

Support Vector Machine - A Supervised machine learning algo. used for classification and regression task.

Idea - Find the best decision boundary (hyperplane) that separates different classes with the maximum margin.

key terms -

Hyperplane - Line/plane that divides data.

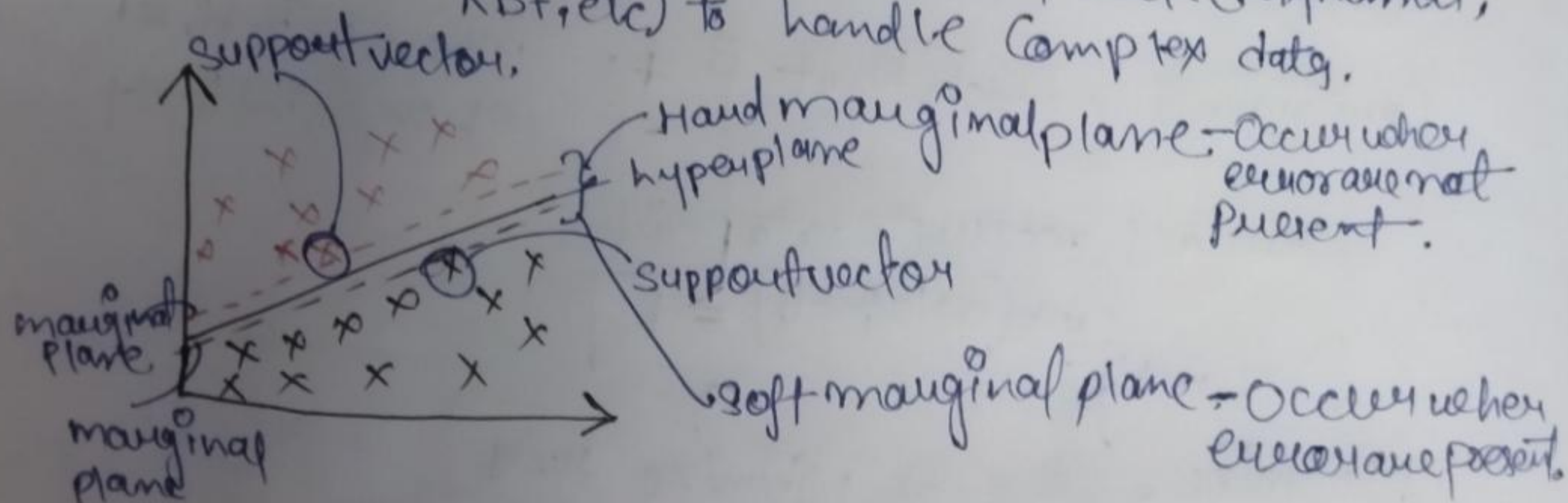
Support vector - Data points closest to the hyperplane, (critical in defining boundary)

Margin - Distance between hyperplane and nearest data points (Support vector)

Types -

Linear SVM - work when data is linearly separable

Non-Linear SVM - Use kernel trick (polynomial, RBF, etc) to handle complex data.



eg. of straight line

$$ax + by + c = C (\leq) y = mx + c$$

$$by = -ax - c$$

$$y = \frac{-a}{b}(x) - \frac{c}{b} \quad m = \frac{-a}{b}$$

$$C = \frac{c}{b}$$

$$y = mx + c$$

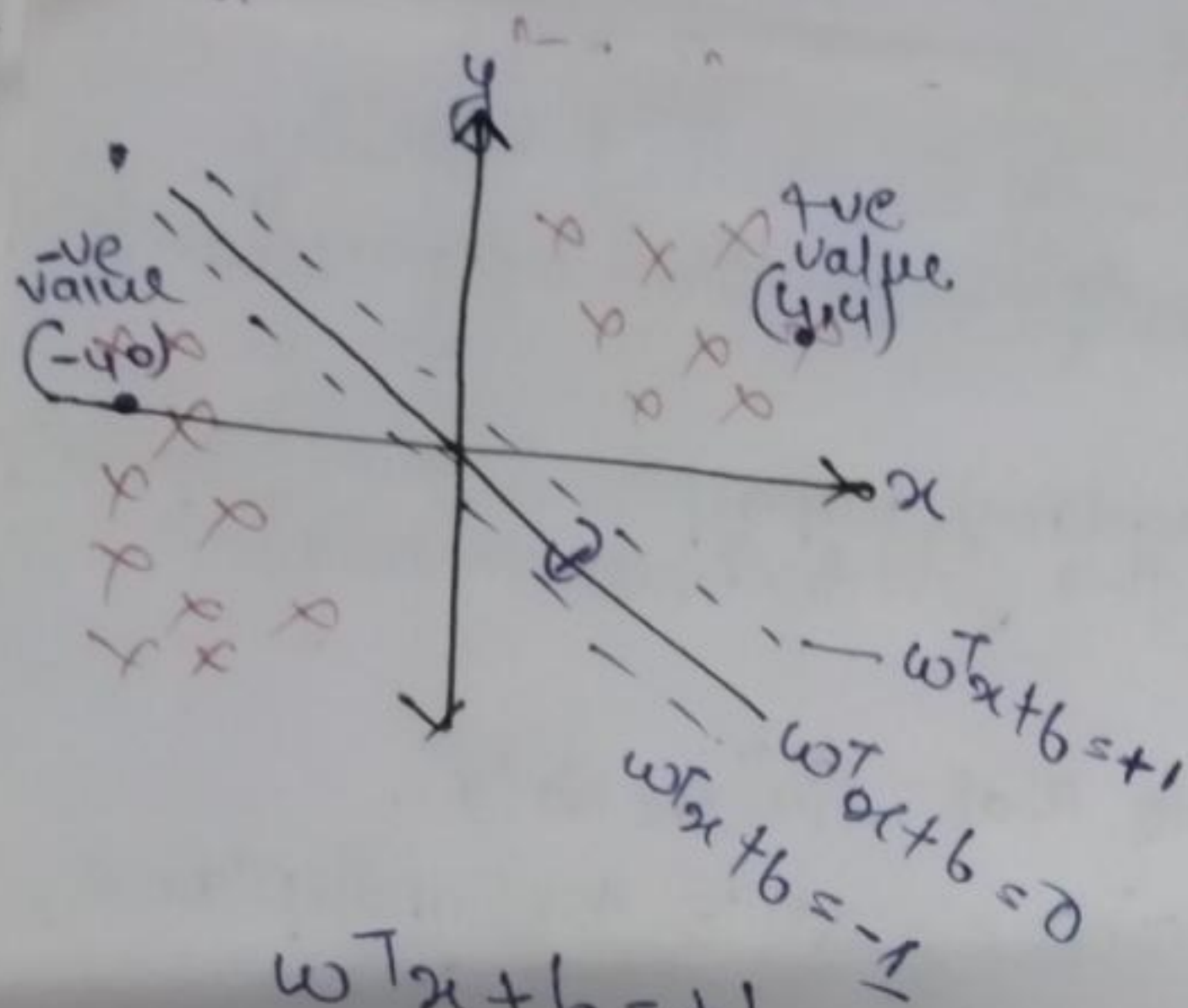
$$y = \beta_0 + \beta_1 x$$

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$$y = w_1 x_1 + b$$

$$y = w_1 x_1 + w_2 x_2 + b$$

$$y = w^T x + b$$



$$3x + 2y + 4 \leq 0$$

$$3(-4) + 2(0) + 4$$

$$-12 + 0 + 4$$

$$= \boxed{-8}$$

$$3(4) + 2(4) + 4 \leq 0$$

$$12 + 8 + 4$$

$$= \boxed{24} \text{ true}$$

$w \Rightarrow$ magnitude
 \rightarrow vector

$$w^T x + b = +1$$

$$(-) w^T x + b = -1$$

$$\vec{w} = \frac{w^T (x_1 - x_2)}{\|w\|} = \frac{2}{\|w\|} \Rightarrow \text{Maximize (mean distance is high)}$$

$$\frac{\text{Maximize}}{(w, b)} = \frac{2}{\|w\|} \Rightarrow \text{marginal plane distance.}$$

Constraints = Such that $\begin{cases} +1 & \text{when } w^T x + b \geq 1 \\ -1 & \text{when } w^T x + b \leq -1 \end{cases}$

For all accurate data point

$$y x (w^T x + b) \geq 1$$

$$\text{Maximize } (w, b) = \frac{2}{\|w\|} \Rightarrow \boxed{\text{Minimize } \frac{\|w\|}{2}}_{(w, b)}$$

$$\text{Cost function} = \text{Minimize } \frac{\|w\|}{2} + C_i \sum_{i=1}^n w_i$$

\downarrow
 How many points can avoid misclassification

summation of the distance of misclassification Point from marginal plane