308.
- 38. Bansal R (2014). Humanized and chimeric anti-properdin antibodies. US Patent 8,664,362.
- 39. Vogel CW, Fritzinger DC, Hew BE, Thorne M, Bammert H (2004) Recombinant cobra
 venom factor. Molecular immunology: 191–199.
- 40. Sagar A, Varner JD (2015) Dynamic modeling of the human coagulation cascade
 using reduced order effective kinetic models. Processes 3: 178.
- 41. Sobol I (2001) Global sensitivity indices for nonlinear mathematical models and their
 monte carlo estimates. MATH COMPUT SIMULAT 55: 271 280.

- Saltelli A, Annoni P, Azzini I, Campolongo F, Ratto M, et al. (2010) Variance based
 sensitivity analysis of model output. design and estimator for the total sensitivity index.
 Comput Phys Commun 181: 259–270.
- 558 43. Herman J. Salib: Sensitivity analysis library in python (numpy). con-559 tains sobol, morris, fractional factorial and fast methods. available online: 560 https://github.com/jdherman/salib.
- 44. Tasseff R, Nayak S, Song SO, Yen A, Varner JD (2011) Modeling and analysis
 of retinoic acid induced differentiation of uncommitted precursor cells. Integr Biol
 (Camb) 3: 578-91.



Fig. 1: Simplified schematic of the human complement system. The complement cascade is activated through three pathways: the classical, the lectin, and the alternate pathways. Complement initiation results in the formation of classical or alternative C3 convertases, which amplify the initial complement response and signal to the adaptive immune system by cleaving C3 into C3a and C3b. C3 convertases further react to form C5 convertases which catalyze the cleavage of the C5 complement protein to C5a and C5b. C5b is critical to the formation of the membrane attack complex (MAC), while C5a recruits an adaptive immune response.

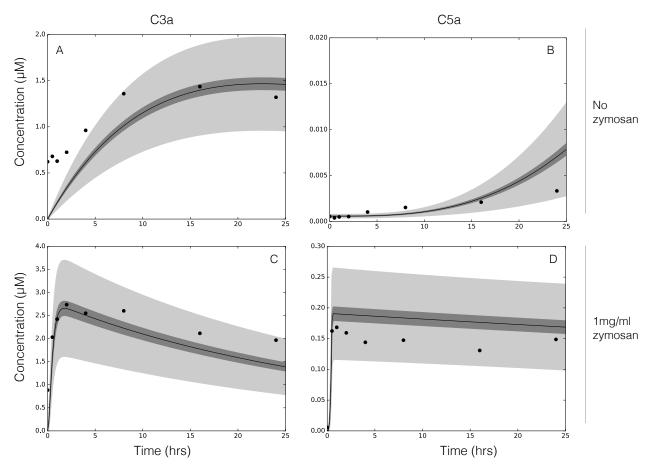


Fig. 2: Reduced order complement model training. Model parameters were estimated using Dynamic Optimization with Particle Swarms (DOPS) from C3a and C5a measurements with and without zymosan (20). The model was trained using C3a and C5a data generated from the alternative pathway (**A–B**) and lectin pathway initiated with 1g zymosan (**C–D**). The solid red line shows the simulation with the best-fit parameter set, the solid black lines show the simulated mean value of C3a or C5a for the ensemble (N = 50). The dark shaded region denotes the 99% confidence interval of the simulated mean concentrations, while the light shaded region denotes the 99% confidence interval of the best-fit simulation for C3a and C5a. All initial conditions were assumed to be at their physiological serum levels unless otherwise noted.

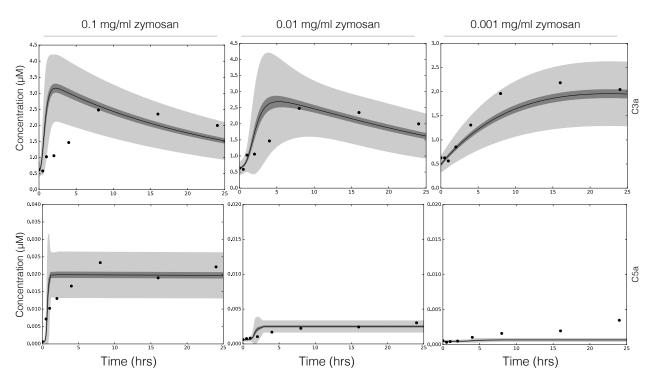


Fig. 3: Reduced order complement model predictions. The reduced order coagulation model parameter estimates were tested against data not used during model training (20). Simulations of C3a and C5a generated in the lectin pathway using 0.1g, 0.01g, and 0.001g zymosan were compared with the corresponding experimental measurement. The solid red line shows the simulation with the best-fit parameter set, the solid black lines show the simulated mean value of C3a or C5a for the ensemble (N = 50). The dark shaded region denotes the 99% confidence interval of the simulated mean concentrations, while the light shaded region denotes the 99% confidence interval of the best-fit simulation for C3a and C5a. All initial conditions were assumed to be at their physiological serum levels unless otherwise noted.

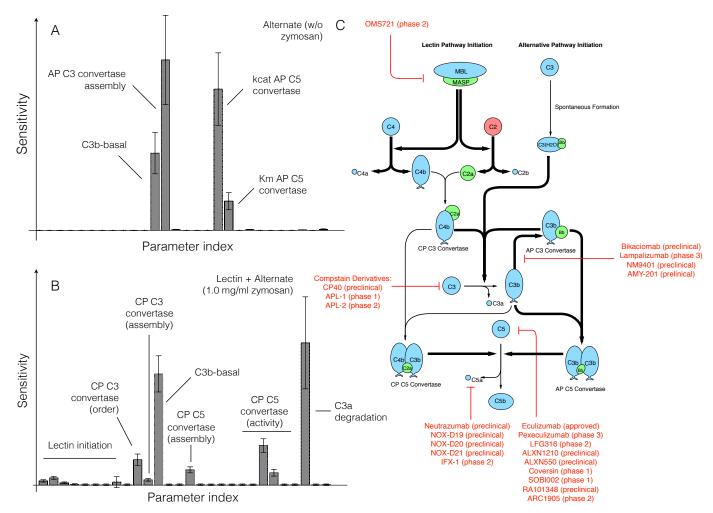
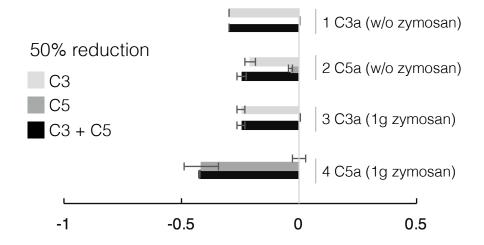


Fig. 4: Global sensitivity analysis of the reduced order complement model. Sensitivity analysis was conducted on the two objectives used for model training. **A:** Sensitivity of the C3a and C5a residual w/o zymosan, **B:** Sensitivity of the C3a and C5a residual with 1mg/ml zymosan. The bars denote the mean total sensitivity index for each parameter, while the error bars denote the 95% confidence interval. **C:** Pathways controlled by the sensitivity parameters. Bold black lines indicate the pathway involves one or more sensitive parameters, while the red lines show current therapeutics targets. Current complement therapeutics were taken from the review of Morgan and Harris (21).

Α



В

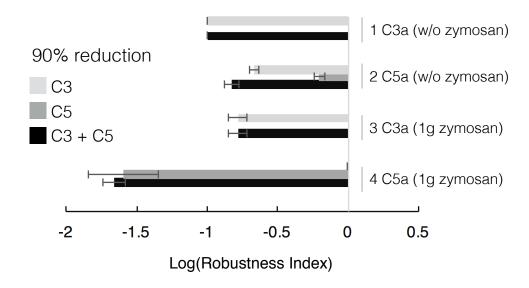


Fig. 5: Robustness analysis of the complement model with respect to C3 and C5 initial conditions. Robustness analysis was conducted on the four cases used for model training: C3a alternate (w/o zymosan), C5a alternate (w/o zymosan), C3a lectin (1g zymosan), and C5a lectin (1g zymosan), by reducing the initial concentration of C3 and/or C5 by 50% or 90 %. **A:** Robustness results for a 50% decrease in the C3, C5, or C3 and C5 initial condition. **B:** Robustness results for a 90% decrease in the C3, C5, or C3 and C5 initial condition. The bars denote the log-transformated robustness index while error bars denote one standard deviation. At zero, the perturbed initial concentration has no impact on the measured output. A log-transformed robustness index less than zero indicates a negative relation between the perturbed initial concentration and the measured output.