

Upon solving the integral  $\int_0^{\Delta s_j} (as_j + b) \frac{As_j + B}{s_j^2 + Cs_j + D} ds_j$  in Python, the following solution was obtained:

$$-(\gamma_{j+1} - \gamma_j) \cos(\theta i - \theta j) - \left( \frac{((-xi + \hat{x}i) \cos(\theta j) + (-yj + \hat{y}i) \sin(\theta j)) (\gamma j + 1 - \gamma j)}{2\Delta s j} + \frac{(\gamma j + 1 - \gamma j) (2 \sin(\theta j))}{2\Delta s j} \right)$$

$$\left( \frac{((-xi + \hat{x}i) \cos(\theta j) + (-yj + \hat{y}i) \sin(\theta j)) (\gamma j + 1 - \gamma j)}{2\Delta s j} + \frac{(\gamma j + 1 - \gamma j) (2 \sin(\theta j) yj - 2 \sin(\theta j) \hat{y}i + 2 \cos(\theta j))}{2\Delta s j} \right)$$

$$\left( \frac{((-xi + \hat{x}i) \cos(\theta j) + (-yj + \hat{y}i) \sin(\theta j)) (\gamma j + 1 - \gamma j)}{2\Delta s j} + \frac{(\gamma j + 1 - \gamma j) (2 \sin(\theta j) yj - 2 \sin(\theta j) \hat{y}i + 2 \cos(\theta j))}{2\Delta s j} \right)$$

$$\left( \frac{((-xi + \hat{x}i) \cos(\theta j) + (-yj + \hat{y}i) \sin(\theta j)) (\gamma j + 1 - \gamma j)}{2\Delta s j} + \frac{(\gamma j + 1 - \gamma j) (2 \sin(\theta j) yj - 2 \sin(\theta j) \hat{y}i + 2 \cos(\theta j))}{2\Delta s j} \right)$$