

Support Vector Machine - A Supervised machine learning algo. used for classification and regression tasks.

Idea - Find the best decision boundary (hyperplane) that separates different classes with the maximum margin.

key terms -

Hyperplane - Line/Plane that divides data.

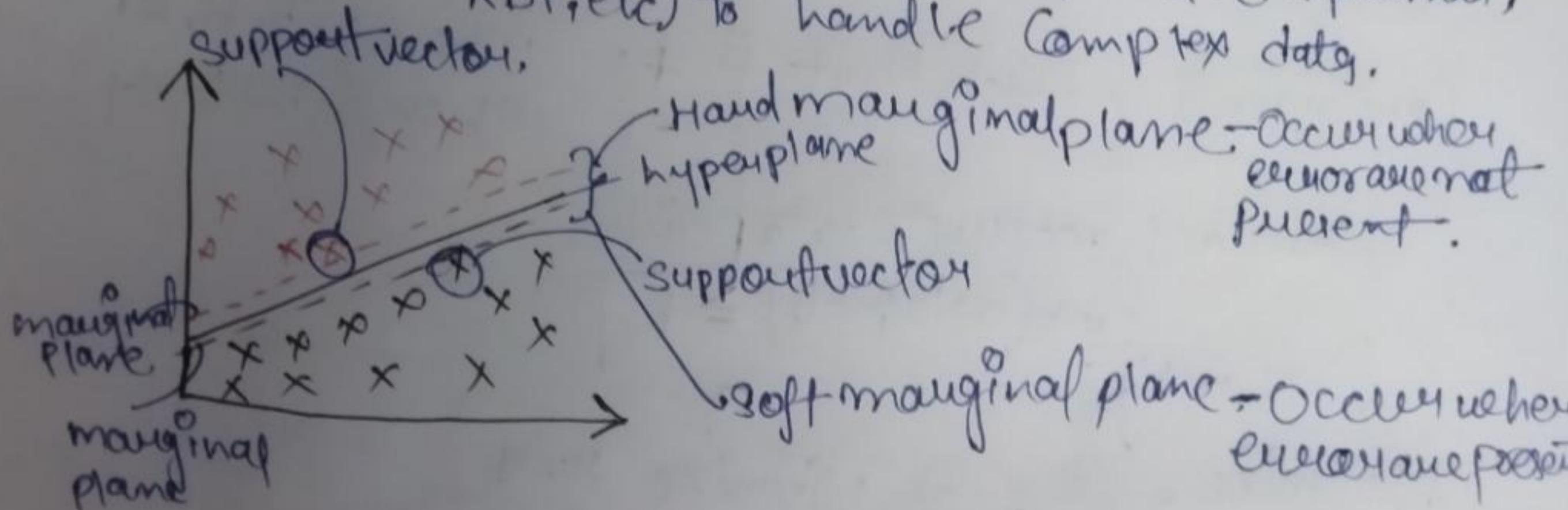
Support vector - Data points closest to the hyperplane, (critical in defining boundary)

Margin - Distance between hyperplane and nearest data points (Support vector)

Types -

Linear SVM - Work when data is linearly separable

Non-Linear SVM - Use kernel trick (Polynomial, RBF, etc) to handle complex data.



Eq. of straight line

$$ax_1 + bx_2 + c = 0 \Leftrightarrow y = mx + c$$

$$by = -ax_1 - c$$

$$\boxed{y = \frac{-a}{b}x_1 - \frac{c}{b}}$$

$$m = -\frac{a}{b}$$

$$c = \frac{c}{b}$$

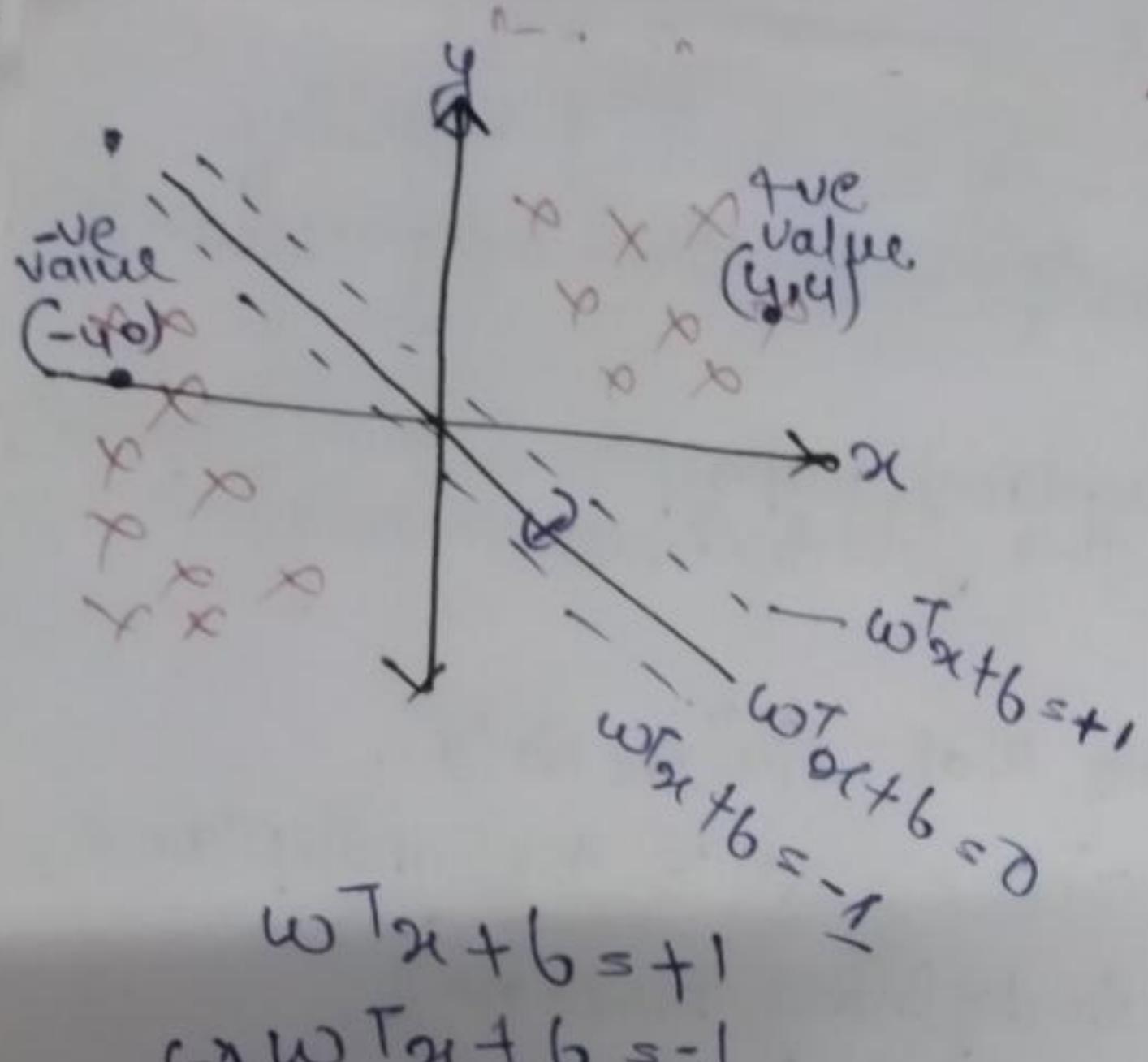
Ysmax

$$y = \beta_0 + \beta_1 x_1$$

$$y = \alpha_0 + \alpha_1 x_1 + b$$

$$y = w_0 + w_1 x_1 + w_2 x_2 + b$$

$$\boxed{y = w^T x + b}$$



$$\begin{aligned} 3x+2y+4 &= 0 \\ 3(4)+2(0)+4 &= 0 \\ -12+0+4 &= -8 \end{aligned}$$

$$\begin{aligned} 3(4)+2(4)+4 &= 0 \\ 12+8+4 &= 24 \end{aligned}$$

$w \Rightarrow$ Magnitude
 \rightarrow Vector

$$\vec{w} = \frac{\vec{w}^T_{\text{axis}}(\vec{x}_1 - \vec{x}_2)}{\|\vec{w}\|} = 2 \quad \left. \right\} \Rightarrow \text{Maximize (mean distance is high)}$$

$$\frac{\text{Maximize}}{(w,b)} = \frac{2}{\|\vec{w}\|} \Rightarrow \text{Marginal plane distance.}$$

Constraints - Such that $s = \begin{cases} +1 & \text{when } \vec{w}^T x + b \geq 1 \\ -1 & \text{when } \vec{w}^T x + b \leq -1 \end{cases}$

For all accurate data point

$$y \times (\vec{w}^T x_i + b) \geq 1$$

$$\text{Maximize}_{(w,b)} = \frac{2}{\|\vec{w}\|} \Rightarrow \boxed{\text{Minimize}_{(w,b)} \frac{\|\vec{w}\|}{2}}$$

$$\text{Cost function} = \text{Minimize}_{(w,b)} \frac{\|\vec{w}\|}{2} + C_i \sum_{i=1}^n$$

\downarrow
How many points
are misclassified
and can avoid
misclassification

Summation of
the distance of
misclassified
Point from
marginal
Plane