

CS148: Introduction to Computer Graphics and Imaging

Image Compositing



Colbert Challenge

Key Concepts

Optical compositing and mattes

The alpha channel

Compositing operators

Premultiplied alpha

Matte extraction

Optical Compositing

Image Composition

Defn: Combine foreground element with background

Examples:

- Graphics arts: masking tape, friskets, stencils
- Animation: cels, multiplane camera
- Film: optical printing, blue screen matting
- Video: chroma-keying
- Computer graphics: alpha channel

Multiplane Camera – Walt Disney

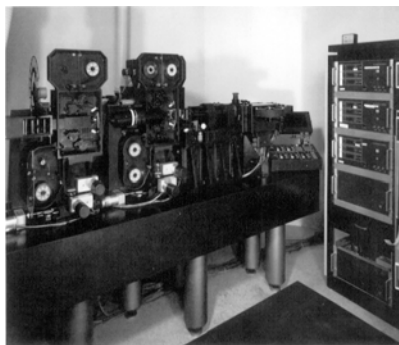


<http://disneyandmore.blogspot.com/2007/09/walt-disney-multiplane-camera-and.html>

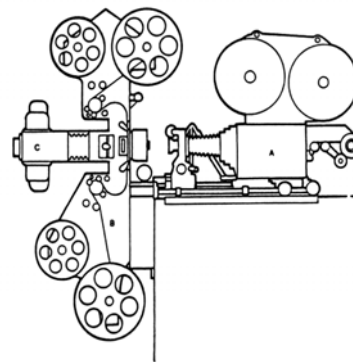
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Optical Printing



From: "Industrial Light and Magic,"
Thomas Smith (p. 181)



From: "Special Optical Effects,"
Zoran Perisic

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Composing Two Elements



Background Holdout Matte



Foreground Traveling Matte

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The Alpha Channel

The Alpha Channel

A alpha channel is an additional image that defines:

- The transparency or opacity of an image
- The presence or absence of imagery
 - Geometric coverage: soft-edge
- Or both coverage and transparency

Alpha channels may be

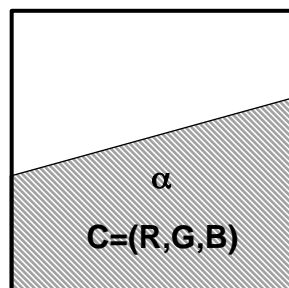
- Masks: all or none, binary
- Mattes: 0 to 1, n-ary

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Fragment: Color + Coverage

Pixel



$\alpha = A$
= Coverage
= Area
= Opacity
= 1 - Transparency

Color c of pixel is an area-weighted average of C

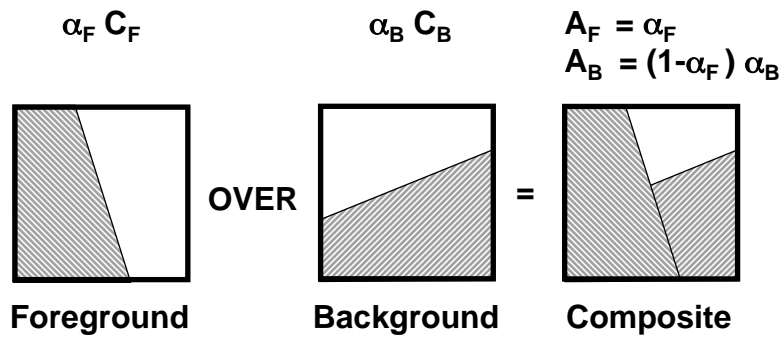
$$c = \alpha C$$

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Image Composition

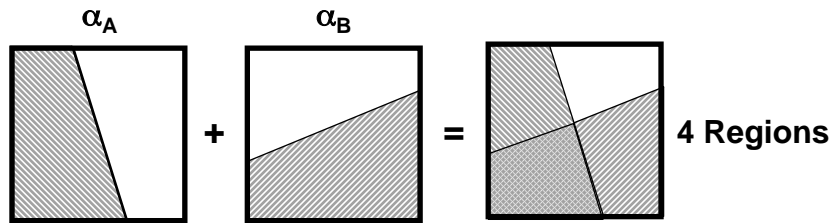
OVER Operator



Composite color: $c = A_F C_F + A_B C_B = (\alpha_F C_F) + (1 - \alpha_F) (\alpha_B C_B)$

Composite alpha: $\alpha = A_F + A_B = \alpha_F + (1 - \alpha_F) \alpha_B$

Region Coverage

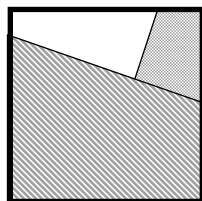


Region	Fraction
$A \cap B$	$\alpha_A \alpha_B$
$\sim A \cap B$	$(1 - \alpha_A) \alpha_B$
$A \cap \sim B$	$\alpha_A (1 - \alpha_B)$
$\sim A \cap \sim B$	$(1 - \alpha_A) (1 - \alpha_B)$

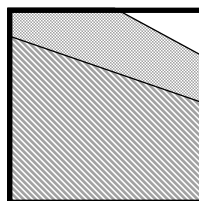
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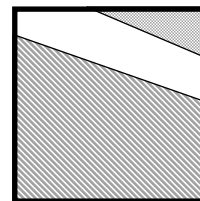
Assumptions



Uncorrelated



Correlated



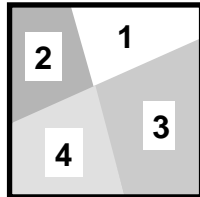
Anticorrelated

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Porter-Duff Compositing Algebra

How many ways can two pixels be combined?



4 Regions

Region 1: 1 possibility - 0

Region 2: 2 possibilities - A or 0

Region 3: 2 possibilities - B or 0

Region 4: 3 possibilities - A, B or 0

Operators: 12 total possibilities

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Porter-Duff Compositing Algebra

Operation	F_A	F_B
Clear	0	0
A	1	0
B	0	1
A over B	1	$1 - \alpha_A$
B over A	$1 - \alpha_B$	1
A in B	α_B	0
B in A	0	α_A
A out B	$1 - \alpha_B$	0
B out A	0	$1 - \alpha_A$
A atop B	α_B	$1 - \alpha_A$
B atop A	$1 - \alpha_B$	α_A
A xor B	$1 - \alpha_B$	$1 - \alpha_A$

$$c = F_A C_A + F_B C_B$$

OpenGL blendfunction

Specify src and dst F's

0, 1,
As, Ad, 1-As, 1-Ad,
min(As, 1-Ad),
Cs, Cd, 1-Cs, 1-Cd,

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Premultiplied Alpha

Represent as $c = \alpha C = (\alpha r, \alpha g, \alpha b, \alpha)$

- One formula for compositing color and alpha

$$c = c_F + (1 - \alpha_F) c_B$$

- Less arithmetic

Associated: OVER (1 sub, 4 muls, 4 adds)

Unassociated: OVER (1 sub, 7 muls, 4 adds)

- Closure

- Recovering C from c would require divide by α

- Display c ; c over $K = c + (1 - \alpha_C) K = c$

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Interpolation

Interpolate $c = (\alpha r, \alpha g, \alpha b, \alpha)$

Two ways of interpolating an image:

Compositing over the background and then interpolating

Interpolating and then compositing over the background

These should be the same!

Work it out (only works if interpolate c)

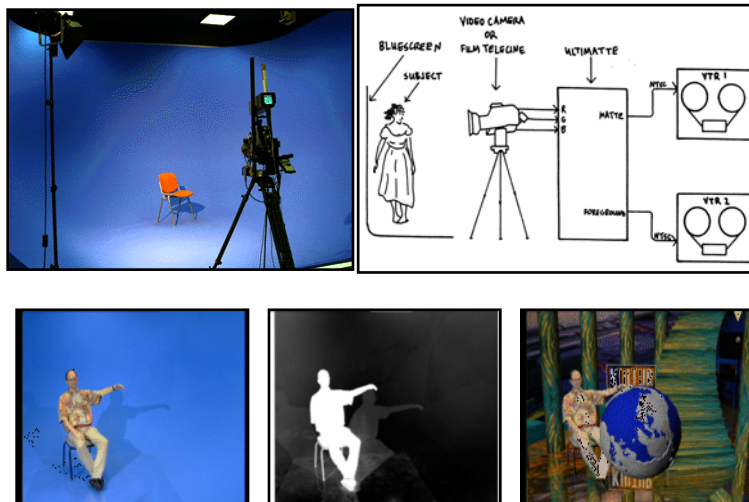
Similar reasoning applies to filtering, antialiasing, ...

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Matte Extraction

Blue Screen



“Pulling a Matte” - Matte Creation

From digitized images

- **Image processing**
 - Set of colors marked transparent, region growing ...
 - Demonstration: Photoshop Magic Wand
- **Video or chroma-keying**
 - Range of luminances marked transparent
- **Blue-screen matting (Petro Vlahos)**
 - Separate blue background from foreground image

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Blue/Green-Screen Matte Extraction

Given:

- C** - Observed color
- C_B** - Backing color

Compute:

$$\mathbf{C}_F = (\alpha_F R_F, \alpha_F G_F, \alpha_F B_F, \alpha_F)$$

Matte equation: $\mathbf{C} = \mathbf{C}_F + (1 - \alpha_F) \mathbf{C}_B$

Three equations (R, G, B) in four unknowns

$$R = R_F + (1 - \alpha_F) R_B$$

$$G = G_F + (1 - \alpha_F) G_B$$

$$B = B_F + (1 - \alpha_F) B_B$$

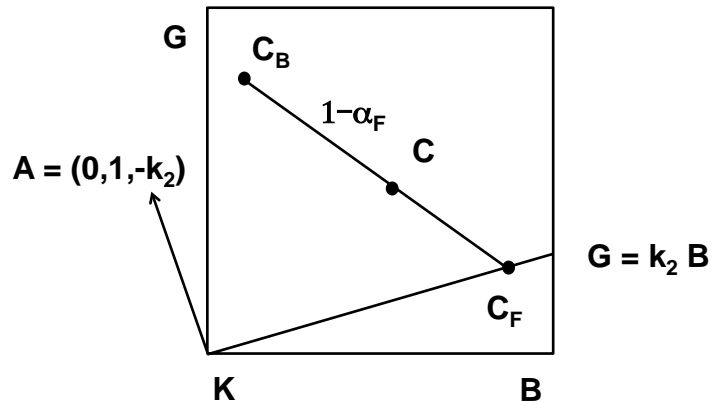
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Petros Vlahos Algorithm

$$C = C_F + (1-\alpha_F) C_B \rightarrow C_F = C - (1-\alpha_F) C_B$$

$$A \cdot C_F = A \cdot C - (1-\alpha_F) A \cdot C_B = 0$$



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Things to Remember

Classic techniques: masks, mattes, optical printing

Definition of the alpha channel as opacity/coverage

Premultiplied alpha

Porter-Duff image compositing algebra

Vlahos matte extraction algorithm

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