

There exists a collection of risky assets in the portfolio \mathcal{P} . An oracle provides the current price $p_i \in \mathbb{R}_+$ for each asset $i \in \mathcal{P}$, and a binary action vector $a \in \{0, 1\}^{|\mathcal{P}|}$ indicating whether each asset is available for investment ($a_i = 1$) or not ($a_i = 0$). The goal of the investment agent is to allocate a fixed budget B across these assets to **maximize the utility** of the portfolio.

Utility Function: Cobb-Douglas utility measures investor satisfaction:

$$U(n_1, \dots, n_P) = \kappa(\gamma) \prod_{i \in \mathcal{P}} n_i^{\gamma_i}$$

where γ_i is the preference for asset i (output of a preference model), $\kappa(\gamma)$ scales the function, and n_i is the number of shares (what we compute).