Chapter 1

What is functional programming?

In a nutshell:

- Functional programming is a method of program construction that emphasises functions and their application rather than commands and their execution.
- Functional programming uses simple mathematical notation that allows problems to be described clearly and concisely.
- Functional programming has a simple mathematical basis that supports equational reasoning about the properties of programs.

Our aim in this book is to illustrate these three key points, using a specific functional language called Haskell.

1.1 Functions and types

We will use the Haskell notation

```
f :: X -> Y
```

to assert that f is a function taking arguments of type X and returning results of type Y. For example,

```
sin :: Float -> Float age :: Person -> Int
```

add :: (Integer,Integer) -> Integer
logBase :: Float -> (Float -> Float)

Float is the type of floating-point numbers, things like 3.14159, and Int is the type of limited-precision integers, integers n that lie in a restricted range such as

 $-2^{29} \le n < 2^{29}$. The restriction is lifted with the type Integer, which is the type of unlimited-precision integers. As we will see in Chapter 3, numbers in Haskell come in many flavours.

In mathematics one usually writes f(x) to denote the application of the function f to the argument x. But we also write, for example, $\sin \theta$ rather than $\sin(\theta)$. In Haskell we can always write f x for the application of f to the argument f. The operation of application can be denoted using a space. If there are no parentheses the space is necessary to avoid confusion with multi-letter names: latex is a name but late f denotes the application of a function late to an argument f.

As examples, sin 3.14 or sin (3.14) or sin(3.14) are three legitimate ways of writing the application of the function sin to the argument 3.14.

Similarly, logBase 2 10 or (logBase 2) 10 or (logBase 2) (10) are all legitimate ways of writing the logarithm to base 2 of the number 10. But the expression logBase (2 10) is incorrect. Parentheses are needed in writing add (3,4) for the sum of 3 and 4 because the argument of add is declared above as a pair of integers and pairs are expressed with parentheses and commas.

Look again at the type of logBase. It takes a floating point number as argument, and returns a function as result. At first sight that might seem strange, but at second sight it shouldn't: the mathematical functions \log_2 and \log_e are exactly what is provided by logBase 2 and logBase e.

In mathematics one can encounter expressions like $\log \sin x$. To the mathematician that means $\log(\sin x)$, since the alternative $(\log \sin) x$ doesn't make sense. But in Haskell one has to say what one means, and one has to write $\log (\sin x)$ because $\log \sin x$ is read by Haskell as $(\log \sin) x$. Functional application in Haskell associates to the left in expressions and also has the highest binding power. (By the way, \log is the Haskell abbreviation for \log Base e.)

Here is another example. In trigonometry one can write

$$\sin 2\theta = 2\sin\theta\cos\theta$$
.

In Haskell one has to write

```
sin (2*theta) = 2 * sin theta * cos theta
```

Not only do we have to make the multiplications explicit, we also have to put in parentheses to say exactly what we mean. We could have added a couple more and written

```
sin (2*theta) = 2 * (sin theta) * (cos theta)
```

but the additional parentheses are not necessary because functional application binds tighter than multiplication.

1.2 Functional composition

Suppose $f :: Y \rightarrow Z$ and $g :: X \rightarrow Y$ are two given functions. We can combine them into a new function

that first applies g to an argument of type X, giving a result of type Y, and then applies f to this result, giving a final result of type Z. We always say that functions take *arguments* and return *results*. In fact we have

$$(f \cdot g) x = f (g x)$$

The order of composition is from right to left because we write functions to the left of the arguments to which they are applied. In English we write 'green pig' and interpret adjectives such as 'green' as functions taking noun phrases to noun phrases. Of course, in French...

1.3 Example: common words

Let us illustrate the importance of functional composition by solving a problem. What are the 100 most common words in *War and Peace*? What are the 50 most common words in *Love's Labours Lost*? We will write a functional program to find out. Well, perhaps we are not yet ready for a complete program, but we can construct enough of one to capture the essential spirit of functional programming.

What is given? Answer: a *text*, which is a list of characters, containing visible characters like 'B' and ',', and blank characters like spaces and newlines (' ' and '\n'). Note that individual characters are denoted using single quotes. Thus 'f' is a character, while f is a name. The Haskell type Char is the type of characters, and the type of lists whose elements are of type Char is denoted by [Char]. This notation is not special to characters, so [Int] denotes a list of integers, and [Float -> Float] a list of functions.

What is wanted as output? Answer: something like

the: 154 of: 50

a: 18 and: 12 in: 11

This display is also a list of characters, in fact it is the list

```
" the: 154\n of: 50\n a: 18\n and: 12\n in: 11\n"
```

Lists of characters are denoted using double quotes. More on this in the exercises.

So we want to design a function, commonWords say, with type

```
commonWords :: Int -> [Char] -> [Char]
```

The function commonWords n takes a list of characters and returns a list of the n most common words in the list as a *string* (another name for a list of characters) in the form described above. The type of commonWords is written without parentheses, though we can put them in:

```
commonWords :: Int -> ([Char] -> [Char])
```

Whenever two \rightarrow signs are adjacent in a type, the order of association is from right to left, exactly the opposite convention of functional application. So A \rightarrow B \rightarrow C means A \rightarrow (B \rightarrow C). If you want to describe the type (A \rightarrow B) \rightarrow C you have to put in the parentheses. More on this in the next chapter.

Having understood precisely what is given and what is wanted, different people come up with different ways of solving the problem, and express different worries about various parts of the problem. For example, what is a 'word' and how do you convert a list of characters into a list of words? Are the words "Hello", "hello" and "Hello!" distinct words or the same word? How do you count words? Do you count all the words or just the most common ones? And so on. Some find these details daunting and overwhelming. Most seem to agree that at some intermediate point in the computation we have to come up with a list of words and their frequencies, but how do we get from there to the final destination? Do we go through the list n times, extracting the word with the next highest frequency at each pass, or is there something better?

Let's start with what a word is, and just assert that a word is a maximal sequence of characters not containing spaces or newline characters. That allows words like "Hello!", or "3*4" or "Thelma&Louise" but never mind. In a text a word is identified by being surrounded by blank characters, so "Thelma and Louise" contains three words.

We are not going to worry about how to split a text up into a list of its component words. Instead we just assume the existence of a function

```
words :: [Char] -> [[Char]]
```

that does the job. Types like [[Char]] can be difficult to comprehend, but in Haskell we can always introduce *type synonyms*:

```
type Text = [Char]
type Word = [Char]
```

So now we have words :: Text -> [Word], which is much easier on the brain. Of course, a text is different from a word in that the former can contain blank characters and the latter cannot, but type synonyms in Haskell do not support such subtle distinctions. In fact, words is a library function in Haskell, so we don't have to define it ourselves

There is still the issue of whether "The" and "the" denote the same or different words. They really should be the same word, and one way of achieving this is to convert all the letters in the text to lowercase, leaving everything else unchanged. To this end, we need a function toLower: Char -> Char that converts uppercase letters to lowercase and leaves everything else unchanged. In order to apply this function to every character in the text we need a general function

```
map :: (a -> b) -> [a] -> [b]
```

such that map f applied to a list applies f to every element of the list. So, converting everything to lowercase is done by the function

```
map toLower :: Text -> Text
```

Good. At this point we have words . map toLower as the function which converts a text into a list of words in lowercase. The next task is to count the number of occurrences of each word. We could go through the list of words, checking to see whether the next word is new or has been seen before, and either starting a new count for a new word or incrementing the count for an existing word. But there is a conceptually simpler method, namely to *sort* the list of words into alphabetical order, thereby bringing all duplicated words together in the list. Humans would not do it this way, but the idea of sorting a list to make information available is probably the single most important algorithmic idea in computing. So, let us assume the existence of a function

```
sortWords :: [Word] -> [Word]
```

that sorts the list of words into alphabetical order. For example,

```
sortWords ["to","be","or","not","to","be"]
= ["be","be","not","or","to","to"]
```

Now we want to count the runs of adjacent occurrences of each word in the sorted list. Suppose we have a function

```
countRuns :: [Word] -> [(Int,Word)]
```

that counts the words. For example,

```
countRuns ["be","be","not","or","to","to"]
= [(2,"be"),(1,"not"),(1,"or"),(2,"to")]
```

The result is a list of words and their counts in alphabetical order of the words.

Now comes the key idea: we want the information in the list to be ordered not by word, but by decreasing order of count. Rather than thinking of something more clever, we see that this is just another version of sorting. As we said above, sorting is a *really* useful method in programming. So suppose we have a function

```
sortRuns :: [(Int,Word)] -> [(Int,Word)]
```

that sorts the list of runs into descending order of count (the first component of each element). For example,

```
sortRuns [(2,"be"),(1,"not"),(1,"or"),(2,"to")]
= [(2,"be"),(2,"to"),(1,"not"),(1,"or")]
```

The next step is simply to take the first n elements of the result. For this we need a function

```
take :: Int -> [a] -> [a]
```

so that take n takes the first n elements of a list of things. As far as take is concerned it doesn't matter what a 'thing' is, which is why there is an a in the type signature rather than (Int, Word). We will explain this idea in the next chapter.

The final steps are just tidying up. We first need to convert each element into a string so that, for example, (2, "be") is replaced by "be 2\n". Call this function

```
showRun :: (Int, Word) -> String
```

The type String is a predeclared Haskell type synonym for [Char]. That means

```
map showRun :: [(Int,Word)] -> [String]
```

is a function that converts a list of runs into a list of strings.

The final step is to use a function

```
concat :: [[a]] -> [a]
```

that concatenates a list of lists of things together. Again, it doesn't matter what the 'thing' is as far as concatenation is concerned, which is why there is an a in the type signature.

Now we can define

```
\label{eq:commonWords} \begin{tabular}{ll} $\operatorname{commonWords} \ :: \ Int \ -> \ Text \ -> \ String \\ $\operatorname{commonWords} \ n \ = \ concat \ . \ map \ showRun \ . \ take \ n \ . \\ & sortRuns \ . \ countRuns \ . \ sortWords \ . \\ & words \ . \ map \ toLower \end{tabular}
```

The definition of commonWords is given as a pipeline of eight component functions glued together by functional composition. Not every problem can be decomposed into component tasks in quite such a straightforward manner, but when it can, the resulting program is simple, attractive and effective.

Notice how the process of decomposing the problem was governed by the declared types of the subsidiary functions. Lesson Two (Lesson One being the importance of functional composition) is that deciding on the type of a function is the very first step in finding a suitable definition of the function.

We said above that we were going to write a *program* for the common words problem. What we actually did was to write a functional definition of commonWords, using subsidiary definitions that we either can construct ourselves or else import from a suitable Haskell library. A list of definitions is called a *script*, so what we constructed was a script. The order in which the functions are presented in a script is not important. We could place the definition of commonWords first, and then define the subsidiary functions, or else define all these functions first, and end up with the definition of the main function of interest. In other words we can tell the story of the script in any order we choose. We will see how to compute with scripts later on.

1.4 Example: numbers into words

Here is another example, one for which we will provide a complete solution. The example demonstrates another fundamental aspect of problem solving, namely that a good way to solve a tricky problem is to first simplify the problem and then see how to solve the simpler problem.

Sometimes we need to write numbers as words. For instance

Our aim is to design a function

```
convert :: Int -> String
```

that, given a nonnegative number less than one million, returns a string that represents the number in words. As we said above, String is a predeclared type synonym in Haskell for [Char].

We will need the names of the component numbers. One way is to give these as three lists of strings:

Oh, what is the > character doing at the beginning of each line above? The answer is that, in a script, it indicates a line of Haskell code, not a line of comment. In Haskell, a file ending with the suffix .1hs is called a *Literate Haskell Script* and the convention is that every line in such a script is interpreted as a comment unless it begins with a > sign, when it is interpreted as a line of program. Program lines are not allowed next to comments, so there has to be at least one blank line separating the two. In fact, the whole chapter you are now reading forms a legitimate .1hs file, one that can be loaded into a Haskell system and interacted with. We won't carry on with this convention in subsequent chapters (apart from anything else, it would force us to use different names for each version of a function that we may want to define) but the present chapter does illustrate *literate* programming in which we can present and discuss the definitions of functions in any order we wish.

Returning to the task in hand, a good way to tackle tricky problems is to solve a simpler problem first. The simplest version of our problem is when the given number n contains only one digit, so $0 \le n < 10$. Let convert1 deal with this version. We can immediately define

```
> convert1 :: Int -> String
> convert1 n = units!!n
```

This definition uses the list-indexing operation (!!). Given a list xs and an index n, the expression xs!!n returns the element of xs at position n, counting from 0. In particular, units!!0 = "zero". And, yes, units!!10 is undefined because units contains just ten elements, indexed from 0 to 9. In general, the functions we define in a script are *partial* functions that may not return well-defined results for each argument.

The next simplest version of the problem is when the number n has up to two digits, so $0 \le n < 100$. Let convert2 deal with this case. We will need to know what the digits are, so we first define

```
> digits2 :: Int -> (Int,Int)
> digits2 n = (div n 10, mod n 10)
```

The number div n k is the whole number of times k divides into n, and mod n k is the remainder. We can also write

```
digits2 n = (n `div` 10, n `mod` 10)
```

The operators 'div' and 'mod' are infix versions of div and mod, that is, they come between their two arguments rather than before them. This device is useful for improving readability. For instance a mathematician would write $x \operatorname{div} y$ and $x \operatorname{mod} y$ for these expressions. Note that the back-quote symbol ' is different from the single quote symbol ' used for describing individual characters.

Now we can define

```
> convert2 :: Int -> String
> convert2 = combine2 . digits2
```

The definition of combine2 uses the Haskell syntax for *guarded equations*:

To understand this code you need to know that the Haskell symbols for equality and comparison tests are as follows:

```
== (equals to)
/= (not equals to)
<= (less than or equal to)
```

These functions have well-defined types that we will give later on.

You also need to know that the conjunction of two tests is denoted by &&. Thus a && b returns the boolean value True if both a and b do, and False otherwise. In fact

```
(&&) :: Bool → Bool → Bool
```

The type Bool will be described in more detail in the following chapter.

Finally, (++) denotes the operation of concatenating two lists. It doesn't matter what the type of the list elements is, so

```
(++) :: [a] -> [a] -> [a]
```

For example, in the equation

```
[\sin,\cos] ++ [\tan] = [\sin,\cos,\tan]
```

we are concatenating two lists of functions (each of type Float -> Float), while in

```
"sin cos" ++ " tan" = "sin cos tan"
```

we are concatenating two lists of characters.

The definition of combine2 is arrived at by carefully considering all the possible cases that can arise. A little reflection shows that there are three main cases, namely when the tens part t is 0, 1 or greater than 1. In the first two cases we can give the answer immediately, but the third case has to be divided into two subcases, namely when the units part u is 0 or not 0. The order in which we write the cases, that is, the order of the individual guarded equations, is unimportant as the guards are disjoint from one another (that is, no two guards can be true) and together they cover all cases.

We could also have written

but now the order in which we write the equations is crucial. The guards are evaluated from top to bottom, taking the right-hand side corresponding to the first guard that evaluates to True. The identifier otherwise is just a synonym for True, so the last clause captures all the remaining cases.

There is yet another way of writing convert2:

This makes use of a where *clause*. Such a clause introduces a *local* definition or definitions whose *context* or *scope* is the whole of the right-hand side of the definition of convert2. Such clauses are very useful in structuring definitions and making them more readable. In the present example, the where clause obviates the need for an explicit definition of digits2.

That was reasonably easy, so now let us consider convert3 which takes a number n in the range $0 \le n < 1000$, so n has up to three digits. The definition is

We break up the number in this way because we can make use of convert2 for numbers that are less than 100.

Now suppose n lies in the range $0 \le n < 1,000,000$, so n can have up to six digits. Following exactly the same pattern as before, we can define

There will be a connecting word 'and' between the words for m and h just in the case that 0 < m and 0 < h < 100. Thus

```
> link :: Int -> String
> link h = if h < 100 then " and " else " "</pre>
```

This definition makes use of a conditional expression

```
if <test> then <expr1> else <expr2>
```

We could also have used guarded equations:

```
link h | h < 100 = " and " | otherwise = " "
```

Sometimes one is more readable, sometimes the other. The names if, then and else, along with some others, are *reserved words* in Haskell, which means that we cannot use them as names for things we want to define.

Notice how the definition of convert6 has been constructed in terms of the simpler function convert3, which in turn has been defined in terms of the even simpler function convert2. That is often the way with function definitions. In this example consideration of the simpler cases is not wasted because these simple cases can be used in the final definition.

One more thing: we have now named the function we are after as convert6, but we started off by saying the name should be convert. No problem:

```
> convert :: Int -> String
> convert = convert6
```

What we would like to do now is actually use the computer to apply convert to some arguments. How?

1.5 The Haskell Platform

If you visit the site www.haskell.org, you will see how to download *The Haskell Platform*. This is a large collection of tools and packages that can be used to run Haskell scripts. The platform comes in three versions, one for each of Windows, Mac and Linux. We deal only with the Windows version, the others being similar.

One of the tools is an interactive calculator, called GHCi. This is short for *Glasgow Haskell Compiler Interpreter*. The calculator is available as a Windows system called WinGHCi. If you open this window, you will get something like

```
GHCi, version 7.6.3: http://www.haskell.org/ghc/ :? for help Loading package ghc-prim ... linking ... done.
Loading package integer-gmp ... linking ... done.
Loading package base ... linking ... done.
Prelude>
```

The prompt Prelude> means that the standard library of prelude functions, predeclared types and other values is loaded. You can now use GHCi as a supercalculator:

```
Prelude> 3^5
243
Prelude> import Data.Char
Prelude Data.Char> map toLower "HELLO WORLD!"
"hello world!"
Prelude Data.Char>
```

The function toLower resides in the library Data. Char. After importing this library you have access to the functions defined in the library. Note that the prompt changes and now indicates the libraries that have been loaded. Such prompts can grow in size very quickly. But we can always change the prompt:

```
Prelude> :set prompt ghci>
ghci>
```

For brevity we will use this prompt throughout the book.

You can load a script, Numbers2Words.lhs say, that contains the definition of convert as follows:

```
ghci> :load "Numbers2Words.lhs"
[1 of 1] Compiling Main ( Numbers2Words.lhs, interpreted )
Ok, modules loaded: Main.
ghci>
```

We will explain what modules are in the next chapter. Now you can type, for example,

```
ghci> convert 301123
"three hundred and one thousand one hundred and twenty-three"
ghci>
```

We end the chapter with some exercises. These contain additional points of interest

and should be regarded as an integral part of the text. The same is true for all subsequent chapters, so please read the questions even if you do not answer them. The answers are given afterwards.

1.6 Exercises

Exercise A

Consider the function

```
double :: Integer -> Integer
double x = 2*x
```

that doubles an integer. What are the values of the following expressions?

```
map double [1,4,4,3]
map (double . double) [1,4,4,3]
map double []
```

Suppose sum :: [Integer] -> Integer is a function that sums a list of integers. Which of the following assertions are true and why?

```
sum . map double = double . sum
sum . map sum = sum . concat
sum . sort = sum
```

You will need to recall what the function concat does. The function sort sorts a list of numbers into ascending order.

Exercise B

In Haskell, functional application takes precedence over every other operator, so double 3+4 means (double 3)+4, not double (3+4). Which of the following expressions is a rendering of $\sin^2 \theta$ into Haskell?

```
sin^2 theta sin theta^2 (sin theta)^2
```

(Exponentiation is denoted by (^).) How would you express $\sin 2\theta/2\pi$ as a well-formed Haskell expression?

Exercise C

As we said in the text, a character, i.e. an element of Char, is denoted using single quotes, and a string is denoted using double quotes. In particular the string "Hello World!" is just a much shorter way of writing the list

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```
['H','e','l','l','o',' ','W','o','r','l','d','!']
```

General lists can be written with brackets and commas. (By the way, parentheses are round, brackets are square, and braces are curly.) The expressions 'H' and "H" therefore have different types. What are they? What is the difference between 2001 and "2001"?

The operation ++ concatenates two lists. Simplify

```
[1,2,3] ++ [3,2,1]
"Hello" ++ " World!"
[1,2,3] ++ []
"Hello" ++ "" ++ "World!"
```

Exercise D

In the common words example we started off by converting every letter in the text to lowercase, and then we computed the words in the text. An alternative is to do things the other way round, first computing the words and then converting each letter in each word to lowercase. The first method is expressed by words . map toLower. Give a similar expression for the second method.

Exercise E

An operator \oplus is said to be *associative* if $x \oplus (y \oplus z) = (x \oplus y) \oplus z$. Is numerical addition associative? Is list concatenation associative? Is functional composition associative? Give an example of an operator on numbers that is not associative.

An element *e* is said to be an *identity element* of \oplus if $x \oplus e = e \oplus x = x$ for all *x*. What are the identity elements of addition, concatenation and functional composition?

Exercise F

My wife has a book with the title

EHT CDOORRSSW AAAGMNR ACDIINORTY.

It contains lists of entries like this:

```
6-letter words
-----
...
eginor: ignore,region
eginrr: ringer
eginrs: resign,signer,singer
```

Yes, it is an anagram dictionary. The letters of the anagrams are sorted and the results are stored in dictionary order. Associated with each anagram are the English words with the same letters. Describe how you would go about designing a function

```
anagrams :: Int -> [Word] -> String
```

so that anagrams n takes a list of English words in alphabetical order, extracts just the *n*-letter words and produces a string that, when displayed, gives a list of the anagram entries for the *n*-letter words. You are not expected to be able to define the various functions; just give suitable names and types and describe what each of them is supposed to do.

Exercise G

Let's end with a song:

```
One man went to mow
Went to mow a meadow
One man and his dog
Went to mow a meadow
```

Two men went to mow
Went to mow a meadow
Two men, one man and his dog
Went to mow a meadow

Three men went to mow
Went to mow a meadow
Three men, two men, one man and his dog
Went to mow a meadow

Write a Haskell function song :: Int -> String so that song n is the song when there are n men. Assume n<10.

To print the song, type for example

```
ghci> putStrLn (song 5)
```

The function putStrLn will be explained in the following chapter. I suggest starting with

```
song n = if n==0 then ""

else song (n-1) ++ "\n" ++ verse n

verse n = line1 n ++ line2 n ++ line3 n ++ line4 n
```

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This defines song recursively.

1.7 Answers

Answer to Exercise A

```
map double [1,4,4,3] = [2,8,8,6] map (double . double) [1,4,4,3] = [4,16,16,12] map double [] = []
```

You will gather from this that [] denotes the empty list.

All the following equations hold:

```
sum . map double = double . sum
sum . map sum = sum . concat
sum . sort = sum
```

In fact, each of these three equations are consequences of the three simpler laws:

```
a*(x+y) = a*x + a*y

x+(y+z) = (x+y)+z

x+y = y+x
```

Of course, we don't know yet how to *prove* that the equations hold. (By the way, to avoid fuss we will often use a typewriter = sign to denote the equality of two Haskell expressions written in typewriter font. But a mathematical = sign is used in equations such as $\sin 2\theta = 2\sin \theta \cos \theta$.)

Answer to Exercise B

Both sin theta^2 and (sin theta)^2 are okay, but not sin^2 theta.

Here is the rendering of $\sin 2\theta/2\pi$ in Haskell:

```
sin (2*theta) / (2*pi)
```

Note that

```
sin (2*theta) / 2 * pi = (sin (2*theta) / 2) * pi
```

which is not what we want. The reason is that operators such as / and * at the same level of precedence associate to the left in expressions. More on this in the next chapter.

Answer to Exercise C

```
'H' :: Char
"H" :: [Char]
2001 :: Integer
"2001" :: [Char]
```

By the way, '\' is used as an *escape* character, so '\n' is the newline character, and '\t' is the tab character. Also, '\\' is the backslash character, and "\\n" is a list of two characters, a backslash and the letter n. As a consequence, the file path C:\firefox\stuff is written as the Haskell string "C:\\firefox\\stuff".

```
[1,2,3] ++ [3,2,1] = [1,2,3,3,2,1]
"Hello" ++ " World!" = "Hello World!"
[1,2,3] ++ [] = [1,2,3]
"Hello" ++ "" ++"World!" = "HelloWorld!"
```

If you got the last two right, you will have appreciated that [] is an empty list of anything, but "" is an empty list of characters.

Answer to Exercise D

The clue is in the phrase 'converting each letter in each word to lowercase'. Converting each letter in a single word is expressed by map toLower, so the answer is map (map toLower) . words. That means the following equation holds:

```
words . map toLower = map (map toLower) . words
```

Answer to Exercise E

Numerical addition, list concatenation and functional composition are all associative. But of course, numerical subtraction isn't. Nor is exponentiation. The identity element of addition is 0, the identity element of concatenation is the empty list, and the identity element of functional composition is the identity function:

```
id :: a \rightarrow a
id x = x
```

Answer to Exercise F

This exercise follows Section 1.3 quite closely. One way of computing the function anagrams n is as follows:

1. Extract the words of length n, using a function

```
getWords :: Int -> [Word] -> [Word]
```

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2. Take each word and add a label to it. The label consists of the characters of the word, sorted into alphabetical order. For example, word is turned into the pair ("dorw", "word") This labelling is achieved by the function

```
addLabel :: Word -> (Label, Word)
```

where

```
type Label = [Char]
```

3. Sort the list of labelled words into alphabetical order of label, using the function

```
sortLabels :: [(Label, Word)] -> [(Label, Word)]
```

4. Replace each group of adjacent labelled words with the same label with a single entry consisting of a pair in which the first component is the common label and the second component is a list of words with that label. This uses a function

```
groupByLabel :: [(Label, Word)] -> [(Label, [Word])]
```

5. Replace each entry by a string using a function

```
showEntry :: [(Label, [Word])] -> String
```

and concatenate the results.

That gives

Answer to Exercise G

One possible solution:

Notice that we have omitted to declare the types of the component functions and values in this script. Although Haskell will infer the correct types, it is usually a good idea to put them in for all functions and other values, however simple the types may be. Scripts with explicit type signatures are clearer to read and provide a useful check on the validity of definitions.

1.8 Chapter notes

If you are interested in the origins of Haskell, you should definitely read *The History of Haskell*, a copy of which is obtainable at

```
research.microsoft.com/~simonpj/papers/history-of-haskell
```

One of the abiding strengths of Haskell is that it wasn't designed to be a closed language, and researchers were encouraged to implement novel programming ideas and techniques by building language extensions or libraries. Consequently, Haskell is a large language and there are numerous books, tutorials and papers devoted to various aspects of the subject, including the recent *Parallel and Concurrent Programming in Haskell* by Simon Marlow (O'Reilly, 2013). Pointers to much of the material can be found at www.haskell.org. But three books in particular were open on my desk while writing this text. The first is *Haskell 98*, *Languages and Libraries*, *The Revised Report* (Cambridge University Press, 2003), edited by Simon Peyton Jones. This is an indispensable aid in understanding the nitty-gritty of the first standard version of Haskell, called Haskell 98. An online version of the report is available at

```
www.haskell.org/onlinereport
```

The present book mostly follows this standard, though it does not cover the whole language by any means.

Since then a new standard, Haskell 2010, has been released; see

haskell.org/onlinereport/haskell2010/

One change is that module names are now hierarchical, so we write Data.List rather than just List for the library of list utilities.

The second two are textbooks: *Real World Haskell* (O'Reilly, 2009) by Bryan O'Sullivan, John Goerzen and Don Stewart; and *Programming in Haskell* (Cambridge, 2007) by Graham Hutton. As its name implies, the former deals mostly with highly practical applications, while the latter is another introductory text. Graham Hutton did suggest to me, albeit with a grin, that my book should be called *Ivory Tower Haskell*.

There is a fascinating history concerning the common words problem. Jon Bentley invited one programmer, Don Knuth, to write a literate WEB program for the problem, and another programmer, Doug McIlroy, to write a literary review of it. The result was published in Bentley's *Programming Pearls* column in *Communications of the ACM*, vol. 29, no. 6 (June 1986).